

What Every Scientist Needs to Know

Lessons Learned from the World of Cosmology

Amir Shahmoradi

Research Scientist Associate III / Peter O'Donnell, Jr. Fellow
Institute for Computational Engineering and Sciences
The University of Texas at Austin

presented at

Department of Physics
Sharif University of Technology

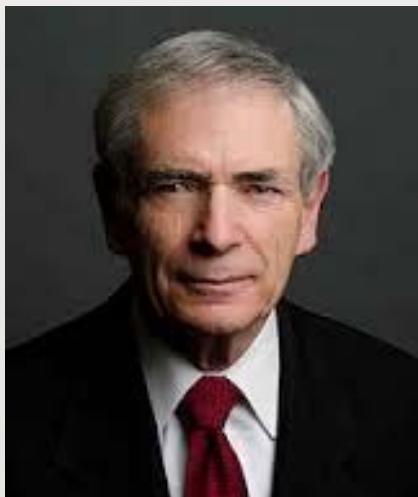
Tehran, April 19 2016

Collaborators



Robert J. Nemiroff

Astrophysicist, NASA Goddard Space Flight Center
Professor of Physics, Michigan Tech University
Editor, Astronomy Picture of the Day (APOD)



J. Tinsley Oden

Associate Vice President for Research, University of Texas at Austin
Director, Institute for Computational Engineering and Sciences
Cockrell Family Regents' Chair in Engineering No. 2, UT Austin
Peter O'Donnell Jr. Centennial Chair in Computing Systems, UT Austin
Professor of Aerospace Engineering and Engineering Mechanics
Professor of Computer Science, UT Austin
Professor of Mathematics, UT Austin

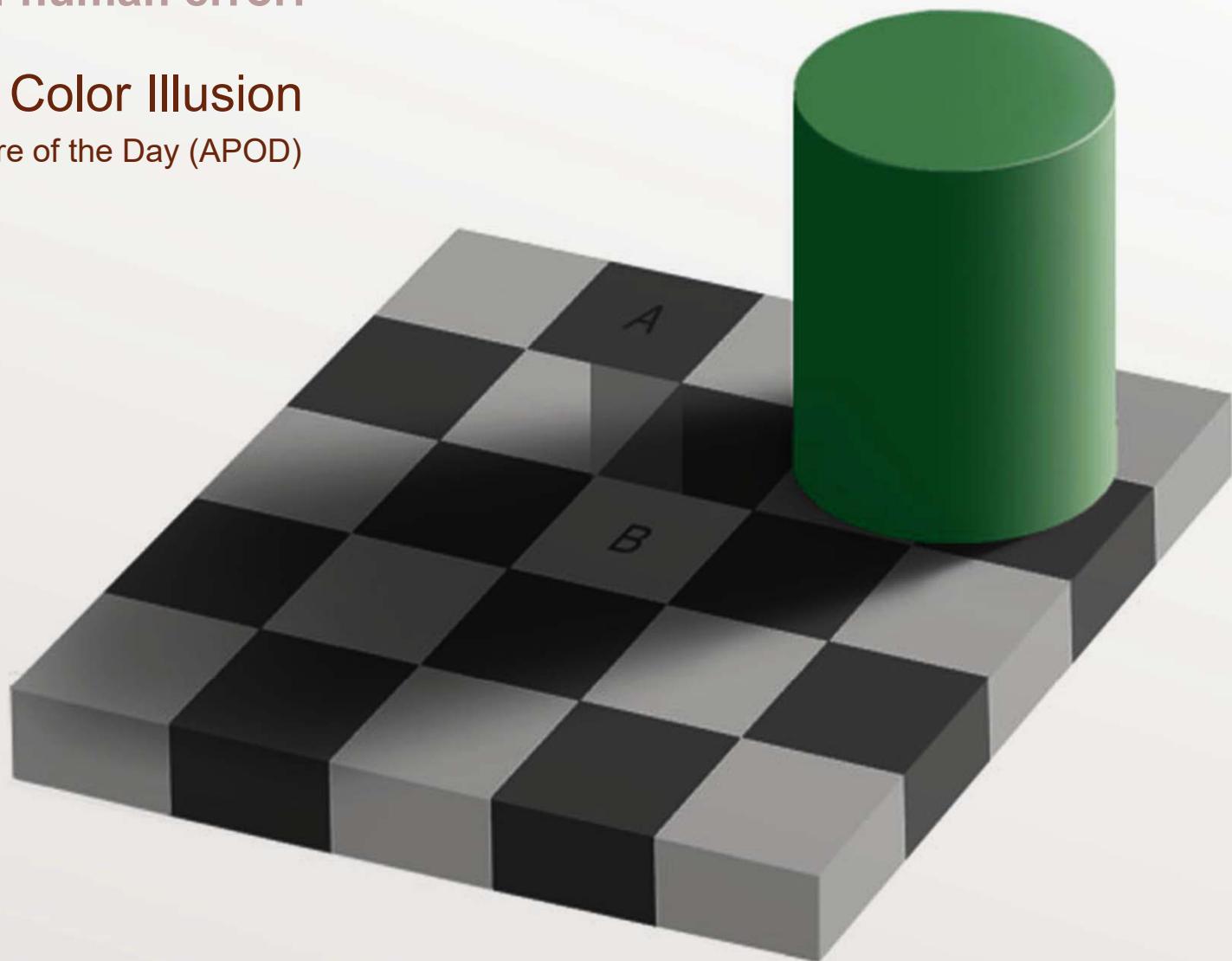
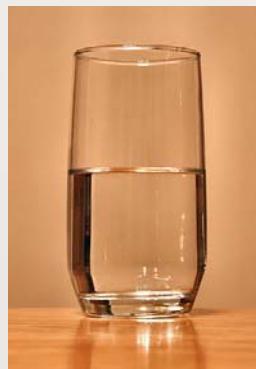
Cognitive biases are everywhere in human life

Example of human error:

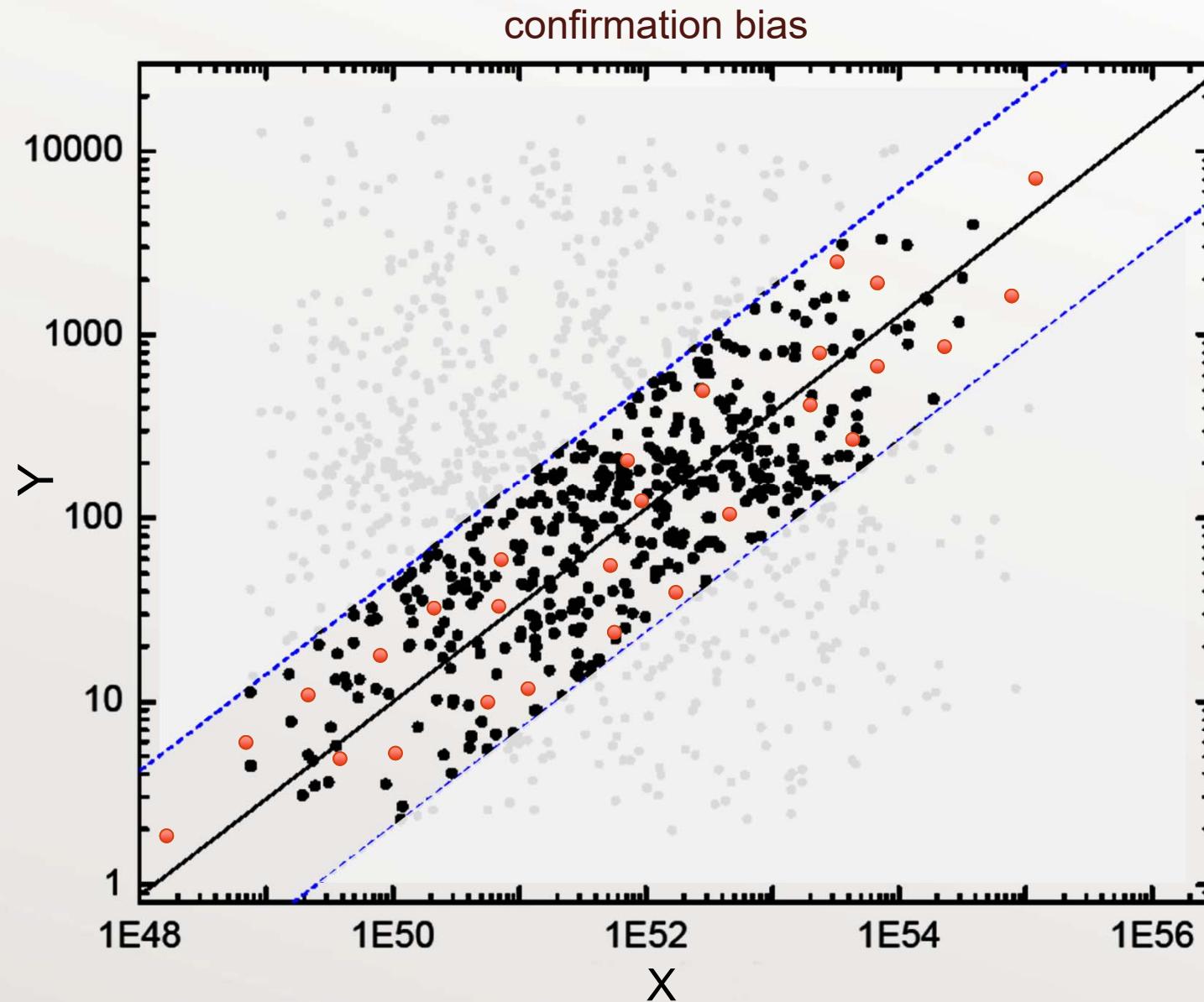
The Same Color Illusion

Astronomy Picture of the Day (APOD)
2007 July 17

half full? or
half empty?

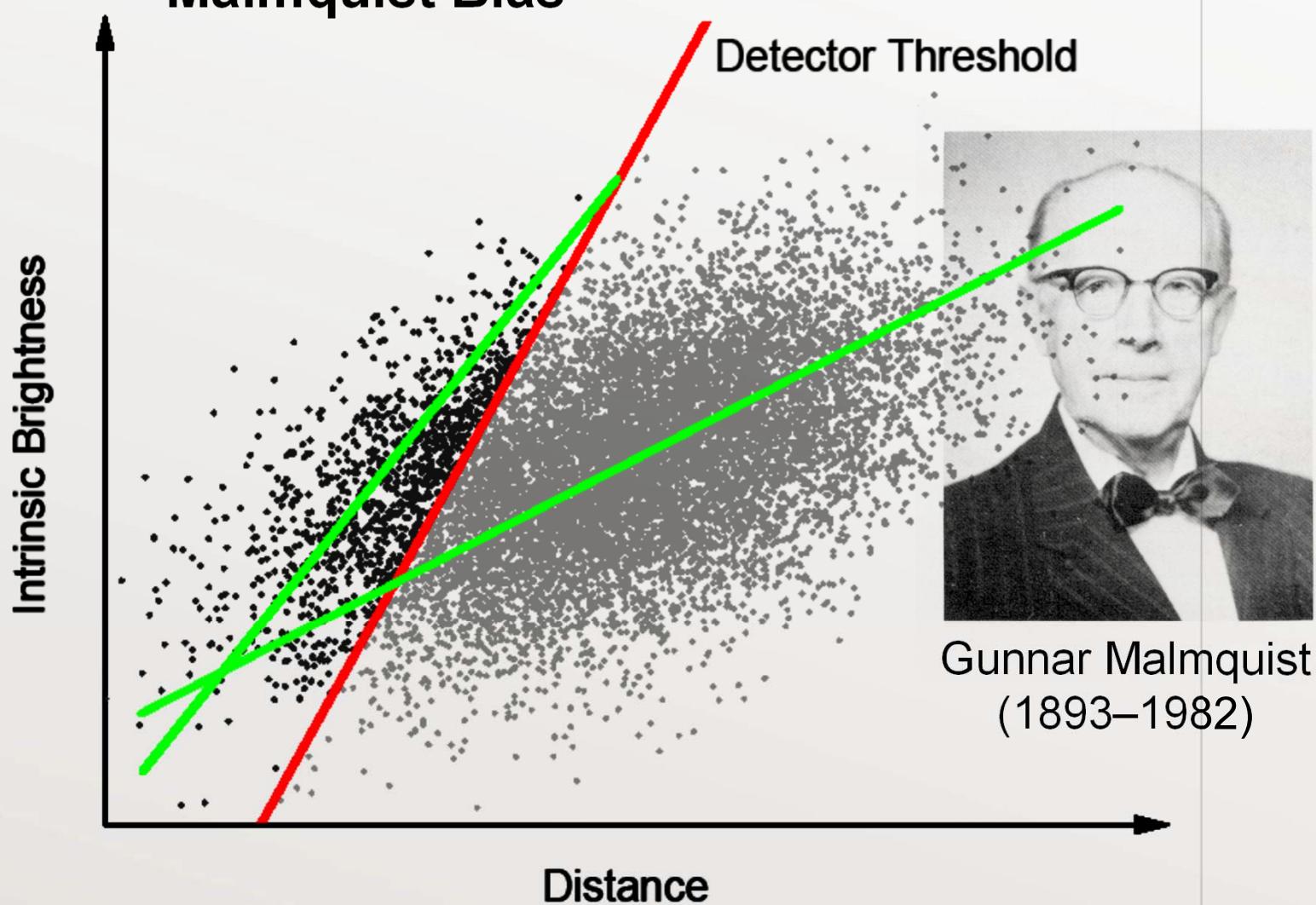


Statistical tests are often unable to capture human/instrumental biases



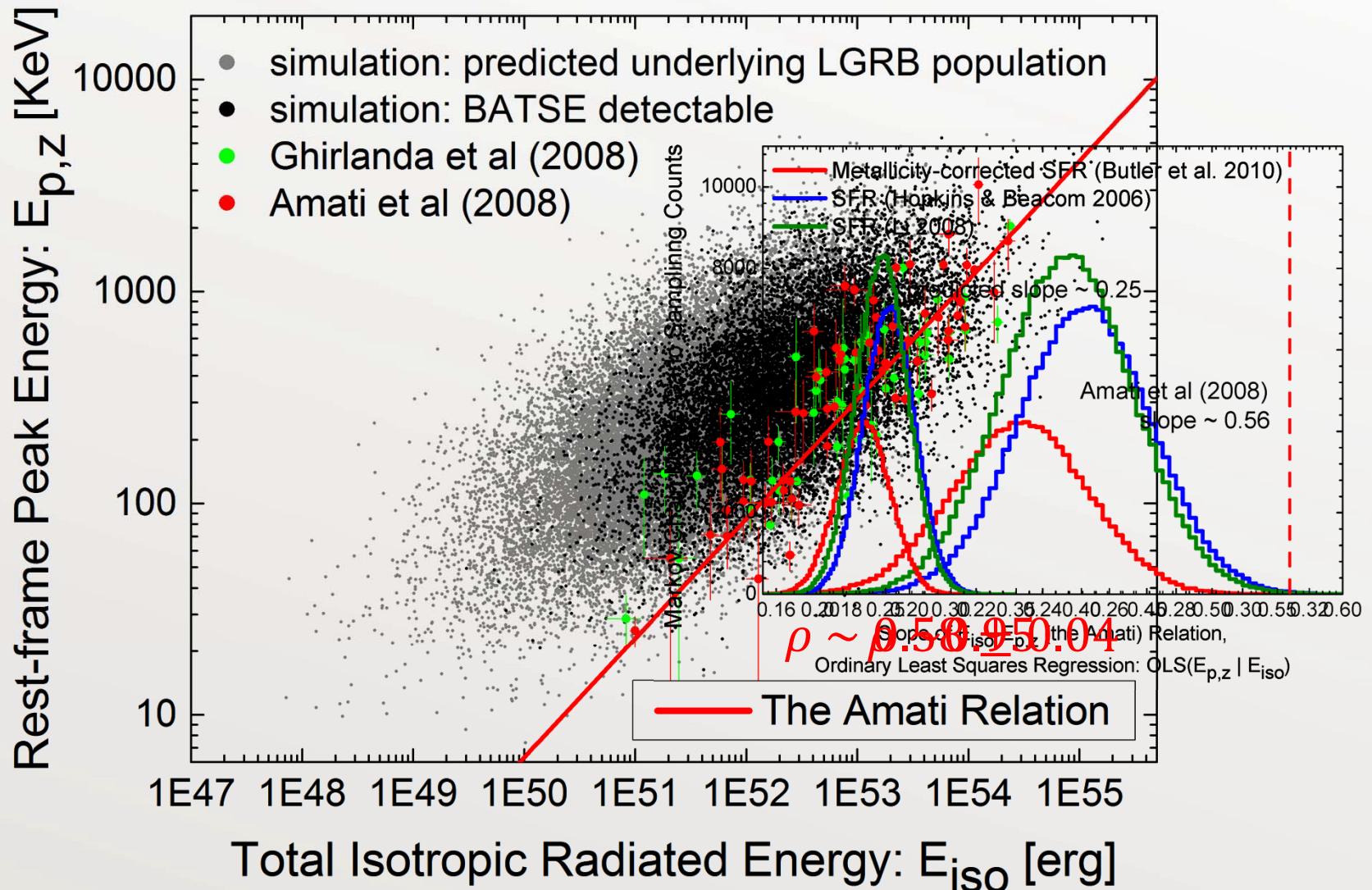
Instrumental bias: well-known in the field of Astronomy

Example of Instrumental bias Malmquist Bias



The Amati Relation

A combination of human biases, gamma-ray detector limitations, and sample incompleteness, as well as some real physics behind it.



Overview

- I. Why are Gamma-Ray Bursts (GRBs) of interest to cosmologists?
- II. What are Gamma-Ray Bursts?
- III. Can we use GRBs as standard candles in cosmology?
- IV. Take-home message for all scientists in any field of science

I. Why are Gamma-Ray Bursts (GRBs) of interest to cosmologists?

Short answer:

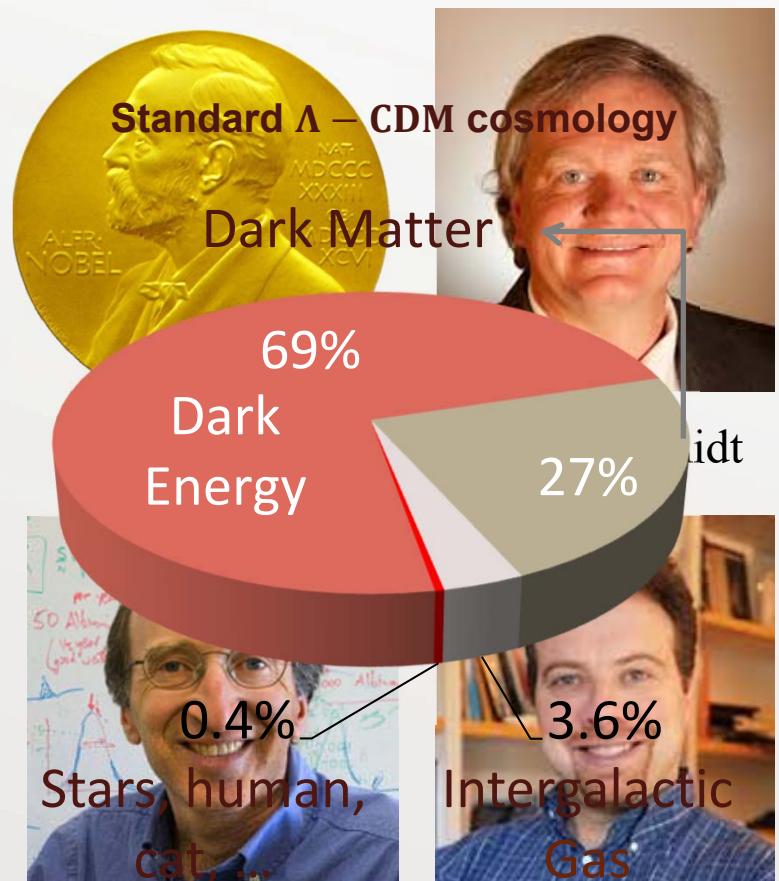
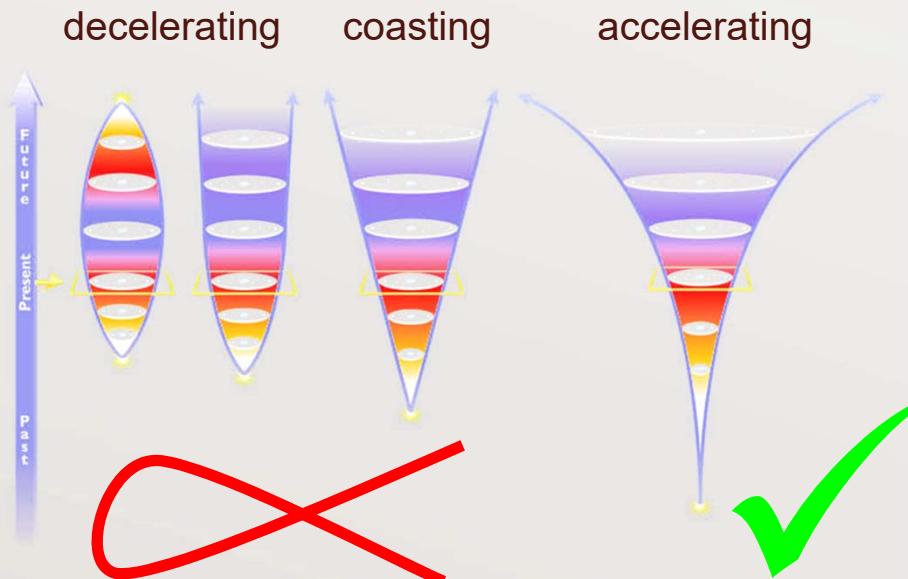
Since GRBs can be **potentially** used to test and validate cosmological models.

