

# THEORY OF AUTOMATA & FORMAL LANGUAGES

## HANDOUTS 03

📍 Department of Information Technology  
Hazara University, Mansehra

## **Recursive definition of languages**

The following three steps are used in recursive definition

1. Some basic words are specified in the language.
2. Rules for constructing more words are defined in the language.
3. No strings except those constructed in above, are allowed to be in the language.

### **Examples**

#### **Defining language of INTEGER**

Step 1: 1 is in **INTEGER**.

Step 2: If  $x$  is in **INTEGER** then  $x+1$  and  $x-1$  are also in **INTEGER**.

Step 3: No strings except those constructed in above, are allowed to be in **INTEGER**.

#### **Defining language of EVEN**

Step 1: 2 is in **EVEN**.

Step 2: If  $x$  is in **EVEN** then  $x+2$  and  $x-2$  are also in **EVEN**.

Step 3: No strings except those constructed in above, are allowed to be in **EVEN**.

#### **Defining the language factorial**

Step 1: As  $0!=1$ , so 1 is in **factorial**.

Step 2:  $n!=n*(n-1)!$  is in **factorial**.

Step 3: No strings except those constructed in above, are allowed to be in **factorial**.

#### **Defining the language PALINDROME, defined over $\Sigma = \{a,b\}$**

Step 1:  $a$  and  $b$  are in **PALINDROME**

Step 2: if  $x$  is palindrome, then  $s(x)\text{Rev}(s)$  and  $xx$  will also be palindrome, where  $s$  belongs to  $\Sigma^*$

Step 3: No strings except those constructed in above, are allowed to be in palindrome

#### **Defining the language $\{a^n b^n\}$ , $n=1,2,3,\dots$ , of strings defined over $\Sigma=\{a,b\}$**

Step 1:  $ab$  is in  $\{a^n b^n\}$

Step 2: if  $x$  is in  $\{a^n b^n\}$ , then  $axb$  is in  $\{a^n b^n\}$

Step 3: No strings except those constructed in above, are allowed to be in  $\{a^n b^n\}$

**Defining the language L, of strings ending in a , defined over  $\Sigma=\{a,b\}$**

Step 1: a is in L

Step 2: if x is in L then s(x) is also in L, where s belongs to  $\Sigma^*$

Step 3: No strings except those constructed in above, are allowed to be in L

**Defining the language L, of strings beginning and ending in same letters , defined over  $\Sigma=\{a, b\}$**

Step 1: a and b are in L

Step 2: (a)s(a) and (b)s(b) are also in L, where s belongs to  $\Sigma^*$

Step 3: No strings except those constructed in above, are allowed to be in L

**Defining the language L, of strings containing aa or bb , defined over  $\Sigma=\{a, b\}$**

Step 1: aa and bb are in L

Step 2: s(aa)s and s(bb)s are also in L, where s belongs to  $\Sigma^*$

Step 3: No strings except those constructed in above, are allowed to be in L

**Defining the language L, of strings containing exactly one a, defined over  $\Sigma=\{a, b\}$**

Step 1: a is in L

Step 2: s(a)s is also in L, where s belongs to  $b^*$

Step 3: No strings except those constructed in above, are allowed to be in L