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PRACTICAL - 01

- R is a software for statistical analysis and data computing.
- It is an effective data handling software and outcome storage is possible.
- It is capable of graphical display
- R is a free software.

Q1] Solve the following

Code:-

1. $4+6+8 \div 2-5$

[1] $4+6+8/2$

[1] 14

2. $2^2 + |-3| + \sqrt{45}$

[2] $2^2 + \text{abs}(-3) + \sqrt{45}$

[1] 13.7082

3. $5^3 + 7 \times 5 \times 8 + 46/5$

[3] $5^3 + 7 * 5 * 8 + 46/5$

[1] 414.2

4. $\sqrt{4^2 + 5 \times 3 + 7/6}$

[4] $\sqrt{4^2 + 5 * 3 + 7/6}$

[1] 5.671567

5. Round off

$46+7+9 \times 8$

[5] $46/7+9 * 8$

[1] 78.57143

Q2] Solve the following

- ① $c(2, 3, 5, 7) * 2$
→ [1] 4 6 10 14
- ② $c(2, 3, 5, 7) * c(2, 3)$
→ [1] 4 9 10 21
- ③ $c(2, 3, 5, 7) * c(2, 3, 6, 2)$
→ [1] 4 9 30 14
- ④ $c(1, 6, 2, 3) * c(-2, -3, -4, -1)$
→ [1] -2 -18 -8 -3
- ⑤ $c(2, 3, 5, 7)^2$
→ [1] 4 9 25 49
- ⑥ $c(4, 6, 8, 9, 4, 5)^2 * c(1, 2, 3)$
→ [1] 4 36 512 9 16 125
- ⑦ $c(6, 2, 7, 5) / c(4, 5)$

Q3] Solve the following

$$x = 20, y = 30, z = 2.$$

Find 1) $x^2 + y^3 + z$

2) $\sqrt{x^2 + y^2}$

3) $x^2 \cdot y^z$

i) $a = x^2 + y^3 + z$

$\geq a$

[1] 27402

ii) $b = \sqrt{x^2 + y^2}$

$\geq b$

[1] 20.73644

iii) $x = x^1z + y^1z$
 $\Rightarrow x$
[1] 1300

Q4] Convert the data in Matrix Form:-

1	5
2	6
3	7
4	8

$x = \text{matrix}(\text{nrow} = 4, \text{ncol} = 2, \text{data} = c(1, 2, 3, 4, 5, 6, 7, 8))$

> x
[1] [2]
[1,] 1 5
[2,] 2 6
[3,] 3 7
[4,] 4 8

Q5] Find xy and $2x+3y$ where

$$x = \begin{bmatrix} 4 & -2 & 6 \\ 7 & 0 & 7 \\ 9 & -5 & 3 \end{bmatrix}, y = \begin{bmatrix} 10 & -5 & 7 \\ 12 & -4 & 9 \\ 15 & -6 & 5 \end{bmatrix}$$

> x = matrix(nrow = 3, ncol = 3, data = c(4, 7, 9, -2, 0, -5, 6, 7, 3))

> x
[1] [2] [3]
[1,] 4 -2 6
[2,] 7 0 7
[3,] 9 -5 3

> y = matrix(nrow = 3, ncol = 3, data = c(10, 12, 15, -5, -4, -6, 7, 9, 5))

> y
[1] [2] [3]
[1,] 10 -5 7
[2,] 12 -4 9
[3,] 15 -6 5

```

> 2^x + 3^y
 [,1] [,2] [,3]
      38   -19    33
 [,1]      50   -12    41
 [,2]      63   -28    21

```

> x + y

```

[,1] [,2] [,3]
 [,1] 14   -7    13
 [,2] 19   -4    15
 [,3] 24   -11   8

```

Q6] Marks of statistics of Computer Science student
 59, 20, 35, 24, 46, 56, 55, 45, 27, 22, 27, 58, 54, 40,
 50, 32, 36, 29, 35, 39

```

> x = c(59, 20, 35, 24, 46, 56, 55, 45, 27, 22, 27, 58, 54,
  40, 50, 32, 36, 29, 35, 39)

```

```

> breaks = seq(20, 60, 5)

```

```

> a = cut(x, breaks, right=FALSE)
> b = table(a)
> c = transform(b)

```

\propto

	a	Freq					
1	(20, 25)	3					
2	(25, 30)	2					
3	(30, 35)	1					
4	(35, 40)	4					
5	(40, 45)	1					
6	(45, 50)	3					
7	(50, 55)	2					
8	(55, 60)	4					

RM

freq of intervals + 1
 $(40, 45, 50, 55, 60, 65)$

$(40+1), (45+1), (50+1), (55+1)$

02 03 02 02 01 5 10
10 21 0 26 0 5 0 10 (avg
 $(10, 21, 0, 26, 0, 5, 0, 10)$)

PRACTICAL - 2

Aim: Probability Distribution.

Check whether the following are pmf or not.

x	p(x)
0	0.1
1	0.2
2	-0.5
3	0.4
4	0.3
5	0.5

⇒ Since, $p(2) = -0.5$, cannot be pmf because $\nexists p(x) \geq 0 \forall x$.

x	1	2	3	4	5
p(x)	0.2	0.2	0.3	0.2	0.2

⇒ $\sum p(x) = 0.2 + 0.2 + 0.3 + 0.2 + 0.2 = 1$ It cannot be pmf. as in pmf., $\sum p(x) = 1$

x	10	20	30	40	50
p(x)	0.2	0.2	0.35	0.15	0.1
Sum (prob)					
[1]	1				

It is a pmf as $\sum p(x) = 1$ & $p(x) \geq 0 \forall x$

Q2] i) Find c.d.f for the following p.m.f and sketch the graph.

