

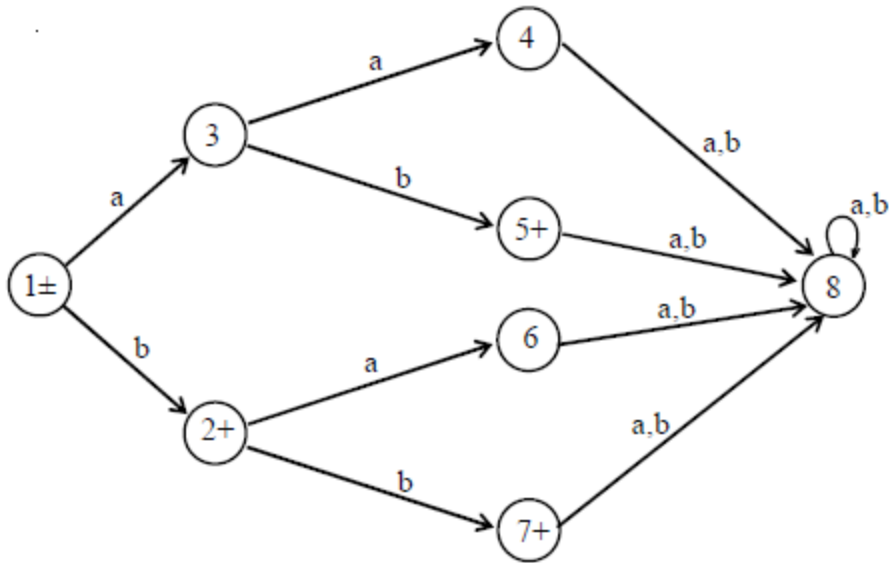
# THEORY OF AUTOMATA & FORMAL LANGUAGES

## HANDOUTS 07

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# **FA tree structure & FA structure proposed by J.Martin**

It is to be noted that to build an FA accepting the language having less number of strings, the tree structure may also help in this regard, which can be observed in the following transition diagram for the Language L, discussed in the above example



Example

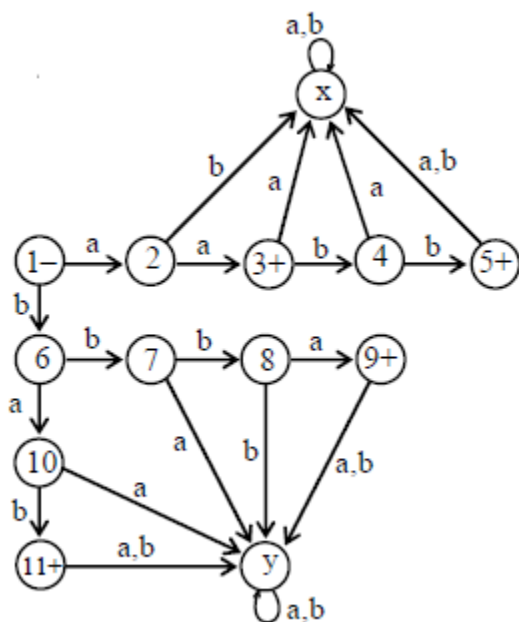
Consider the language

$L = \{aa, bab, aabb, bbba\}$ , defined over  $\Sigma = \{a, b\}$ , expressed by  $aa + bab + aabb + bbba$

OR

$aa (\Lambda + bb) + b (ab + bba)$

The above language may be accepted by the FA as shown below

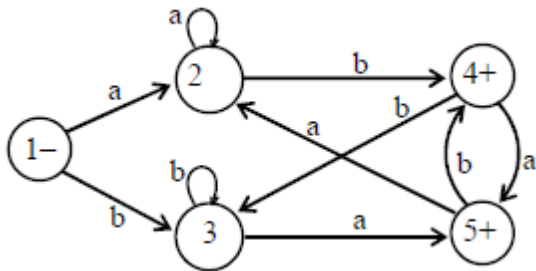


### Example

Consider the language  $L = \{w \text{ belongs to } \{a,b\}^*: \text{length}(w) \geq 2 \text{ and } w \text{ neither ends in } \mathbf{aa} \text{ nor } \mathbf{bb}\}$ .

The language  $L$  may be expressed by the regular expression  $(a+b)^*(ab+ba)$

This language may be accepted by the following FA



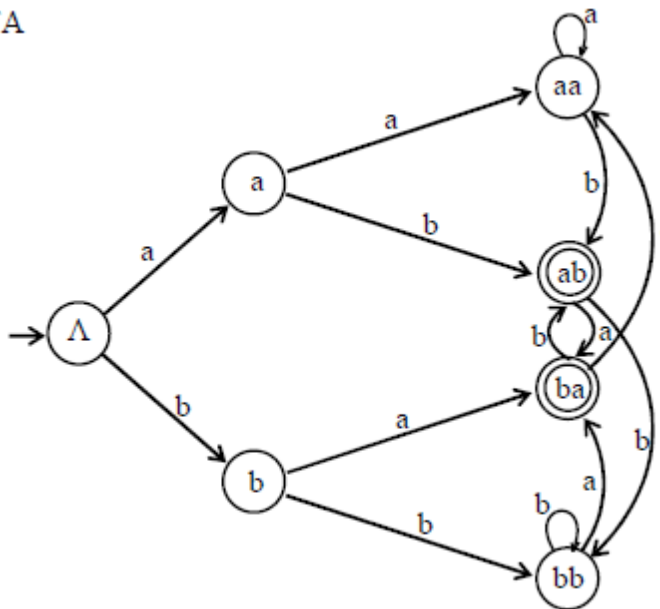
### Note

It is to be noted that building an FA corresponding to the language  $L$ , discussed in the above example, seems to be quite difficult, but the same can be done using tree structure along with the technique discussed in the book

*Introduction to Languages and Theory of Computation*, by J. C. Martin

so that the strings ending in  $aa$ ,  $ab$ ,  $ba$  and  $bb$  should end in the states labeled as  $aa$ ,  $ab$ ,  $ba$  and  $bb$ , respectively; as shown in the following

### FA



### Example

Consider the language FA corresponding to  $r_1 + r_2$  can be determined as

$L = \{w \text{ belongs to } \{a,b\}^*: w \text{ does not end in } \mathbf{aa}\}$ .

The language L may be expressed by the regular expression  $\Lambda + a + b + (a+b)^*(ab+ba+bb)$ . This language may be accepted by the following FA

