

How Real Detector Thresholds Create False Standard Candles

Amir Shahmoradi

Research Scientist Associate / Peter O'Donnell, Jr. Fellow
Institute for Computational Engineering and Sciences
The University of Texas at Austin

presented at

Department of Physics
Sharif University of Technology

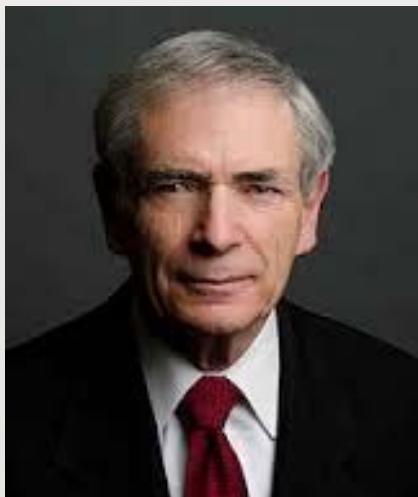
Tehran, May 1 2016

Collaborators



Robert J. Nemiroff

Astrophysicist, NASA Goddard Space Flight Center
Professor of Physics, Michigan Tech University
Editor, Astronomy Picture of the Day (APOD)



J. Tinsley Oden

Associate Vice President for Research, University of Texas at Austin
Director, Institute for Computational Engineering and Sciences
Cockrell Family Regents' Chair in Engineering No. 2, UT Austin
Peter O'Donnell Jr. Centennial Chair in Computing Systems, UT Austin
Professor of Aerospace Engineering and Engineering Mechanics
Professor of Computer Science, UT Austin
Professor of Mathematics, UT Austin

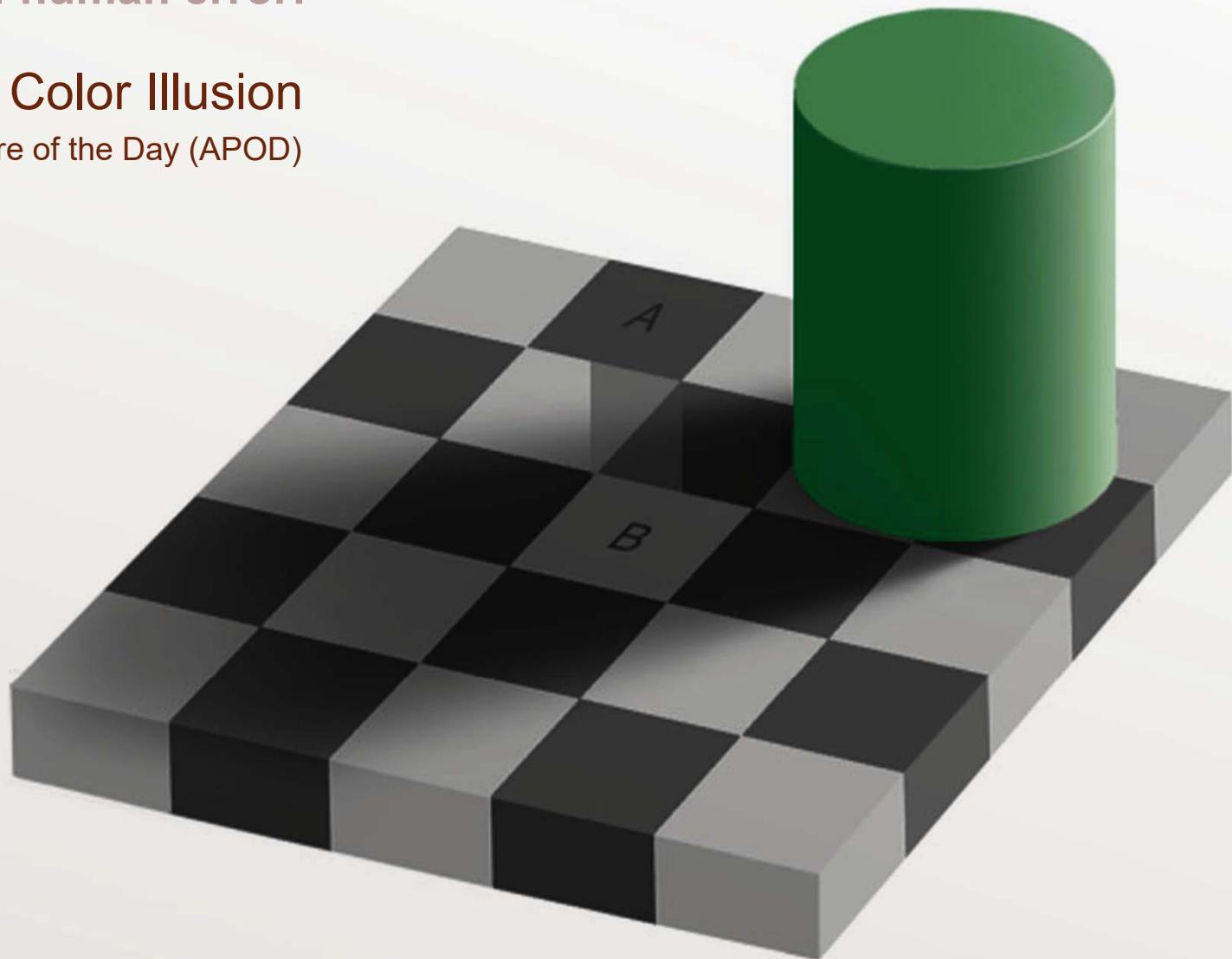
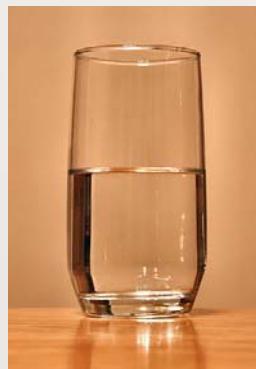
Cognitive biases are everywhere in human life

Example of human error:

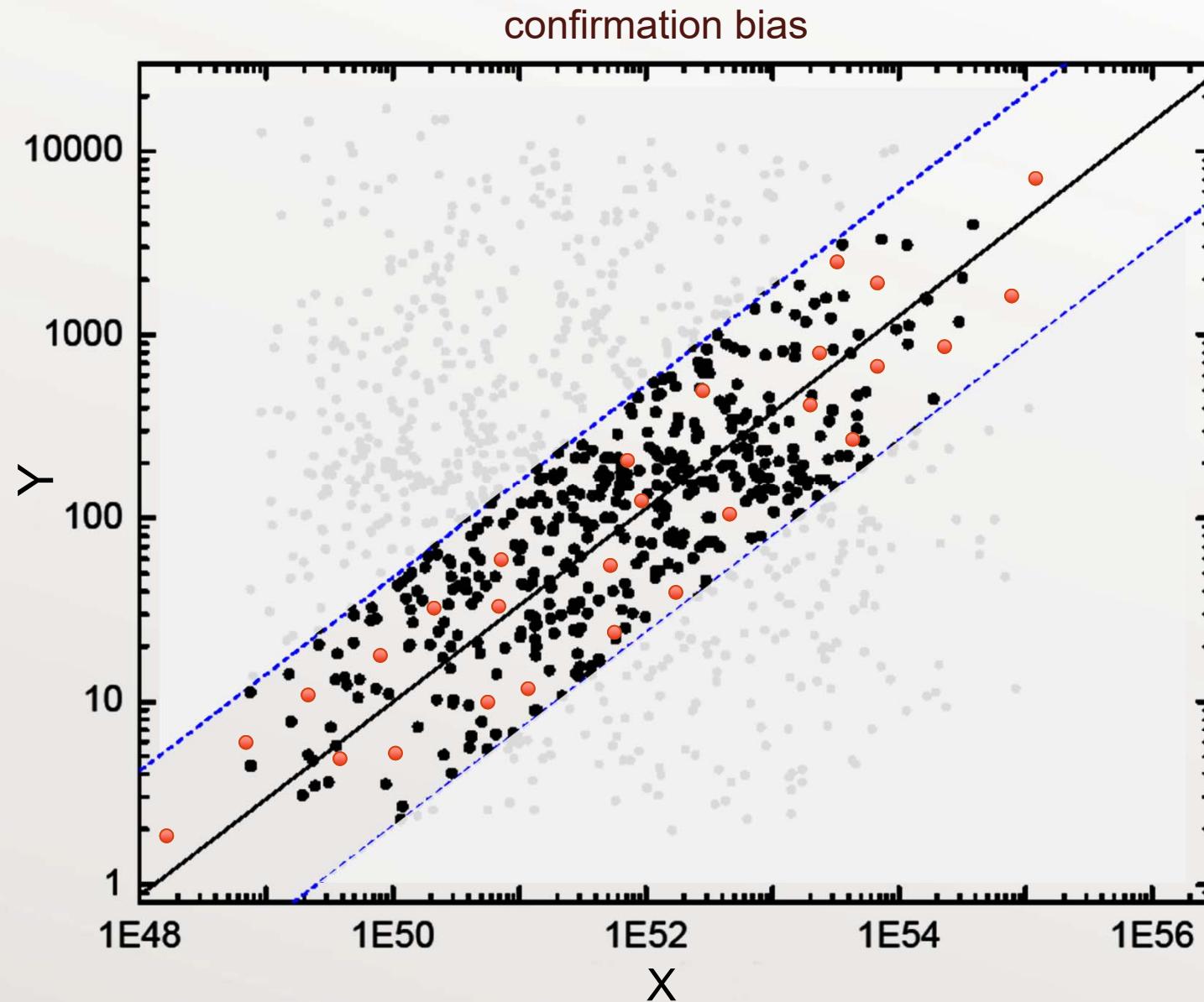
The Same Color Illusion

Astronomy Picture of the Day (APOD)
2007 July 17

half full? or
half empty?

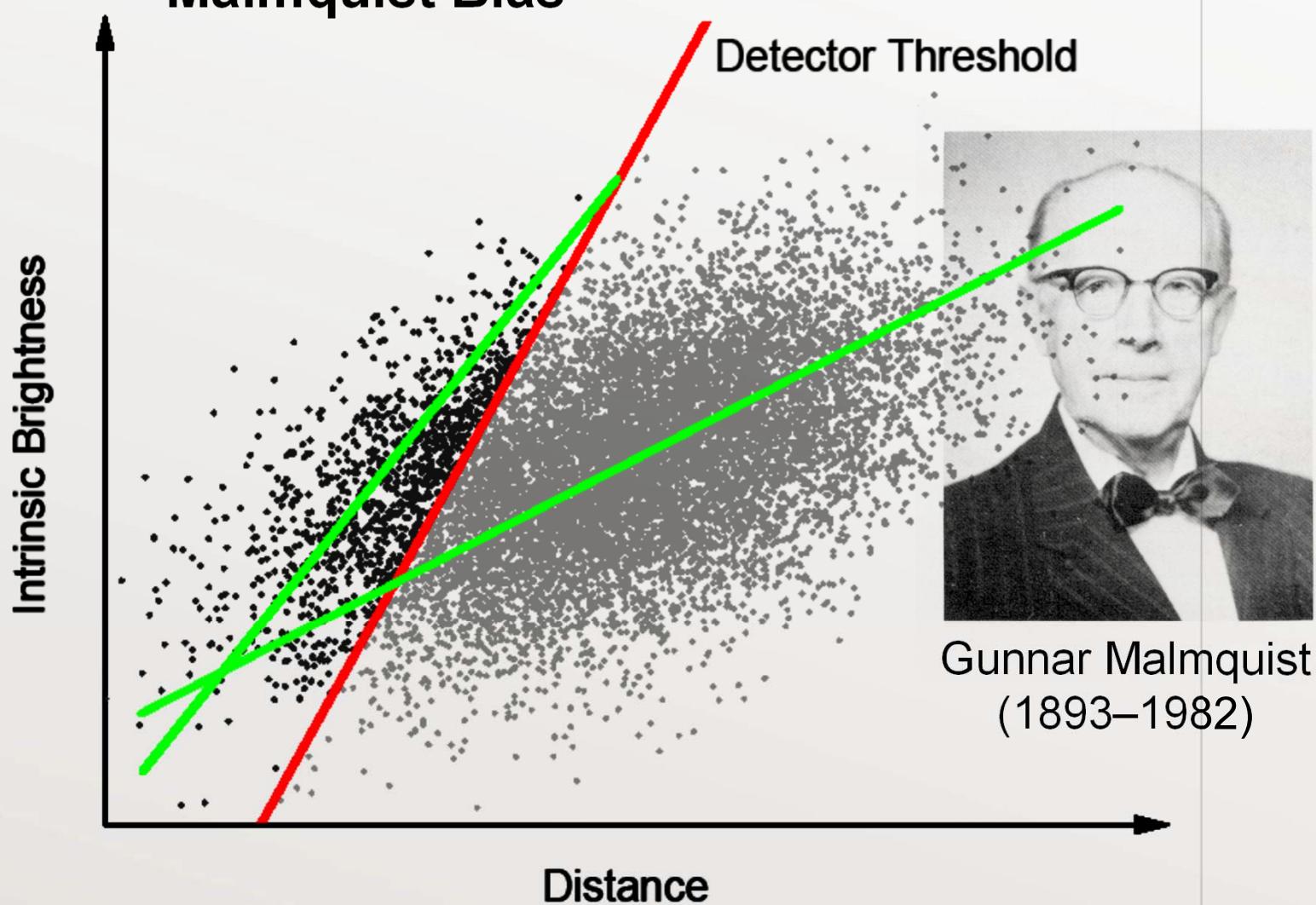


Statistical tests are often unable to capture human/instrumental biases



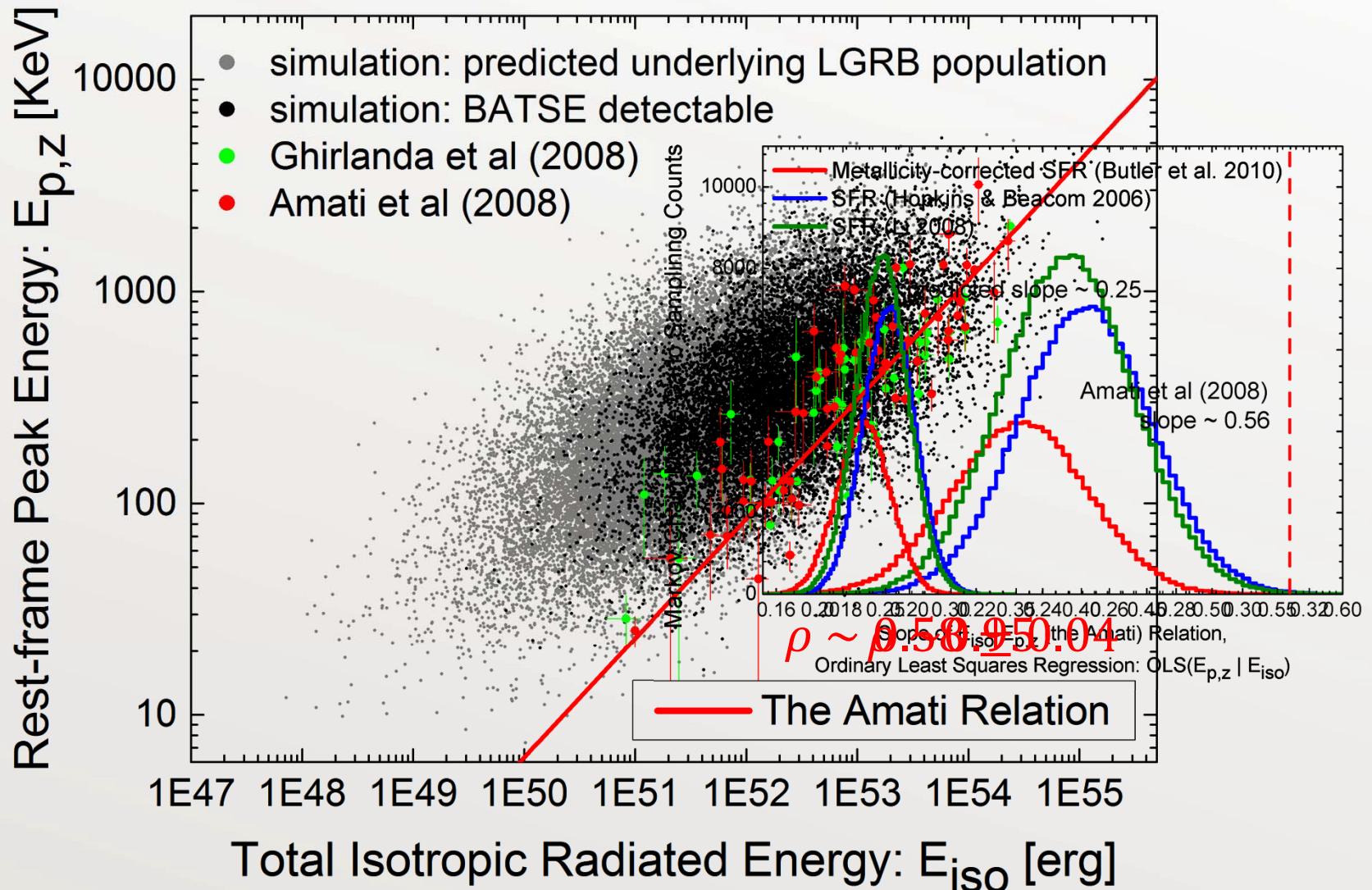
Instrumental bias: well-known in the field of Astronomy