2011 Nobel Prize in Physics

The discovery of the accelerating expansion of the Universe

- Riess et al., 1998, ApJ, **116**, 1009-1038
- Perlmutter, 1999, ApJ, **517**, 565-586

Possible models of expanding universe



Saul Perlmutter

Adam Riess

How do astronomers measure the expansion rate of the universe?

Recipe for measuring the expansion rate of the universe:

What is the meaning of cosmological redshift?

1. Assume a cosmological model.

2. Find a celestial object that has a known fixed luminosity (a **standard candle**) and Given the **redshift** (z) of a celestial object, and a **cosmological model** for the evolution and expansion of the universe, we can calculate the object's distance from the earth.

$$z \equiv \frac{\lambda_{obs} - \lambda_{rest}}{\lambda_{rest}}$$
$$D_L = \frac{c}{H_0} (1 + z) \int_0^z \frac{dz'}{\sqrt{(D_{L,obs} + z')^3 \Omega_M(z') + \Omega_\Lambda(z')}}$$

3. Somehow magically measure the redshift (z) of the standard candle. Then calculate,

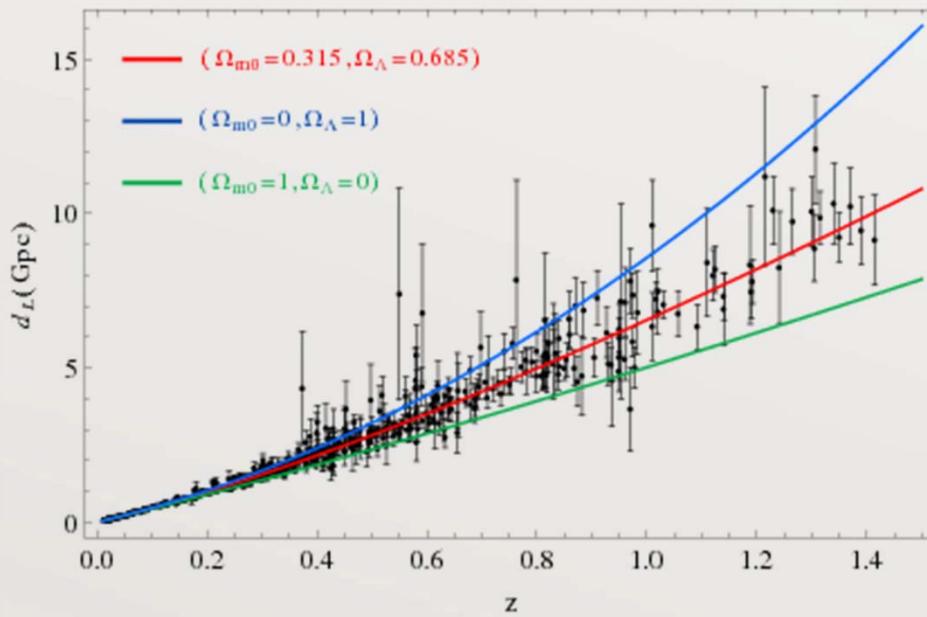
$$D_{L,theory} = \frac{c}{H_0} (1 + z) \int_0^z \frac{dz'}{\sqrt{(1 + z')^3 \Omega_M(z') + \Omega_\Lambda(z')}}$$

4. Now compare $D_{L,obs}$ with $D_{L,theory}$.

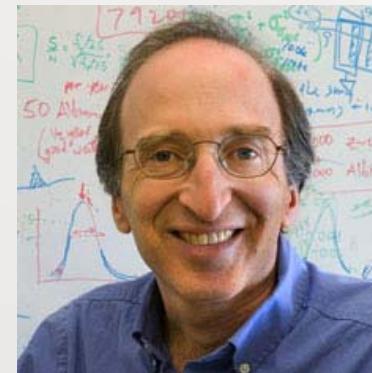
2011 Nobel Prize in Physics

What did these gentlemen do to get the Nobel prize?

1. They found a cosmological standard candle (supernova Ia).
2. They measured their distances from the earth.
3. They measured their redshifts, as well.
4. Given their redshifts and a cosmological model, they calculated their theoretical distance from the earth.
5. They compared observational distance with calculated theoretical distance.



Brian Schmidt



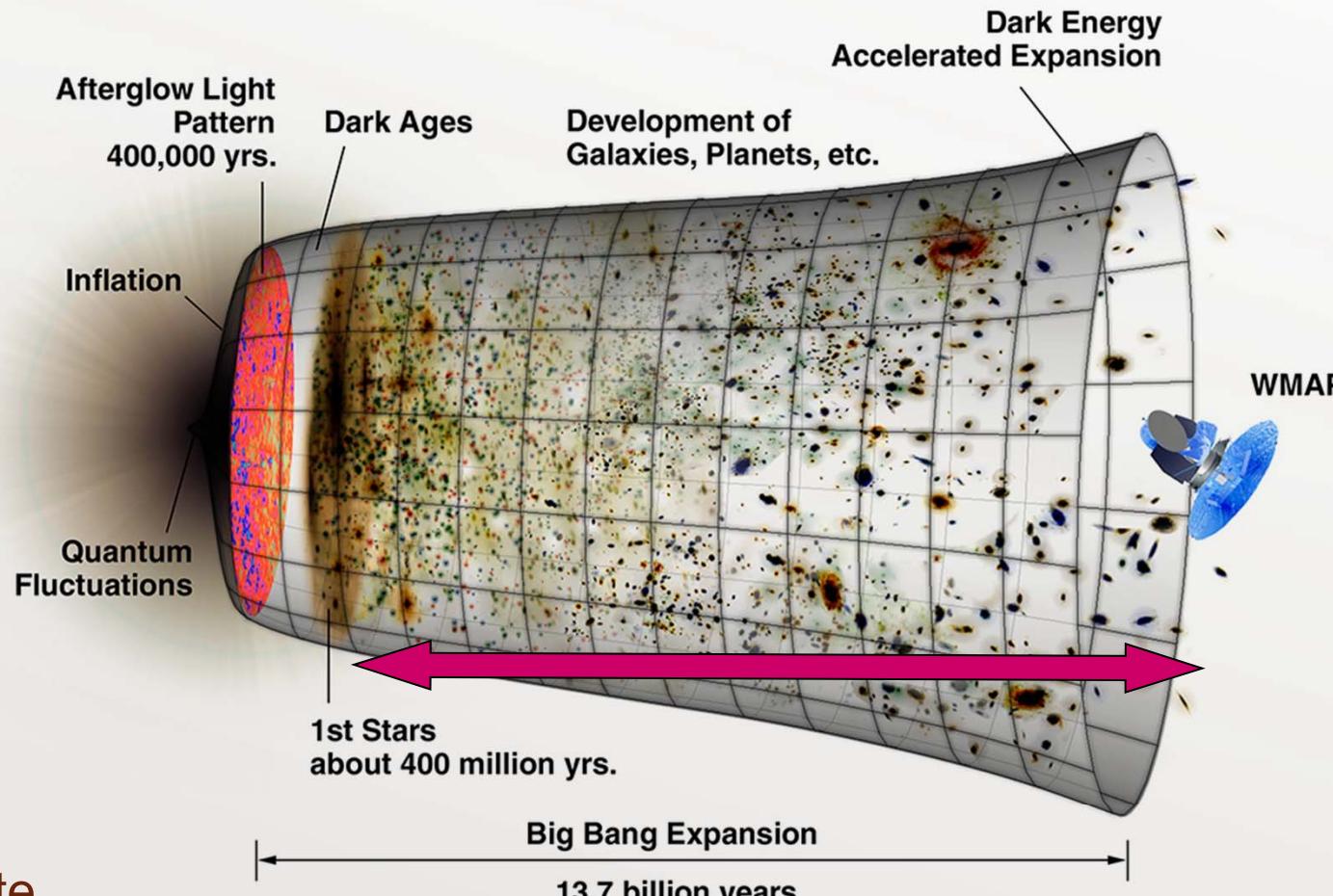
Saul Perlmutter



Adam Riess

Major problem with supernovae-Ia as standard candles?

Limited detectability out to $z \sim 1.7$



Candidate
Standard Candle:
Gamma-Ray Bursts: $Z < 65$

Supernovae projects: $Z < 1.7$

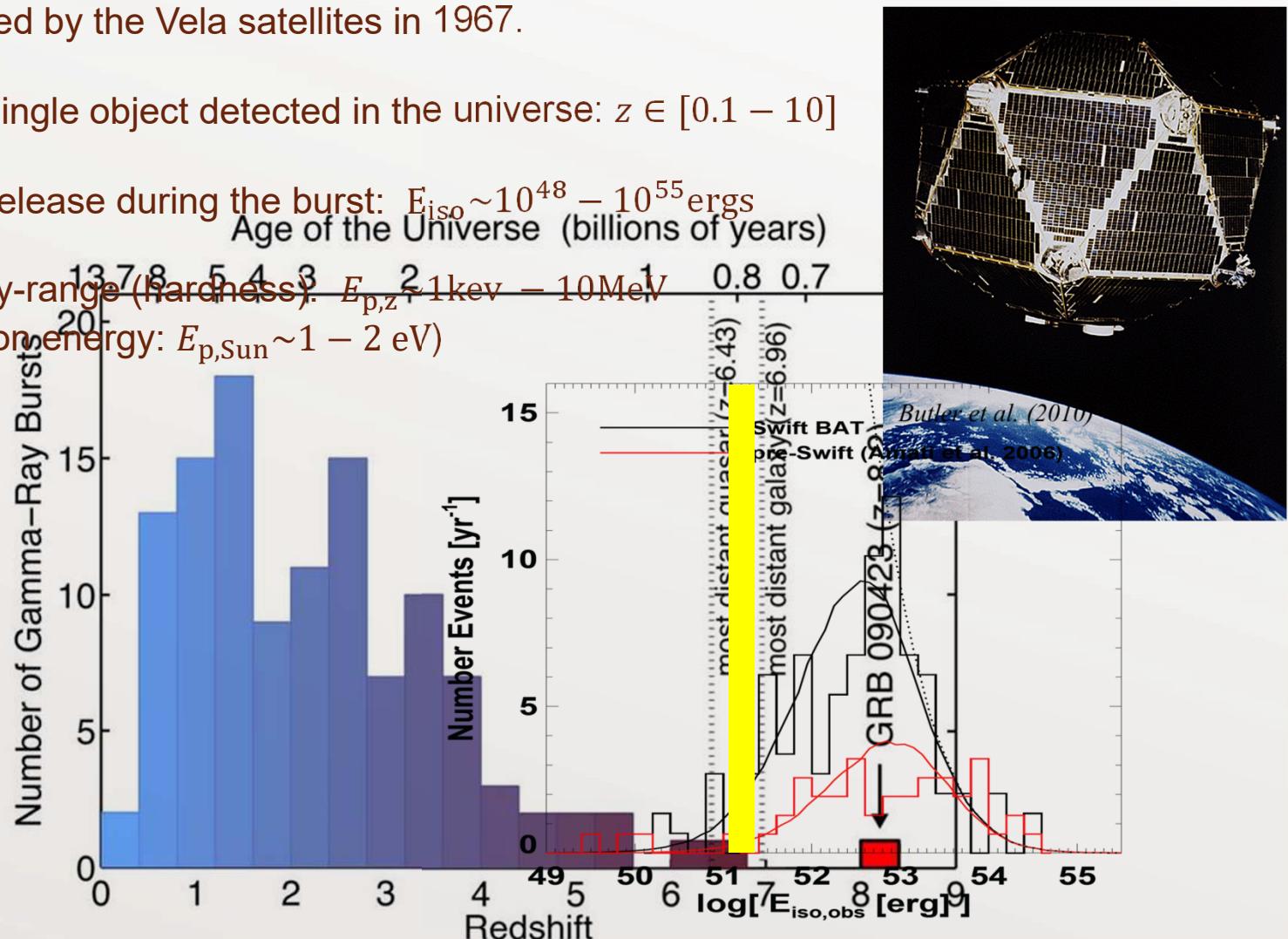
II. What are Gamma-Ray Bursts (GRBs)?

Short answer:

The brightest most powerful electromagnetic explosions in the universe,
ever observed by humans.

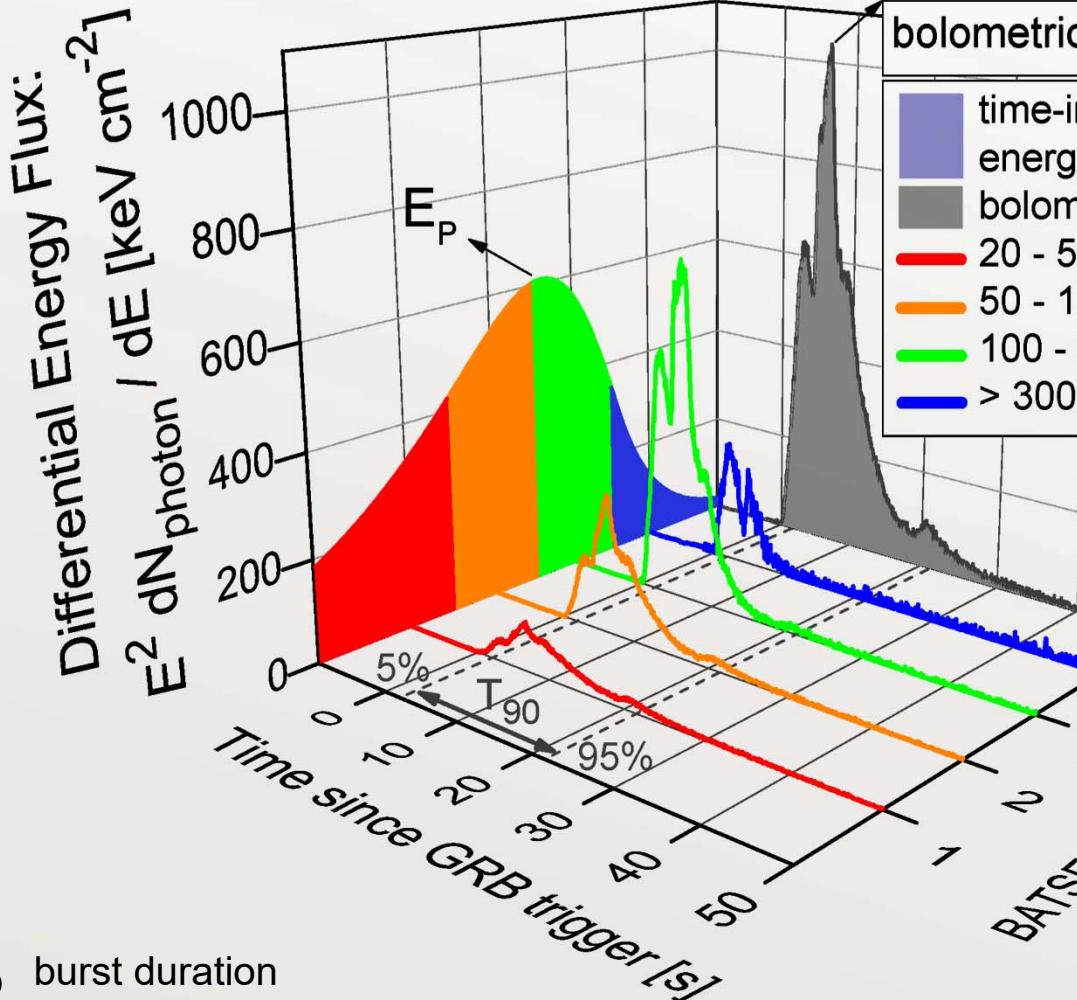
Gamma-ray bursts are flashes of gamma rays associated with extremely energetic explosions that have been observed in distant galaxies.

