

# Multiple Regression

## Part 2

### Using RStudio for Ag Data

STAT 441/541 Statistical Methods II

# Information in the Model Summary Table

Residual standard error: 7.642 on 43 degrees of freedom  
Multiple R-squared: 0.7396, Adjusted R-squared: 0.7275  
F-statistic: 61.06 on 2 and 43 DF, p-value: 2.737e-13

- Estimate of the model standard deviation

$$s_{\varepsilon} = 7.642$$

- Adjusted R-squared = 0.7275

# Assess Multicollinearity

```
> VIF(model)
      x6      x9
1.753282 1.753282
```

- The Variance Inflation Factor for independent variable x6 is 1.75
- The Variance Inflation Factor for independent variable x9 is 1.75

# Confidence Interval for the Mean, $E(y)$

```
> # confidence interval on E(y) for specified values of all
> # independent variables
> forecastdata = data.frame(x6=90,
+                           x9=70)
> predict(model,newdata=forecastdata,interval="confidence")
      fit      lwr      upr
1 134.0359 99.9341 168.1377
```

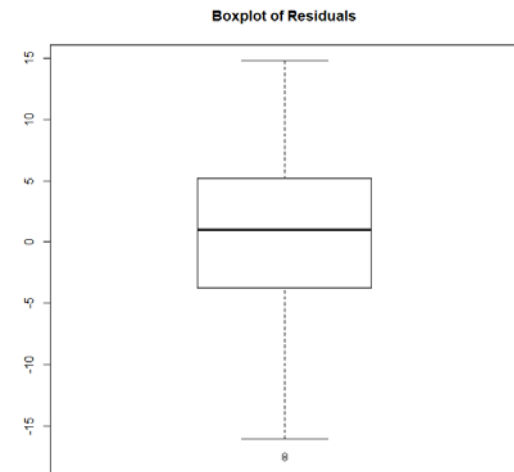
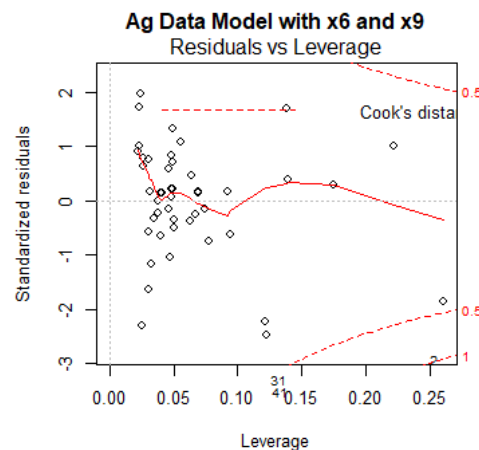
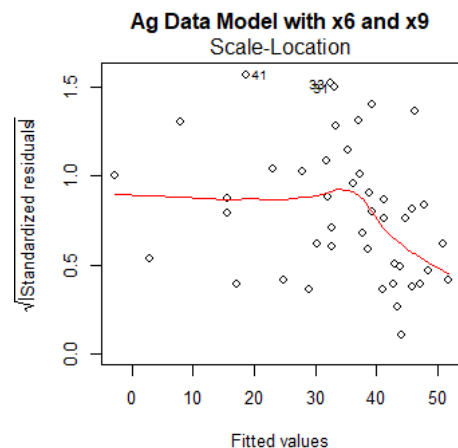
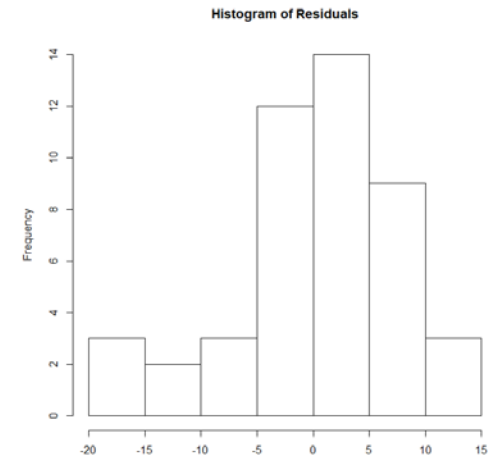
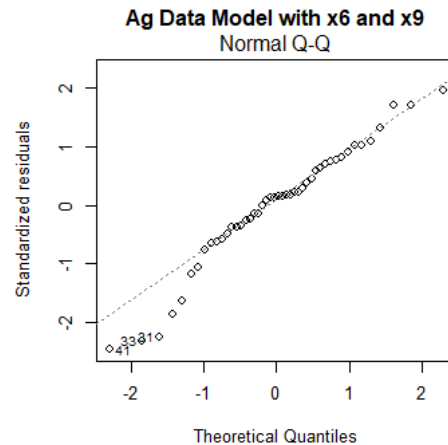
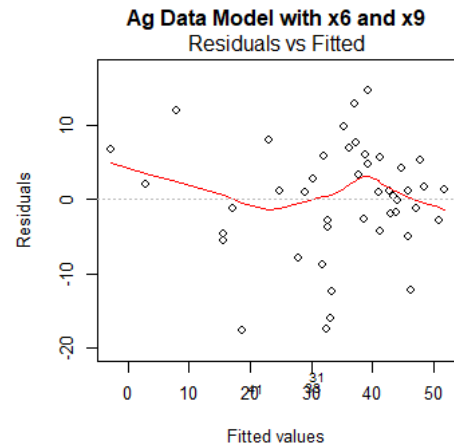
- The predicted value when  $x_6=90$  and  $x_9=70$  is 134.04
- The lower confidence limit is 99.93 and the upper confidence limit is 168.14 when  $x_6=90$  and  $x_9=70$