Example of Instrumental bias Malmquist Bias



The Amati Relation

A combination of human biases, gamma-ray detector limitations, and sample incompleteness, as well as some real physics behind it.



Overview

- I. Why are Gamma-Ray Bursts (GRBs) of interest to cosmologists?
- II. What are Gamma-Ray Bursts?
- III. Can we use GRBs as standard candles in cosmology?
- IV. Take-home message for all scientists in any field of science

I. Why are Gamma-Ray Bursts (GRBs) of interest to cosmologists?

Short answer:

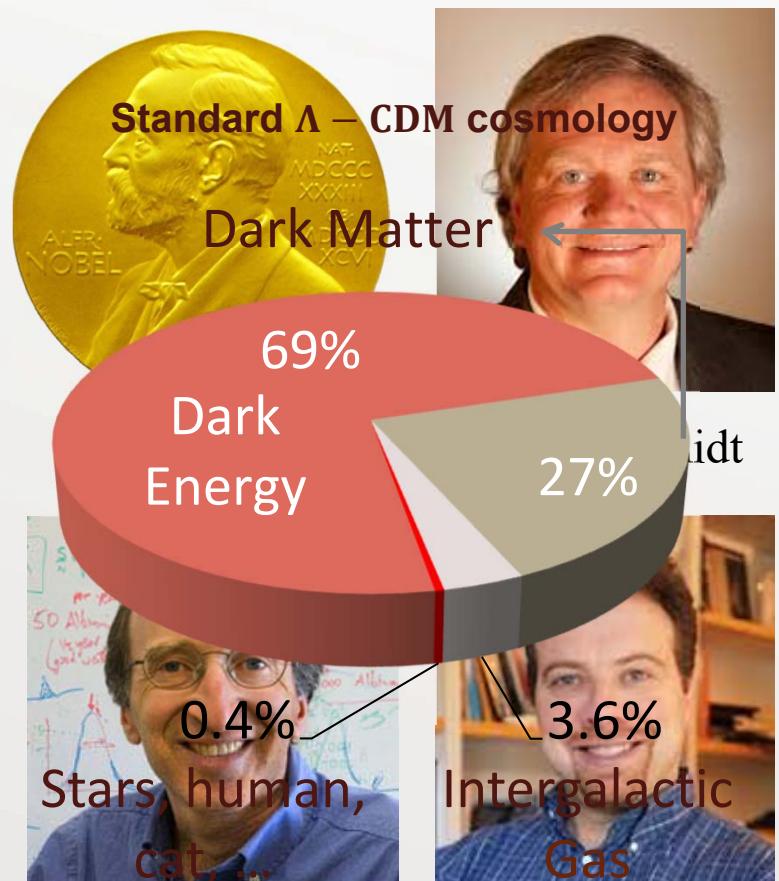
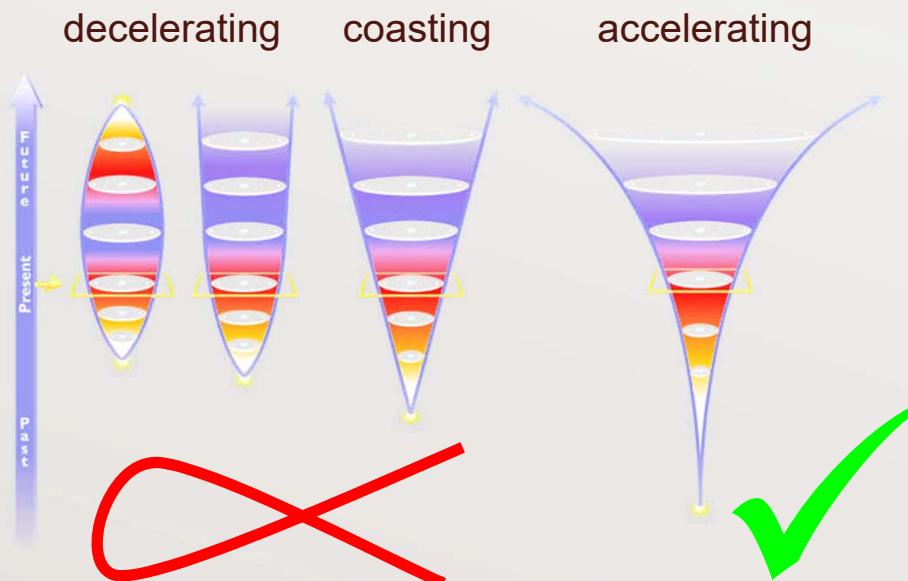
Since GRBs can be **potentially** used to test and validate cosmological models.

2011 Nobel Prize in Physics

The discovery of the accelerating expansion of the Universe

- Riess et al., 1998, ApJ, **116**, 1009-1038
- Perlmutter, 1999, ApJ, **517**, 565-586

Possible models of expanding universe



Saul Perlmutter

Adam Riess

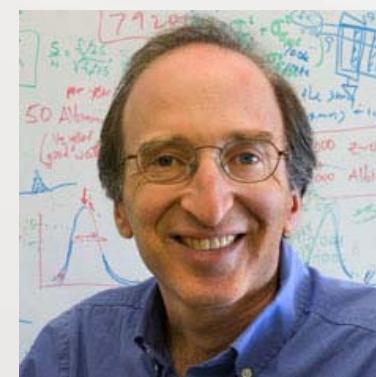
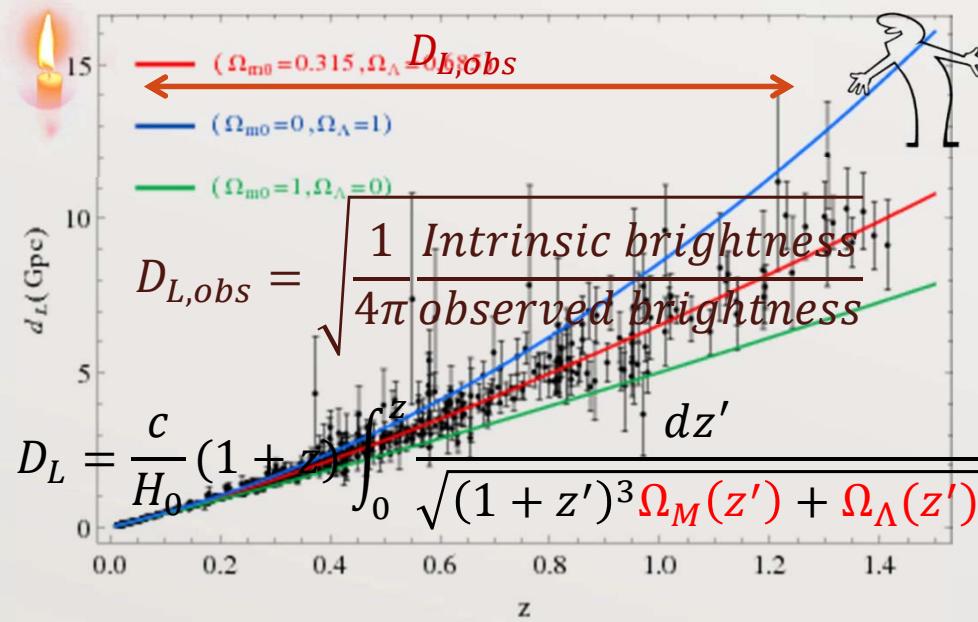
2011 Nobel Prize in Physics

What did these gentlemen do to get the Nobel prize?

1. Find a cosmological standard candle (supernova Ia).
2. Measure their distances from the earth ($D_{L,obs}$).
3. Measure their redshifts (z), as well.
4. Given their redshifts and a cosmological model, calculate their theoretical distance (D_L) from the earth.
5. Compare D_L with $D_{L,obs}$.



Brian Schmidt

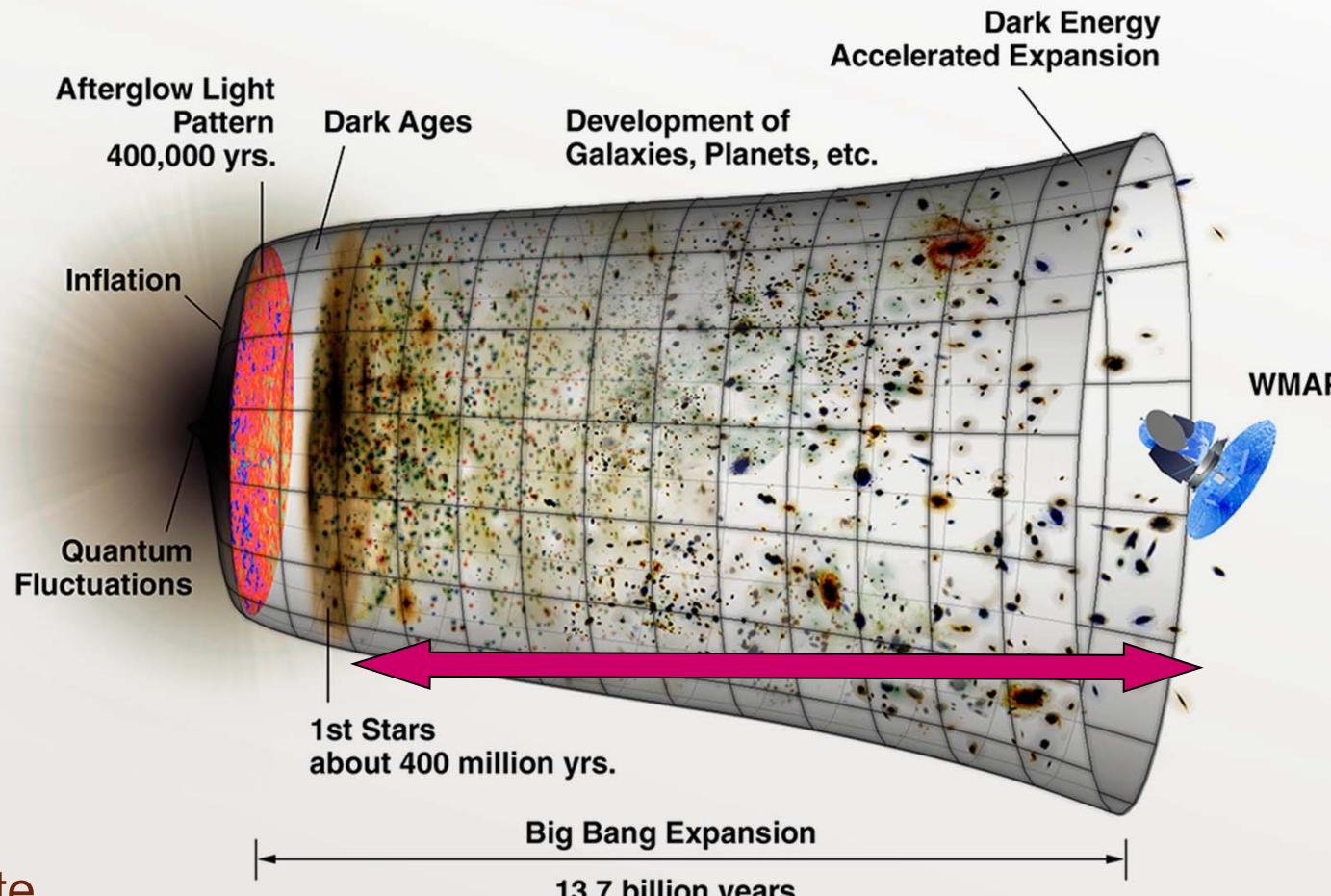


Saul Perlmutter



Adam Riess

Major problem with supernovae-Ia as standard candles? Limited detectability out to $z \sim 1.7$