- First discovered by the Vela satellites in 1967.
- Most distant single object detected in the universe: $z \in [0.1 - 10]$
- Total energy release during the burst: $E_{\text{iso}} \sim 10^{48} - 10^{55} \text{ ergs}$
- Photon energy-range (hardness): $E_{p,z} \sim 1 \text{ keV} - 10 \text{ MeV}$
(Sun's photon energy: $E_{p,\text{Sun}} \sim 1 - 2 \text{ eV}$)



Example GRB light-curve and spectrum

and the four most important characteristics of GRBs

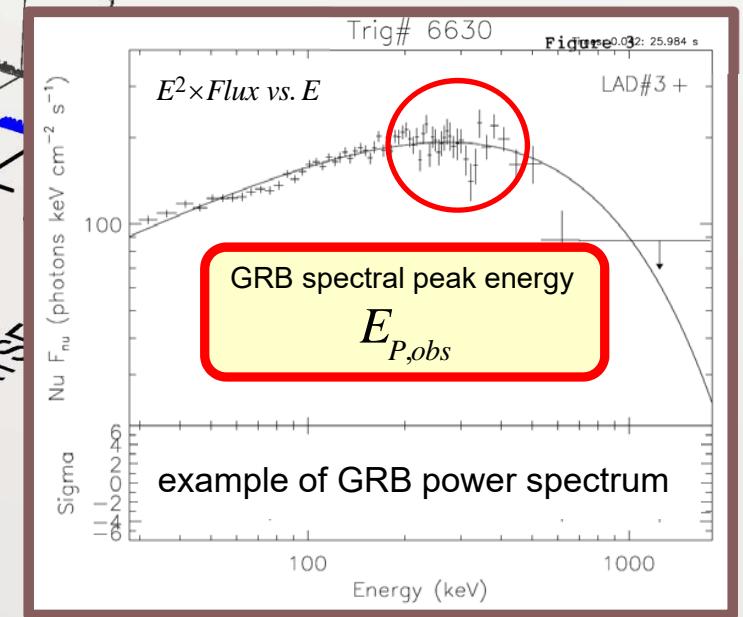
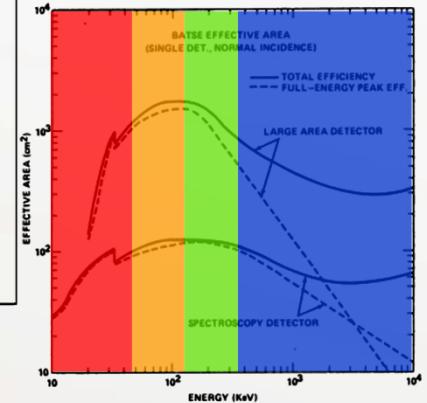
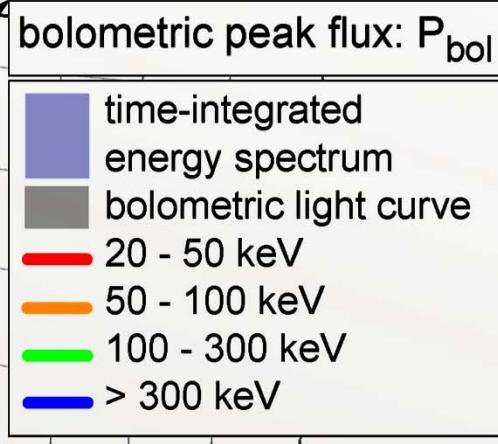


T_{90} burst duration

P_{bol} burst peak photon flux

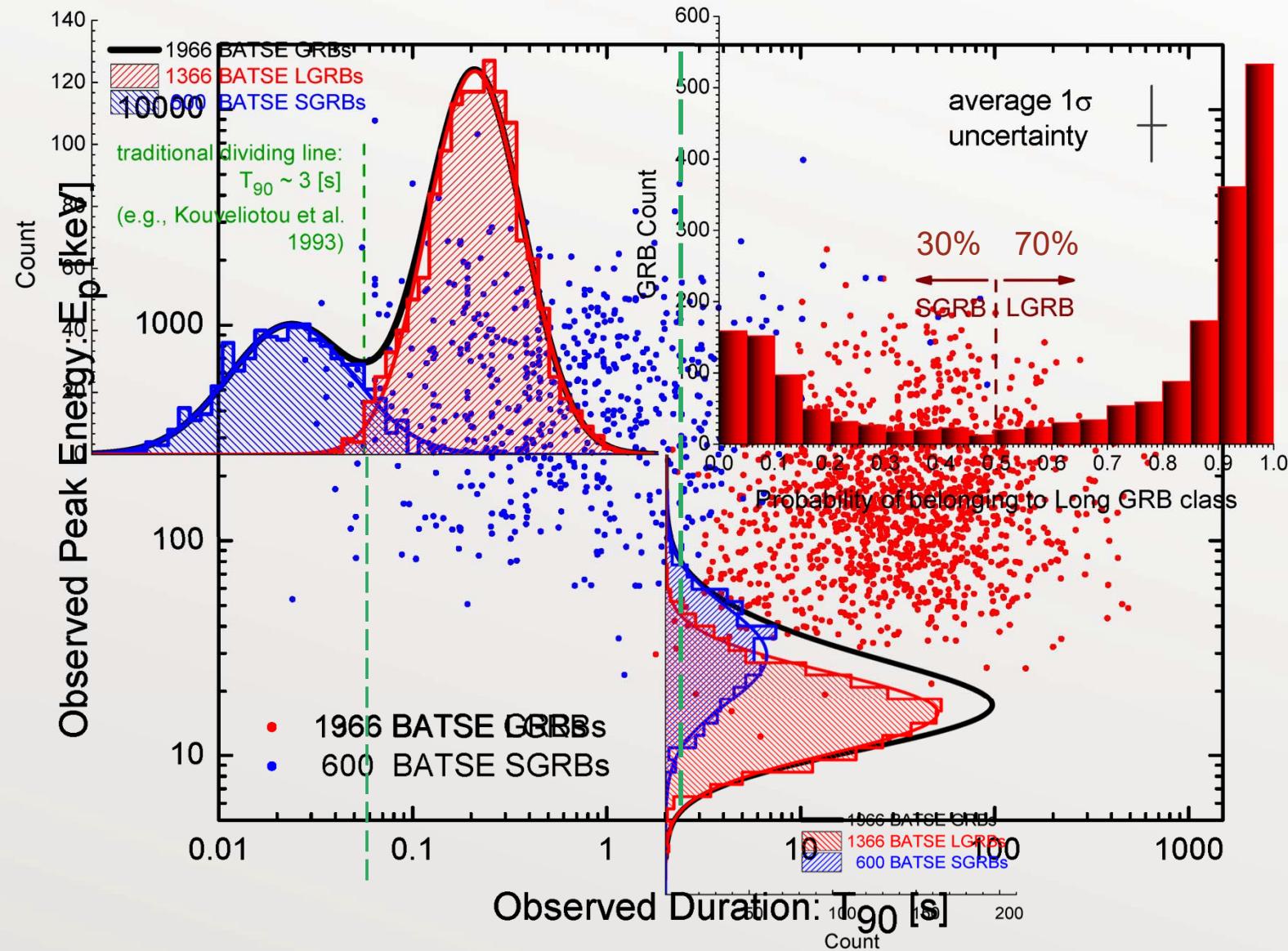
S_{bol} burst total energy (received on earth)

E_p burst spectral peak energy



Classification of BATSE GRBs: fuzzy clustering vs. cutoff line

(Shahmoradi & Nemiroff, 2011, MNRAS, 411, 1843–1856)



There are two types of Gamma-Ray Bursts (GRBs)



Short-duration class



Long-duration class
Time (s)

Discovery of Gravitational Wave Radiation in Feb 2016
Predicted by Albert Einstein in 1916

Each and every GRB has two sets of properties

Observer-frame

GRB observed duration: T_{90}

GRB peak photon flux: P_{bol}

GRB total observed energy: S_{bol}

GRB observed peak energy: E_p

Rest-frame

GRB intrinsic duration: $T_{90,z} = \frac{T_{90}}{1+z}$

GRB peak luminosity: $L_{iso} = 4\pi D_L (z)^2 P_{bol}$

GRB total energy release $E_{iso} = 4\pi D_L (z)^2 S_{bol}$

GRB intrinsic peak energy: $E_{p,z} = E_p(1 + z)$



z transformation

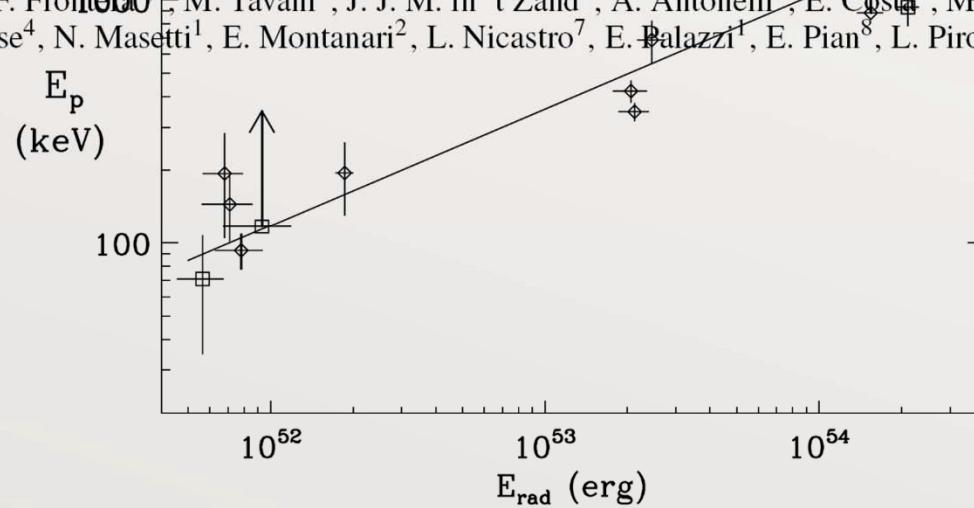
III. Can we use GRBs as standard candles in cosmology?

Short answer:

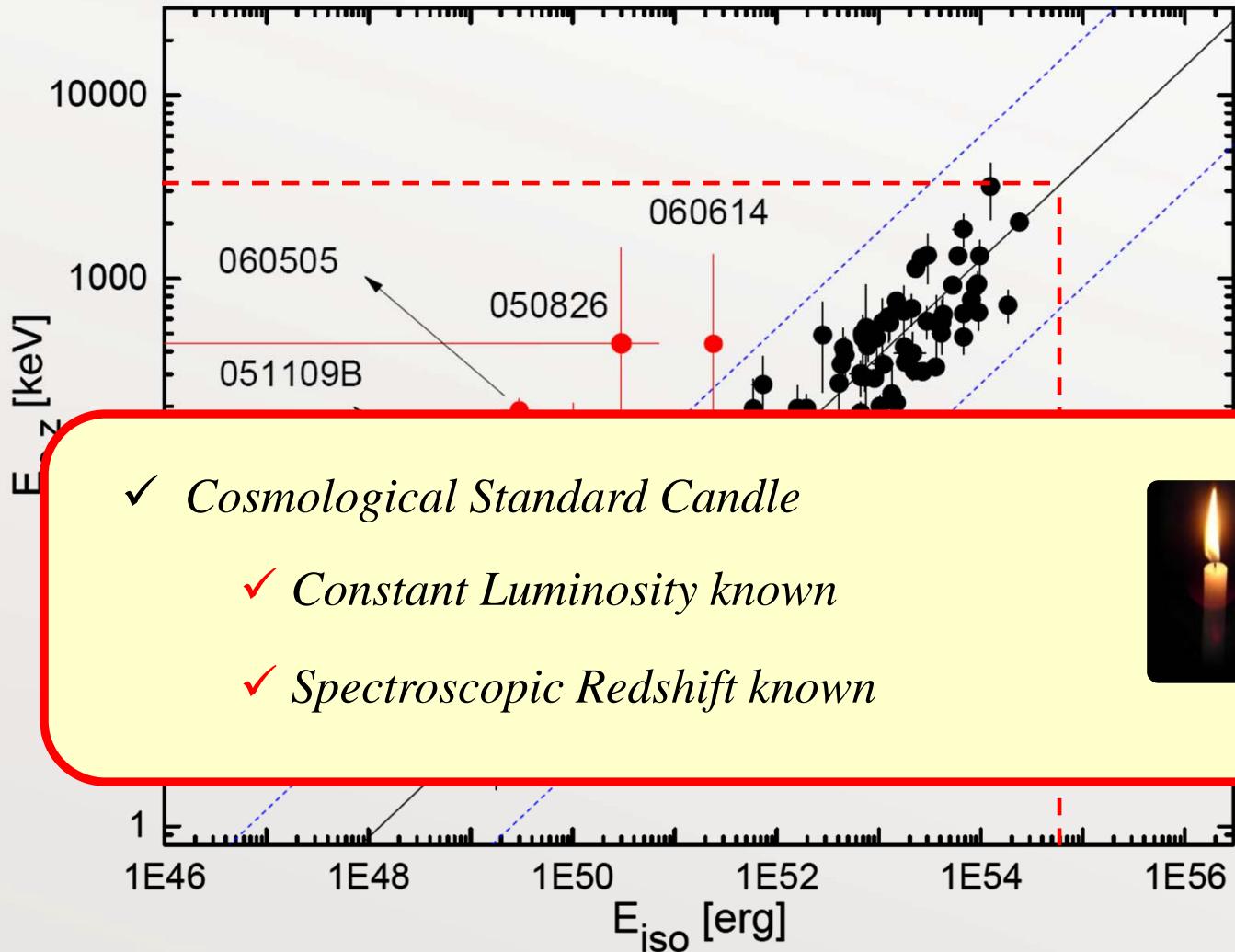
No, at the moment. Maybe yes in future.

Intrinsic spectra and energetics of BeppoSAX Gamma-Ray bursts with QPOs redshifts

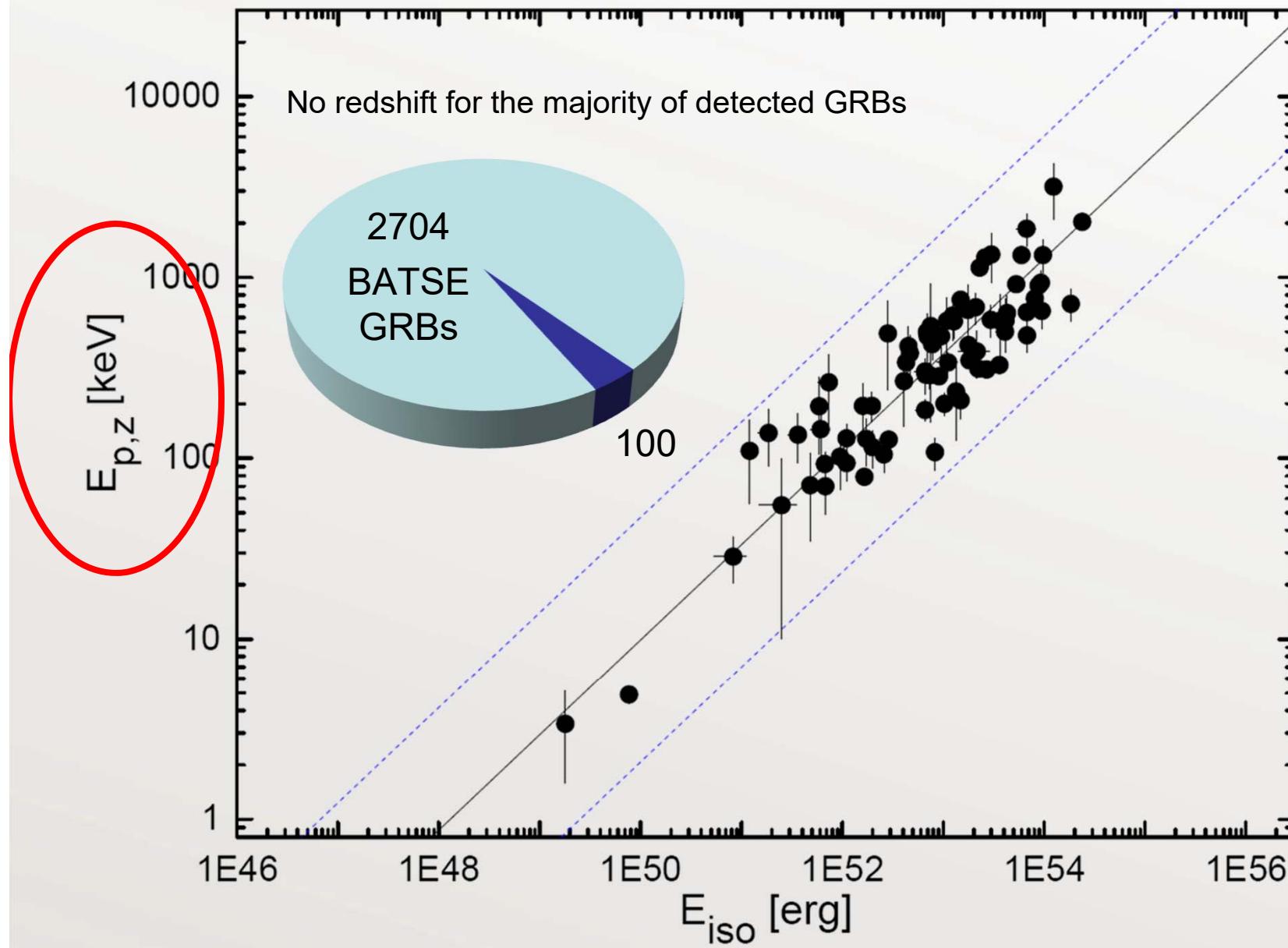
L. Amati¹, F. Frontera^{1,2}, M. Tavani³, J. J. M. in 't Zand⁴, A. Antonelli⁵, E. Costa⁶, M. Feroci⁶, C. Guidorzi²,
J. Heise⁴, N. Masetti¹, E. Montanari², L. Nicastro⁷, E. Palazzi¹, E. Pian⁸, L. Piro⁶, and P. Soffitta⁶



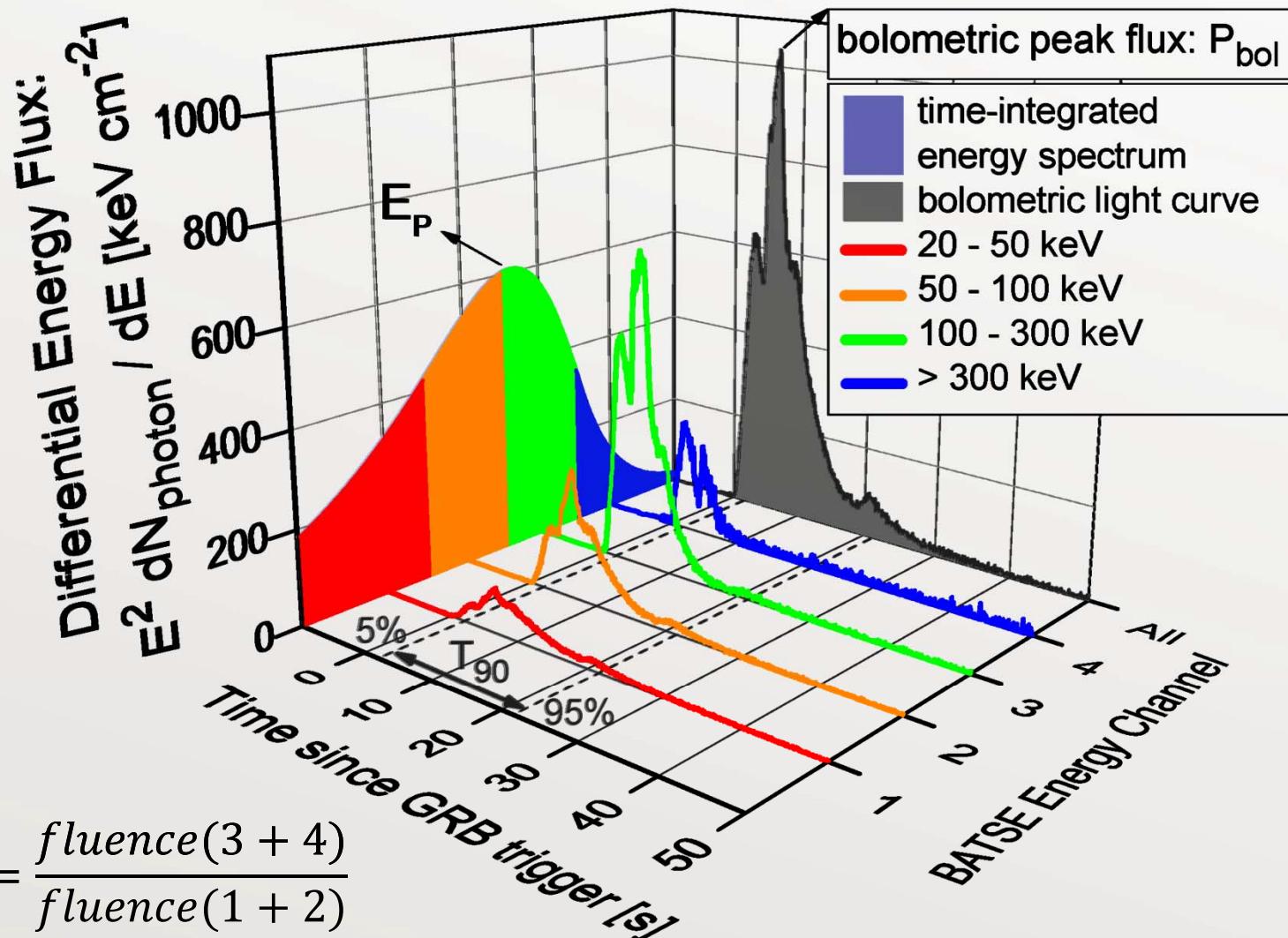
The spectral peak energy ($E_{p,z}$) of GRBs can be a standard candle, thanks to the Amati relation



The Amati relation has been constructed by less than 10% of all GRBs detected by all gamma-ray satellites

