

Last NAME: EMDAD

First Name: MDSHAHID

## Computer Science C.Sc. 342

### Quiz No.1

Time of performance 5:00-6:15 PM on February 23, 2022 Please

write your Last Name on every page:

**NO CORRECTIONS ARE ALLOWED IN ANSWER CELLS!!!!**

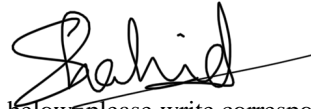
You may use the back page for computations.

Please answer all questions. **Not all questions are of equal difficulty. Please review the entire quiz first and then budget your time carefully.**

**Please HAND WRITE and sign statements affirming that you will not cheat:**

*"I will neither give nor receive unauthorized assistance on this exam. I will use only one computing device to perform this test"*

**Please HAND WRITE and sign here:**



1. [10 points] For **each 8 BIT** binary pattern in the table below please write corresponding values of the following interpretations: **UNSIGNED INT, SIGNED INT, UNSIGNED Fixed Point, SIGNED Fixed Point.**

Each correctly answered column is **2.5** points. **FIXED POINT IS LOCATED TWO POSITIONS FROM THE RIGHT!**

**MOST SIGNIFICANT BIT IS 7. LEAST SIGNIFICANT BIT IS 0.**

76543210	UNSIGNED INT	SIGNED INT	UNSIGNED Fixed Point	SIGNED Fixed Point
10000000	$10000000 - [1 \times 2^7 + 0 \times 2^6 + 0 \times 2^5 + 0 \times 2^4 + 0 \times 2^3 + 0 \times 2^2 + 0 \times 2^1 + 0 \times 2^0 = 128]$ 128	$10000000 = 01111111 + 1 = 10000000$ 10000000	$100000 = 1 \times 2^5 + 0 \times 2^4 + 0 \times 2^3 + 0 \times 2^2 + 0 \times 2^1 + 0 \times 2^0 = 32$ 32	$-2^5 = -32$ -32
10000011	$10000011 = 128 + 2 + 1 = 131$ 131	-128 + 3 = -125	$32 + 1/2 + 1/4 = 32 + 3/4 = 131/4$	$-32 + 1/2 + 1/4 = -125/4$
10000001	$10000001 = 128 + 1 = 129$	-128 + 1 = -127	$32 + 1/4 = 129/4$	$32 + 1/4 = -127/4$
01000001	$01000001 = [0 \times 2^7 + 1 \times 2^6 + 0 \times 2^5 + 0 \times 2^4 + 0 \times 2^3 + 0 \times 2^2 + 0 \times 2^1 + 1 \times 2^0 = 65]$ 65	+65	$010000 = 0 \times 2^5 + 1 \times 2^4 + 0 \times 2^3 + 0 \times 2^2 + 0 \times 2^1 + 0 \times 2^0 = 16$ 16 + 1/4 = 65/4	$16 + 1/4 = +65/4$
01111111	$01111111 - [0 \times 2^7 + 1 \times 2^6 + 1 \times 2^5 + 1 \times 2^4 + 1 \times 2^3 + 1 \times 2^2 + 1 \times 2^1 + 1 \times 2^0 = 127]$	+127	$31 + 1/2 + 1/4 = 127/4$	$31 + 1/2 + 1/4 = +127/4$
11111111	$11111111 - [1 \times 2^7 + 1 \times 2^6 + 1 \times 2^5 + 1 \times 2^4 + 1 \times 2^3 + 1 \times 2^2 + 1 \times 2^1 + 1 \times 2^0 = 255]$	$11111111 - 00000000 + 1 = 00000001$	$111111 = 1 \times 2^5 + 1 \times 2^4 + 1 \times 2^3 + 1 \times 2^2 + 1 \times 2^1 + 1 \times 2^0 = 63$ 63 + 1/2 + 1/4 = 255/4	$-1 + 1/2 + 1/4 = -1/4$

11111100	$11111100 - [1 \times 2^7 + 1 \times 2^6 + 1 \times 2^5 + 1 \times 2^4 + 1 \times 2^3 + 1 \times 2^2 + 0 \times 2^1 + 0 \times 2^0 = 252]$	$11111100 - 00000011 + 1 = 00000100$	$111111 = 1 \times 2^5 + 1 \times 2^4 + 1 \times 2^3 + 1 \times 2^2 + 1 \times 2^1 + 1 \times 2^0 = 63$	$111111 000000 + 1 000001 - 1$
00000000	0	0	0	0
01111110	$01111110 - [0 \times 2^7 + 1 \times 2^6 + 1 \times 2^5 + 1 \times 2^4 + 1 \times 2^3 + 1 \times 2^2 + 1 \times 2^1 + 0 \times 2^0 = 126]$	+126	$31 + \frac{1}{2} = 63/2$	$31 + \frac{1}{2} = +63/2$
10001110	$10001110 - [1 \times 2^7 + 0 \times 2^6 + 0 \times 2^5 + 0 \times 2^4 + 1 \times 2^3 + 1 \times 2^2 + 1 \times 2^1 + 0 \times 2^0 = 142]$	$10001110 - 01110001 + 1 = 01110010$	$100011 = 1 \times 2^5 + 0 \times 2^4 + 0 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 1 \times 2^0 = 35$ $35 + 1/2 = 71/2$	57/2
00010011	19	+19	$\frac{3}{4+4} = \frac{1}{1}$	$\frac{3}{4+4} + \frac{19}{4} = \frac{1}{4}$

Fixed Point

2. [10 points] What is the most negative number (largest absolute value negative) that can be represented using 16 bit signed integer representation? Please CIRCLE AROUND over all the correct ones:

**-32768**, -65536, -16384, -32767, NONE

$$-2^{n-1} = -2^{16-1} = -2^{15} = \mathbf{-32768}$$

3. [ 10 points] Please subtract two number in Hex. Then convert each operand to binary and perform the same operation in binary, then repeat BASE 10. The signed integers are represented using two's complement.