Candidate
Standard Candle:
Gamma-Ray Bursts: $Z < 65$

Supernovae projects: $Z < 1.7$

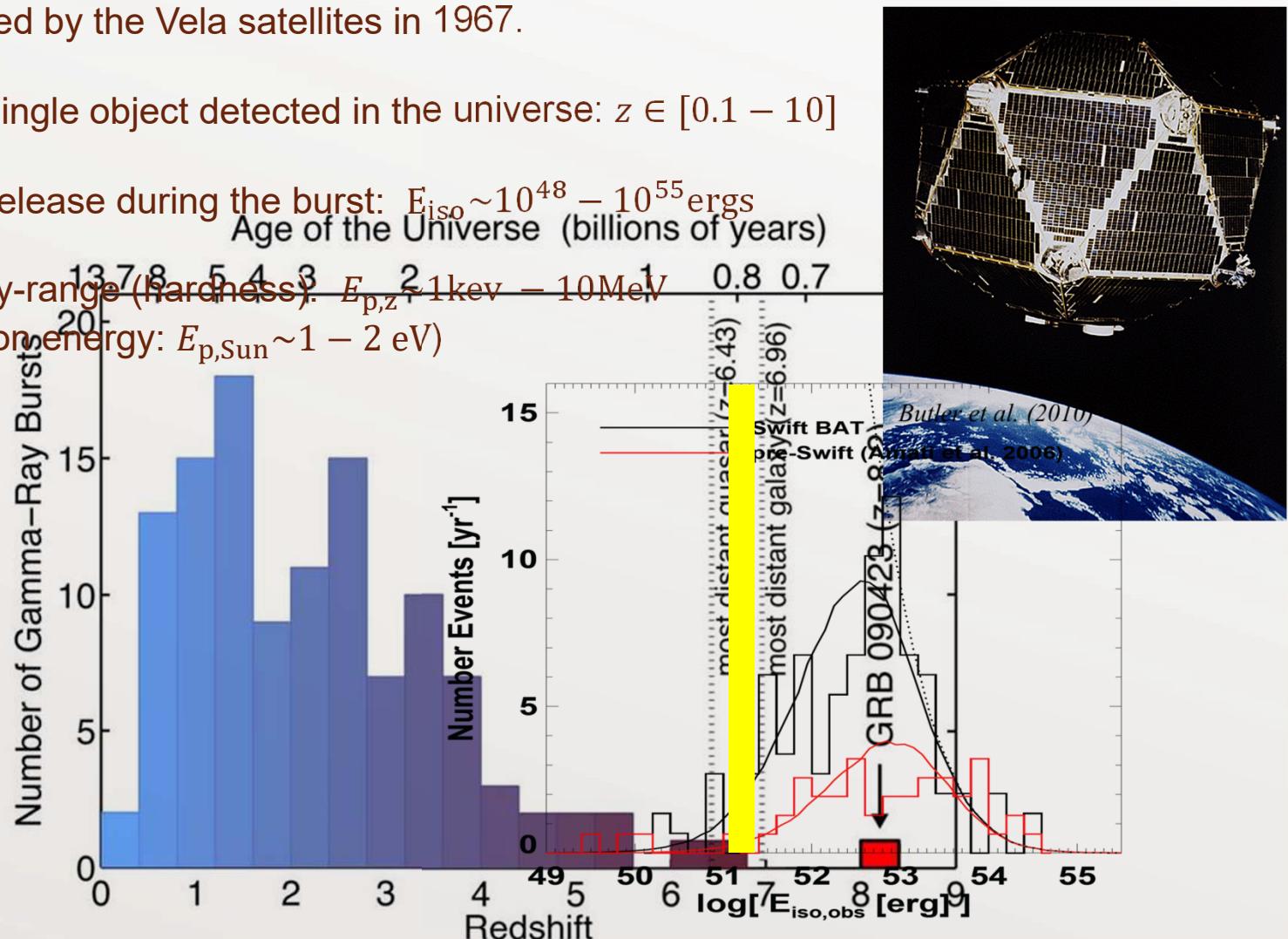
II. What are Gamma-Ray Bursts (GRBs)?

Short answer:

The brightest most powerful electromagnetic explosions in the universe,
ever observed by humans.

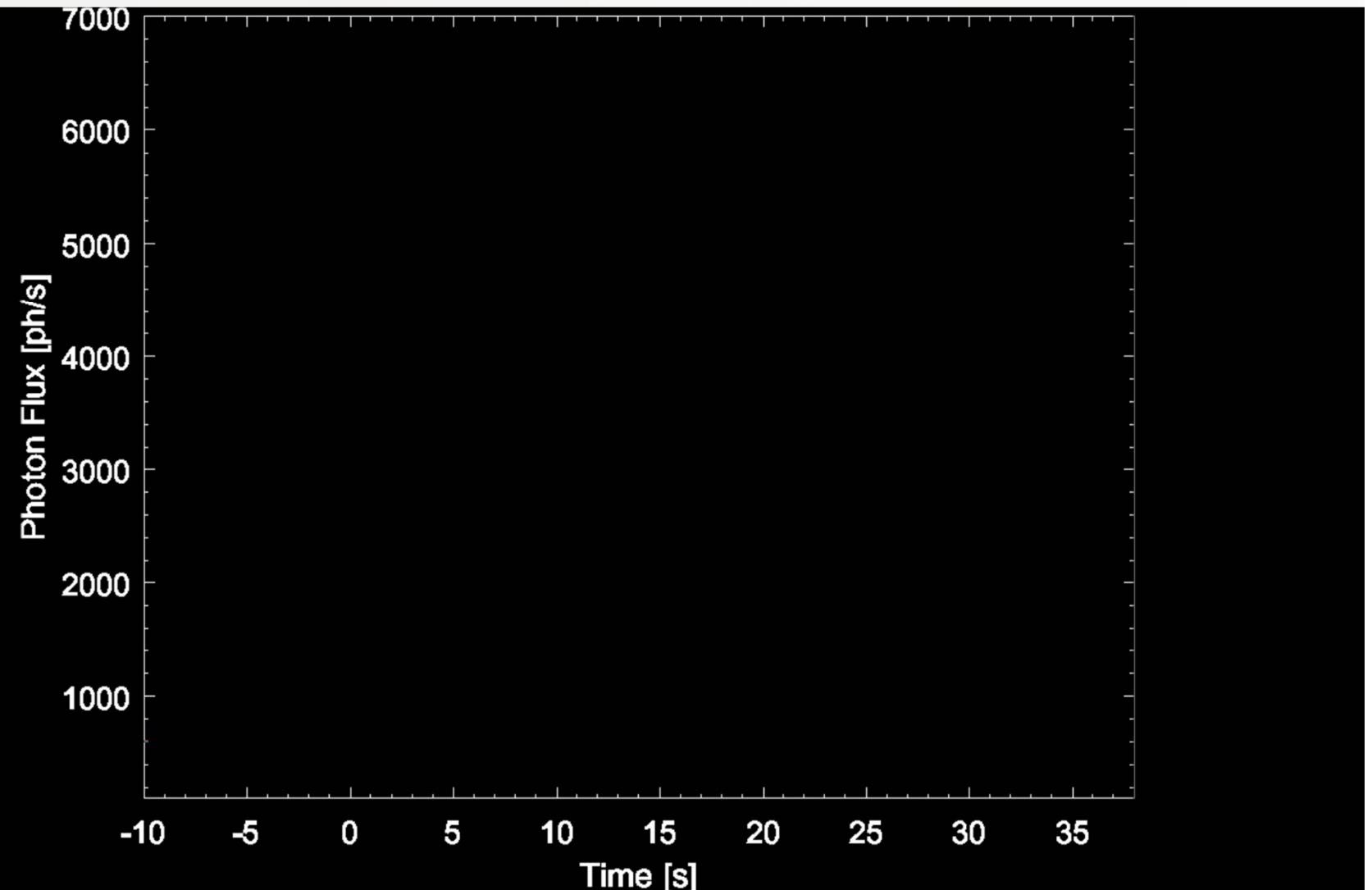
Gamma-ray bursts are flashes of gamma rays associated with extremely energetic explosions that have been observed in distant galaxies.

- First discovered by the Vela satellites in 1967.
- Most distant single object detected in the universe: $z \in [0.1 - 10]$
- Total energy release during the burst: $E_{\text{iso}} \sim 10^{48} - 10^{55} \text{ ergs}$
- Photon energy-range (hardness): $E_{p,z} \sim 1 \text{ keV} - 10 \text{ MeV}$
(Sun's photon energy: $E_{p,\text{Sun}} \sim 1 - 2 \text{ eV}$)



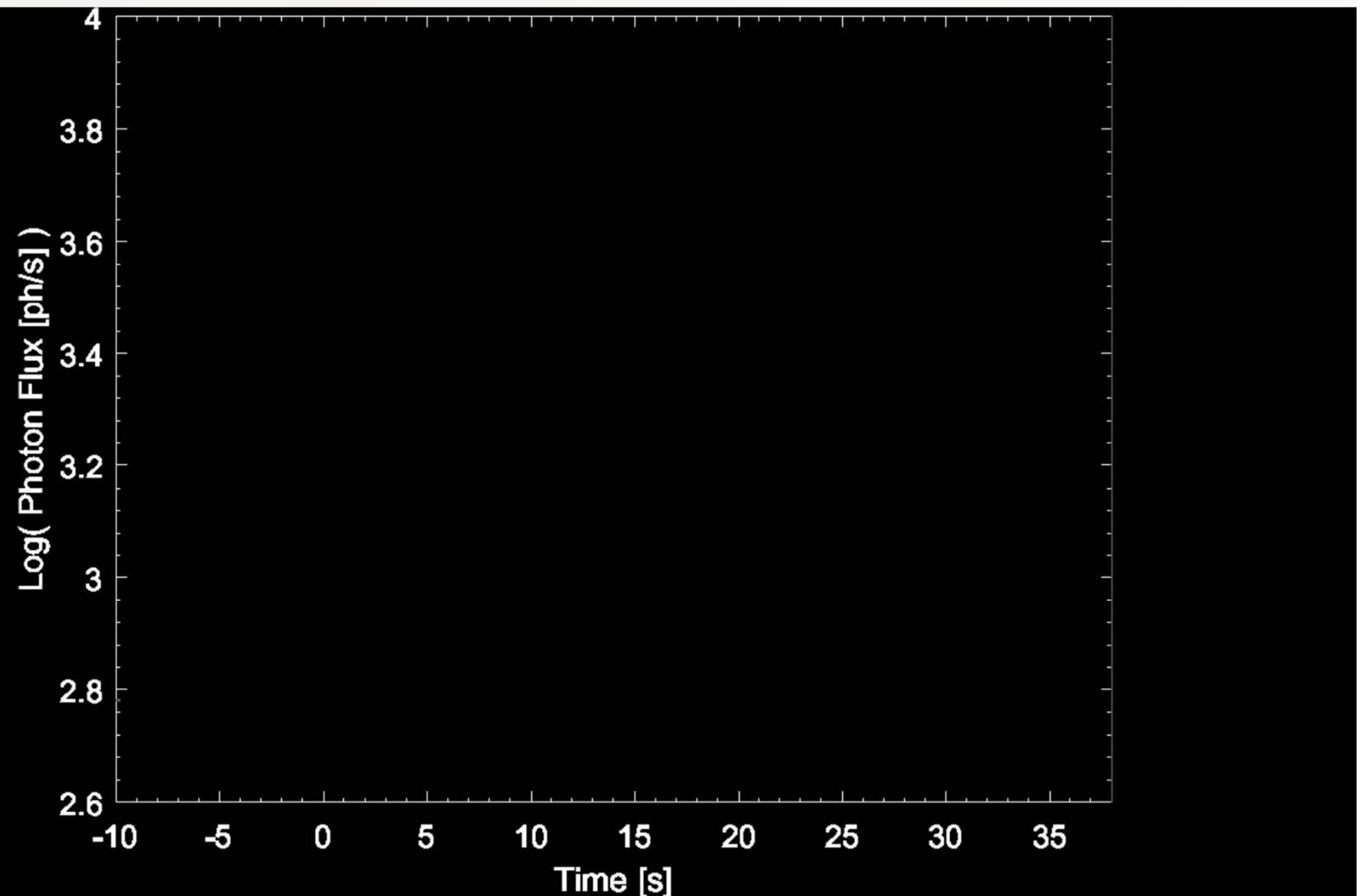
Example GRB lightcurve and spectrum

(BATSE GRB trigger 1085)

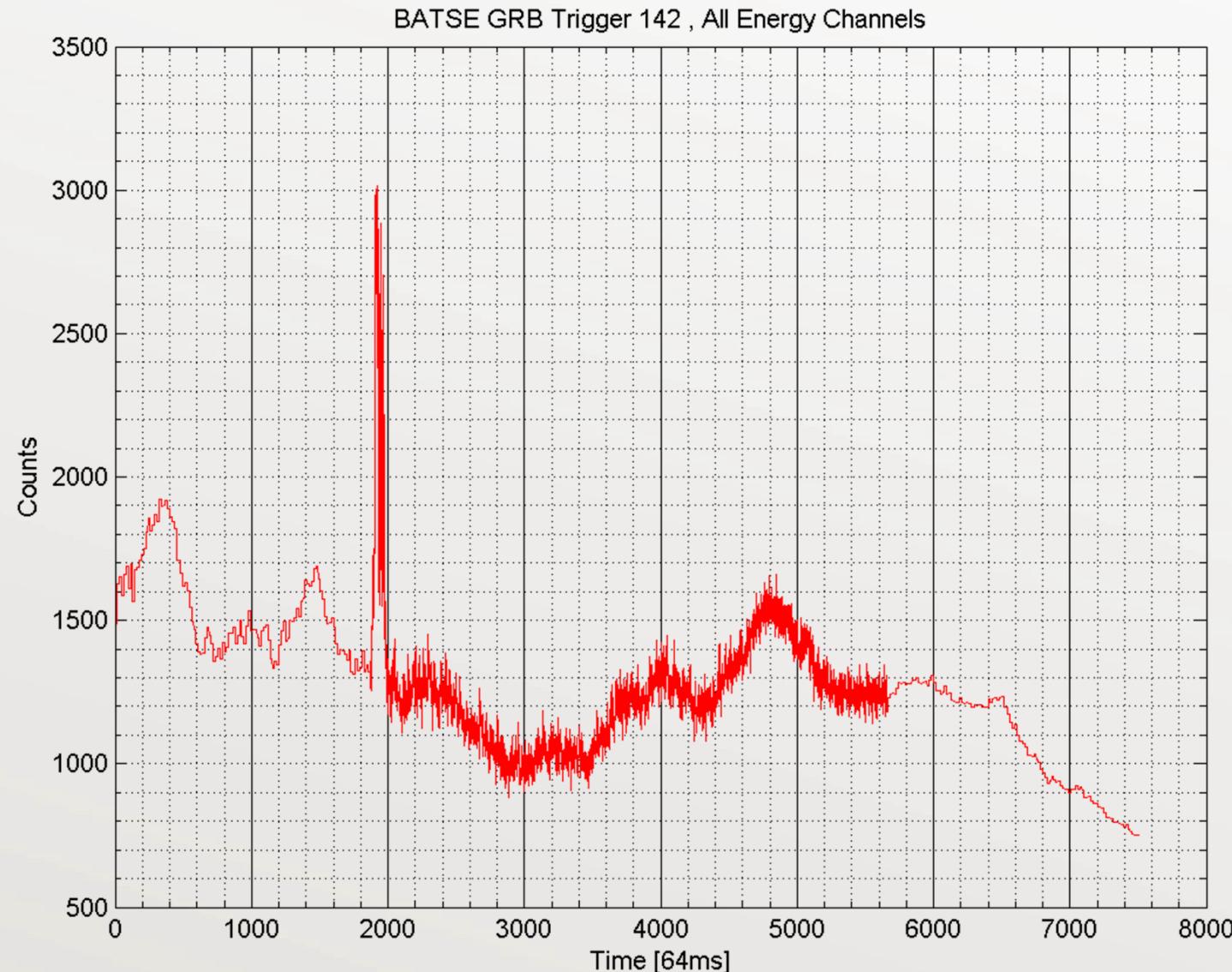


Example GRB lightcurve and spectrum

(BATSE GRB trigger 1085)