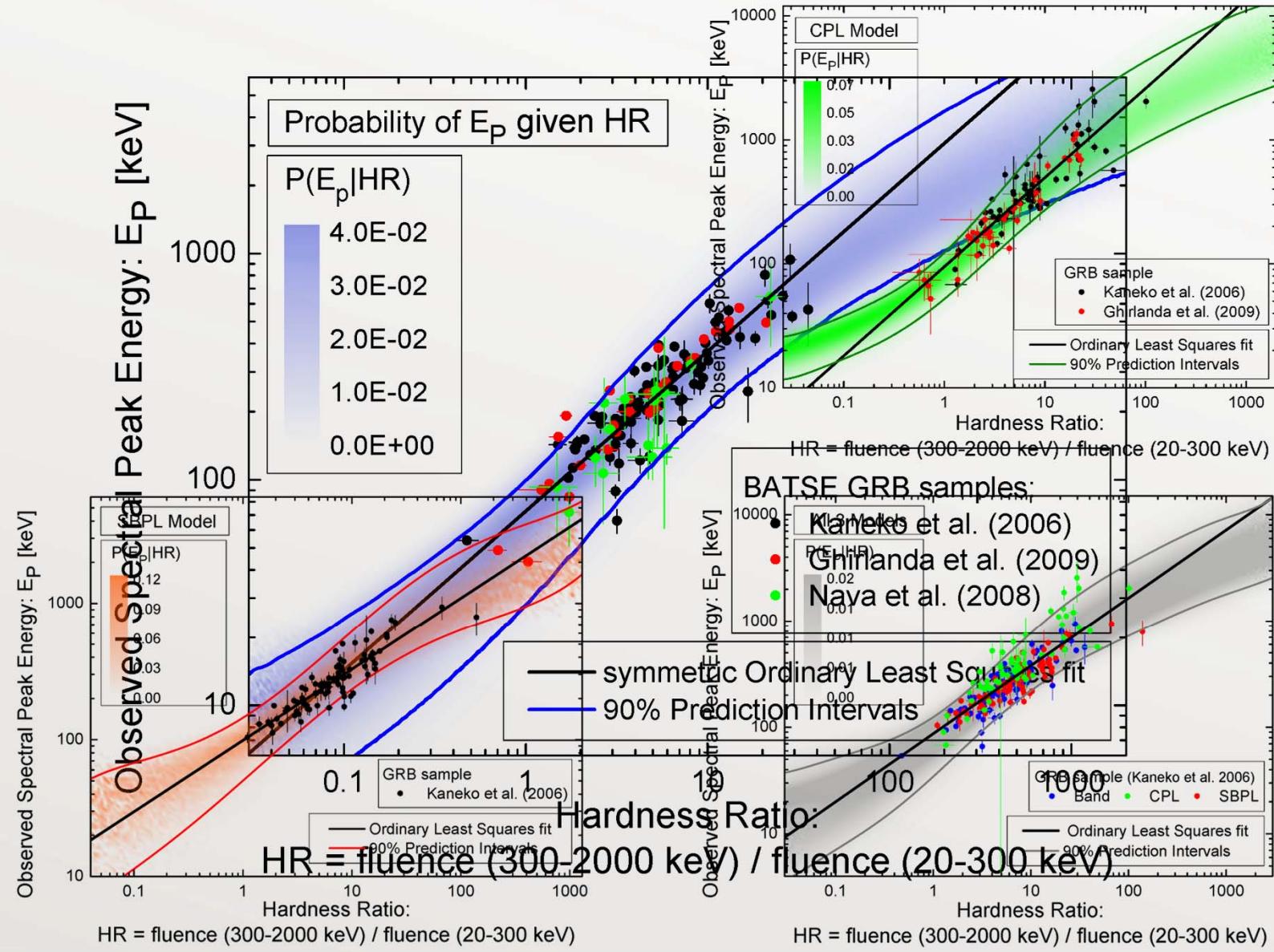


Example GRB lightcurve and spectrum (BATSE GRB trigger 1085)



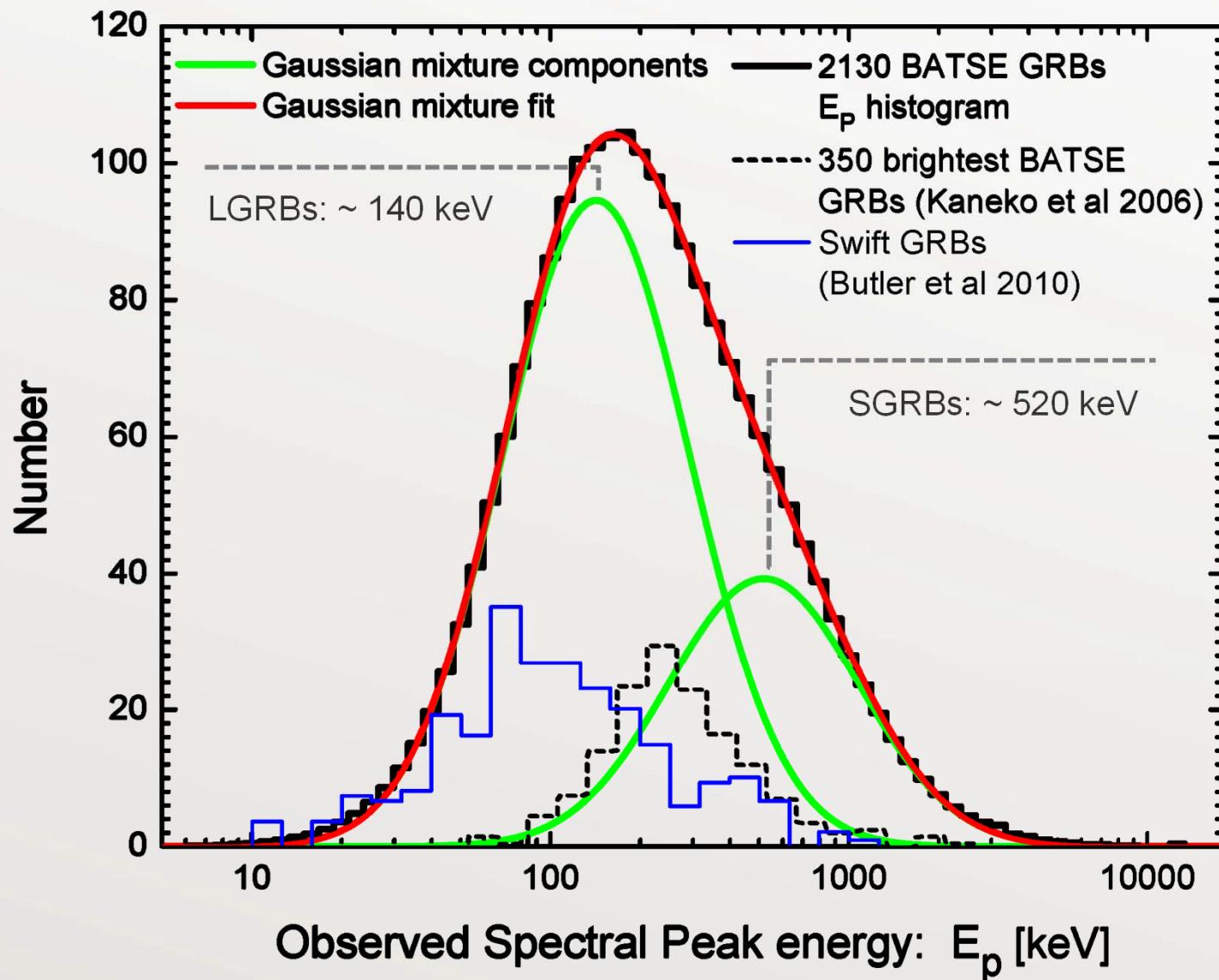
Hardness is a proxy measure of spectral peak energy of GRBs

(Shahmoradi & Nemiroff, 2010, MNRAS, **407**, 2075–2090)

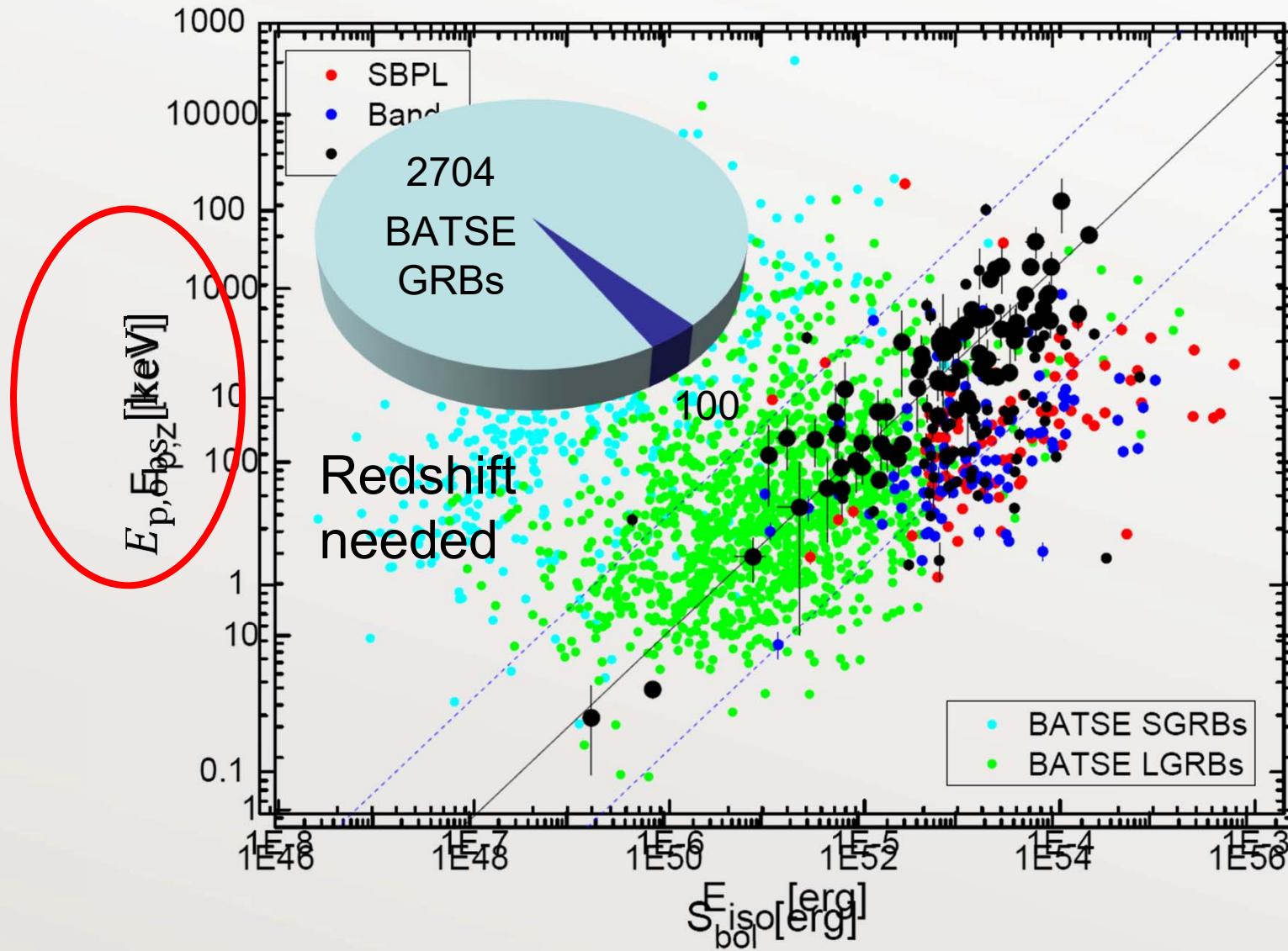


The peak energy distribution of 2130 BATSE GRBs

(Shahmoradi & Nemiroff, 2010, MNRAS, **407**, 2075–2090)

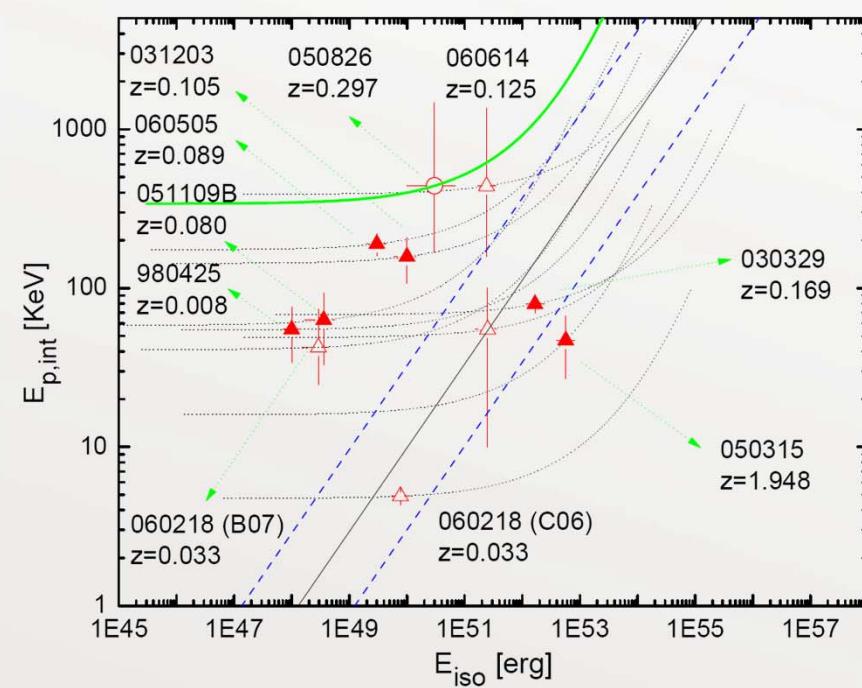
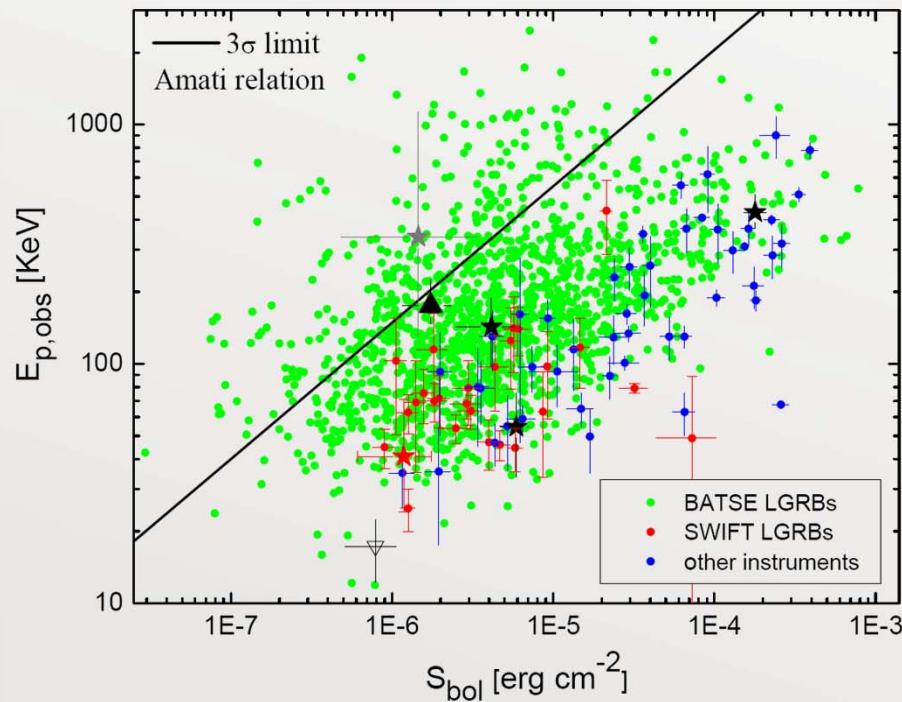


GRB astronomers are only seeing the tip of the iceberg



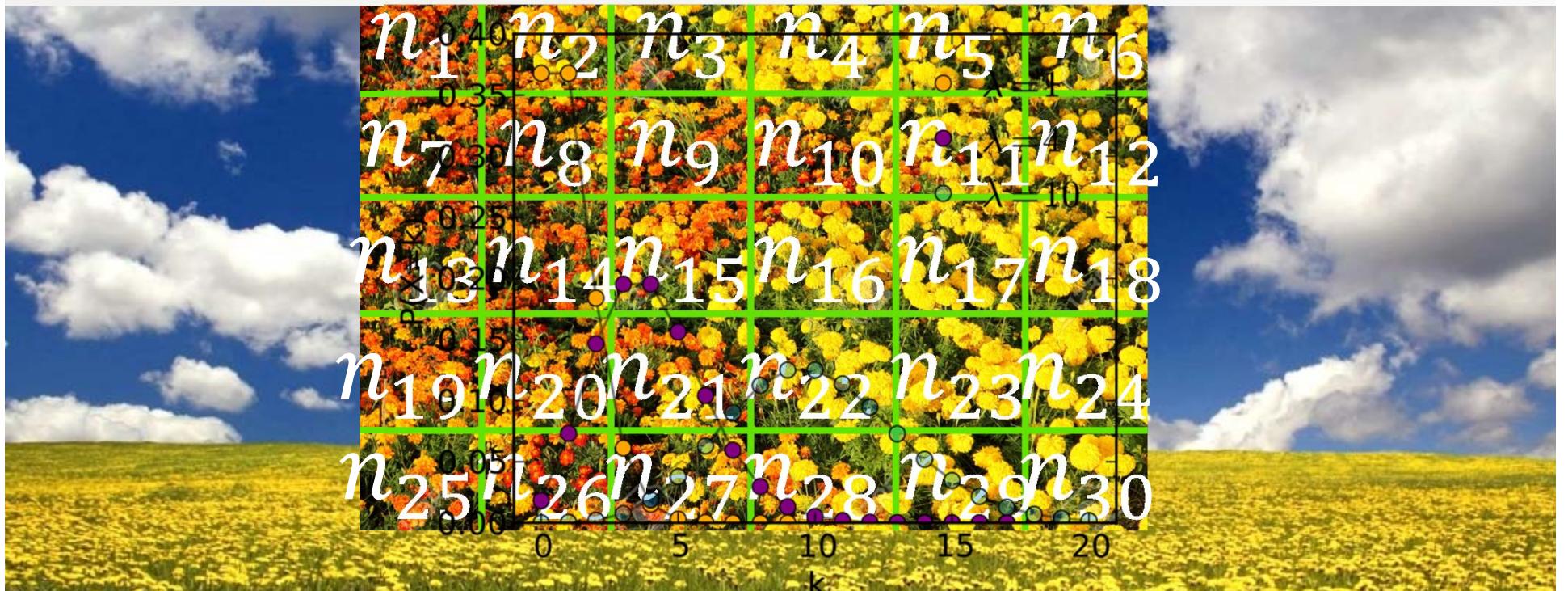
The Amati relation is heavily affected by sample incompleteness bias

At least 19% of all detected GRBs with no redshift are not consistent with the Amati relation at $> 3\sigma$ significance level.



Is there also a sample incompleteness bias due to gamma-ray detector threshold?

Poisson distribution: The distribution of counts of independent events within a given interval of time, space, ...