# Prediction Interval for Individual Values of $y$

```
> # prediction interval on y for specified values of all  
> # independent variables  
> predict(model,newdata=forecastdata,interval="prediction")  
      fit      lwr      upr  
1 134.0359 96.61352 171.4583
```

- The predicted value when  $x_6=90$  and  $x_9=70$  is 134.04
- The lower prediction limit is 96.61 and the upper prediction limit is 171.46 when  $x_6=90$  and  $x_9=70$

# Various Diagnostic Plots for Checking Assumptions



# Shapiro-Wilk Test

```
> # Shapiro-Wilk test for normality of errors and use alpha=0.01  
> shapiro.test(resid(model))
```

```
      Shapiro-Wilk normality test
```

```
data:  resid(model)
```

```
W = 0.96418, p-value = 0.1665
```



Test Statistic

# Breusch-Pagan Test

```
> # Breusch-Pagan Test for a common error variance and use alpha=0.01  
> bptest(model)
```

```
studentized Breusch-Pagan test
```

```
data: model
```

```
BP = 4.6148, df = 2, p-value = 0.09952
```



Test Statistic



# Potential Outliers

dfbetas

```
> influence.measures(model)
Influence measures of
lm(formula = y ~ x6 + x9, data = dataobj) :
```

	dfb.1_	dfb.x6	dfb.x9	dffit	cov.r	cook.d	hat	inf
1	0.027301	-0.02895	-0.018427	0.03491	1.152	4.16e-04	0.0697	
2	-1.073012	0.91723	1.042055	-1.13557	1.130	4.05e-01	0.2608	*
3	0.139330	-0.14036	-0.106024	0.15406	1.235	8.07e-03	0.1398	*
4	0.041139	-0.04640	-0.024258	0.05387	1.180	9.90e-04	0.0923	
5	0.097695	-0.08655	-0.088674	0.11841	1.130	4.76e-03	0.0643	
6	0.029586	-0.20565	0.220084	0.54005	1.284	9.72e-02	0.2221	*
7	0.026174	-0.06583	0.034510	0.13050	1.292	5.80e-03	0.1745	*
8	-0.274608	0.05972	0.519511	0.69611	1.010	1.54e-01	0.1378	
9	-0.143161	0.08664	0.198147	0.26409	1.046	2.32e-02	0.0557	
10	-0.046490	0.03927	0.052977	0.12740	1.056	5.46e-03	0.0264	

Observations flagged  
as influential