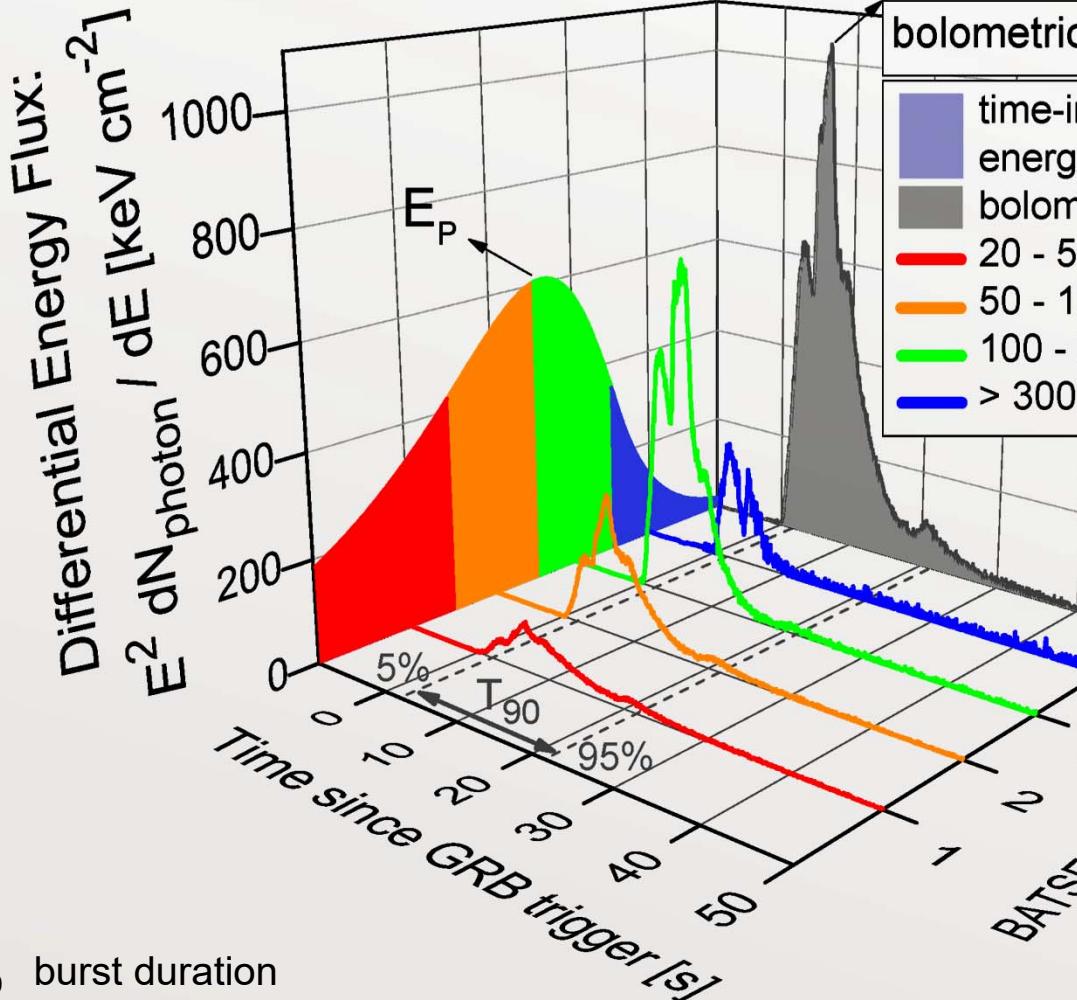


Example GRB lightcurve and spectrum (BATSE GRB trigger 142)



Example GRB light-curve and spectrum

and the four most important characteristics of GRBs

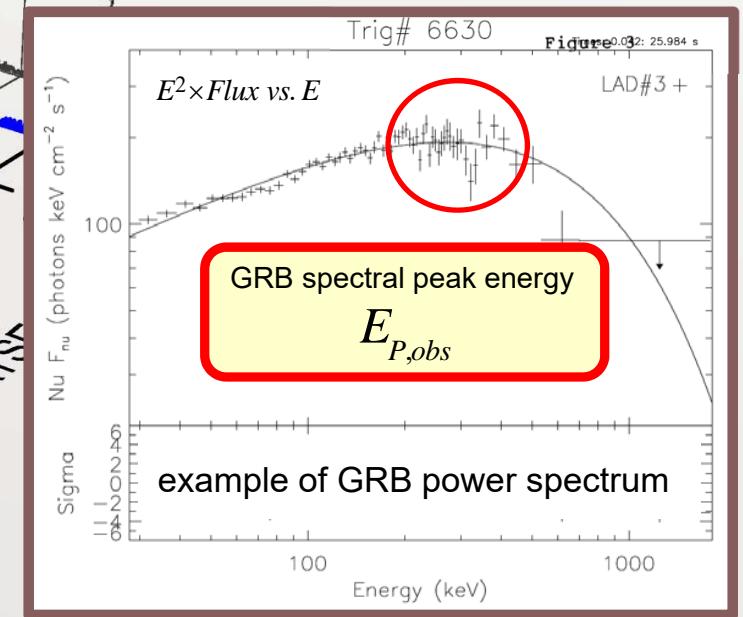
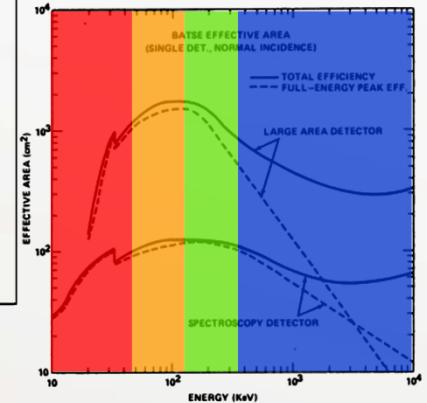
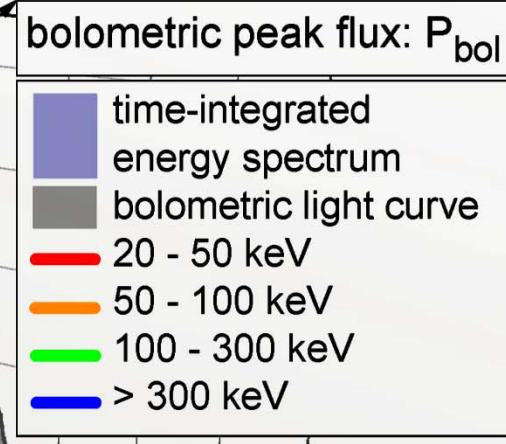


T_{90} burst duration

P_{bol} burst peak photon flux

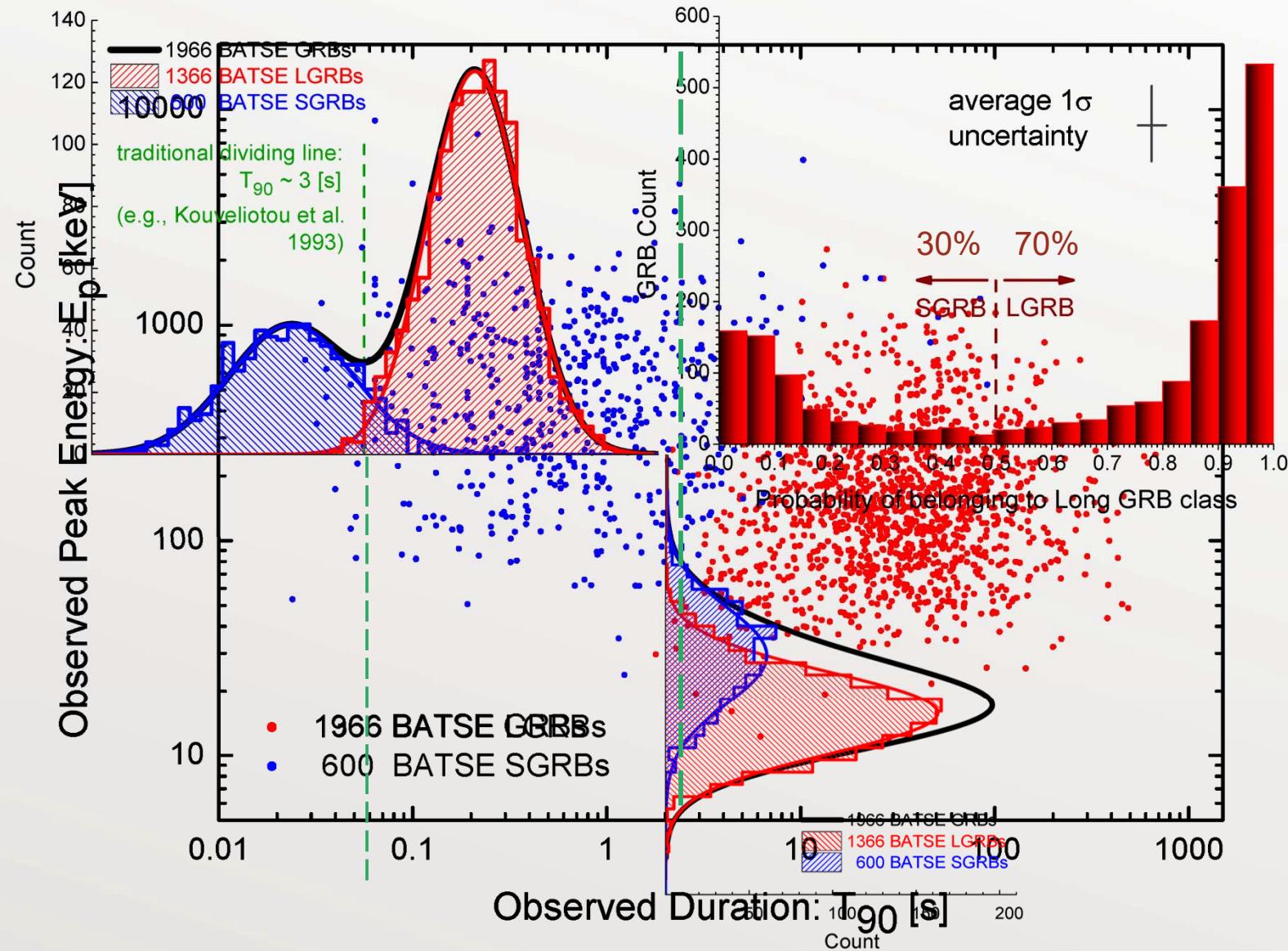
S_{bol} burst total energy (received on earth)

E_p burst spectral peak energy



Classification of BATSE GRBs: fuzzy clustering vs. cutoff line

(Shahmoradi & Nemiroff, 2011, MNRAS, 411, 1843–1856)



There are two types of Gamma-Ray Bursts (GRBs)



Short-duration class



Discovery of Gravitational Wave Radiation in Feb 2016
Predicted by Albert Einstein in 1916

Each and every GRB has two sets of properties

Observer-frame

GRB observed duration: T_{90}

GRB peak photon flux: P_{bol}

GRB total observed energy: S_{bol}

GRB observed peak energy: E_p

Rest-frame

z transformation



GRB intrinsic duration: $T_{90,z} = \frac{T_{90}}{1+z}$

GRB peak luminosity: $L_{iso} = 4\pi D_L (z)^2 P_{bol}$

GRB total energy release $E_{iso} = 4\pi D_L (z)^2 S_{bol}$

GRB intrinsic peak energy: $E_{p,z} = E_p(1 + z)$

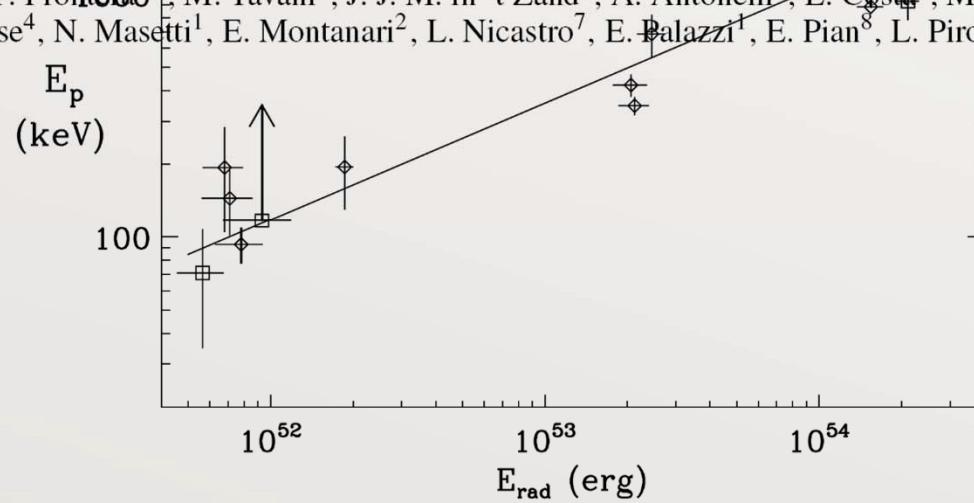
III. Can we use GRBs as standard candles in cosmology?

Short answer:

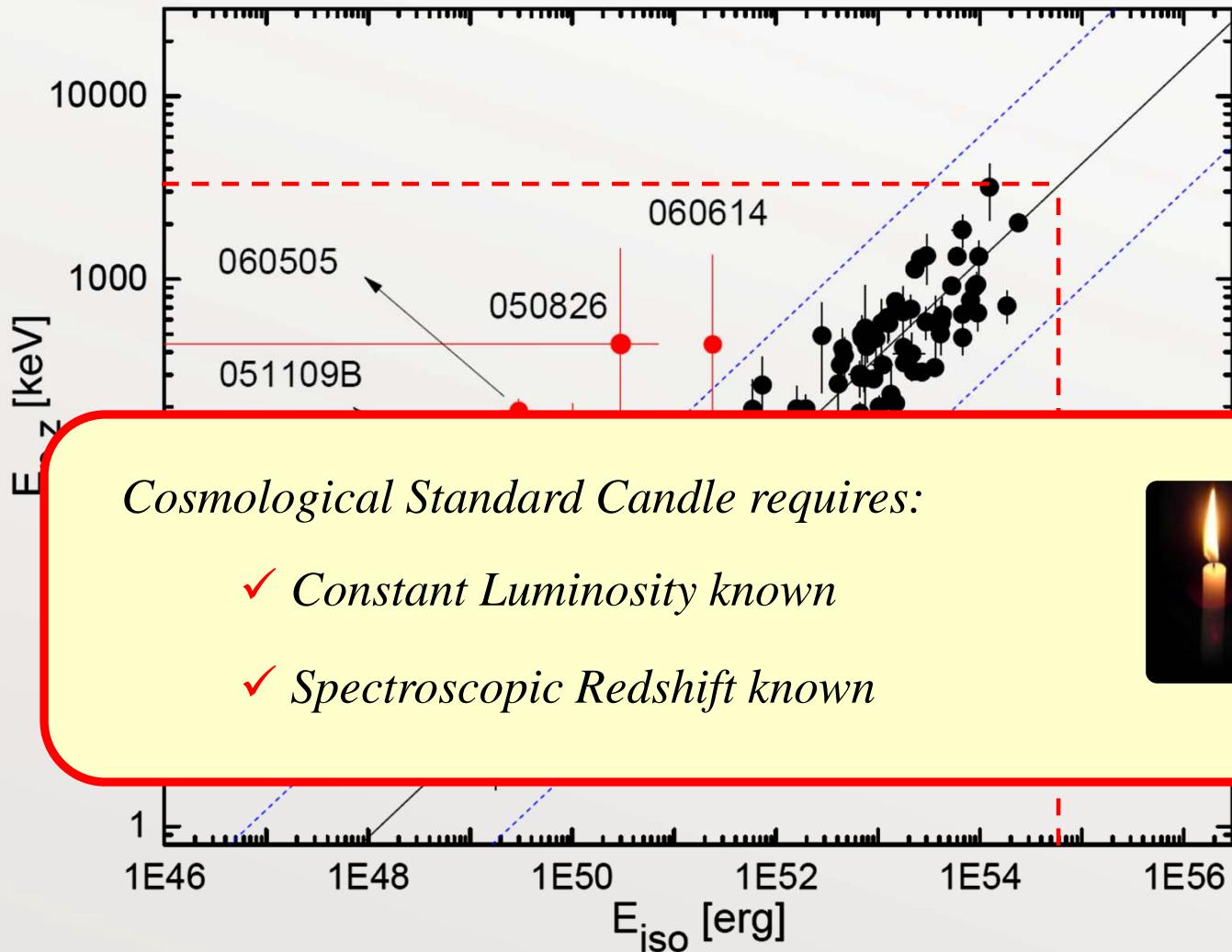
No, at the moment. Maybe yes in future.