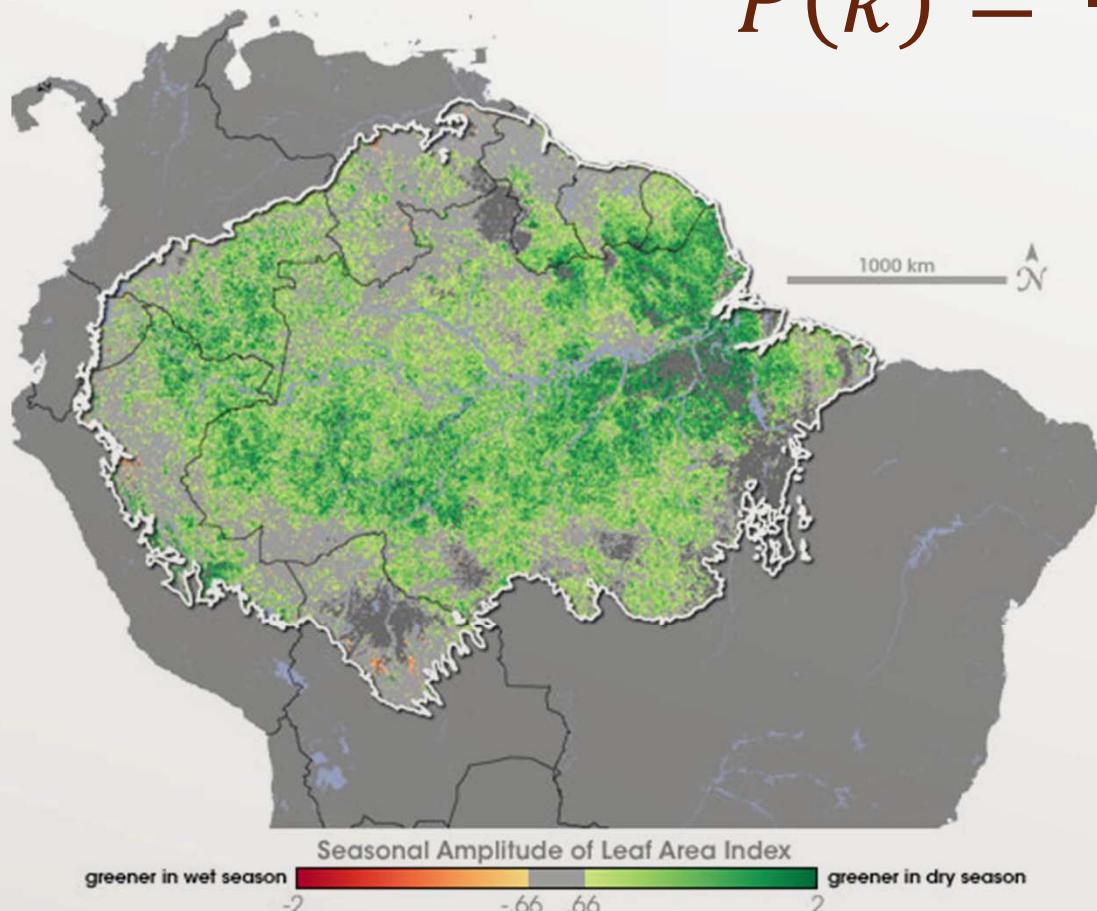
$$\lambda = \frac{1}{N} \sum_{N=0}^{N=30} n_i$$

$$P(k) = \frac{\lambda^k}{k!} e^{-\lambda}$$

Non-homogeneous spatial-temporal Poisson point process:

A Poisson point process with a Poisson parameter λ set as some location-dependent function in the underlying space on which the Poisson process is defined.

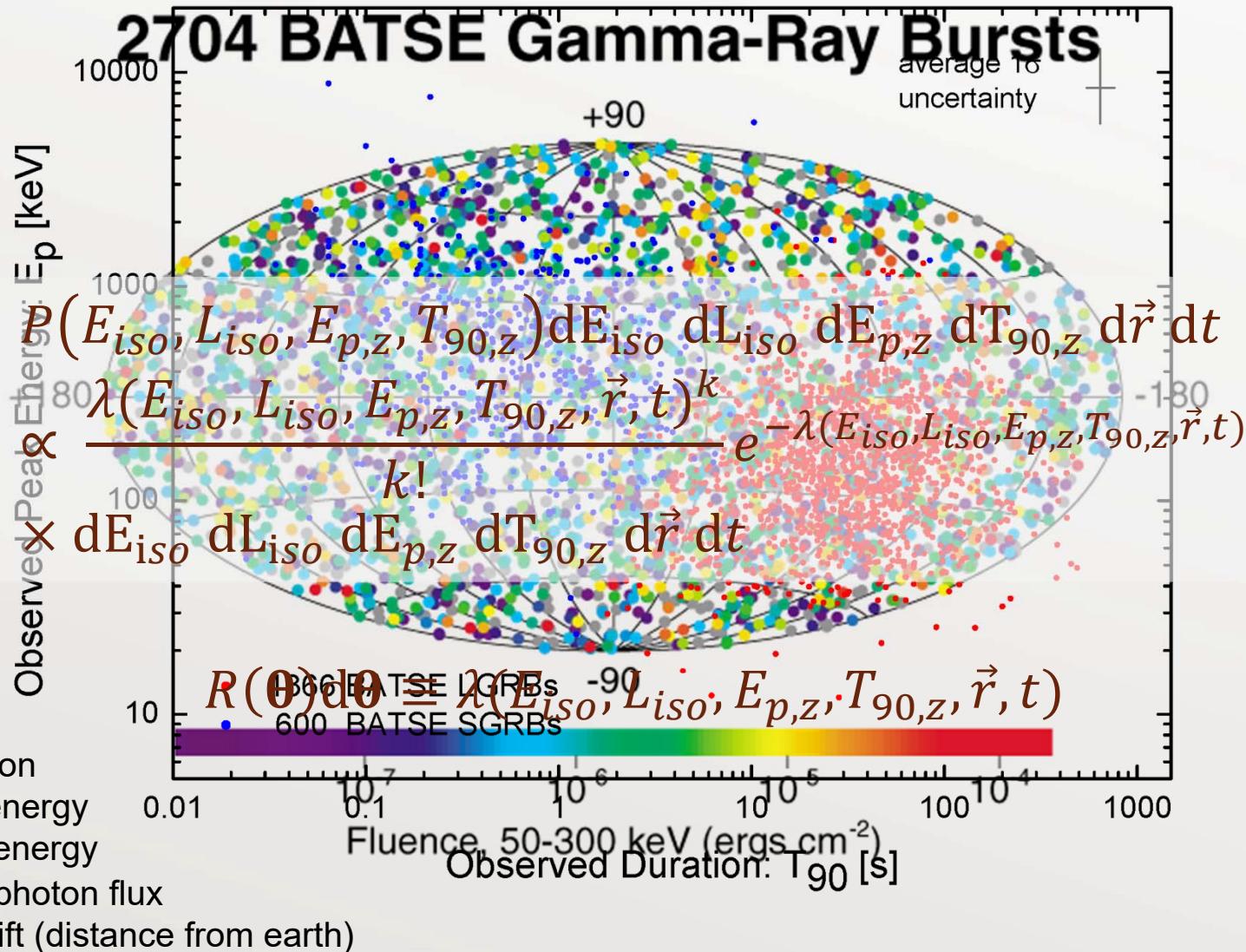
$$P(k) = \frac{\lambda(\vec{r}, t)^k}{k!} e^{-\lambda(\vec{r}, t)}$$



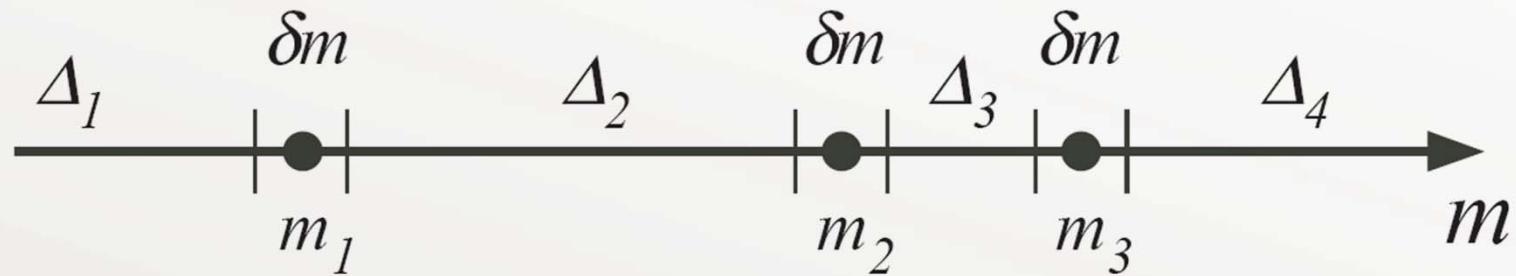
Poisson processes
are additive!

GRB detection process can be modeled as a non-homogenous Poisson process

What is the rate of occurrence of GRBs as a function of their distance and properties, $R(\theta)$?



With a statistical model in hand, we can proceed to construct the likelihood function of the model to estimate model parameters



$$P(k) = \frac{\lambda(m)^k}{k!} e^{-\lambda(m)} \quad P_0(m) = \frac{(R(m)\Delta m)^0}{0!} e^{-R(m)\Delta m} = e^{-R(m)\Delta m}$$

$$P_1(m) = \frac{(R(m)\Delta m)^1}{1!} e^{-R(m)\Delta m} = R(m)\Delta m e^{-R(m)\Delta m}$$

$$\begin{aligned} L(\text{DATA}|R(m)) &= \prod_{i=1}^N P_1(m_i) \prod_{j=1}^M P_0(m_j) = (\Delta m)^N \left[\prod_{i=1}^N R(m_i) \right] \left[e^{-\sum_{j=1}^{N+M} R(m_j)\Delta m} \right] \\ &= (\Delta m)^N \left[\prod_{i=1}^N R(m_i) \right] \exp \left(- \int_M \dots \int_M R(m) dm \right) \end{aligned}$$

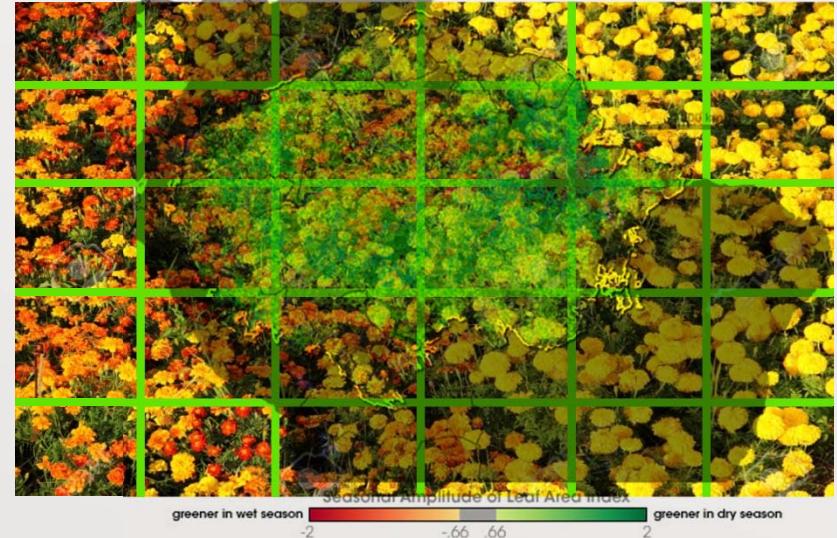
How about the likelihood function for the non-homogenous Poisson process of GRB detection

$$L(\text{DATA}|R(m)) = (\Delta m)^N \left[\prod_{i=1}^N R(m_i) \right] \exp \left(- \int_M R(m) dm \right)$$

$$L(\text{GRB DATA}|R(\boldsymbol{\theta})) = (\Delta \boldsymbol{\theta})^N \left[\prod_{i=1}^N R(\boldsymbol{\theta}_i) \right] \exp \left(- \int_{\boldsymbol{\Theta}} R(\boldsymbol{\theta}) d\boldsymbol{\theta} \right)$$

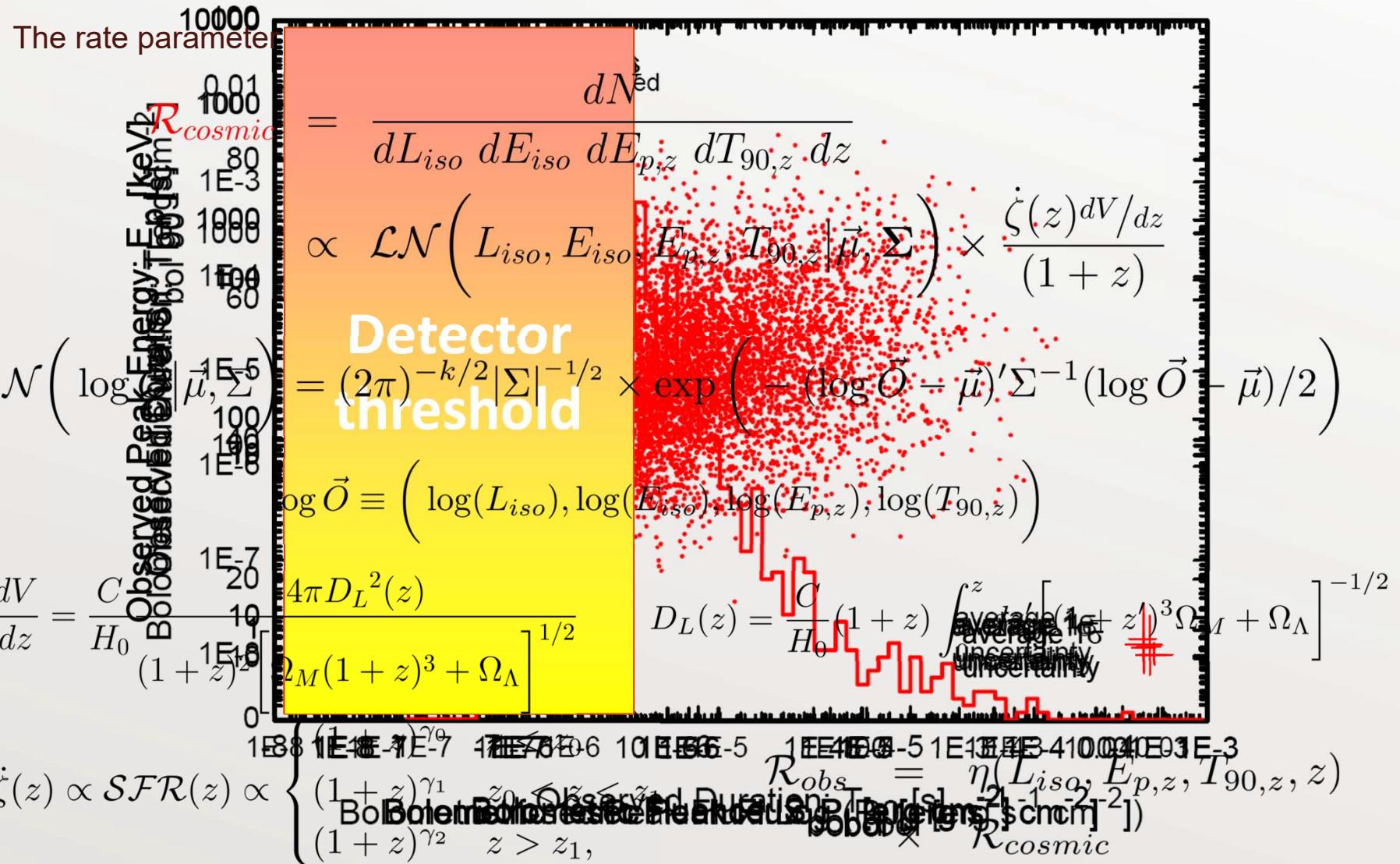
$$\boldsymbol{\theta} \equiv \vec{\theta} \equiv [E_{iso}, L_{iso}, E_{p,z}, T_{90,z}, z, t]$$

$$R(\boldsymbol{\theta}) = ?$$

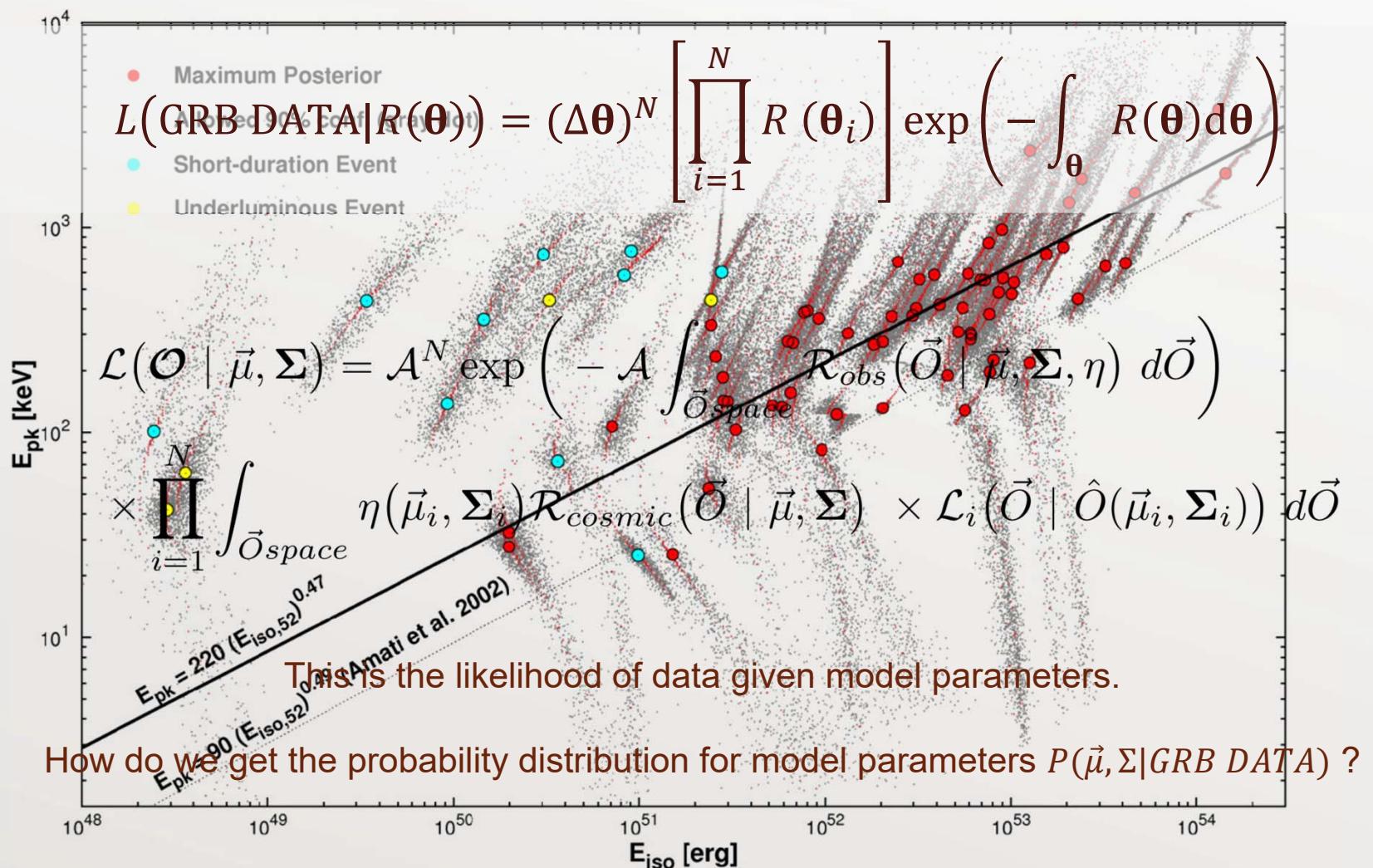


Multivariate Log-normal distribution

The simplest most natural model of GRB occurrence rate R_{cosmic} as a function of GRB properties ($E_{\text{iso}}, L_{\text{iso}}, E_{p,z}, T_{90,z}, z$)

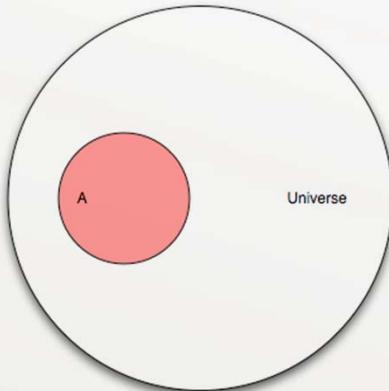


Observational data uncertainties are very important and must be taken into account