x	10	20	30	40	50
$p(x)$	0.2	0.2	0.35	0.15	0.1

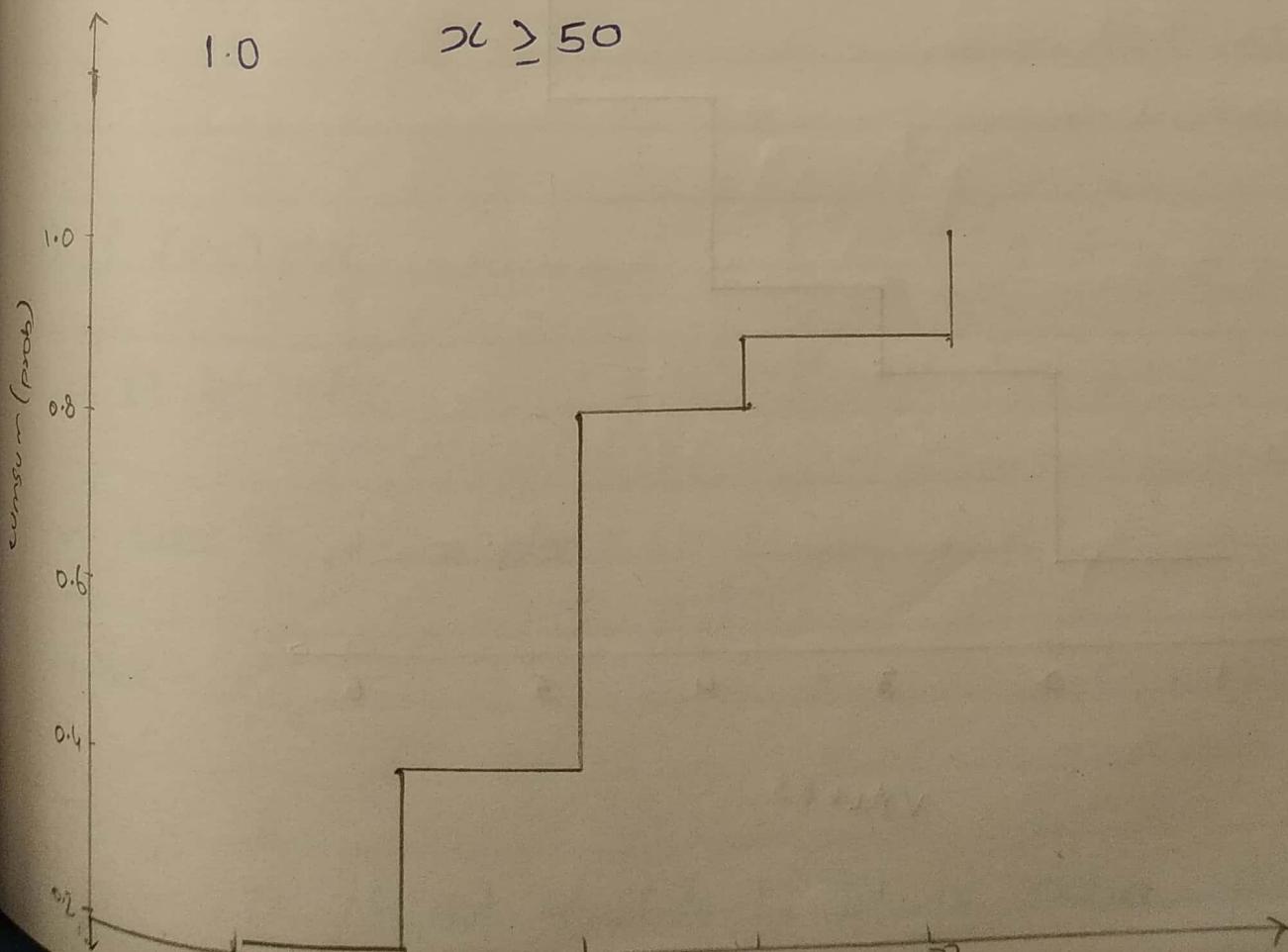
$$\text{prob} = (0.2, 0.2, 0.35, 0.15, 0.1)$$

$$\text{sum(prob)}$$

$$\text{cumsum(prob)}$$

$$[1] 0.20 \quad 0.40 \quad 0.75 \quad 0.90$$

$$\begin{aligned} f(x) &= 0 & x < 10 \\ &0.2 & 10 \leq x < 20 \\ &0.4 & 20 \leq x < 30 \\ &0.75 & 30 \leq x < 40 \\ &0.90 & 40 \leq x < 50 \end{aligned}$$



Q2]	x	1	2	3	4	5	6
ii]	p(x)	0.15	0.25	0.1	0.20	0.2	0.1

> prob = c(0.15, 0.25, 0.1, 0.2, 0.2, 0.1)

> sum(prob)

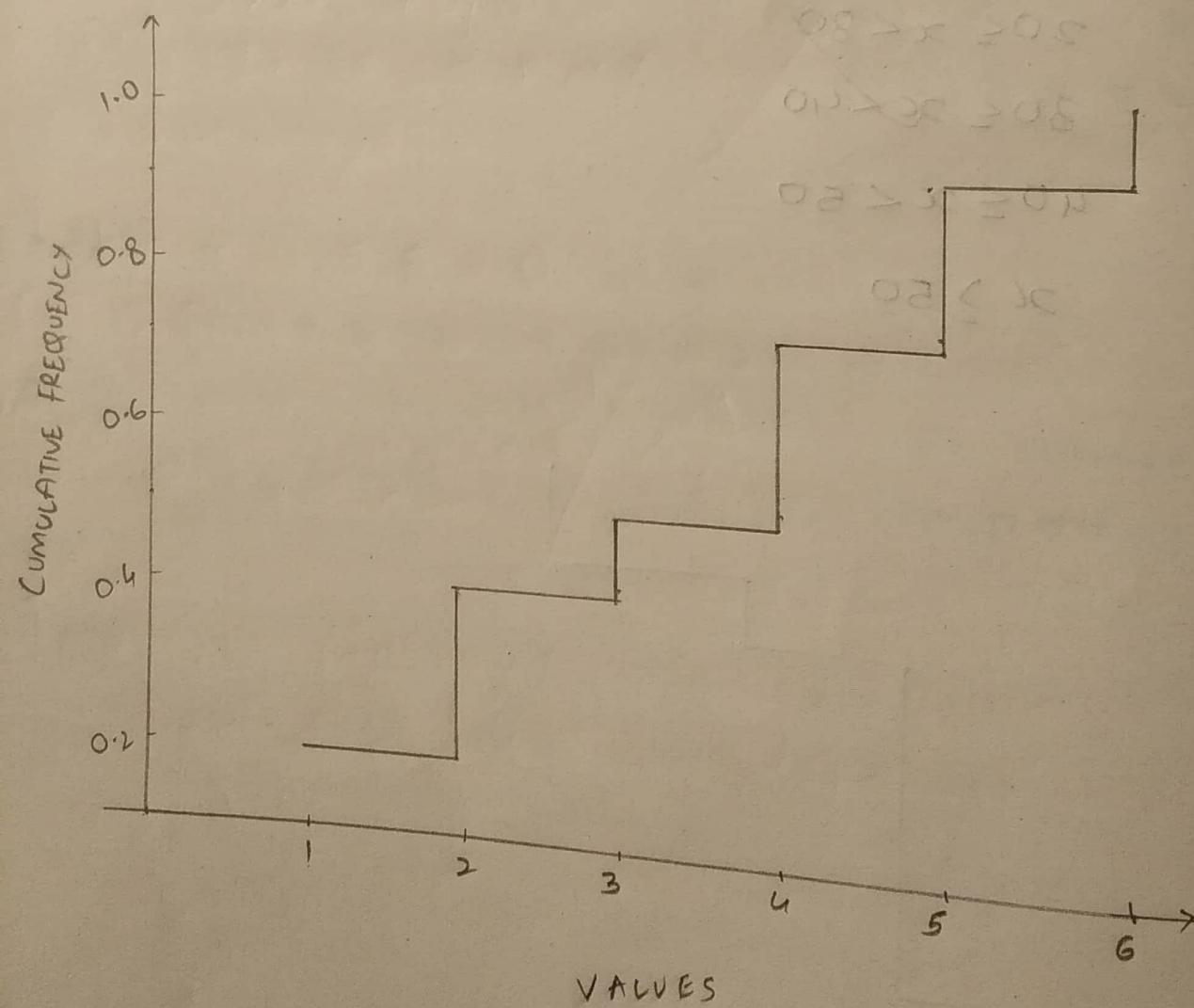
> cumsum(prob)

[1] 0.15 0.40 0.50 0.70 0.90 1.0

> x = c(1, 2, 3, 4, 5, 6)

> plot(x, cumsum(prob), "s", xlab = "VALUES", ylab = "cumulative FREQ", main = "C.D.F")

C.D.F.