Intrinsic spectra and energetics of BeppoSAX Gamma-Ray bursts with QPOs redshifts

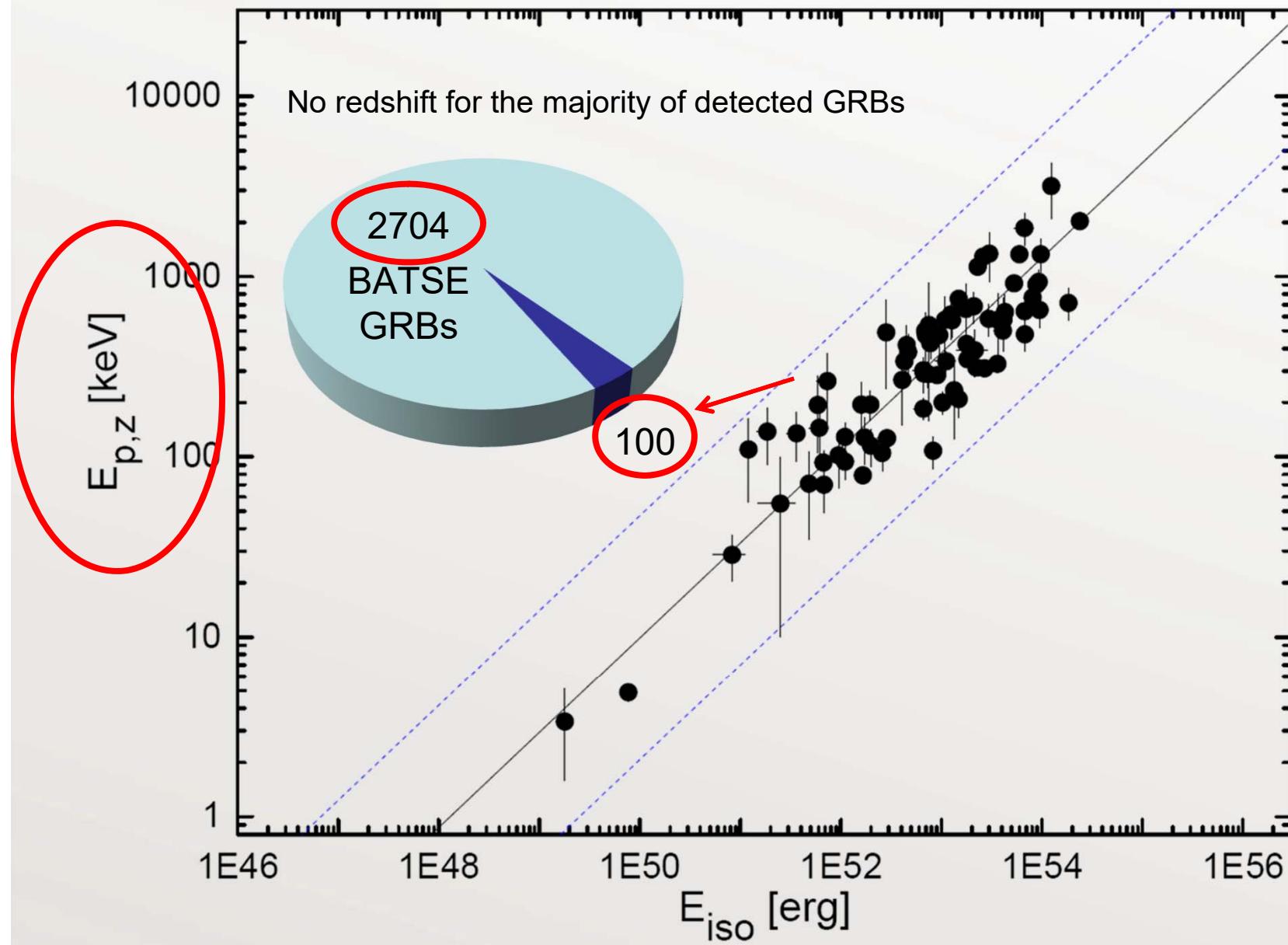
L. Amati¹, F. Frontera^{1,2}, M. Tavani³, J. J. M. in 't Zand⁴, A. Antonelli⁵, E. Costa⁶, M. Feroci⁶, C. Guidorzi², J. Heise⁴, N. Masetti¹, E. Montanari², L. Nicastro⁷, E. Palazzi¹, E. Pian⁸, L. Piro⁶, and P. Soffitta⁶



The spectral peak energy ($E_{p,z}$) of GRBs can be a standard candle, thanks to the Amati relation

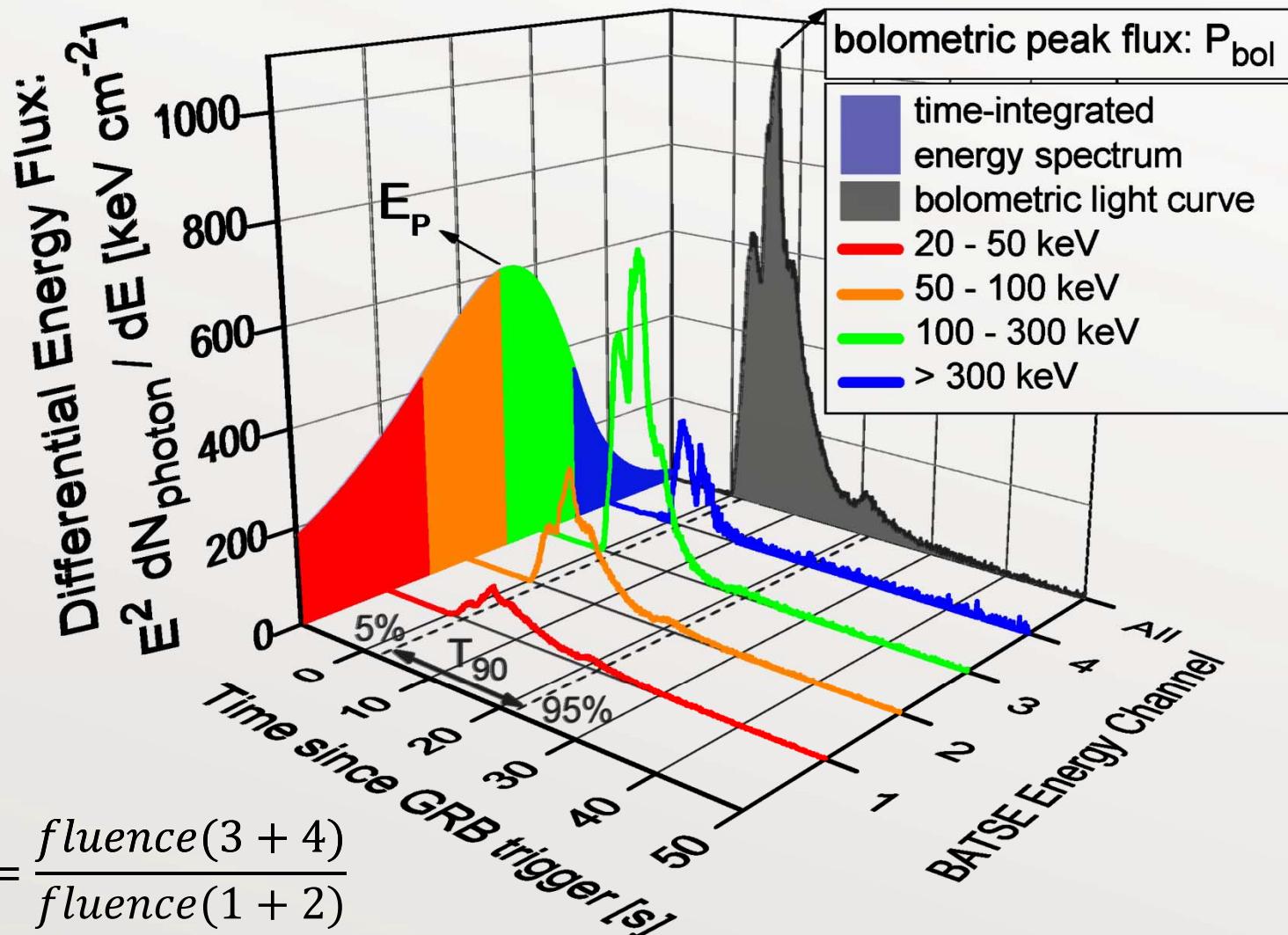


The Amati relation has been constructed by less than 10% of all GRBs detected by all gamma-ray satellites



Example GRB lightcurve and spectrum

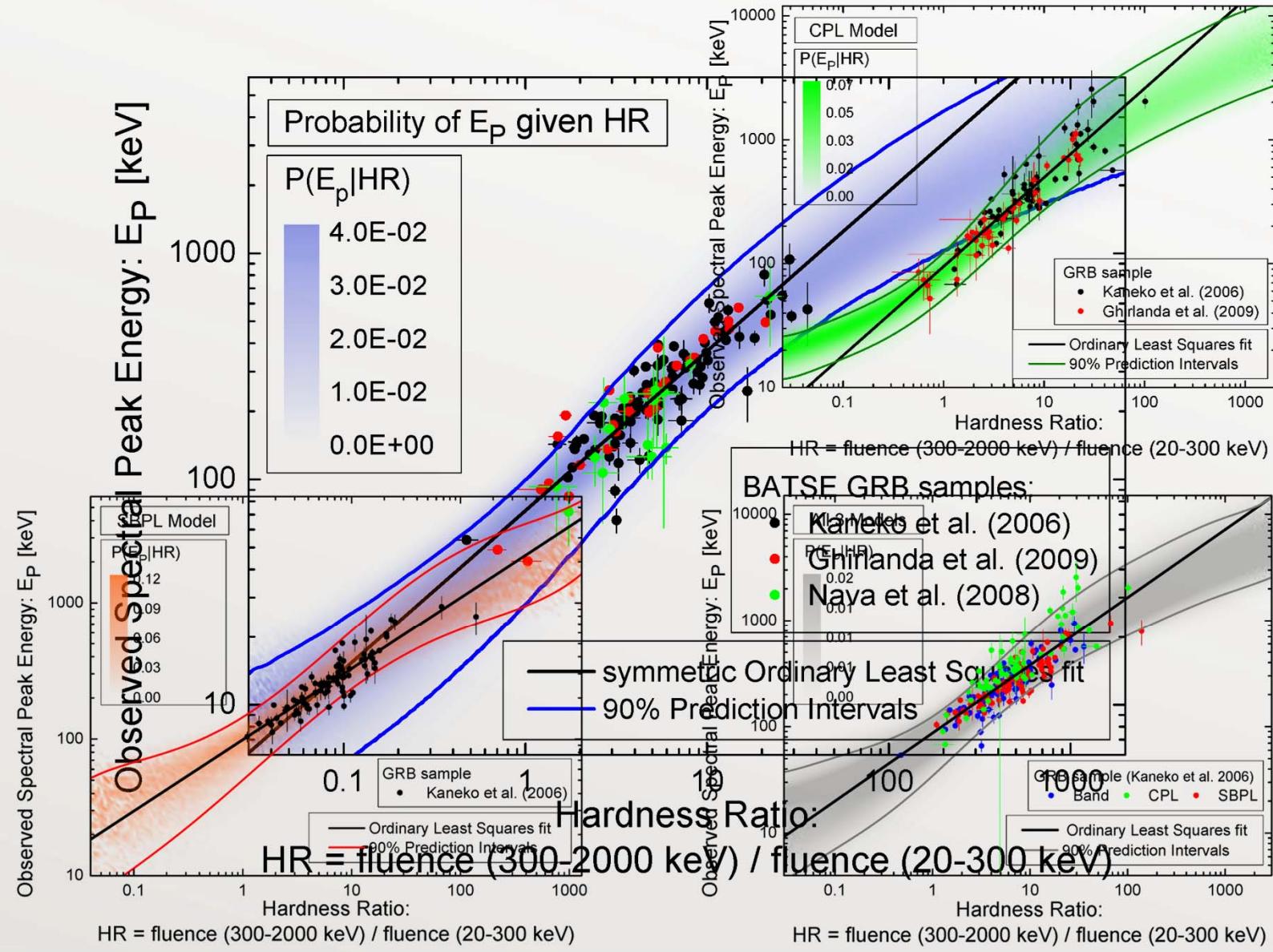
(BATSE GRB trigger 1085)



$$HR = \frac{\text{fluence}(3 + 4)}{\text{fluence}(1 + 2)}$$

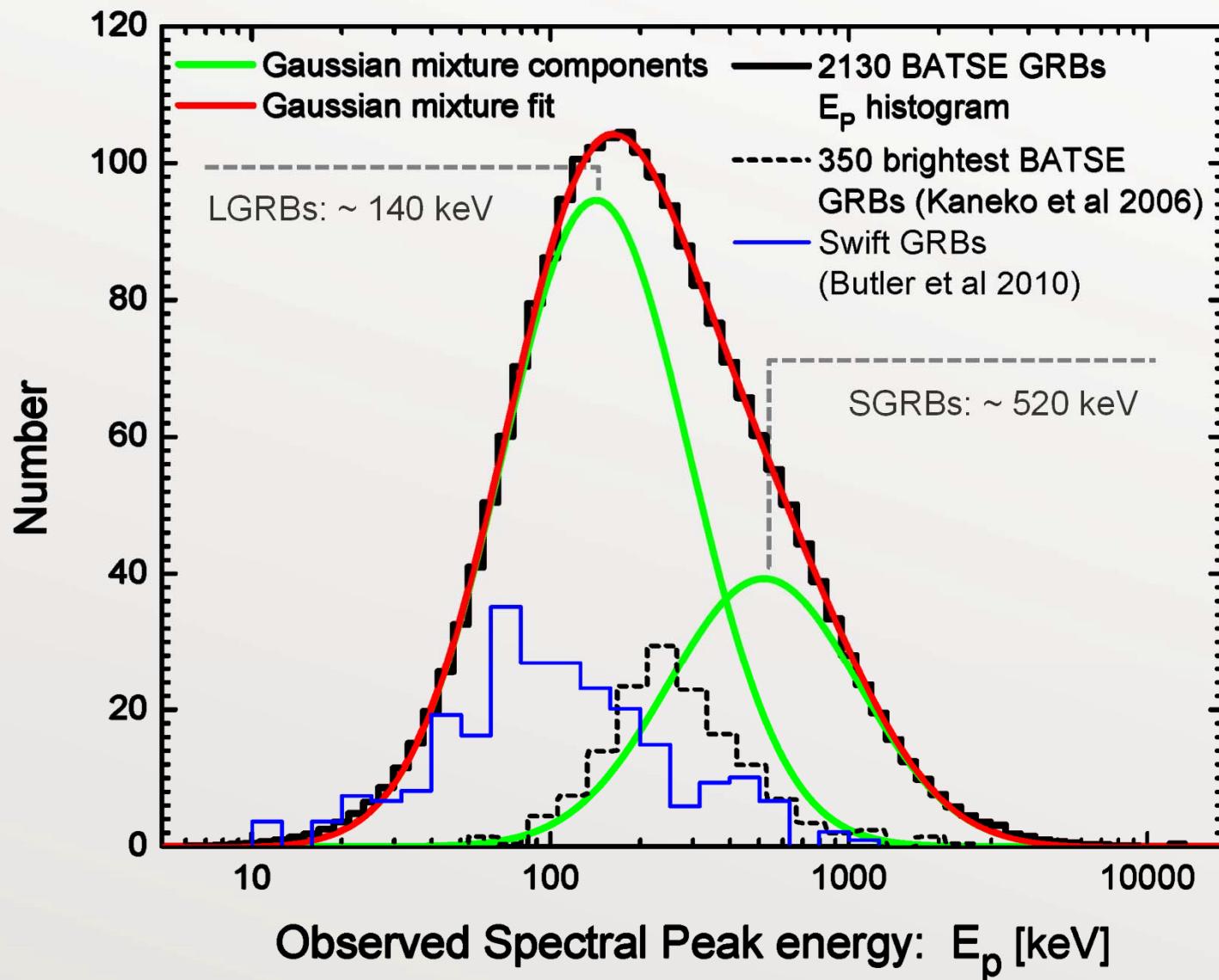
Hardness is a proxy measure of spectral peak energy of GRBs