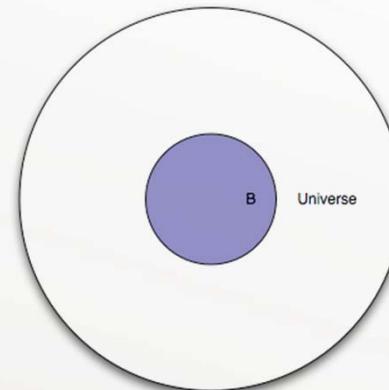


Bayes theorem

$$P(A) = \frac{A}{U}$$

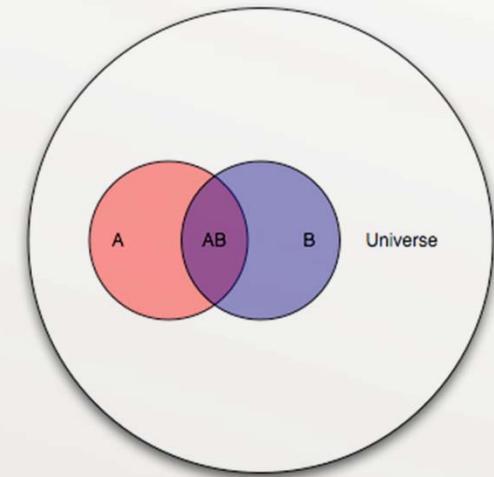


$$P(B) = \frac{B}{U}$$



$$P(A|B) = \frac{AB}{B} = \frac{\frac{AB}{U}}{\frac{B}{U}} = \frac{P(AB)}{P(B)}$$

$$P(AB) = \frac{AB}{U}$$



$$P(B|A) = \frac{AB}{A} = \frac{\frac{AB}{U}}{\frac{A}{U}} = \frac{P(AB)}{P(A)}$$

$$P(A|B) = \frac{P(A)P(B|A)}{P(B)}$$

The posterior probability density of model parameters

$$P(A|B) = \frac{P(A)P(B|A)}{P(B)}$$

$$\begin{aligned} \mathcal{L}(\mathcal{O} \mid \vec{\mu}, \Sigma) &= \mathcal{A}^N \exp \left(-\mathcal{A} \int_{\vec{O}_{space}} \mathcal{R}_{obs}(\vec{O} \mid \vec{\mu}, \Sigma, \eta) d\vec{O} \right) \\ &\times \prod_{i=1}^N \int_{\vec{O}_{space}} \eta(\vec{\mu}_i, \Sigma_i) \mathcal{R}_{cosmic}(\vec{O} \mid \vec{\mu}, \Sigma) \times \mathcal{L}_i(\vec{O} \mid \hat{O}(\vec{\mu}_i, \Sigma_i)) d\vec{O} \end{aligned}$$

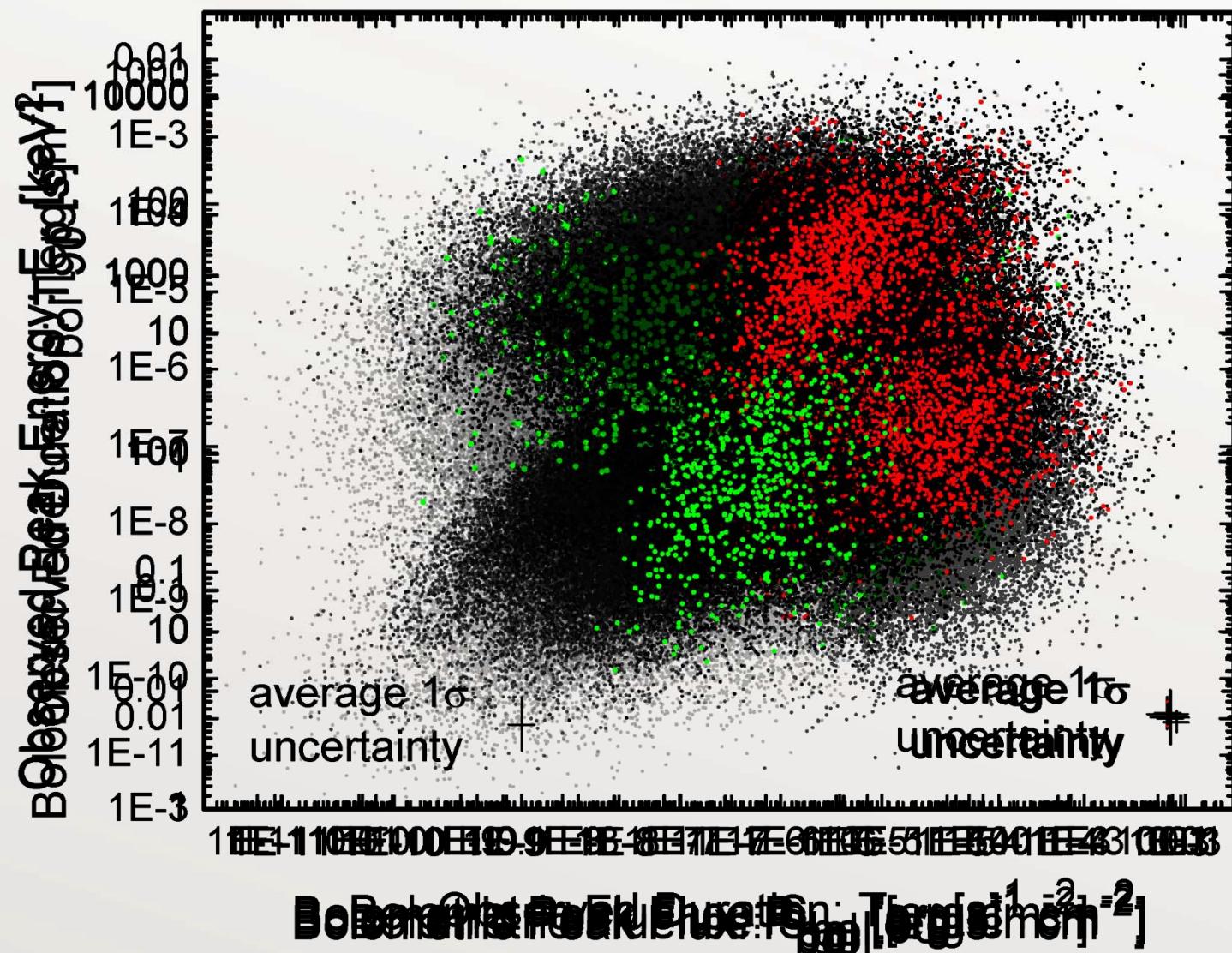
$$\mathcal{P}(\vec{\mu}, \Sigma | \mathcal{O}) = \mathcal{P}(\vec{\mu}, \Sigma) \times \mathcal{L}(\mathcal{O} | \vec{\mu}, \Sigma)$$

The 16-D parameter posterior density is sampled via an Adaptive Metropolis-Hastings Markov Chain Monte Carlo algorithm

www.shahmoradi.org/grb_world

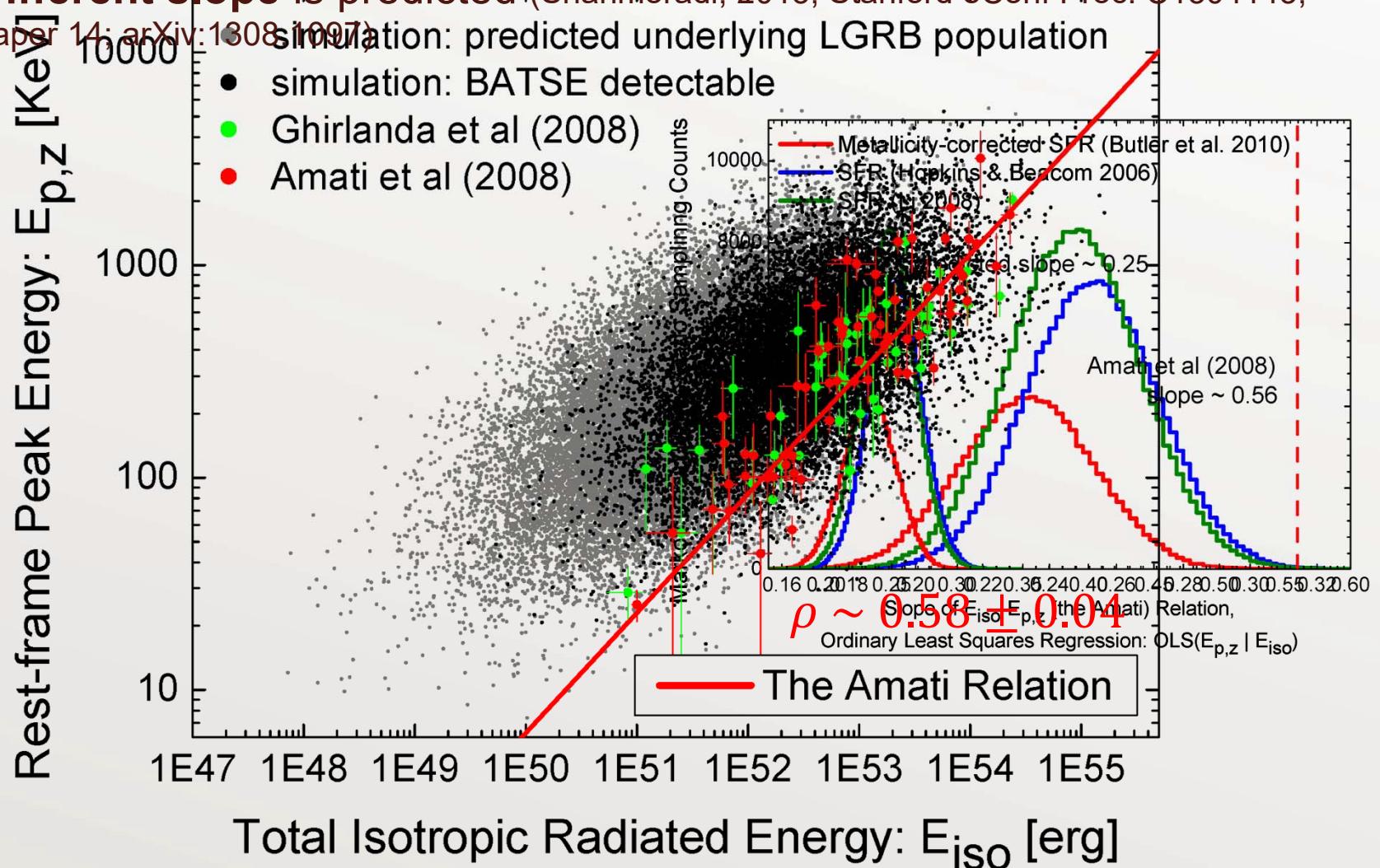


- Colors bear the same meaning in all plots:
- simulation: predicted underlying LGRB population
 - simulation: predicted underlying SGRB population
- 1366 BATSE LGRBs detected
 - 600 BATSE SGRBs detected
 - simulation: BATSE detectable

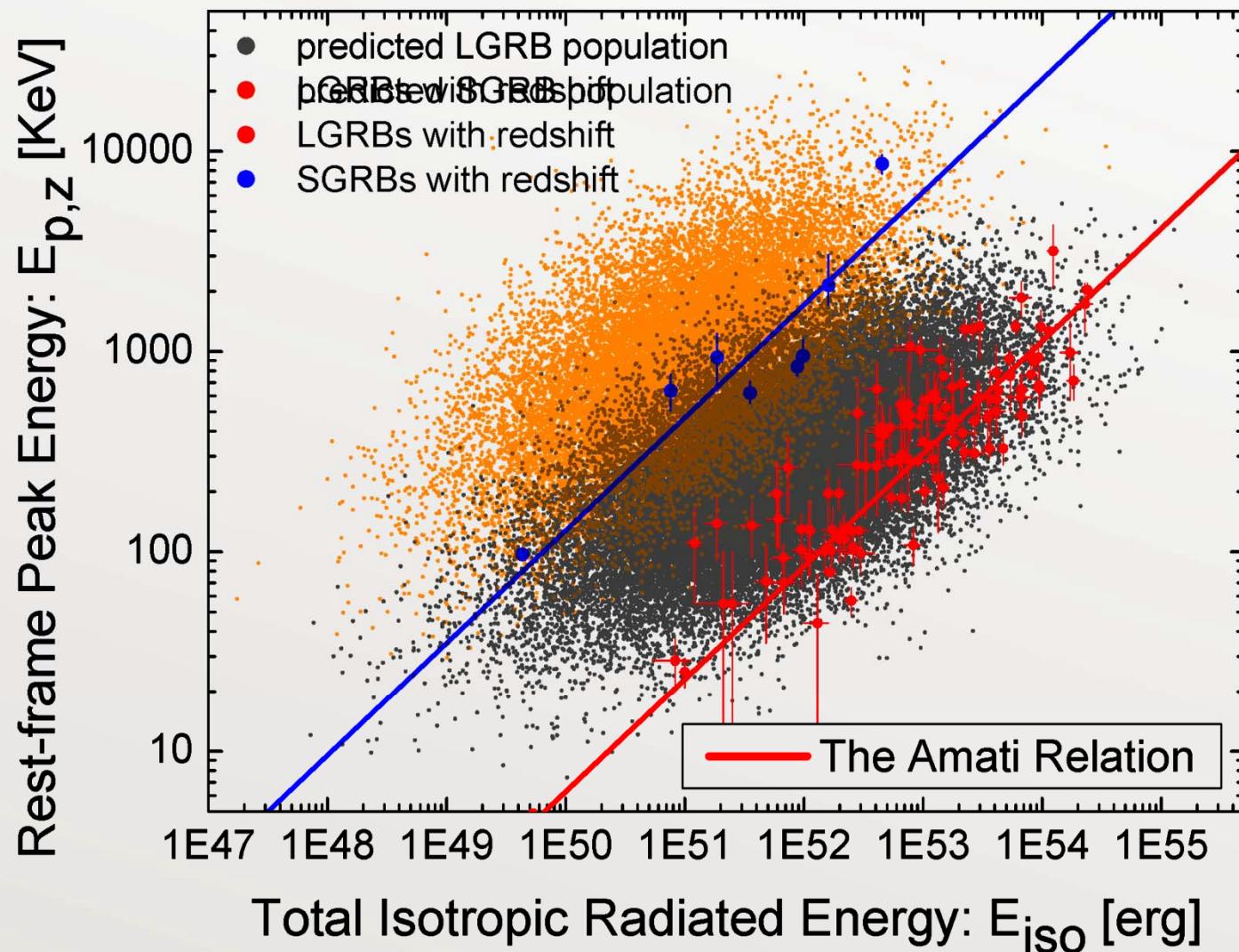


The Amati relation

- Larger dispersion is predicted (Shahmoradi, 2013, ApJ, 766, 111)
- Different slope is predicted (Shahmoradi, 2013, Stanford eConf Proc. C1304143, paper 14; arXiv:1308.1097)



Short and long GRBs exhibit similar prompt correlations



Summary for GRB astronomers

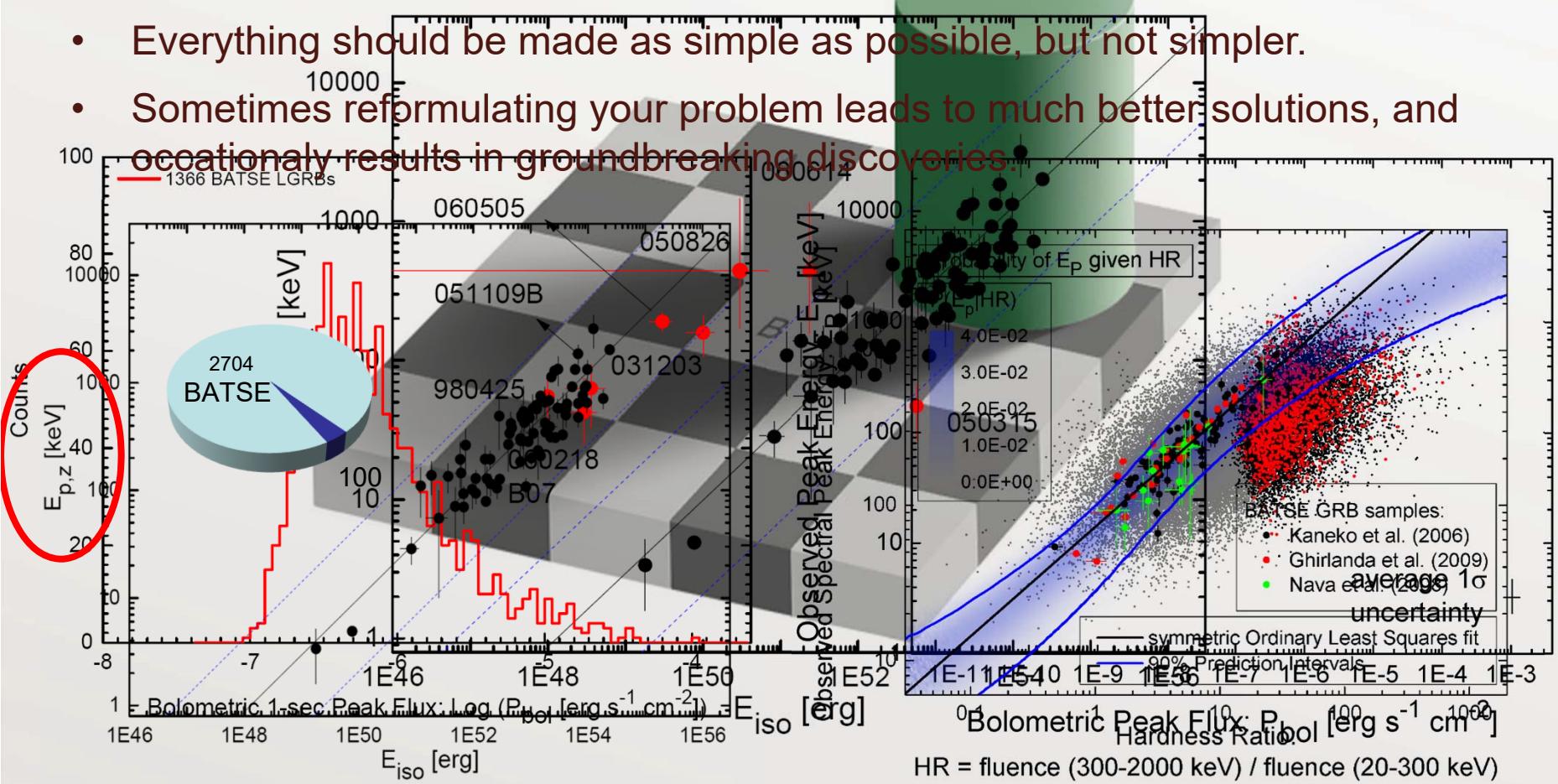
- Multivariate log-normal distribution provides good fit to BATSE short and long GRB prompt emission data (*peak luminosity, isotropic emission, intrinsic peak energy, intrinsic duration*).
- The Amati (E_{iso} - $E_{P,Z}$) relation is confirmed, but with significantly **higher dispersion** and **shallower slope** of the regression line (0.25 vs. 0.55).
- Short GRBs exhibit very similar prompt emission correlations to long GRBs prompt correlations.
- BATSE Long GRBs data favor, though do not necessitate, a cosmic rate tracing metallicity evolution consistent with a cutoff $Z/Z_{\odot} \sim 0.2\text{--}0.5$, assuming no luminosity–redshift evolution.
- The proposed method provides the most accurate, as of today, method of GRB classification based on prompt emission data.