$F(x) = 0$	$x < 1$
0.15	$1 \leq x < 2$
0.40	$2 \leq x < 3$
0.50	$3 \leq x < 4$
0.70	$4 \leq x < 5$
0.90	$5 \leq x < 6$
1.00	$x \geq 6$

(b) check whether the following is p.d.f. or not.

i) $f(x) = 3 - 2x$; $0 \leq x \leq 1$

ii) $f(x) = 3x^2$; $0 < x < 1$

Sol:-

i) $\int_0^1 f(x) dx$

$$= \int_0^1 (3 - 2x) dx$$

$$= \int_0^1 3 dx - \int_0^1 2x dx$$

$$= [3x - x^2]_0^1$$

$$= 2$$

\therefore It is not equal to 1, It is not a p.d.f.

$$\text{ii) } \int_0^1 f(x) * dx$$

$$= \int_0^1 3x^2 dx$$

$$= \left[\frac{3x^3}{3} \right]_0^1$$

$$= [x^3]_0^1$$

$$= 1$$

Since, integration is equal to 1,
It is a p.d.f.

Ans
Ans

Sol:-

1) > dbinom(10, 100, 0.1)
[1] 0.1318653

2] i) exactly 4 correct answers

> dbinom(4, 12, 0.2)
[1] 0.1328756

ii) Atmost 4 correct answers

> pbinom(4, 12, 0.2)
[1] 0.9274445

iii) More than 5 correct answers

> 1-pbinom(5, 12, 0.2)
[1] 0.01940528

3] dbinom(0:5, 5, 0.1)

[1] 0.59049 0.32805 0.07290 0.00810 0.0004

4]

i) $P(x=5) = > \text{dbinom}(45, 12, 0.25)$ [1] 0.1032416

ii) $P(x \leq 5) = > \text{pbinom}(5, 12, 0.25)$ [1] 0.9455978

iii) $P(x > 7) = > 1 - \text{pbinom}(7, 12, 0.25)$ [1] 0.00278151

iv) $P(5 < x < 7) = > \text{dbinom}(6, 12, 0.25)$ [1] 0.04014945



PRACTICAL - 3

TOPIC: BINOMIAL DISTRIBUTION

COMMAND:

- $P(x=x) = \text{dbinom}(x, n, p)$
- $P(x \leq x) = \text{pbinom}(x, n, p)$ (at least)
- $P(x > x) = 1 - \text{pbinom}(x, n, p)$ (at most)
- If x is unknown and $P_1 = P(x \leq x)$
 $\rightarrow \text{qbinom}(P_1, n, p)$

- Q1] Find the probability of exactly 10 success in 100 trials, with $P=0.1$.
- Q2] Suppose there ~~are~~ are 12 MCQ. Each question has 5 options out of which one is correct find the probability of having,
- exactly 4 correct answer.
 - Atmost 4 correct answer.
 - More than 5 correct answer.
- Q3] Find the complete distribution when $n=5, p=0.1$.
- Q4] ~~$n=12, p=0.25$~~ Find the following probability,
- $P(x=5)$
 - $P(x \leq 5)$
 - $P(x > 7)$
 - $P(5 < x < 7)$

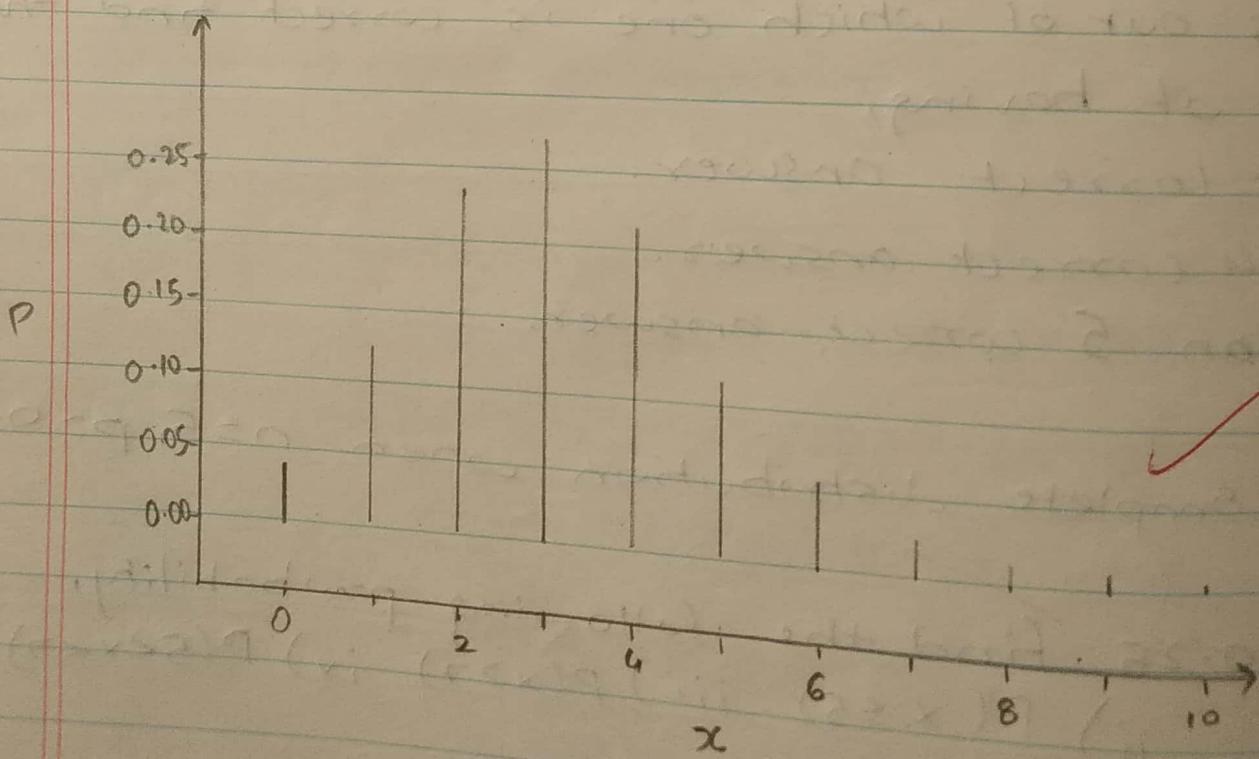
Q5] Probability of a salesman making a sale to a customer 0.15. Find the probability of

i) no sale out of 10 customer.

ii) more than 3 sale out of 20 customer.

Q6] A salesman has a 20% probability of making a sale out of 30 customers. What min. no. of sales he can make with 88% probability.

Q7] X follows binomial distribution with $n=10$, $p=0.3$, plot the graph of p.m.f and c.d.f.