Answer:

$$0x0E = 00001110 = 14$$

$$0xFF = 1111 1111 = 0000 0000 + 1 = 0000 0001 = -1$$

HEX	Binary	Decimal
0x0E	0000 1110	14
-	-	-
0xFF	1111 1111	-1

**Result: 0xF**

**0000 111b**

**dec: 15**

4. [20 points]

Determine the **MINIMAL** number of **bits** required to represent **-127.75** using:

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56 bits

of bits in the cell)

10 bits

in the cell) And the corresponding binary Fixed Point representation here.

0	0	0	0	0	0	0	0	0	1	1	1	1	1	1	1	1
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

## Fixed Point position.

And the corresponding binary Fixed Point representation here. Please use arrow to indicate fixed point position.

[illegible]

4. **4(5 points)** Please write down the signed rational number stored in the 9-bit word below:

1	0	0	0	0	0	0	0	1
---	---	---	---	---	---	---	---	---

$$-1 + (1/2)^8 = 255/256$$
[illegible]

Hence, it is a valid number

representation given below: The top row shows the bit index. **PLEASE SHOW your** work! Just the final result will not count as correct answer. ***If it represents NAN, or Infinity, or zero please state this and justify.***

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3 1	3 0	2 9	2 8	2 7	2 6	3 5	2 4	2 3	2 2	2 1	2 0	1 9	1 8	1 7	1 6	1 5	1 4	1 3	1 2	1 1	1 0	9	8	7	6	5	4	3	2	1
1	1	0	0	0	0	1	0	1	1	1	1	1	1	1	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0

Explanation:

$$10000101 = 131 = 131 - 127 = 6$$

$$(-1)^1 \cdot 2^6 \cdot (1 + .111111110000000000000000) = 127.75 = -127.75$$

Hence, it is a valid number

7. [ 5 points] Please determine the decimal value (scientific notation) of the single precision floating point representation given below: The top row shows the bit index. **PLEASE SHOW your** work! Just the final result will not count as correct answer. **If it represents NAN, or Infinity, or zero please state this and justify.**

3 1	3 0	2 9	2 8	2 7	2 6	3 5	2 4	2 3	2 2	2 1	2 0	1 9	1 8	1 7	1 6	1 5	1 4	1 3	1 2	1 1	1 0	9	8	7	6	5	4	3	2	1
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0

**Explanation:**

If we look closely, we can see all the bits are turned off and it is reversed number. So, the answer is 0.

8. [ 5 points] Please determine the decimal value (scientific notation) of the single precision floating point representation given below: The top row shows the bit index. **PLEASE SHOW your** work! Just the final result will not count as correct answer. **If it represents NAN, or Infinity, or zero please state this and justify.**

3 1	3 0	2 9	2 8	2 7	2 6	3 5	2 4	2 3	2 2	2 1	2 0	1 9	1 8	1 7	1 6	1 5	1 4	1 3	1 2	1 1	1 0	9	8	7	6	5	4	3	2	1
1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1

**Explanation:**

$$11111111 = 255$$

Mantisa bits

$$.111111111111111111111111 = .99$$

$$255 - 127 = 128$$

$$(-1)^1 \cdot 2^{(129)} = -6.8 \cdot 10^{38}$$

Hence, the answer is NAN.

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In EACH Questions 10.1-10.4 you are given SIGNED Integers stored in 32 BIT Registers. (Not 33-BIT Register ). Please write decimal, and binary operands and the results. For each question you have to write the result and **overflow** or **No overflow**. You may override '0' with '1'.

**10.1 (5 points)** What is the result (hexadecimal, decimal and binary) of the following addition:

0x0000000E

+

0xFFFFFFFF

NO OVERFLOW

HEX: 0x00000000

Decimal: 13

Binary: 0000 0000 0000 0000 0000 0000 0000 1101

**10.2 (5 points)** What is the result (hexadecimal, decimal and binary) of the following subtraction:

0x7FFFFFFF

-

0xFFFFFFFF

OVERFLOW

HEX: 0x80000000

Decimal:  $2^{31}=2147483648$

Binary: 10000000000000000000000000000000

**10.3 (5 points)** What is the result (hexadecimal, decimal and binary) of the following subtraction:

0x80000000

-

0xFFFFFFFF

OVERFLOW

HEX: 0x80000001

Decimal:  $2^{31}+1 = 2147483649$

Binary: 10000000000000000000000000000001

**10.4 (5 points)** What is the result (hexadecimal, decimal and binary) of the following addition:

0x7FFFFFFF

+

0xFFFFFFFF

NO OVERFLOW

HEX: 0X7FFF FFFE

Decimal:  $2^{31}-2 = 2147483646$

Binary: 01111111111111111111111111111110

Please write your result in the following form:

0x80000000

OVERFLOW

0xFFFFFFFF

+

HEX: 0x7FFFFFFF

Decimal:  $+2^{31}-1$  Binary: 01111111111111111111111111111111