Further results on GRB energetics & correlations

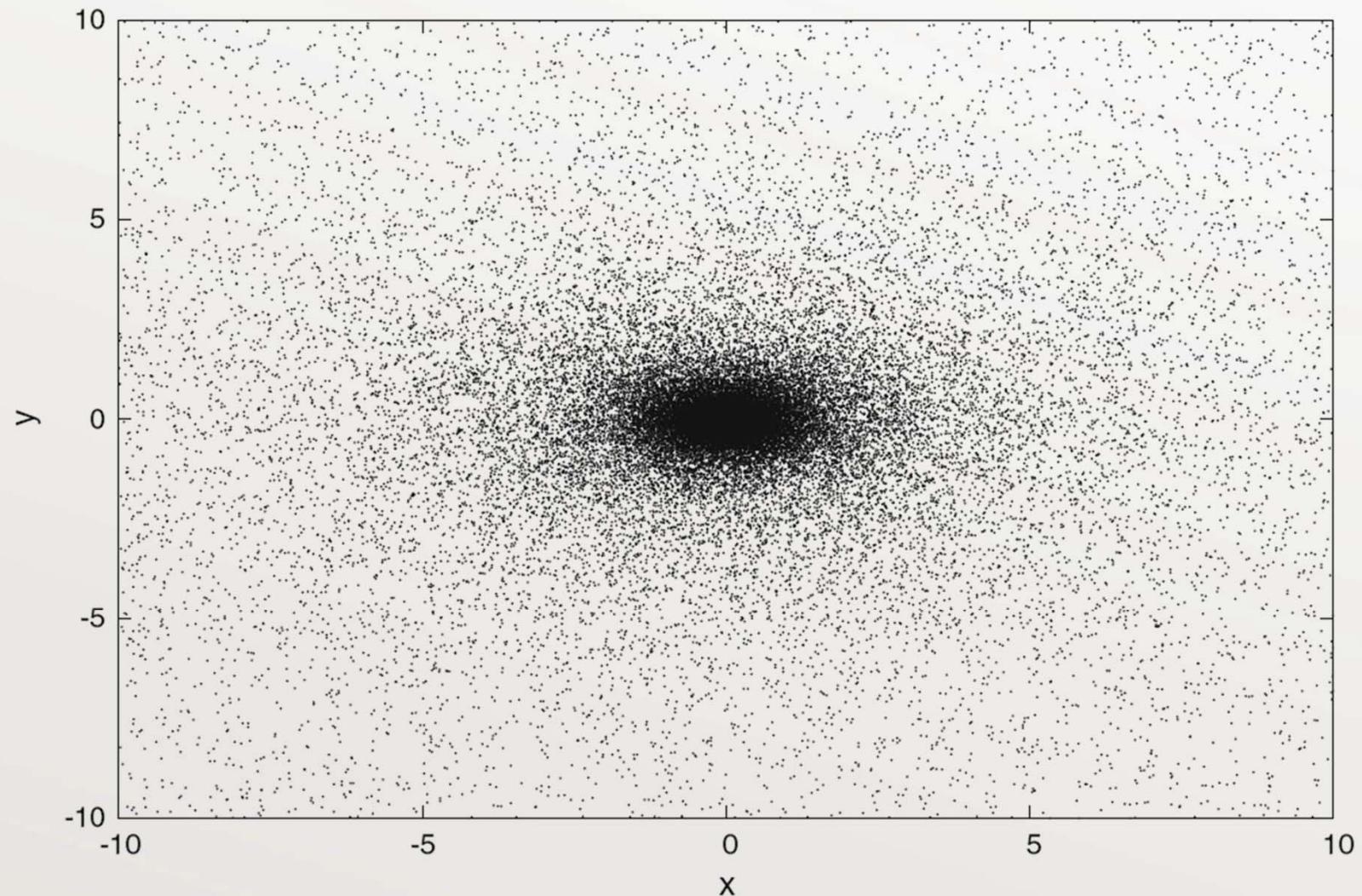
- Shahmoradi, 2013, ApJ, **766**, 111
- Shahmoradi, 2013, Stanford eConf Proc. C1304143, paper 14; arXiv:1308.1097
- Shahmoradi & Nemiroff, 2010, MNRAS, **407**, 2075–2090
- Shahmoradi & Nemiroff, 2011, MNRAS, **411**, 1843–1856
- Shahmoradi & Nemiroff, 2009, AIP Conf Proc, **1133**, 425

Summary: Lessons learned for everyday life (scientific & non-scientific)

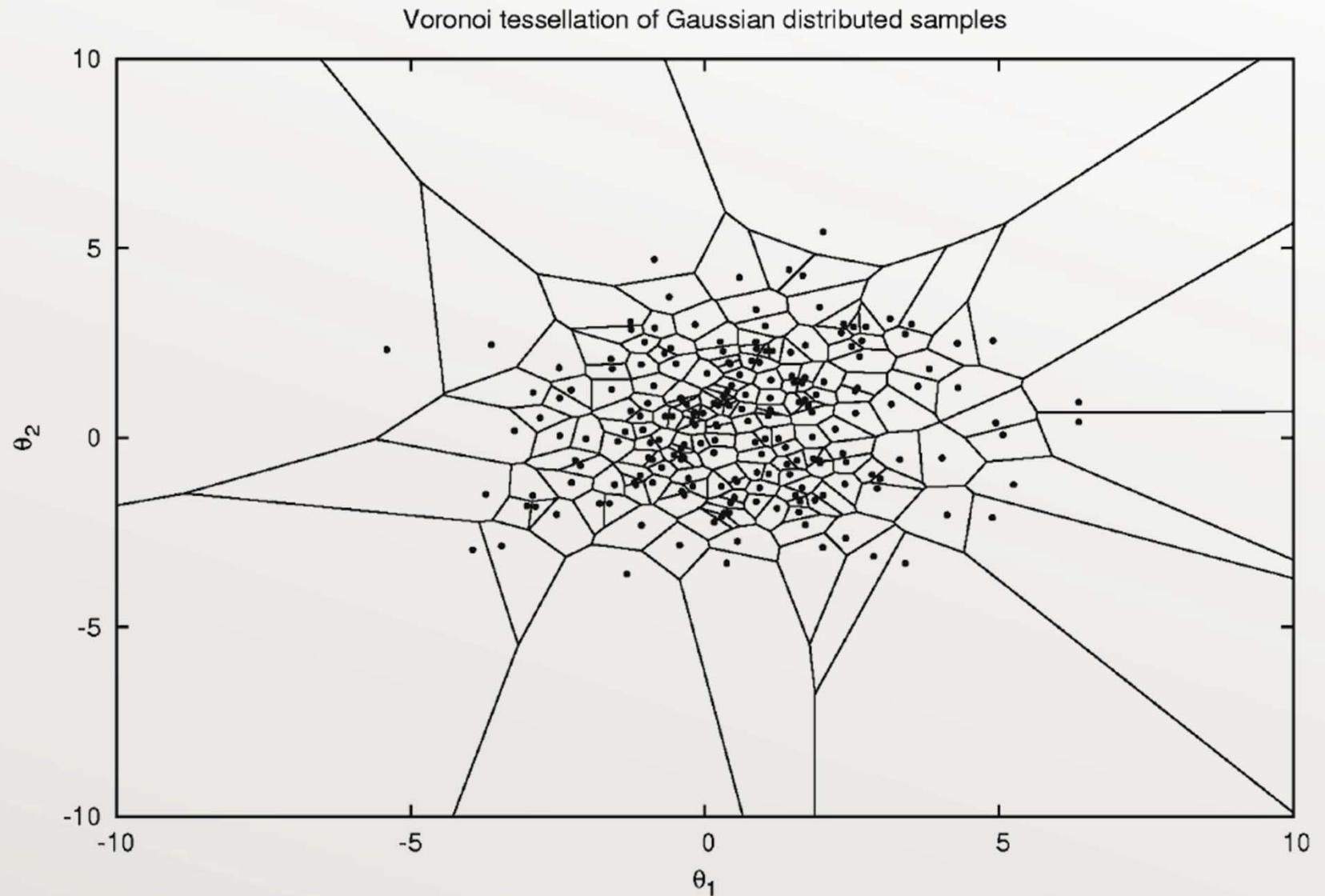
- Never underestimate human cognitive biases in scientific research and life in general
- If you obtain new data in your research that does not match your prior belief, do not discard it as bad-quality data.
- Everything should be made as simple as possible, but not simpler.
- Sometimes reformulating your problem leads to much better solutions, and occasionally results in groundbreaking discoveries.



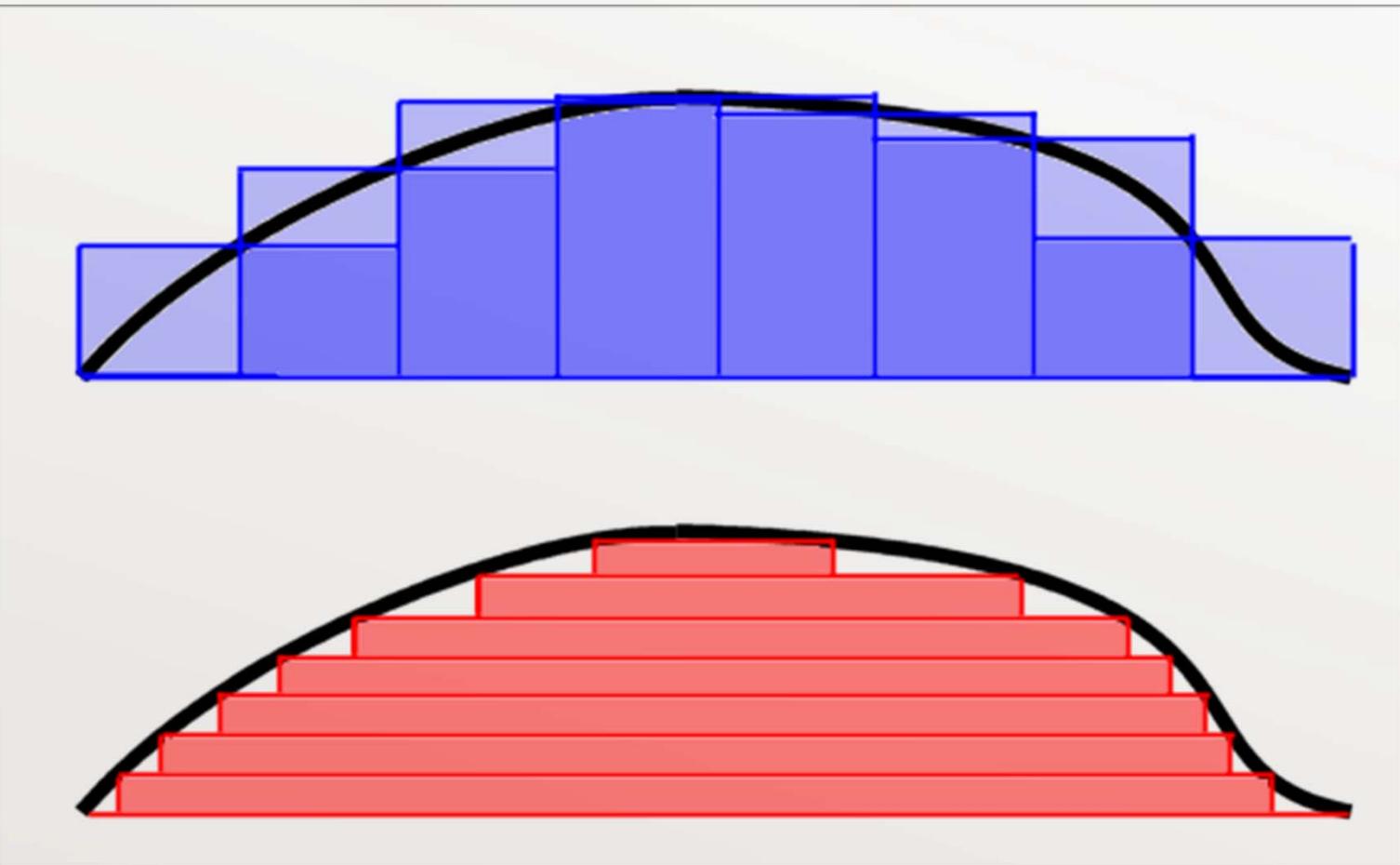
How to calculate evidence?



How to calculate evidence?



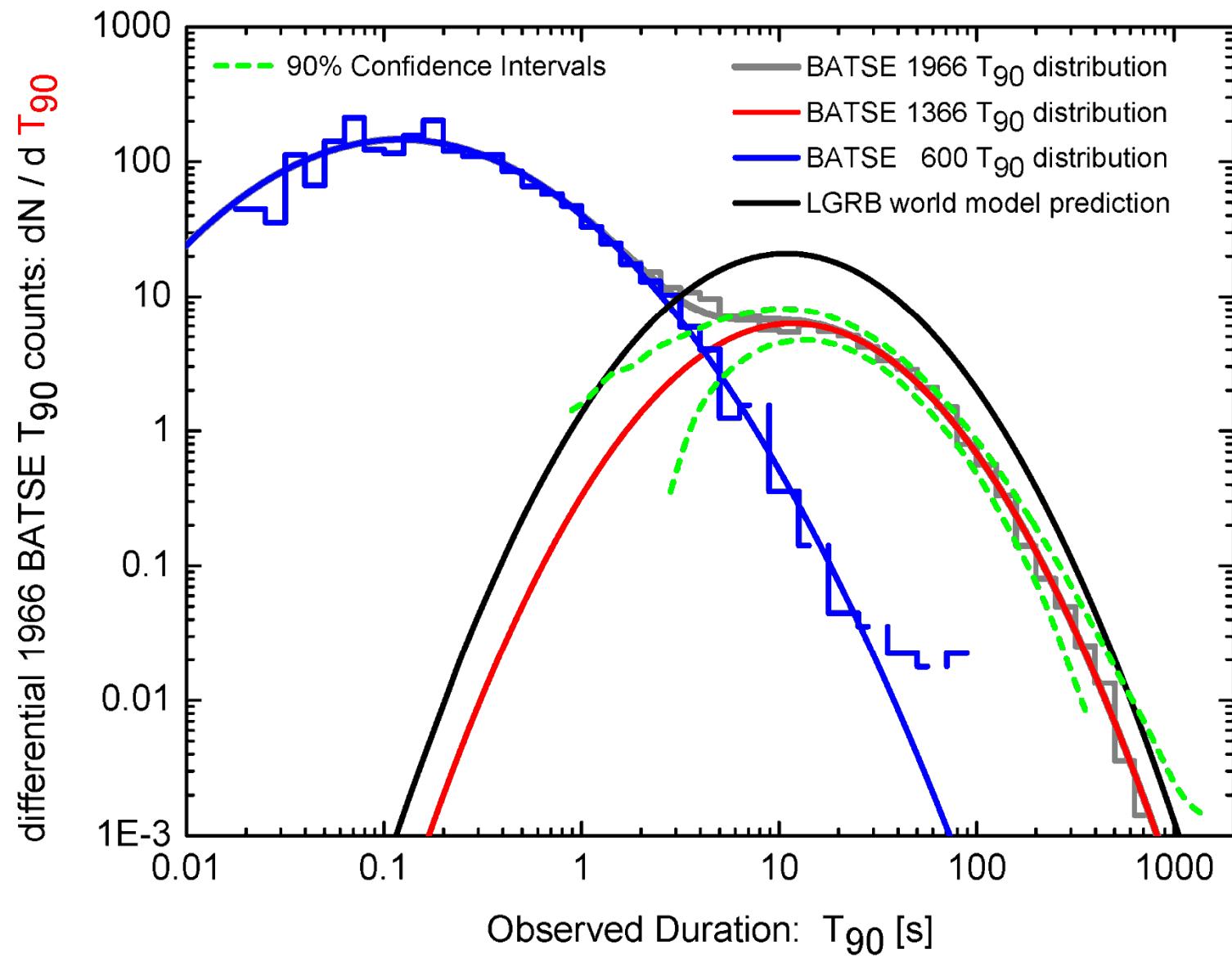
How to calculate evidence?



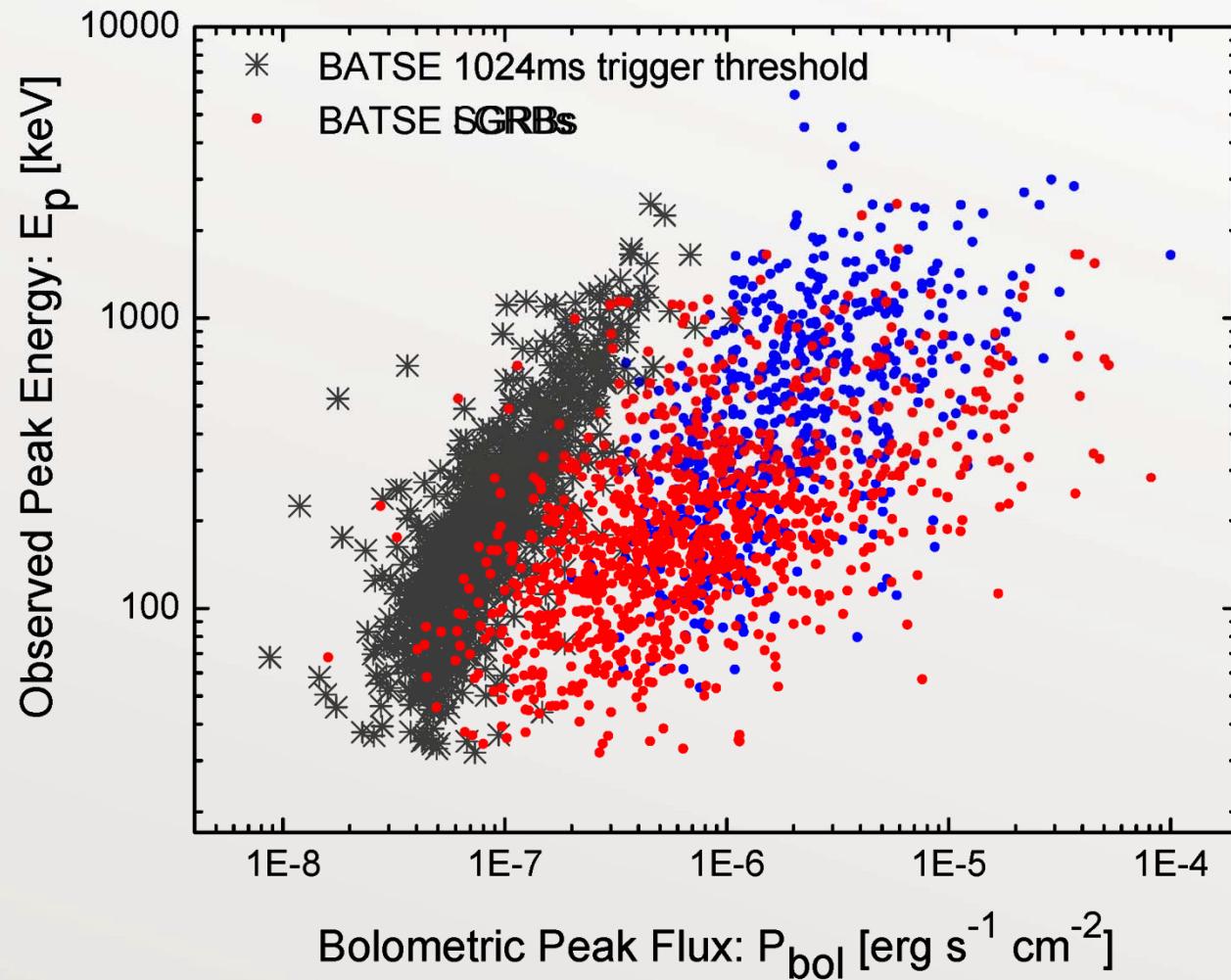
Short and long GRBs exhibit similar prompt correlations

Correlating Parameters	Long GRBs	Short GRBs
	Pearson correlation	Pearson correlation
Peak Luminosity – Isotopic Emission $L_{iso} - E_{iso}$	0.93	0.92
Peak Luminosity - Peak Energy $L_{iso} - E_{P,z}$	0.47	0.54
Peak Luminosity - Duration $L_{iso} - T_{90,z}$	0.43	0.55
Isotropic Emission - Peak Energy $E_{iso} - E_{P,z}$	0.58	0.61
Isotropic Emission - Duration $E_{iso} - T_{90,z}$	0.58	0.63
Peak Energy – Duration $E_{P,z} - T_{90,z}$	0.29	0.14

Intrinsic **prompt duration** and **peak energy** are **similarly** positively correlated with the peak luminosity and isotropic emission.