5] > dbinom(0, 10, 0.15)

[1] 0.1968744

ii] > 1 - pbinom(3, 20, 0.15)

[1] 0.3522748

q6] > qbinom(0.88, 30, 0.2)

[1] 9.

q7]

> n = 10

> p = 0.3

> x = 0:n

> prob = dbinom(x, n, p)

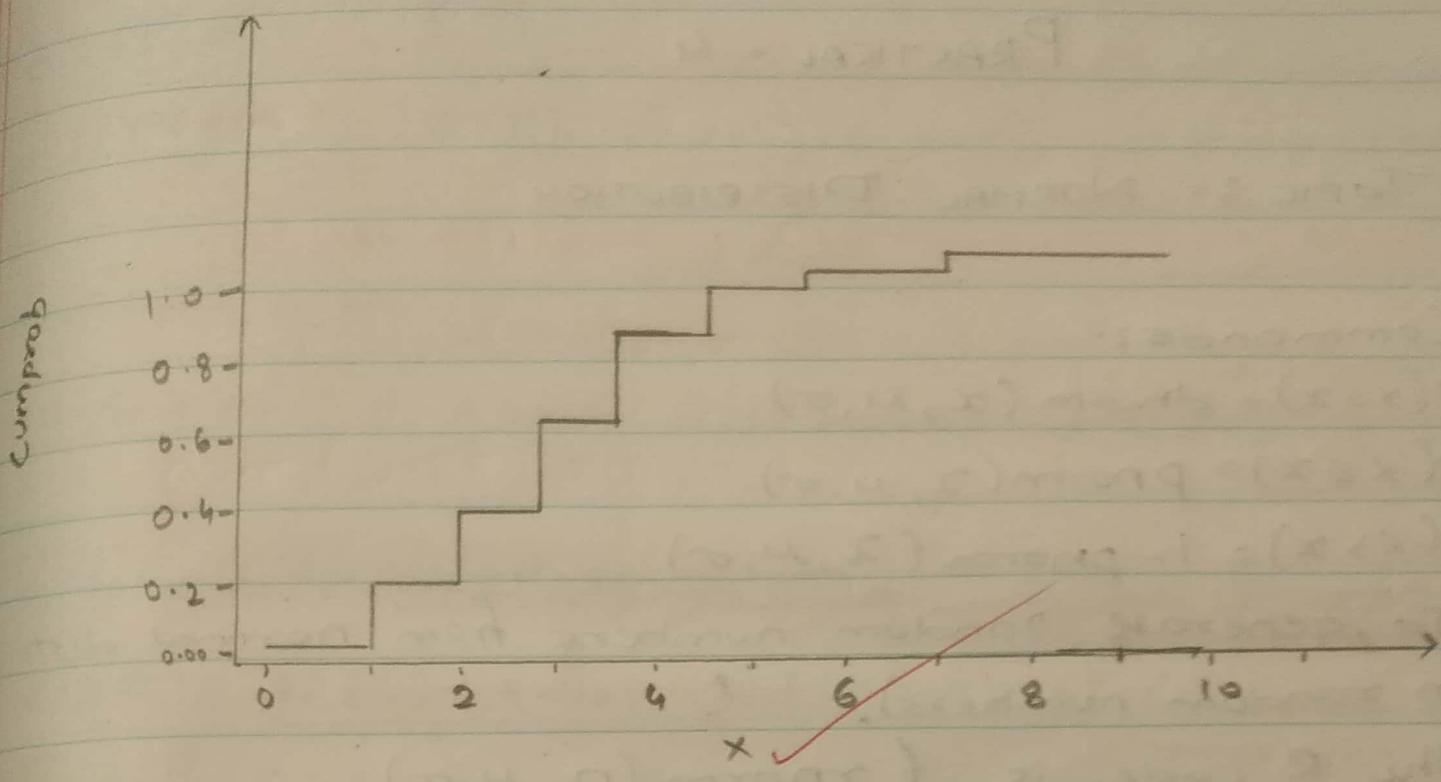
> wmprob = pbinom(x, n, p)

> d = data.frame("x values" = x, "Probability" = prob)

> print(d)

X values	Probability
0	0.02824
1	0.121060
2	0.23334
3	0.26682
4	0.20012
5	0.10291
6	0.03675
7	0.009001
8	0.0014467
9	0.0001377
10	0.00000

plot(x, prob, "h")
plot(x, cumprob, "s")



An
(9-1219)

PRACTICAL - 4

TOPIC :- NORMAL DISTRIBUTION

Commands :-

$$i) P(x=x) = dnorm(x, \mu, \sigma)$$

$$ii) P(x \leq x) = pnorm(x, \mu, \sigma)$$

$$iii) P(x > x) = 1 - pnorm(x, \mu, \sigma)$$

iv) To generate random numbers from normal distribution
(n random numbers),

the R code is, `{ rnorm(n, \mu, \sigma)}`

- Q1] A random variable x follows normal distribution with mean $\mu = 12$ and standard deviation $\sigma = 3$. Find, 1) $P(x \leq 15)$ 2) $P(10 \leq x \leq 13)$ 3) $P(x > 14)$
4) Generate 5 observations (random numbers).

 \Rightarrow

$$1) \mu = 12, \sigma = 3$$

$$> p1 = pnorm(15, 12, 3)$$

$$> cat("P(x \leq 15) = ", p1)$$

$$[1] 0.8413447$$

2)

$$> p2 = pnorm(13, 12, 3) - pnorm(10, 12, 3)$$

$$> p2$$

$$[1] 0.3780661$$

$$> cat("P(10 \leq x \leq 13) = ", p2)$$

3) $p_3 = 1 - \text{pnorm}(14, 12, 3)$

[1] 0.2524925

4) cat("P(x>14) = ", p3)

5) rnorm(5, 12, 3)

[1] 10.512180 11.944169 15.115499 10.366201 8.408162

Q2] x follows normal distribution with $\mu=10, \sigma=2$, find

1) $P(x \leq 7)$ 2) $P(5 < x < 12)$ 3) $P(x > 12)$ 4) Generate 10

5) Find K such that $P(x < K) = 0.4$ observations

→ 1) $P(x \leq 7)$

> p1 = pnorm(7, 10, 2)

> p1

[1] 0.0668072

2) $P(5 < x < 12)$

> p2 = pnorm(12, 10, 2) - pnorm(5, 10, 2)

[1] 0.8351351

3) $P(x > 12)$

> p3 = 1 - pnorm(12, 10, 2)

[1] 0.1586553

4] Generate 10 observations

> rnorm(10, 10, 2)

[1] 7.324489 8.308746 8.394823 11.790873 9.487554
8.835328 10.756449 13.338475 10.366571 12.905423

5] qnorm(0.4, 10, 2)

[1] 9.493306

Q3] Generate 5 random no's from normal distribution
and mean = $\mu = 15$, $S.D = 4$. Find sample mean, med,
S.D and print it.

Q4] X follows $N(30, 100)$

$\mu = 30$, $\sigma = 10$

find 1) $P(X \leq 40)$ 2) $P(X > 35)$ 3) $P(25 < X < 35)$ 4) Find K such
that $P(X < k) = 0.5$

=> 1) $P(X \leq 40)$

> p1 = pnorm(40, 30, 10)

> p1

[1] 0.8413447

2) $P(X > 35)$

> p2 = 1 - pnorm(35, 30, 10)

> p2

[1] 0.3085375

3) $P(25 < x < 35)$

> $p3 = pnorm(35, 30, 10) - pnorm(25, 30, 10)$

> $p3$

[1] 0.3829249

4) $\varnorm(0.6, 30, 10)$

[1] 32.53347

5) Sol^n

$n = 5, M = 15, \sigma = 4$

> $x = rnorm(5, 15, 4)$

[1] 17.1545298 12.799682 12.1468378 15.1948688 9.19771

> x

[1] 15.27357 20.67309 16.30102 15.58444 13.74727

> $am = mean(x)$

> am

[1] 16.31588

> $me = median(x)$

> me

[1] 15.58444

> $n = 5$

> $variance = (n - 1) * var(x) / n$

> $sd = sqrt(variance)$

> sd

[1] 2.332582

```

> cat("sample mean = ", am)
> cat("sample median = ", me)
> cat("sample s.d = ", sd)
> cat("Sample mean = 16.31588")
[1] Sample mean = 16.31588
[1] sample median = 15.58444
[1] sample variance = 2.332583

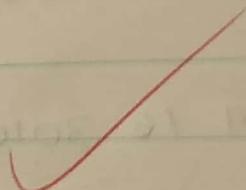
```

Q5] Plot the standard normal graph.