(Shahmoradi & Nemiroff, 2010, MNRAS, **407**, 2075–2090)

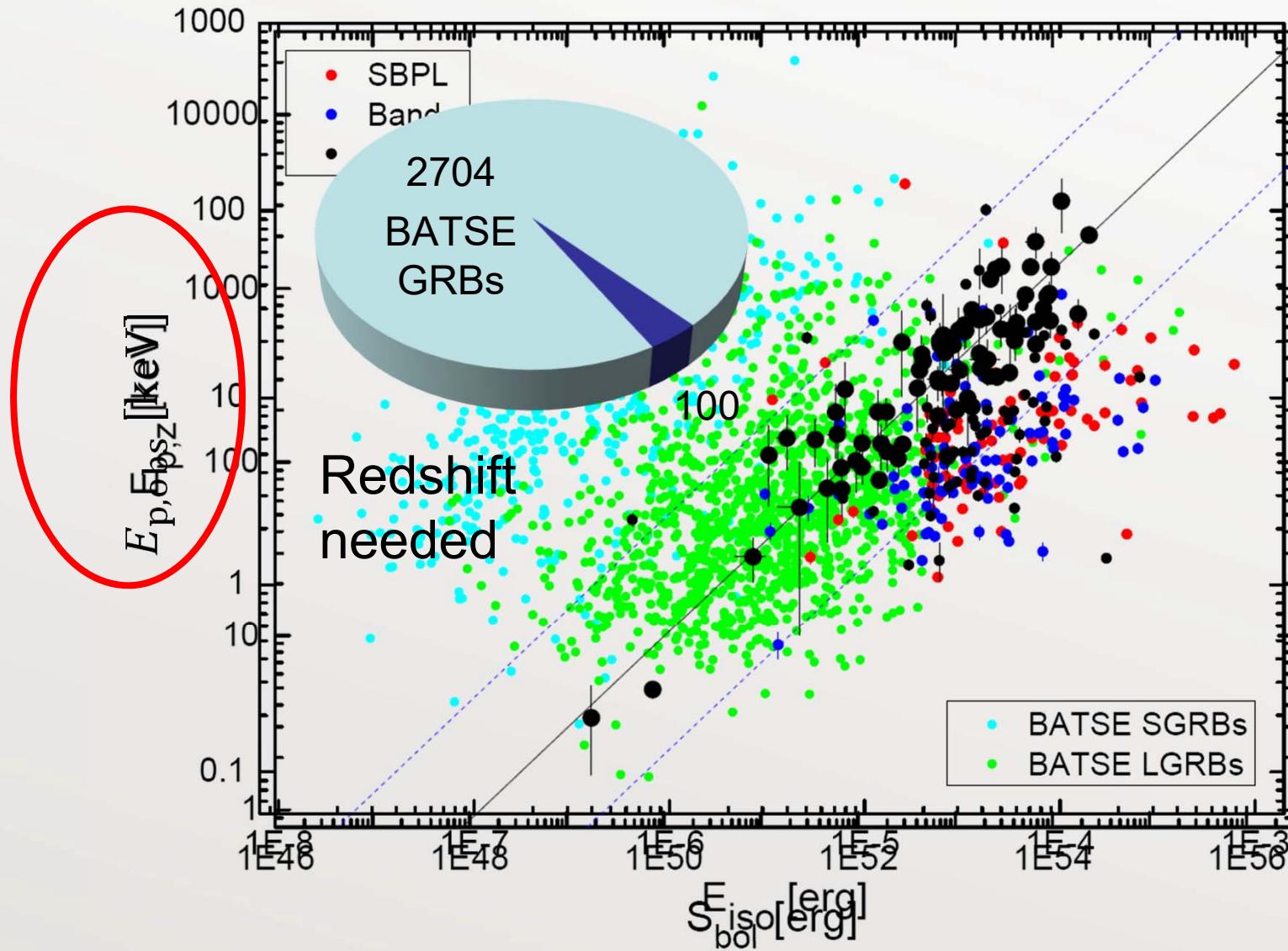


The peak energy distribution of 2130 BATSE GRBs

(Shahmoradi & Nemiroff, 2010, MNRAS, **407**, 2075–2090)

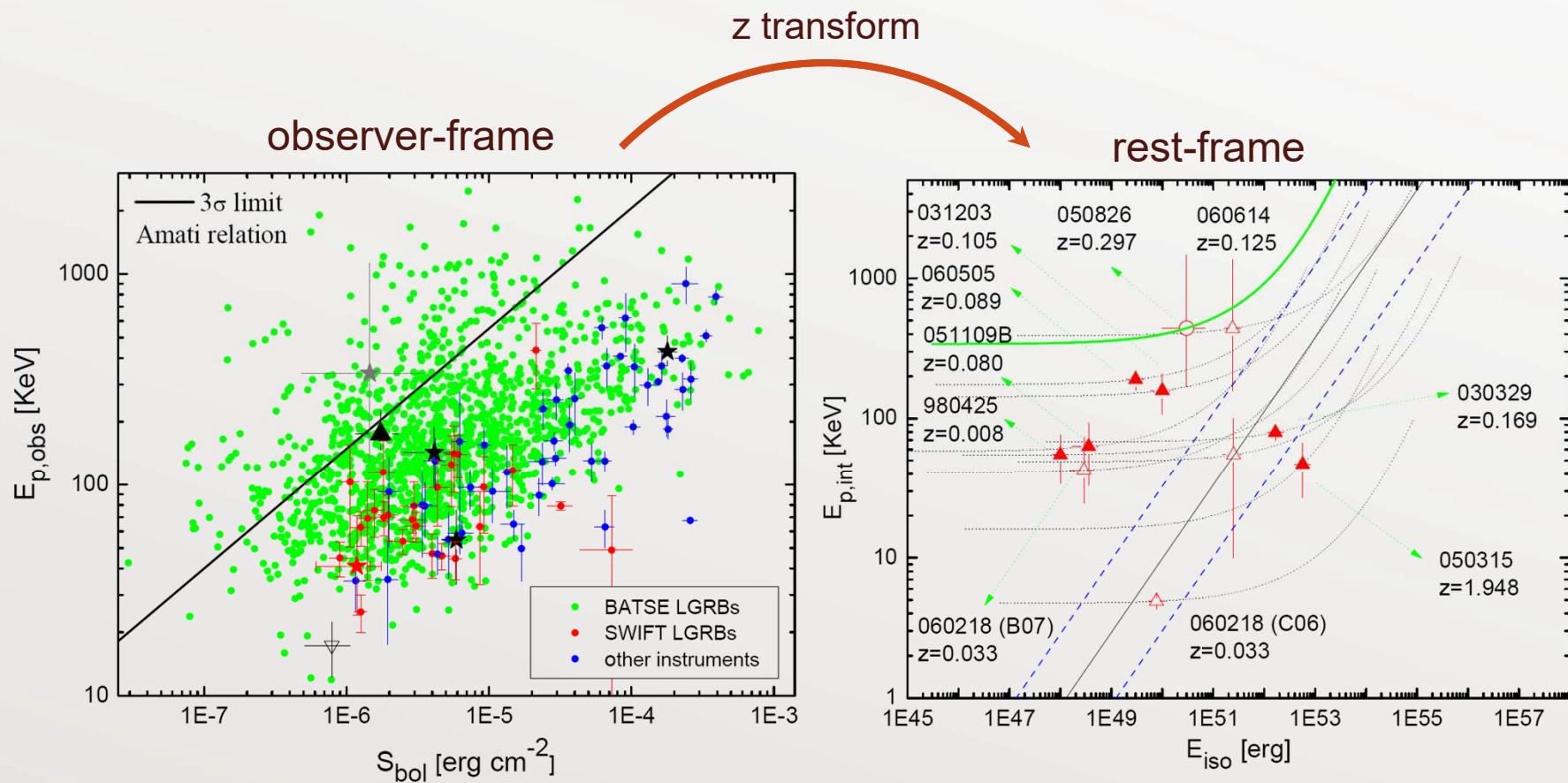


GRB astronomers are only seeing the tip of the iceberg



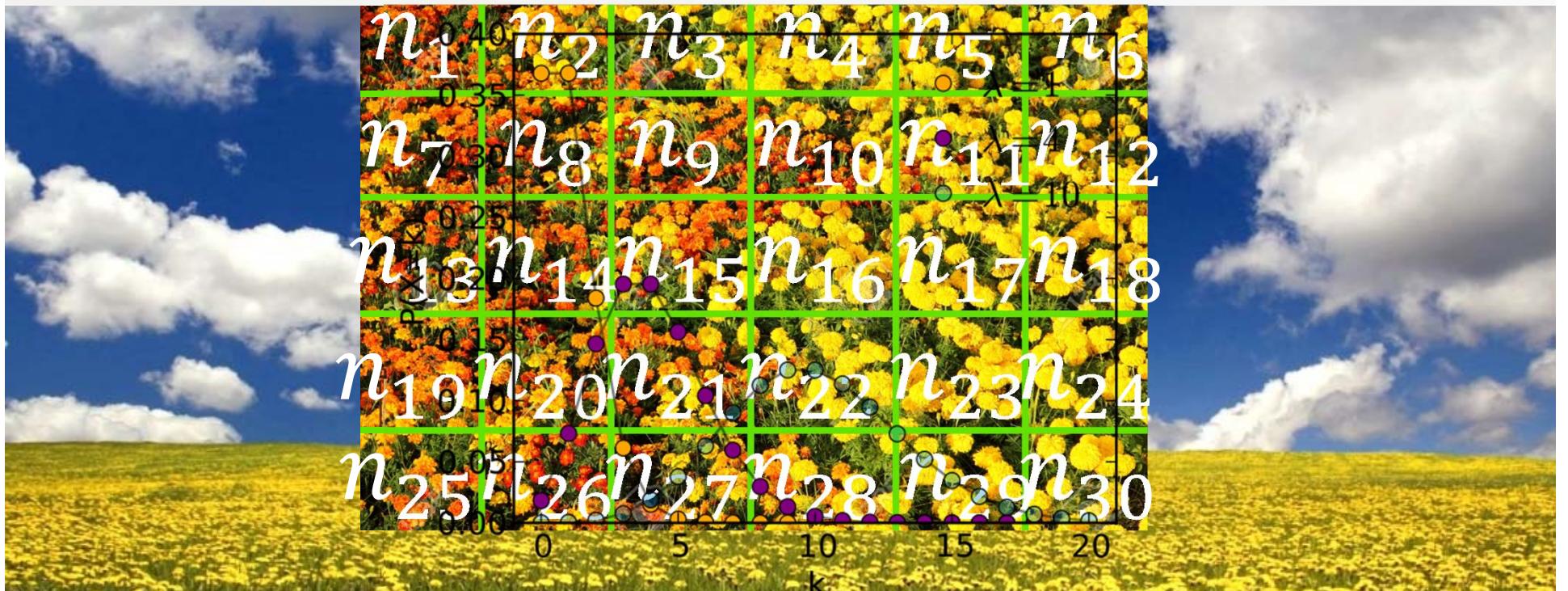
The Amati relation is heavily affected by sample incompleteness bias

At least 19% of all detected GRBs with no redshift are not consistent with the Amati relation at $> 3\sigma$ significance level.



Is there also a sample incompleteness bias due to gamma-ray detector threshold?

Poisson distribution: The distribution of counts of independent events within a given interval of time, space, ...



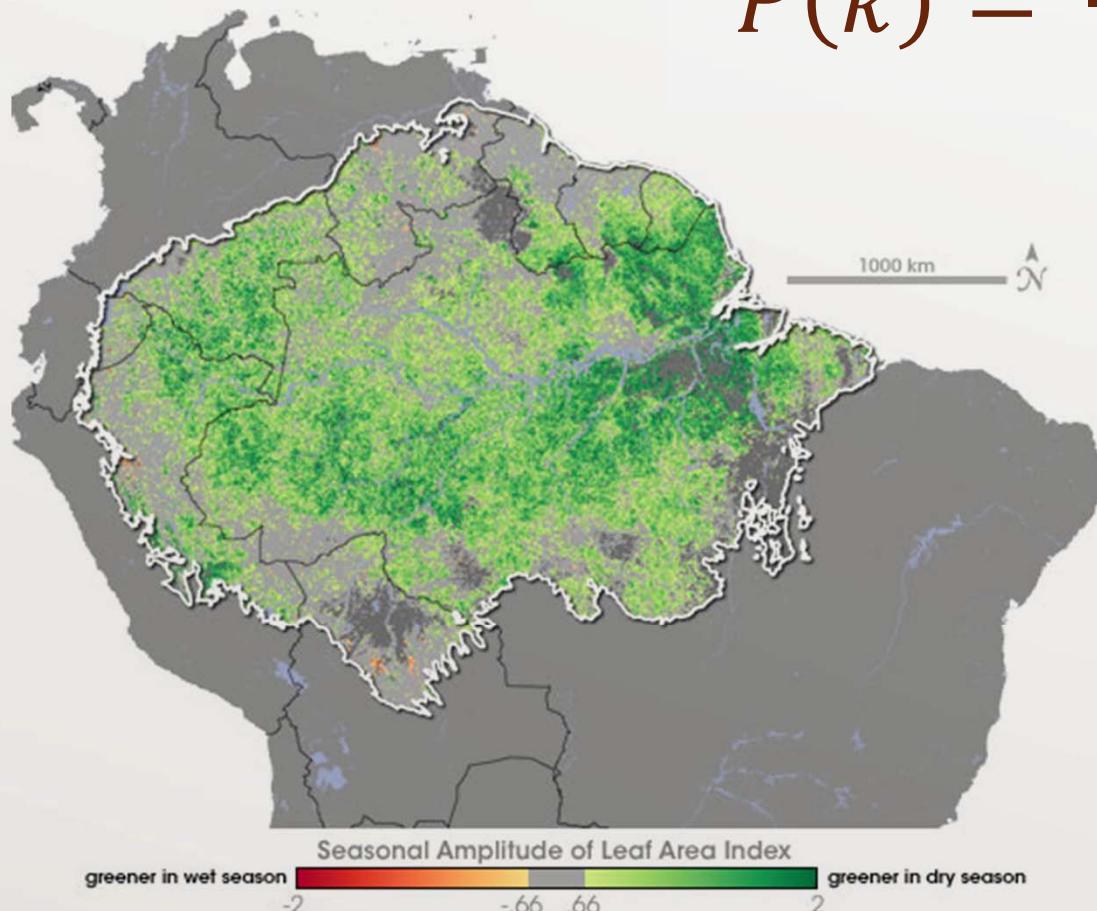
$$\lambda = \frac{1}{N} \sum_{N=0}^{N=30} n_i$$

$$P(k) = \frac{\lambda^k}{k!} e^{-\lambda}$$

Non-homogeneous spatial-temporal Poisson point process:

A Poisson point process with a Poisson parameter λ set as some location-dependent function in the underlying space on which the Poisson process is defined.