Model Construction - There is a need for multivariate Luminosity Functions (Shahmoradi & Nemiroff, 2011, MNRAS, 411, 1843–1856)



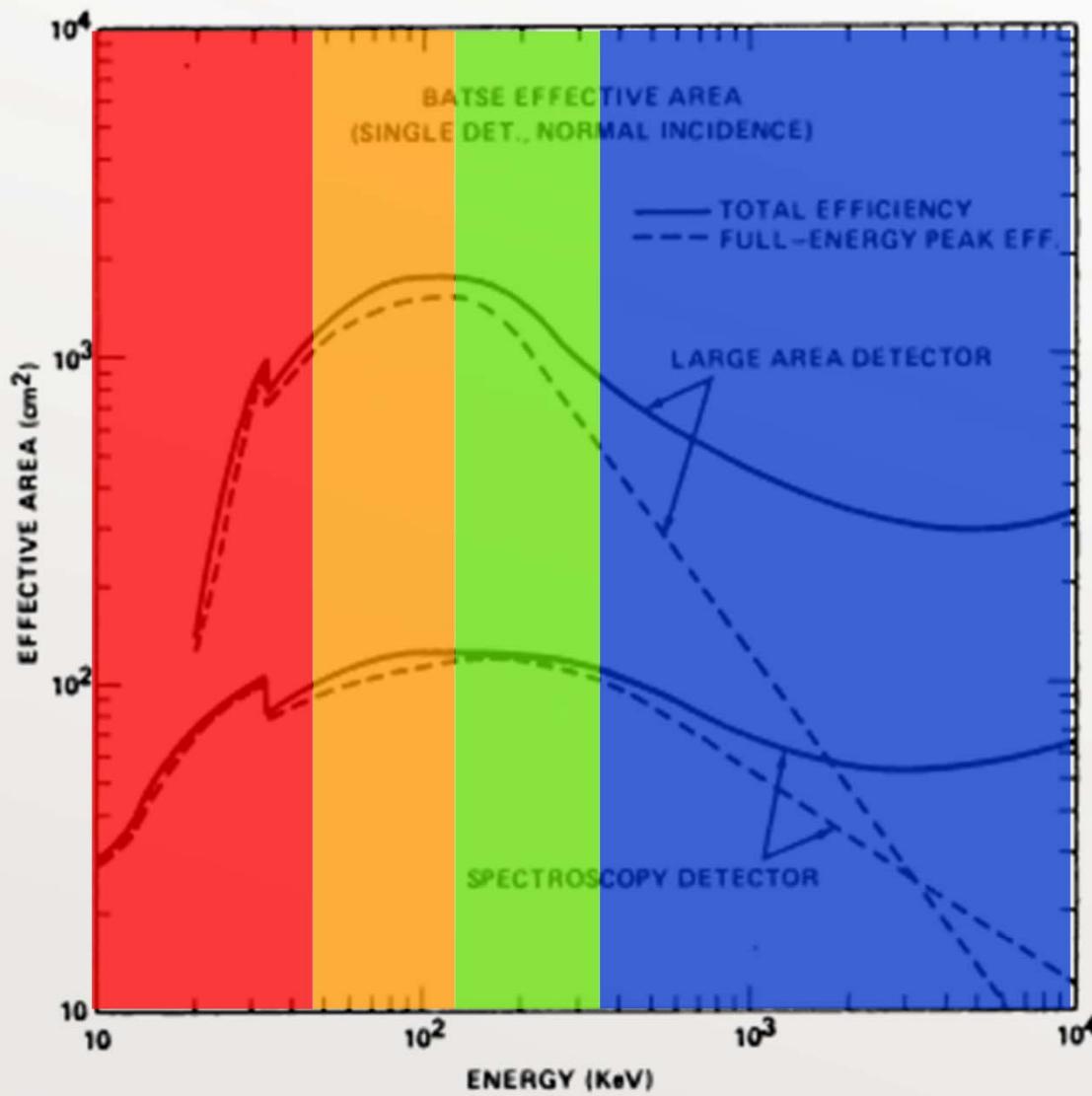
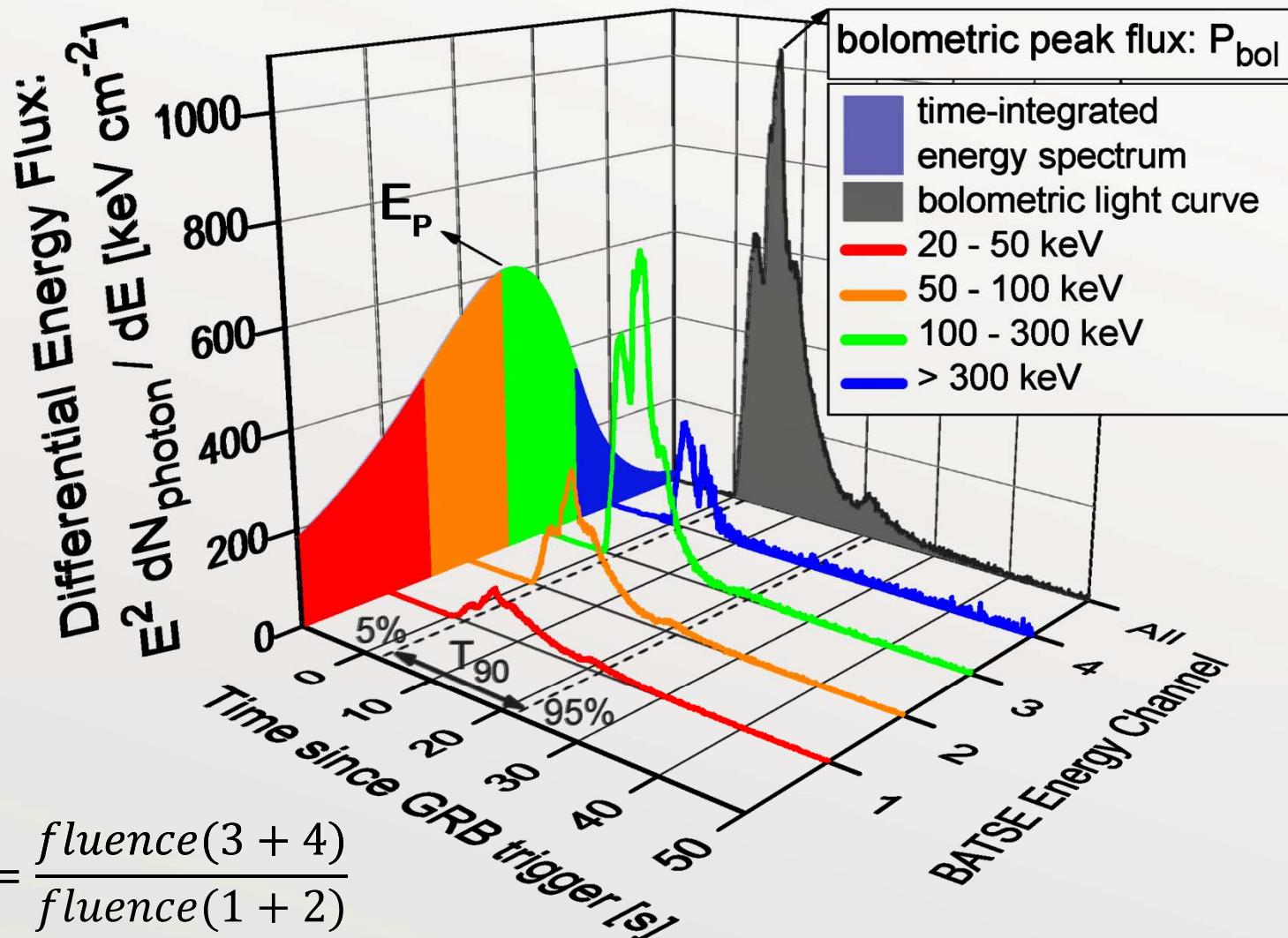


Figure 3

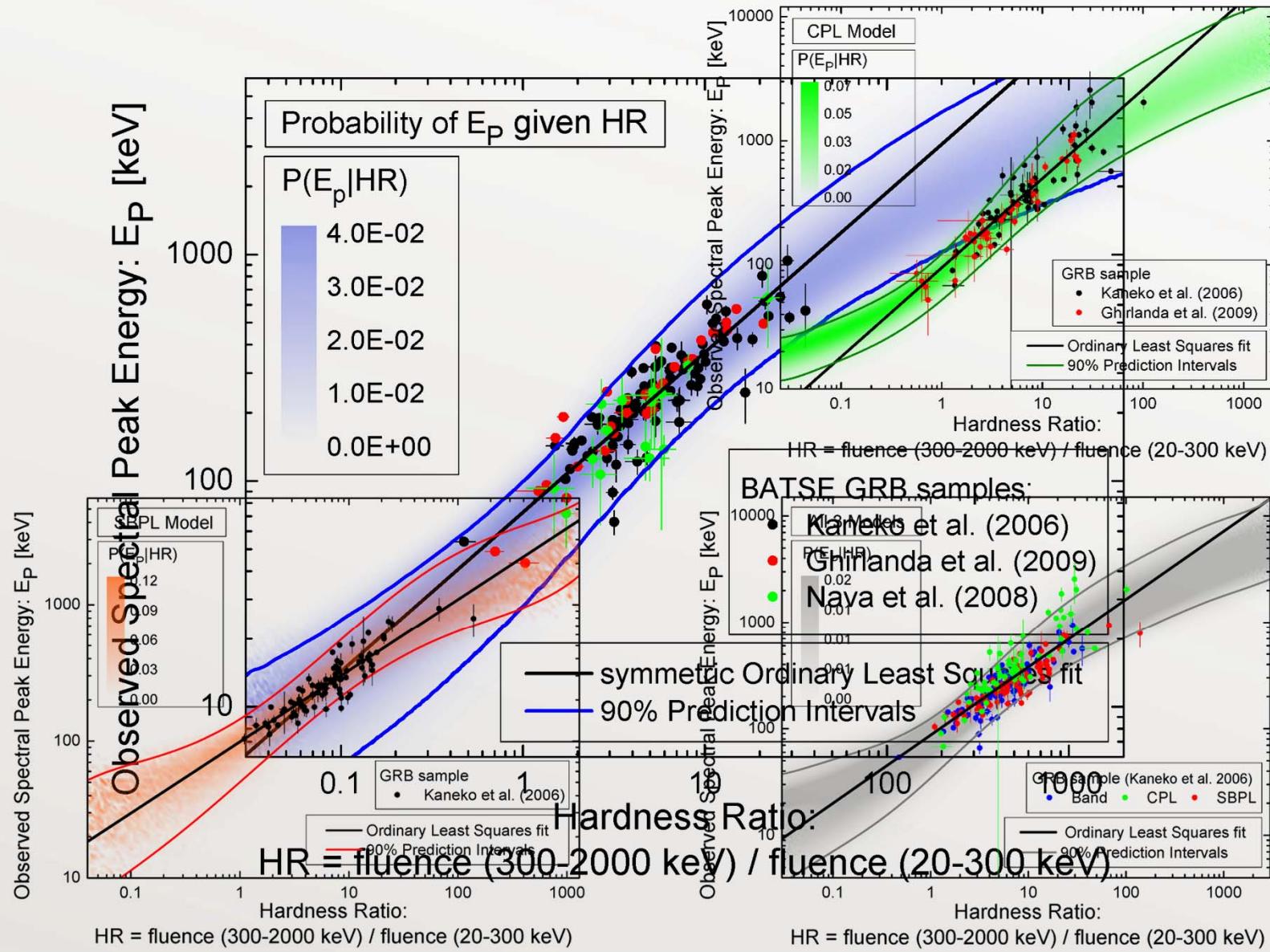
Example GRB lightcurve and spectrum

(BATSE GRB trigger 1085)



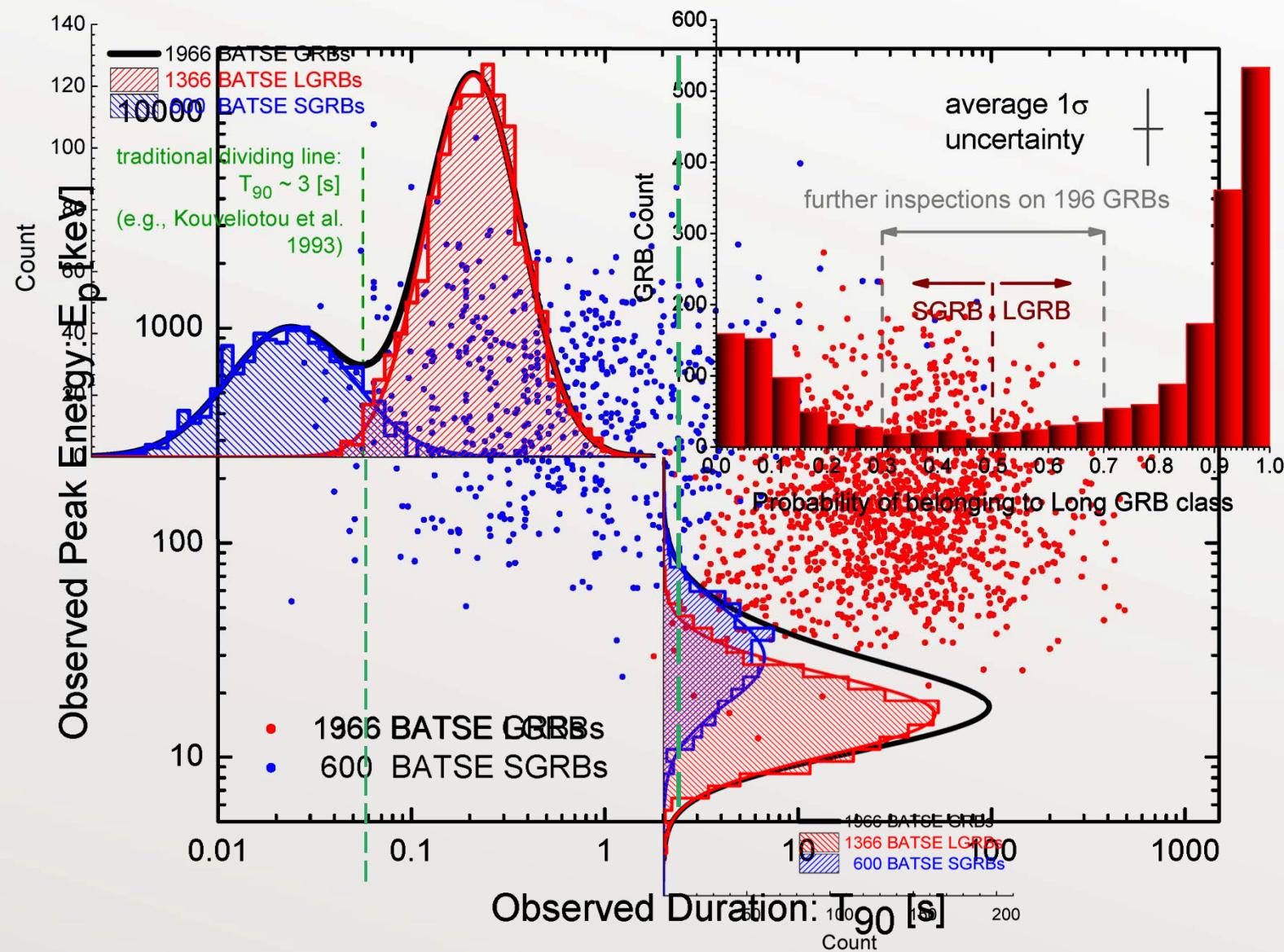
Hardness as spectral peak estimator for GRBs

(Shahmoradi & Nemiroff, 2010, MNRAS, **407**, 2075–2090)



Classification of BATSE GRBs: fuzzy clustering vs. cutoff line

(Shahmoradi & Nemiroff, 2011, MNRAS, 411, 1843–1856)



How do astronomers measure the expansion rate of the universe?

Recipe for measuring the expansion rate of the universe:

1. Assume a cosmological model.
2. Find a celestial object that has a known fixed luminosity (a **standard candle**) and measure its distance according to,

$$D_{L,obs} = \sqrt{\frac{1}{4\pi} \frac{\text{Intrinsic brightness}}{\text{observed brightness}}}$$

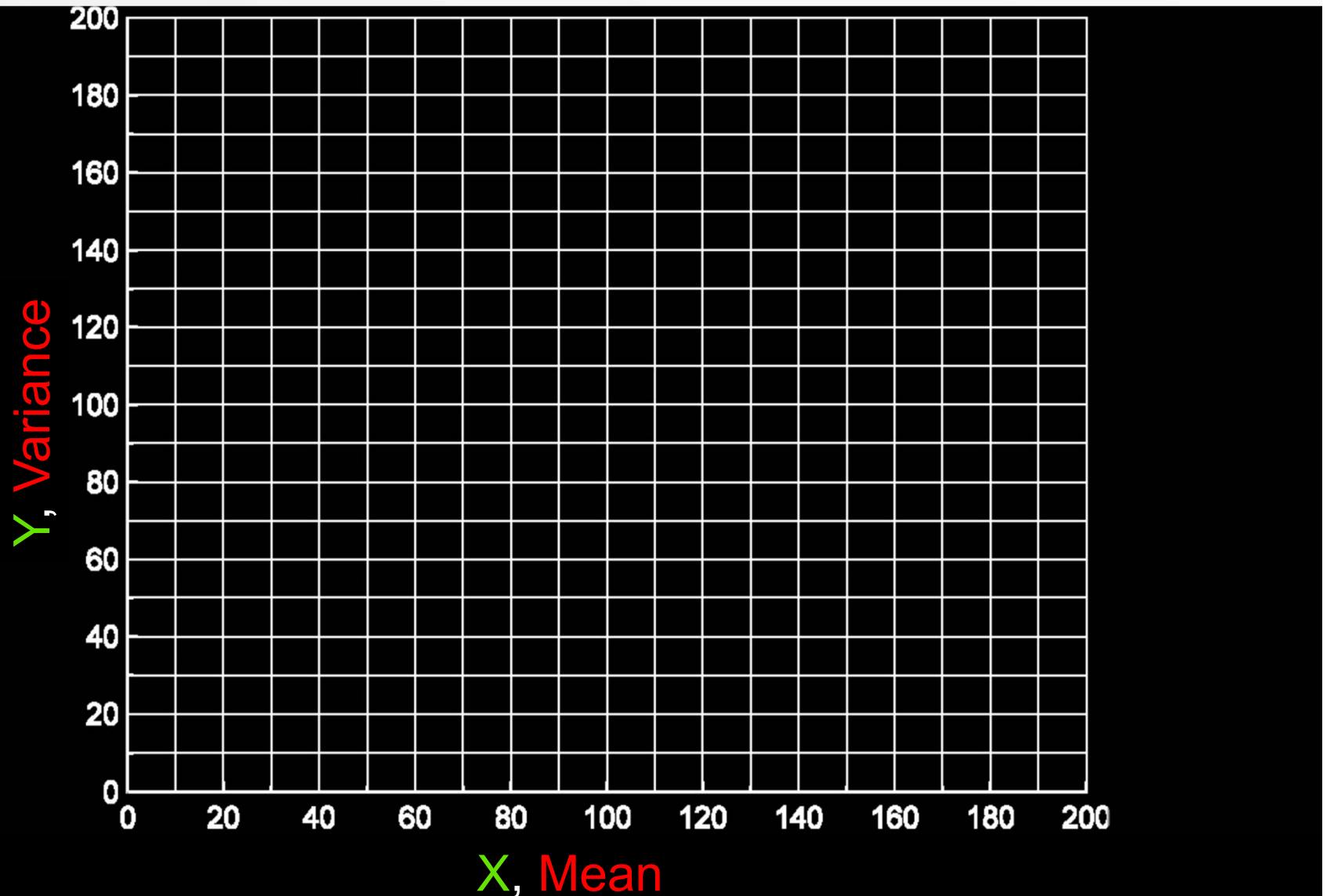


3. Somehow magically measure the redshift (z) of the standard candle. Then calculate,

$$D_{L,theory} = \frac{c}{H_0} (1 + z) \int_0^z \frac{dz'}{\sqrt{(1 + z')^3 \Omega_M(z') + \Omega_\Lambda(z')}}$$

4. Now compare $D_{L,obs}$ with $D_{L,theory}$.

Hallmark of Poisson Stochastic Process: Equal mean and variance of sample



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