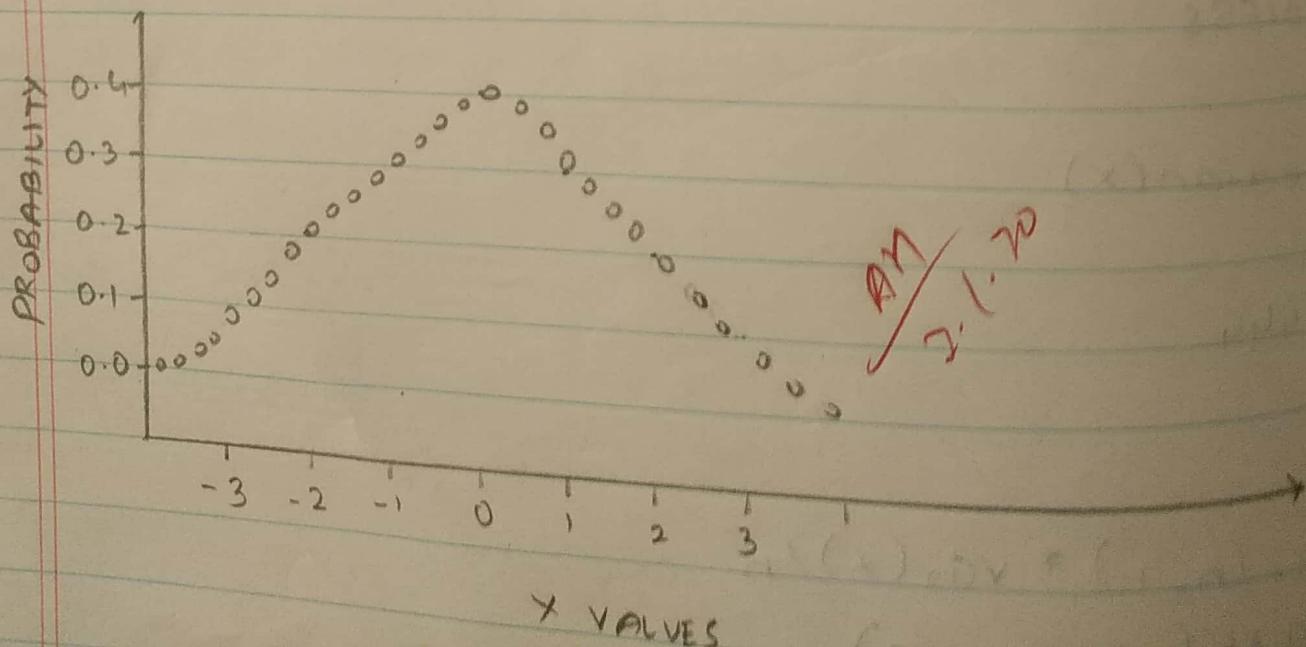
i) $x = seq(-3, 3, by = 0.1)$

$y = dnorm(x)$

plot(x, y, xlab = "x values", ylab = "probability",
 main = "Standard normal graph")



STANDARD NORMAL GRAPH



PRACTICAL - 05

AIM :- Normal and T-test

a) Test the Hypothesis

$$H_0 : \mu = 15$$

$$H_1 : \mu \neq 15$$

Random sample of 400 size is drawn & it is calculated. The sample mean is 14 & standard deviation is 3. Hypothesis at 5% level of significance.

$$\rightarrow m_0 = 15, m_x = 14, s_d = 3, n = 400$$

$$z_{\text{cal}} = (m_x - m_0) / (s_d / \sqrt{n})$$

`zcal = ("calculated value at 2 is =", zcal)`

Calculated value at 2 is - 4.00000

$$pvalue = 2 * (1 - pnorm (abs(zcal)))$$

`pvalue`

$$[1] 2.616796e-11$$

\therefore value of p is less than 0.05,
we reject $H_0 : \mu = 15$.

Q] Test the Hypothesis

$$H_0: \mu = 10$$

$$H_1: \mu \neq 10$$

Random sample of size 400 is drawn with sample mean 10.2 and $s.d = 2.5$. Test the hypothesis at 5% level of significance.

$$\rightarrow > m_0 = 10, mx = 10.2, s.d = 2.5, n = 400$$

$$> zcal = (mx - m_0) / (sd / \sqrt{n})$$

$$> cat("calculated value at 2 is", zcal)$$

calculated value at 2 is = 1.778

>pvalue

$$[1] 0.07544$$

∴ value of P is greater than 0.01

we accept $H_0: \mu = 10$.

Q] Test the Hypothesis of proportion of smokers

in our college is collected & proportion

calculated as 0.125. Test the Hypothesis at

5% level of significance. (sample size is 400)

$$\rightarrow > P = 0.2, p = 0.125, n = 400, Q = 1 - P$$

$$> zcal = (p - P) / (\sqrt{P * Q / n})$$

> zcal

$$[1] -3.75$$

$$> pvalue = 2 * (1 - pnorm(abs(zcal)))$$

>pvalue

$$[1] 0.00017683$$

∴ value of P is less than 0.05 we reject $H_0 = 0.2$

Q] last year farmers lost 20% of their 58 crop. A random sample of 60 field are collected and it is found that 9 field crops are insect polluted. Test the Hypothesis at 1% level of significance.

$$P=0.2, p = 9/60, n = 60, \alpha = 1 - P$$

$$z_{\text{cal}} = (p - P) / (\sqrt{P(1-P)/n})$$

$$\text{pvalue} = ((p - P)) / (\sqrt{P(1-P)/n})$$

pvalue

[1] 0.3329

Ans \rightarrow Since pvalue > 0.01 , we accept $H_0 = 0.2$

Q] Test the hypothesis $H_0: M = 12.5$, from the following sample and 5% level of significance.

x = c(12.25, 11.97, 12.15, 12.08, 12.31, 12.28, 11.94, 11.89, 12.16, 12.04)

n = length(x)

n

[1] 10

m = mean(x)

m

[1] 11.007

variance = (n-1) * var(x) / n

variance

[1] 10.594982

sd = sqrt(variance)

86

```
> mo = 12.5  
> t = (mx - mo) / (sd / sqrt(n))  
> pvalue = 1 - pnorm(abs(t))  
> 0
```

~~AN~~
~~(8.0) > 0.~~

PRACTICAL - 06

Aim: T-test

- Q Let the population mean (the amount spent per customer in a restaurant) is 250 a sample of 100 customers selected the sample mean is calculated as 275 and S.D. 30, test the hypothesis that population mean is 250 or not at 5% level of significance.
- Q In a random sample of 1000 students it is found that 750 use blue pen. Test the hypothesis that the population proportion is 0.8 at 1% level of significance.