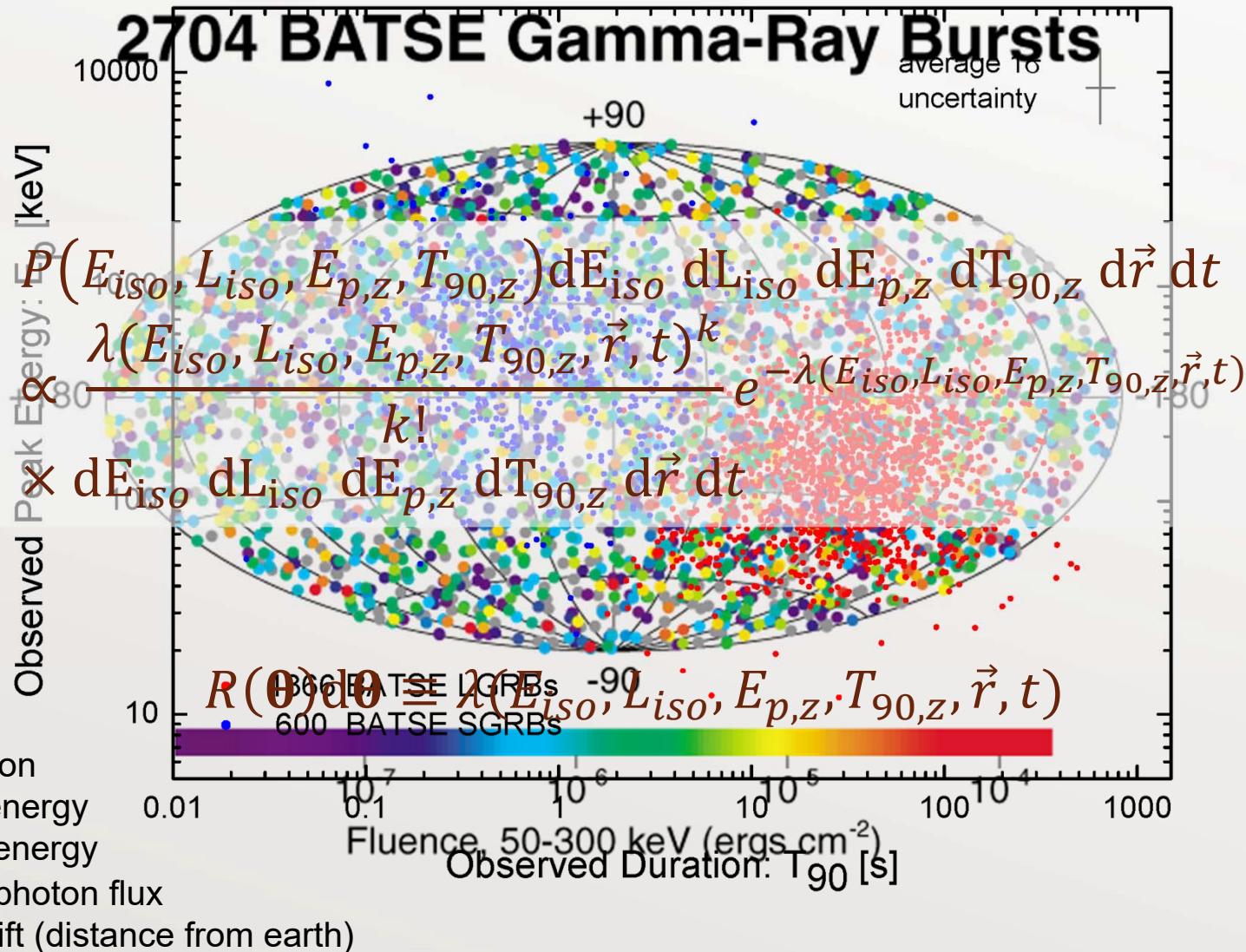
$$P(k) = \frac{\lambda(\vec{r}, t)^k}{k!} e^{-\lambda(\vec{r}, t)}$$



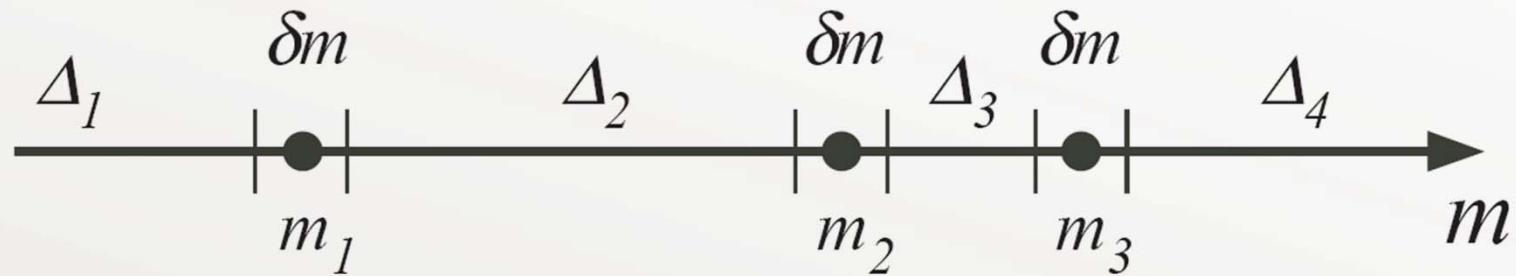
Poisson processes
are additive!

GRB detection process can be modeled as a non-homogenous Poisson process

What is the rate of occurrence of GRBs as a function of their distance and properties, $R(\theta)$?



With a statistical model in hand, we can proceed to construct the likelihood function of the model to estimate model parameters



$$P(k) = \frac{\lambda(m)^k}{k!} e^{-\lambda(m)} \quad P_0(m) = \frac{(R(m)\Delta m)^0}{0!} e^{-R(m)\Delta m} = e^{-R(m)\Delta m}$$

$$P_1(m) = \frac{(R(m)\Delta m)^1}{1!} e^{-R(m)\Delta m} = R(m)\Delta m e^{-R(m)\Delta m}$$

$$\begin{aligned} L(\text{DATA}|R(m)) &= \prod_{i=1}^N P_1(m_i) \prod_{j=1}^M P_0(m_j) = (\Delta m)^N \left[\prod_{i=1}^N R(m_i) \right] \left[e^{-\sum_{j=1}^{N+M} R(m_j)\Delta m} \right] \\ &= (\Delta m)^N \left[\prod_{i=1}^N R(m_i) \right] \exp \left(- \int_M R(m) dm \right) \end{aligned}$$

How about the likelihood function for the non-homogenous Poisson process of GRB detection?

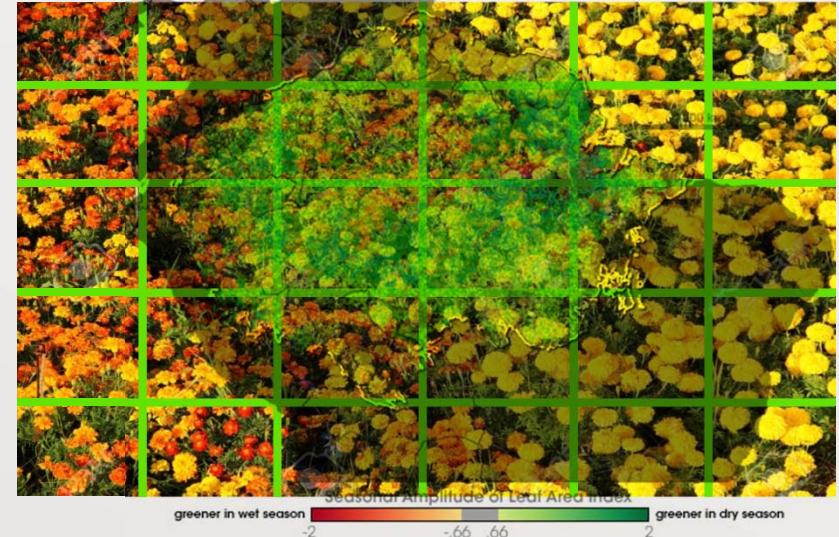
$$L(\text{DATA}|R(m)) = (\Delta m)^N \left[\prod_{i=1}^N R(m_i) \right] \exp \left(- \int_M R(m) dm \right)$$

$$L(\text{GRB DATA}|R(\boldsymbol{\theta})) = (\Delta \boldsymbol{\theta})^N \left[\prod_{i=1}^N R(\boldsymbol{\theta}_i) \right] \exp \left(- \int_{\boldsymbol{\Theta}} R(\boldsymbol{\theta}) d\boldsymbol{\theta} \right)$$

$$\boldsymbol{\theta} \equiv \vec{\theta} \equiv [E_{iso}, L_{iso}, E_{p,z}, T_{90,z}, z, t]$$

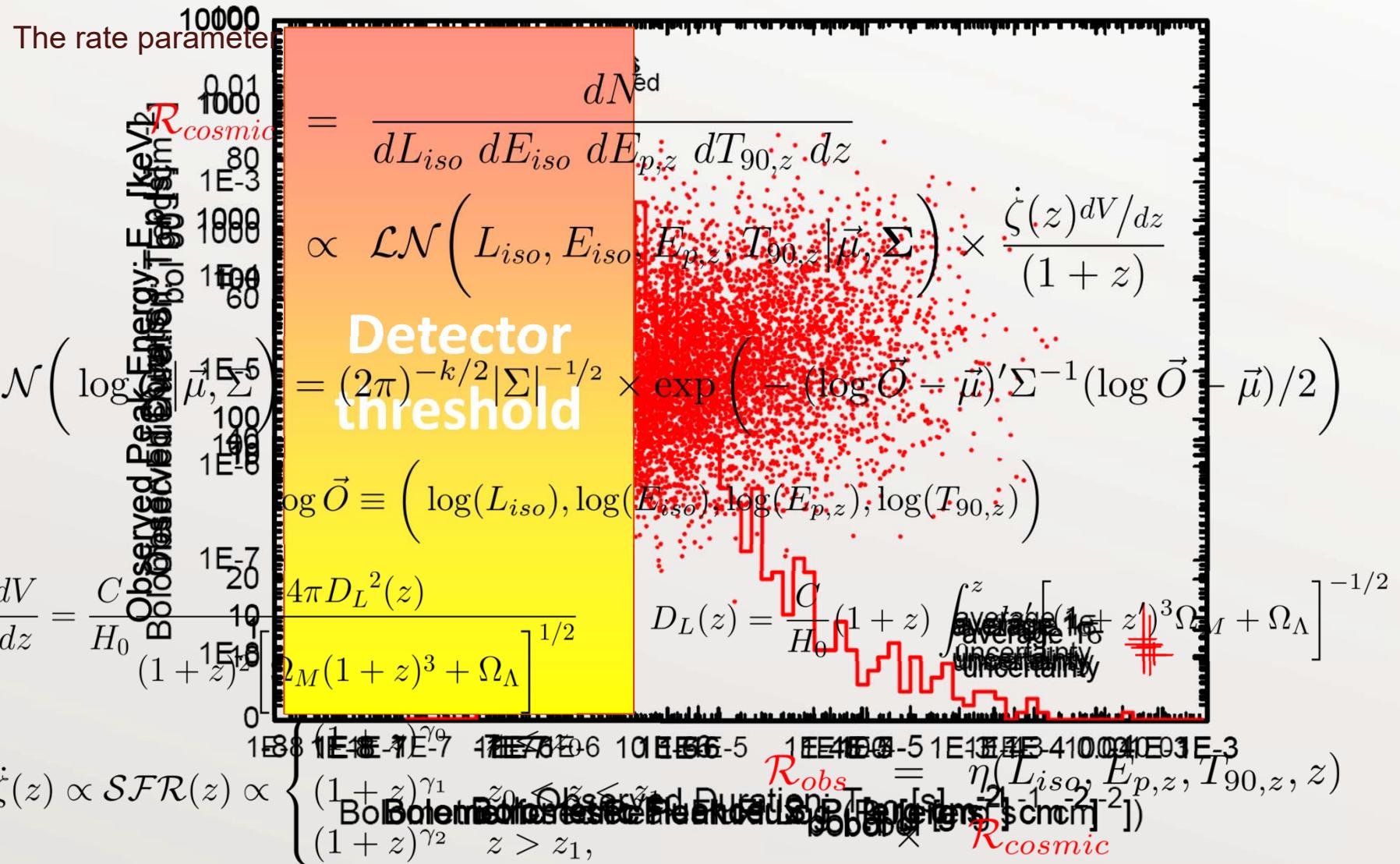
Now that we have the likelihood function, what is the most appropriate model for GRB rate as a function of GRB parameters?

