

Random variable

Random process → Outcomes → numbers

$$X = \begin{cases} 1 & \rightarrow \text{head} \\ 0 & \rightarrow \text{tail} \end{cases}$$

Random variable

متغير عشوائي
يقبل

Y = Sum of upward face after rolling 7 dice

$$P(Y \leq 30) = P(\text{Sum of } \dots \text{ is } \leq 30)$$

X = number of Cars pass in an hour

Ahmed Pick → 2 no. (0 → 9)

pick one letter من 26

ticket matches 2 numbers and 1 letter → Price 10,405

letter match and one or both don't match → loss

X = net profit from play 04R

احتمال ان لا يسد

$$\frac{1}{26} - \frac{1}{2600}$$

$$E(x) = P(\text{big Price}) * (10405 - 5) + P(\text{small Price}) * (100 - 5)$$

expected Profit

احتمال ان يسبب
الكسارة * فيها

$$1 - P(\text{small}) - P(\text{grand})$$

$$+ P(\text{neither}) * (-5)$$

احتمال خسارة
من كل حصة

10 trout

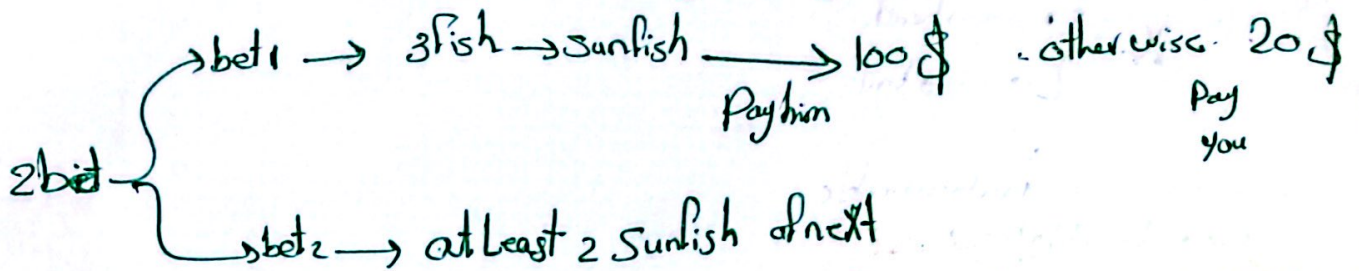
10 sunfish

مع

ال

باخه برجه

مع ال حلال



3 fish → 50\$

otherwise 25\$

11 what is the Expected value of bet 1?

X = (what you profit from bet 1)

$$E(X) = P(3 \text{ sunfish}) \cdot (-100) + (1 - P(3 \text{ sunfish})) \cdot (20)$$

$$P(3 \text{ sunfish}) = \frac{10}{20} = \frac{1}{2}$$

of getting one sunfish

$$P(3 \text{ sunfish}) = \frac{1}{2} * \frac{1}{2} * \frac{1}{2}$$

2 what is the Expected value of bet 2?

Y = what you profit of bet 2

$$E(Y) = P(\text{at least 2 sunfish of 3}) \cdot (50) +$$

$$(1 - P(\text{---})) \cdot (-25) = 12.5$$

$$\frac{4}{8}$$

ttt
tts
tss
sts
stt
stt

✓ sss
✓ sst

✓ sts

✓ tss

x sst

x tst

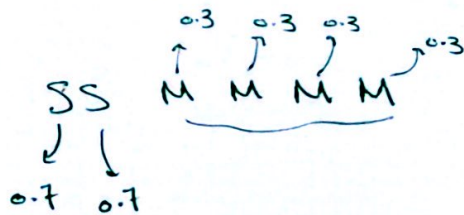
x tss

x ttt

Prob (score) = 0.7

Prob (miss) = 0.3

$P(\text{Exactly 2 Scores in 6 attempts}) = (0.7)^2 \cdot (0.3)^4 = 15$



$0.3 \cdot 0.7 \cdot 0.3 \cdot 0.7 \cdot 0.3 \cdot 0.3 = 15$

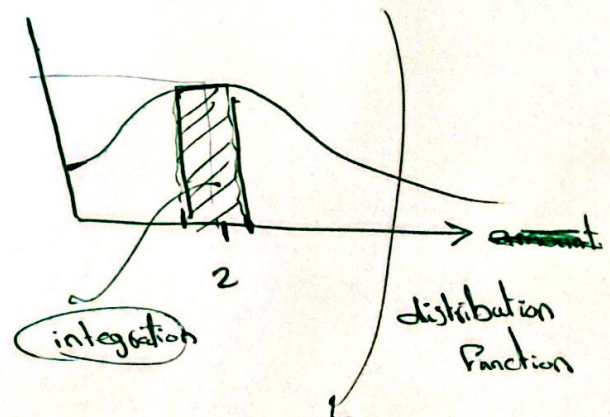
${}^6C_2 = \frac{6!}{2!(6-2)!}$

$= 15$

2 types of random variable

- discrete**
- distinct - separate values
 - finite
 - Can not infinite
 - they do tend to be integers but not have to be integers

- Continuous**
- any value in interval
 - infinite
 - amount ✓

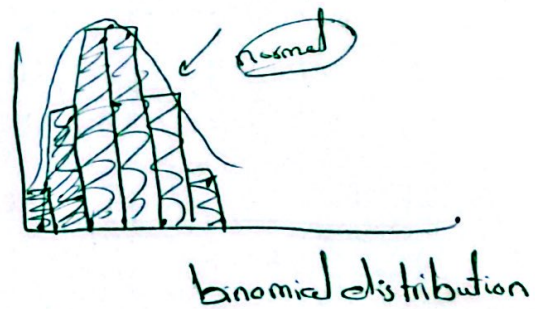


طريق ازالنا هقول اني
عايزة مثلاً exactly حجة
معيّنة

$P(1.9 < Y < 2.1) \equiv P(\underbrace{|Y - 2| < 0.1}_{\text{almost 2}})$

Visualization of binomial distribution

بر
 الاحتمالات
 على
 Histogram
 → discrete ✓



term Life insurance and death prob ✓

X = number of success with probability p after n trials

$$E(X) = n \cdot p$$

X = number of baskets I make after 10 shots

$$p = 48\%$$

$$E(x) = n \cdot p =$$

$$P(X=K) = \binom{n}{K} p^K (1-p)^{n-K}$$

Law of large numbers

$X, E(X)$

mean of n observations of our random variable

$$\bar{X}_n = \frac{X_1 + X_2 + X_3 + \dots}{n}$$

Sample mean

$$\bar{X}_n \rightarrow E(X)$$

$$\bar{X}_n \rightarrow \mu$$

$$n \rightarrow \infty$$

large sample