Solution :-

$$\bar{x} = 275, \mu_0 = 250, S.D. = 30, n = 100$$

$$\rightarrow H_0: \mu = 275 \text{ against } H_1: \mu \neq 275$$

$$z_{\text{cal}} = (275 - 250) / (30 / \sqrt{100})$$

$$z_{\text{cal}} =$$

$$[1] 8.3333$$

$$p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$$p\text{value}$$

$$[1] 0$$

$$\therefore p\text{value} = 0 < 0.05$$

We reject H_0 at 5% level of significance.

Sol
2]

$H_0: P = 0.8$ against $H_1: P \neq 0.8$

$$> P = 0.8$$

$$> Q = 1 - P$$

$$> p = 750/1000$$

$$> n = 10^00$$

$$> z_{\text{cal}} = (p - P) / \text{sqrt}(P * Q / n)$$

$$> z_{\text{cal}}$$

$$[1] -3.952847$$

$$> pvalue = 2 * (1 - pnorm(\text{abs}(z_{\text{cal}})))$$

$$> pvalue$$

$$[1] 7.72268e-05$$

$$\therefore pvalue < 0.1$$

We reject value of H_0 at

1% level of significance.

(3) Two random sample of size 1000 and 600 are drawn from two populations with the same $S.D = 2.5$. The sample means are 67.5 and 68 respectively. Test the hypothesis $H_0: \mu_1 = \mu_2$ against $H_1: \mu_1 \neq \mu_2$ at 5% level of significance.

(4) A study of noise level in two hospitals is given below: Test the claim that the two hospitals have same level of noise at 1% level of significance.

	Hospital A	Hospital B
size	84	(100)
Mean	61.2	59.4
S.D	7.9	7.5

(5) In a sample of 600 students in our college, 400 use blue ink. In another college from sample of 900 students, 450 use blue ink. Test the hypothesis that the proportion of students using blue ink in two colleges are equal or not at 1% level of significance.

Sol:-

Q3] > n₁ = 1000

> n₂ = 2000

> m_{x1} = 67.5

> m_{x2} = 68

> s_{d1} = 2.5

> s_{d2} = 2.5

$$> z_{cal} = (m_{x1} - m_{x2}) / \sqrt{s_{d1}^2/n_1 + s_{d2}^2/n_2}$$

> z_{cal}

[1] -5.1639

> cat("zcalculated is = ", z_{cal})

(1) zcalculated is = -5.1639

> pvalue = 2 * (1 - pnorm(abs(z_{cal})))

> pvalue

[1] 2.4175e-7

∴ Pvalue < 0.05

we reject H₀ at 5% level of significance.

Q4] > n₁ = 84

> n₂ = 34

> m_{x1} = 61.2

> m_{x2} = 59.4

> s_{d1} = 7.9

> s_{d2} = 7.5

$$> z_{cal} = (m_{x1} - m_{x2}) / \sqrt{s_{d1}^2/n_1 + s_{d2}^2/n_2}$$

> z_{cal}

[1] 1.162

> pvalue = $2 * (1 - \text{pnorm}(\text{abs}(zcol)))$

> pvalue
 [1] 0.245

\therefore pvalue > 0.05

~~We accept H_0 at 1% level of significance.~~

[3] $H_0: P_1 = P_2$ ag $H_1: M_1 \neq M_2$

> n1 = 600

> n2 = 900

> p1 = 400 / 600

> p2 = 450 / 900

> p = $(n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$

> q = 1 - p

> zcol = $(p_1 - p_2) / \text{sqrt}(p * q * (1/n_1 + 1/n_2))$

> zcol

[1] 6.3814

> pvalue = $2 * (1 - \text{pnorm}(\text{abs}(zcol)))$

> pvalue

[1] 1.75322e-10

\therefore pvalue < 0.01

We reject H_0 at 1% level of significance

$H_0: P_1 = P_2$ or $H_0: P_1 + P_2 = 1$

(Q6) For sample size, $n_1 \in 200$

> $n_1 = 200$

> $n_2 = 200$

> $P_1 = 44/200$

> $P_2 = 30/200$

> $p = (n_1 * p_1 + n_2 * p_2) / (P_1 + n_2)$

> $q = 1 - p$

> $z_{\text{cal}} = (p_1 - p_2) / \sqrt{p * q * (1/n_1 + 1/n_2)}$

> z_{cal}

>

[1] 1.8027

> $pvalue = 2 * (1 - pnorm(\text{abs}(z_{\text{cal}})))$

> $pvalue$

[1] 0.07142

$\therefore pvalue > 0.05 \therefore$ It accepts H_0 at 5% level of significance

AM
27-01-20

PRACTICAL - 7

TOPIC: Small Sample Test

The marks of 10 students are given by 63, 63, 66, 67, 68, 69, 70, 70, 71, 72. Test the hypothesis that the sample comes from opposition that the sample with average 66.

$$H_0: \mu = 66$$

$$> x = c(63, 63, 66, 67, 68, 69, 70, 70, 71, 72)$$

$$> t = \text{t.test}(x)$$

One Sample t-test

$$\text{data} = x$$

$$t = 68.319, df = 9, p\text{-value} = 1.558e^{-13}$$

alternative hypothesis: mean is not equal to 0.

95 percent confidence interval:

$$65.65171 \quad 70.14829$$

Sample estimates:

mean of x

$$67.9$$

As $1.558e^{-13} < 0.05$, we reject it.

$$> pvalue = 1.558e^{-13}$$

```
> if (pvalue > 0.05) { cat ("accept H_0") } else { cat  
("reject H_0") }
```

reject H_0

- 2] Two groups of students score the following marks
 Test the hypothesis that there is no significant difference between two groups.
- Group 1 - 18, 22, 21, 21, 17, 20, 17, 23, 20, 22, 21
 Group 2 - 16, 20, 14, 21, 20, 18, 13, 15, 17, 21

$H_0: \mu_1 = \mu_2$ = There is no difference between two groups.

```
> x=c(18,22,21,21,17,20,17,23,20,22,21)
> y=c(16,20,14,21,20,18,13,15,17,21)
> t.test(x,y)
```

Welch Two Sample t-test

data : x and y

$t = 2.2573$, $df = 16.376$, p-value = 0.03798

alternative hypothesis : true difference in means is not equal to 0

95 percent confidence interval :

0.1628205 5.0371795

Sample estimates :

mean of x mean of y
 20.1 17.5

> pvalue = 0.03798

if(pvalue > 0.05) {cat("accept H₀")}
 } else {cat("reject H₀")}

> reject H₀

3) Sales data of 6 shops before and after ^{one}
special campaign are given below.

Before: 53, 28, 31, 48, 50, 42

After: 58, 29, 30, 55, 56, 45

Test the hypothesis that campaign is effective or
not.

H_0 : There is no significant difference of sales
before & after the campaign.

Paired t-test

> $x = c(53, 28, 31, 48, 50, 42)$

> $y = c(58, 29, 30, 55, 56, 45)$

> $t.test(x, y, paired = T, alternative = "greater")$

Paired t-test

data: x and y

$t = -2.7815$, $df = 5$, $p\text{-value} = 0.9806$

alternative hypothesis: true difference in means
is greater than 0.

95 percent confidence interval:

-6.035547 Inf

Sample estimates:

mean of the differences

-3.5

```
> pValue = 0.9806
> if(pValue > 0.05) { cat("accept H0") } else { cat("reject H0") }
accept H0
```

4] Two medicines are applied to 10 patients.

Group 1: 10, 12, 13, 11, 14

Group 2: 8, 9, 12, 14, 15, 10, 9

Is there any significant difference betⁿt - medium.

Ansⁿ: There is no significant difference.

> x = c(10, 12, 13, 11, 14)

> y = c(8, 9, 12, 14, 15, 10, 9)

> t.test(x, y)

welch Two sample t-test

data: x and y

t = 0.80384, df = 9.7594, p-value = 0.4406

alternative hypothesis: true difference in means
is not equal to 0.

95 percent confidence interval:

-1.781171 3.781171

Sample estimates:

mean of x mean of y

12 11

p-value = 0.4808

> p-value = 0.4406

> if (p-value > 0.05) {cat ("accept H₀") } else { "reject H₀" }

accept H₀.

The followings are the weight before and after a diet program. Is the diet program effective?

Before: 120, 125, 115, 130, 123, 119

After : 100, 114, 95, 90, 115, 99

Paired t-test

H_0 : There is not significant difference.

$x = c(120, 115, 125, 130, 123, 119)$

$y = c(100, 114, 95, 90, 115, 99)$

$t.test(x, y, paired = T, alternative = "less")$

Paired t-test

data: x and y

$t = 4.3458$, $df = 5$, $p\text{-value} = 0.9963$

alternative hypothesis: true difference in means
is less than 0.

95 percent confidence interval:

-Inf 29.0295

sample estimates:

mean of differences

19.8333

~~A^b/2.70~~

$pvalue = 0.9963$

$\text{if}(pvalue > 0.05) \{ \text{cat}("accept H_0") \}$ use $\{\text{"reject H}_0"\}$

accept H_0

PRACTICAL - 8

Topic : Large and Small Sample Tests.

Q1]

$$H_0: \mu = 55$$

$$H_1: \mu \neq 55$$

$$> mx = 55$$

$$> mo = 52$$

$$> n = 100$$

$$> sd = 7$$

$$> zcal = (mx - mo) / (sd / \sqrt{n})$$

$$> zcal$$

$$[1] 4.285714$$

$$> pval = 2 * (1 - pnorm(abs(zcal)))$$

$$> pval$$

$$[1] 1.82153e-05 \quad (\text{pval is rejected } < 0.05)$$

Q2]

$$H_0: P = 0.5$$

$$H_1: P \neq 0.5$$

$$> P = 0.5$$

$$> p = 350/700$$

$$> n = 700$$

$$> q = 1 - p$$

$$> zcal = (p - P) / \sqrt{P * (q / n)}$$

$$[1] 0$$

$$> pval = 2 * (1 - pnorm(abs(zcal)))$$

$$> pval$$

$$[1] 1$$

(pval is)

$$H_0: P_1 = P_2$$

$$H_1: P_1 \neq P_2$$

> n1 = 1000

> n2 = 1500

> p1 = 0.02

> p2 = 0.01

$$> p = (n1 * p1 + n2 * p2) / (n1 + n2)$$

$$> q = 1 - p$$

$$> p$$

$$[1] 0.5$$

$$> q$$

$$[1] 0.986$$

$$> zcal = (p1 - p2) / sqrt(p * q * (1/n1 + 1/n2))$$

$$> zcal$$

$$[1] 2.084842$$

$$> pval = 2 * (1 - pnorm(abs(zcal)))$$

$$> pval$$

$$[1] 0.03708364 \quad \text{('pval' is rejected < 0.05)}$$

$$H_0: M = 100 \quad \text{against} \quad H_1: M \neq 100$$

$$> mx = 100$$

$$> mo = 99$$

$$> n = 400$$

$$> sd = 8$$

$$> zcal = (mx - mo) / (sd / sqrt(n))$$

$$> zcal$$

$$[1] 2.5$$

$$> pval = 2 * (1 - pnorm(abs(zcal)))$$

$$pval$$

$$[1]$$

Q5] $H_0: \mu = 66$ against $H_1: \mu \neq 66$
 $> x = c(63, 63, 68, 69, 71, 71, 72)$
 $> t.test(x)$
one Sample t-test

data : x

t = 47.94, df = 6, pvalue = 5.2522e-09

alternative hypothesis : true mean is not equal to 0.

95 percent confidence interval :

64.66479 71.62092

sample estimates :

mean of x

68.14286

> pval < 0.01, Hence reject H_0 .

Q6] Q1/10/2023

Q6] $H_0: \sigma_1 = \sigma_2$ against $H_1: \sigma_1 \neq \sigma_2$

> x = c(66, 67, 75, 76, 82, 84, 88, 90, 92)

> y = c(64, 66, 74, 78, 82, 85, 87, 92, 93, 95, 97)

> var.test(x, y)

F test to compare two variances

data : x and y

F = 0.70686, num df = 8, denom df = 10, p-value = 0.6359

alternative hypothesis: true ratio of variances is not equal to 1.

95 percent confidence interval :

0.1833662

3.0360393

sample estimates :

ratio of variances : 0.70686

pval >

Q) $H_0: \mu_1 = 1200$ against $H_1: \mu_1 \neq 1200$

> $n = 100$

> $m_x = 1180$

> $m_0 = 1150$

> $s_d = 125$

> $z_{\text{cal}} = (m_x - m_0) / (s_d / \sqrt{n})$

> $p_{\text{val}} = (1 - \text{pnorm}(\text{abs}(z_{\text{cal}}))) * 2$

> z_{cal}

[1] # 4

> p_{value}

[1] 6.334248×10^{-5}

We reject the p_{value} at $H_0: \mu_1 = 100$

Q) $n_1 = 200$ $H_0: p_1 = p_2$ against $H_1: p_1 \neq p_2$

> $n_2 = 300$

> $p_1 = 44/200$

$$\frac{P_1}{(P_1 + P_2)^{1/2}}$$

> $p_2 = 56/300$

> $p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$

> $\alpha = 1 - p$

> $z_{\text{cal}} = (p_1 - p_2) / \sqrt{p * \alpha * (1 - p) / (n_1 + n_2)}$

> $p_{\text{val}} = (1 - \text{pnorm}(\text{abs}(z_{\text{cal}}))) * 2$

> z_{cal}

[1] 0.9128709

> p_{value}

[1] 0.3613104

We accept the p_{value} at 1% level of significance.

Practical - 9

Topic: Chi square test & ANOVA

- Q] Use the following data to test whether the condition of home & condition of child are independent or not.

child	cond.	cond.
	home	
	clean	dirty
clean	70	50
fairly clean,	80	20
Dirty	35	45

H₀: Condition of Home & child are independent

> x = c(70, 80, 35, 50, 20, 45)

> m = 3

> n = 2

> y = matrix(x, nrow = m, ncol = n)

	[,1]	[,2]
[1,]	70	
[2,]	80	50
[3,]	35	20

		45
--	--	----

> pv = chisq.test(y)

70

> pv
pearson's chi squared test

data : 4

x-squared = 25.646

df = 2

p-value = 2.698e-06

They are dependent.

∴ pvalue is less than 0.05 we reject the hypothesis at 5% level of significance.

(Q2) Test the hypothesis that vaccination & disease are independent or not.

Vaccine	Disease	
Affected	Affected	Not Affected
Affected	70	46
Non Affected	35	37

> pv = chisq.test(y)

> pv

Pearson's chi squared test with continuity

data : 4

x-squared = 2.0275

df = 1

p-value = 0.1545

∴ Pvalue is more than 0.05 we accept the hypothesis at 5% level of Significance.

Q3] Perform a ANOVA for the following data.

Type	Observations
A	50, 52
B	53, 55, 53
C	60, 58, 57, 56
D	52, 54, 54, 55

H_0 : The mean's are equal for A,B,C,D.

```
> x1 = c(50,52)  
> x2 = c(53,55,53)  
> x3 = c(60,58,57,56)  
> x4 = c(52,54,54,55)  
> d = stack(list(b1=x1,b2=x2,b3=x3,b4=x4))  
> names(d)  
[1] "values" "ind"
```

```
> one way.test(values~ind, data=d, var.equal=T)
```

one-way analysis of means

data : values and ind

F = 11.735 ~~and~~ df = 3 , denom df = 9 ,
Pvalue = 0.00183

Pvalue is less than 0.05 we reject the hypothesis

```
> anova = aov(values~ind, data=d)  
> summary(anova)
```

	DF	Sum Sq	Mean Sq	F value	Pr(>F)
ind	3	71.06	23.688	11.73	0.00183
Res	9	18.17	2.019		
Signif. codes:	0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1				

following data gives a life of 4 brands.

Types

Life

A

20, 23, 18, 17, 18, 22, 24

B

19, 15, 10, 20, 16, 17

C

21, 19, 22, 17, 20

D

15, 14, 16, 18, 14, 16

H_0 : The mean's of A, B, C, D, are equal.

$x_1 = c(20, 23, 18, 17, 18, 22, 24)$

$x_2 = c(13)$

$x_3 = c(10)$

$x_4 = c(17)$

$d = \text{stack}(\text{list}(b_1 = x_1, b_2 = x_2, b_3 = x_3, b_4 = x_4))$
names(d)

[1] values "ind"

[2] one way.test (values ~ ind, data=d, var.equal=T)

one-way analysis of means

data : values & ind

f = 6.8445, num df = 3 denom df = 20

p-value = 6.002349

∴ p-value is less than 0.05 we reject the hypothesis.

[3] anova = aov (values ~ ind, data=d)

[4] summary(anova)

	Df	Sumsq	meansq	Fvalue	Pr(>F)
ind	3	91.44	30.44	6.845	6.002349*
Residuals	20	89.06	4.453		

> x = read.csv("C:/users/delmin/Desktop/marksheet.csv")

> x

	Stats	Maths
1	40	60
2	45	48
3	42	67
4	15	20
5	37	25
6	36	27
7	49	57
8	59	58
9	20	25
10	27	27

> am = mean(x\$stats)

> am

[1] 37

> ami = mean(x\$maths)

> ami

[1] 39.4

> ml = median(x\$stats)

> ml

[1] 38.5

> m2 = median(x\$maths)

[1] 37

> n = length(x\$stats)

> n

[1] 10

7 sd = sqrt((n-1) * var(x\$stats)/n)

7 sd

(1) 12.64911

7 n1 = length(x\$maths)

7 n1

(1) 10
7 sd1 = sqrt((n-1) * var(x\$maths)/n)

7 sd1

(1) 15.2

7 cor(x\$stats, x\$maths)

(1) 0.830618.

✓
A-V

Practical - 10

Topic : Non Parametric Test

Following are amounts of sulphuric acid emitted by industries in day. apply sign test. Test hypothesis that the population median is 21.5 at 5% level of significance.

(17, 15, 20, 29, 19, 18, 22, 25, 27, 9, 24, 20, 17, 6, 24, 15, 21, 17, 6, 26, 23, 24, 26)

H_0 : population median is 21.5

$x = c(17, 15, 20, 29, 19, 18, 22, 25, 27, 9, 24, 20, 17, 6, 24, 14, 15, 23, 24, 26)$

$$mc = 21.5$$

$$sp = \text{length}(x[x > mc])$$

$$sn = \text{length}(x[x < mc])$$

$$n = sp + sn$$

n

20

$$pv = \text{pbinom}(sp, n, 0.5)$$

pv

$$0.4119015$$

Since, pvalue is greater, so accepted.

If alternative $mc \neq \underline{H_1: mc <} mc$ as $mc < pv = \text{pbisom}(sn, n, 0)$

Q2] Following is the data of 10 observations apply Sign test to test the hypothesis that the population median is 625 against the alternative it is more than 625.

612, 619, 631, 628; 643, 640, 655, 649, 670, 663

H_0 - Population median 625

> $b = c(612, 619, 631, 628, 643, 640, 655, 649, 670, 655)$

> $me = 625$

> $Sp = \text{length}(b[b > me])$

> $Sn = \text{length}(b[b < me])$

> $n = Sp + Sn$

> $Pv = \text{pbinom}(Sn, n, 0.5)$

> Pv

[1] 0.989

[1] 0.0546875

> n

[1] 10

Since pvalue is greater than 0.05, so we accept

The following are the values of a sample to test the hypothesis that the population median is 60 against the alternative. It is more than 60 at 5% LOS using Wilcoxon Signed Rank Test.

63, 65, 60, 89, 61, 71, 58, 51, 69, 62, 63, 39, 72, 69, 48, 66, 72, 63, 87, 69.

H_0 : population median = 60

H_1 : ... > 60

$x = c(63, 65, 60, 89, 61, 71, 58, 51, 69, 62, 63, 39, 72, 69, 48, 66, 72, 63, 87, 69)$.

wilcox.test(x, alter = "greater", mu = 60)

Wilcoxon signed rank test with continuity correction.

data: w

V = 148.5, P-value = 0.01631

alternative hypothesis : true location is greater than 60.

Since, p-value is less than , since accepted.

When alternative is less : alter = "less"

not equal to : alter = "greater"

WSRT
Q4] Population median is
15, 17, 24, 25, 20, 21, 32, 28, 12, 25, 24, 26.
 H_0 : before and after no change
 H_1 : change

> $x = c(15, 17, 24, 25, 20, 21, 32, 28, 12, 25, 24, 26)$
>wilcox.test(x, alter = "Less", mu = 12)

wilcoxon signed rank test with continuity correction.

data : x

v = 66, pvalue = 0.9986

alternative hypothesis : true location is less than 12.

∴ pvalue is greater, then accepted.

Q5] The weights of students before and after they stop smoking are given below. Using WSRT test that there is no significant change.

Weights Before : 65, 75, 75, 62, 72

Weights After : 72, 74, 72, 66, 73

H_0 : before and after no change
 H_1 : change.

> $x = c(65, 75, 75, 62, 72)$
> $y = c(72, 74, 72, 66, 73)$

> d = x - y > dt [1] -> 1 3 - 4 - 1

, wilcox.test(d, alter = "two.sided", mu=0)

wilcox signed rank test with continuity correction.

data : d

v = 4.5 , Pvalue = 0.4982

alternative hypothesis : true location is not equal to 0.

We accept at 0.05% level of significance.

A.W
8/10/20