$$R(\boldsymbol{\theta}) = ?$$



Multivariate Log-normal distribution

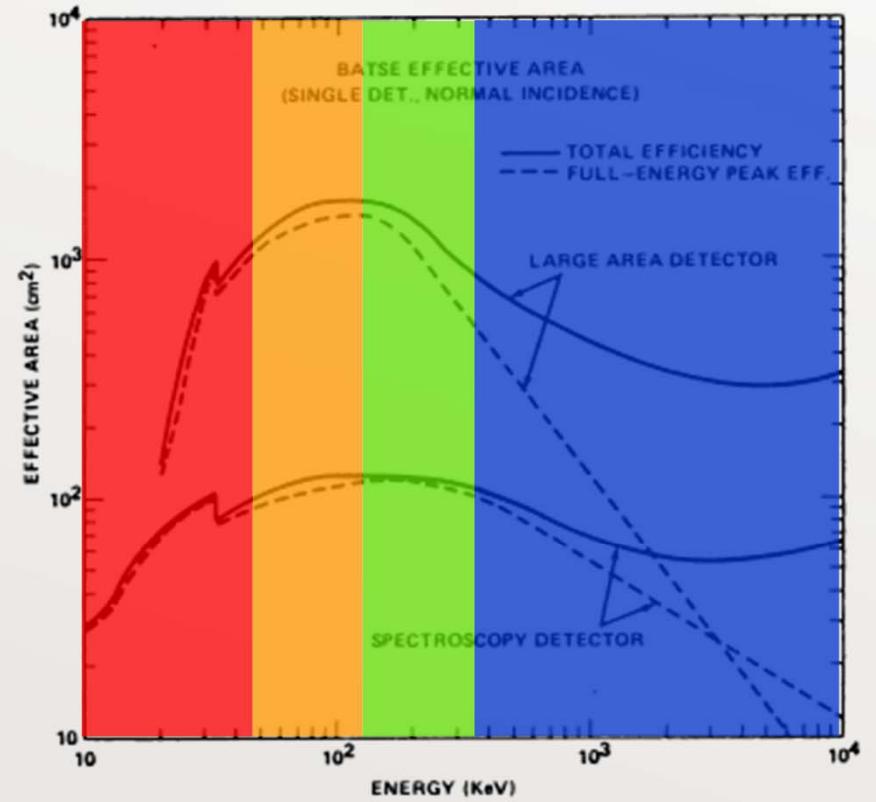
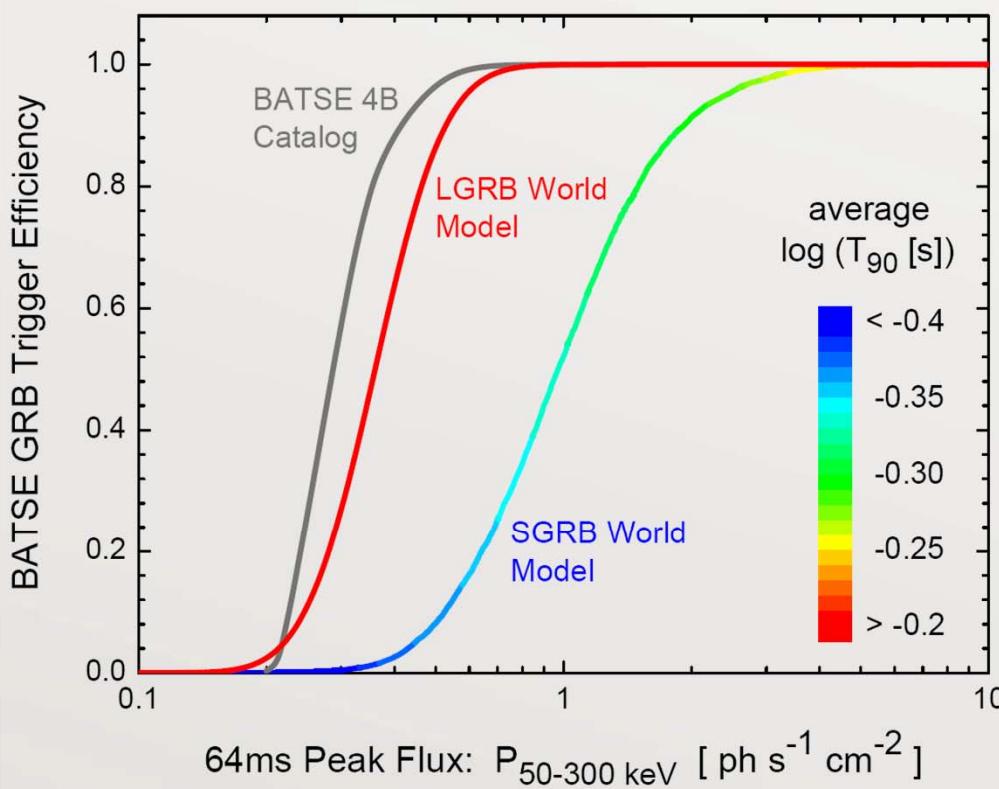
The simplest most natural model of GRB occurrence rate R_{cosmic} as a function of GRB properties ($E_{\text{iso}}, L_{\text{iso}}, E_{p,z}, T_{90,z}, z$)



GRB detection is therefore a Poisson process with mean $\lambda = R_{obs}(\theta)d\theta$

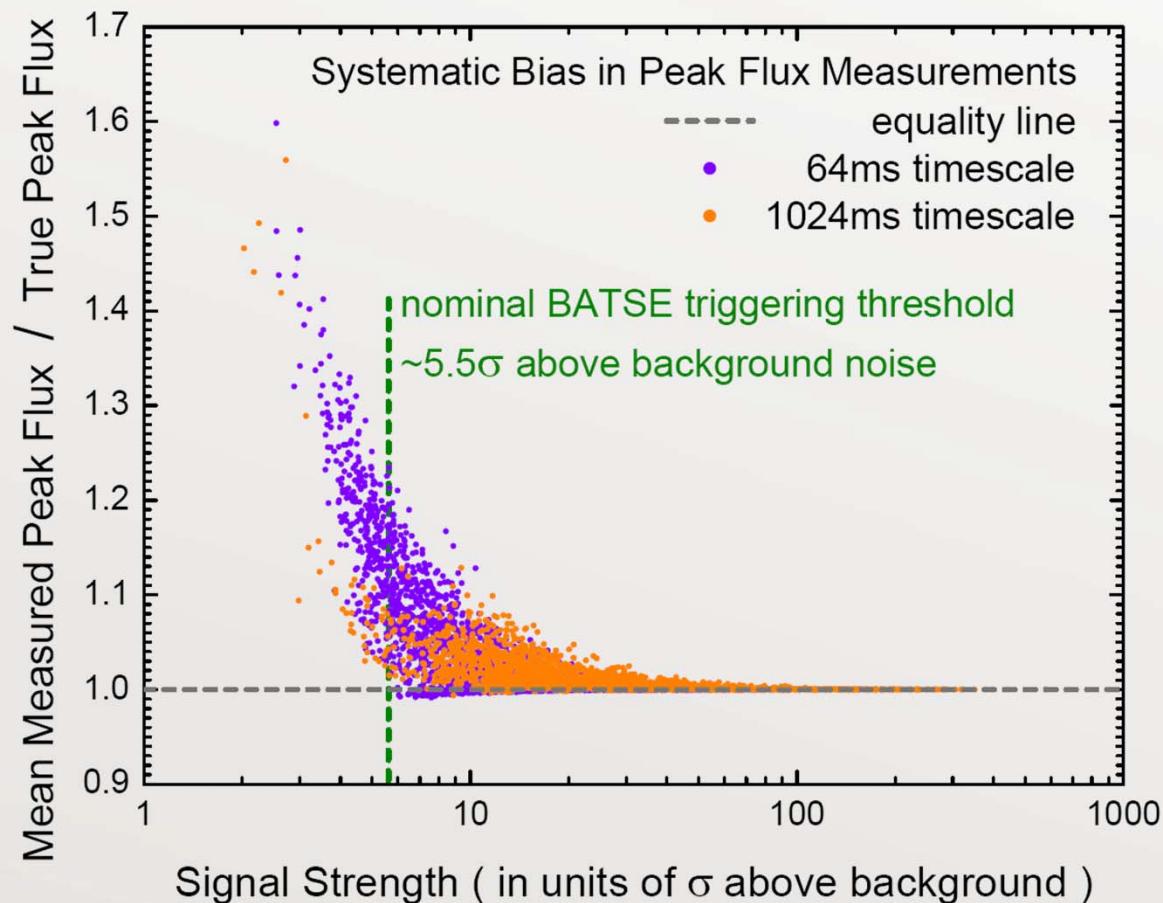
$$\mathcal{R}_{obs} = \eta(L_{iso}, E_{iso}, E_{p,z}, T_{90,z}, z | \mu_{thresh}, \sigma_{thresh}) \times \mathcal{R}_{cosmic}$$

$$\eta(\theta | \mu_{thresh}, \sigma_{thresh}) = \frac{1}{2} + \frac{1}{2} \times \text{erf}\left(\frac{\log(P_{\text{eff}}(L_{iso}, E_{p,z}, T_{90,z}, z) - \mu_{thresh})}{\sqrt{2}\sigma_{thresh}}\right)$$

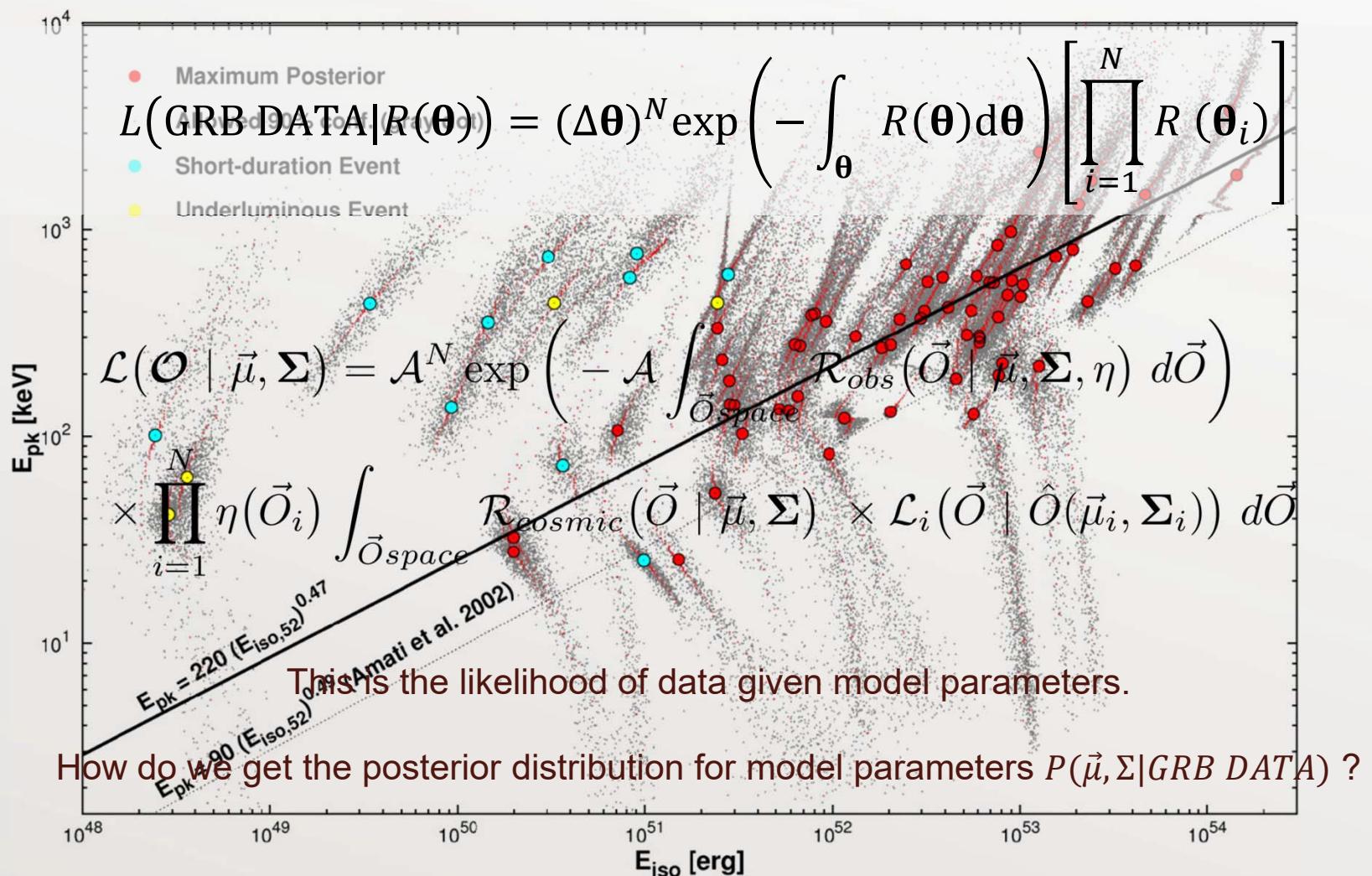


Bayesian Multilevel modeling automatically corrects for systematic biases in data

$$P(S_{true}|S_{obs}) \propto P(S_{obs}|S_{true}) \times P(S_{true})$$

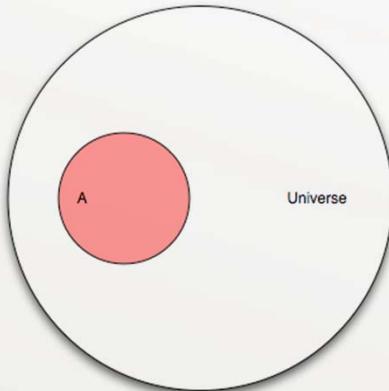


Observational data uncertainties are very important and must be taken into account

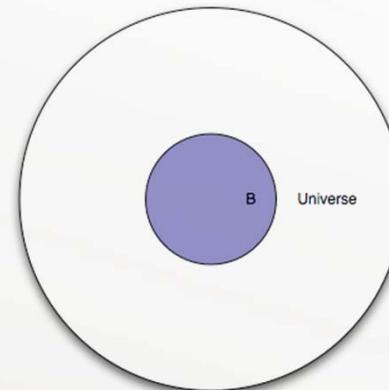


Bayes theorem

$$P(A) = \frac{A}{U}$$

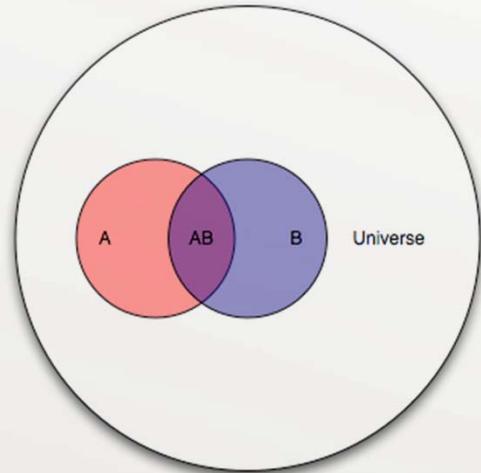


$$P(B) = \frac{B}{U}$$



$$P(A|B) = \frac{AB}{B} = \frac{\frac{AB}{U}}{\frac{B}{U}} = \frac{P(AB)}{P(B)}$$

$$P(AB) = \frac{AB}{U}$$



$$P(B|A) = \frac{AB}{A} = \frac{\frac{AB}{U}}{\frac{A}{U}} = \frac{P(AB)}{P(A)}$$

$$P(A|B) = \frac{P(A)P(B|A)}{P(B)}$$

The posterior probability density of model parameters can be obtained from Bayes rule

$$P(A|B) = \frac{P(A)P(B|A)}{P(B)}$$

$$\begin{aligned} \mathcal{L}(\mathcal{O} | \vec{\mu}, \Sigma) &= \mathcal{A}^N \exp \left(-\mathcal{A} \int_{\vec{O}_{space}} \mathcal{R}_{obs}(\vec{O} | \vec{\mu}, \Sigma, \eta) d\vec{O} \right) \\ &\times \prod_{i=1}^N \int_{\vec{O}_{space}} \eta(\vec{\mu}_i, \Sigma_i) \mathcal{R}_{cosmic}(\vec{O} | \vec{\mu}, \Sigma) \times \mathcal{L}_i(\vec{O} | \hat{O}(\vec{\mu}_i, \Sigma_i)) d\vec{O} \end{aligned}$$

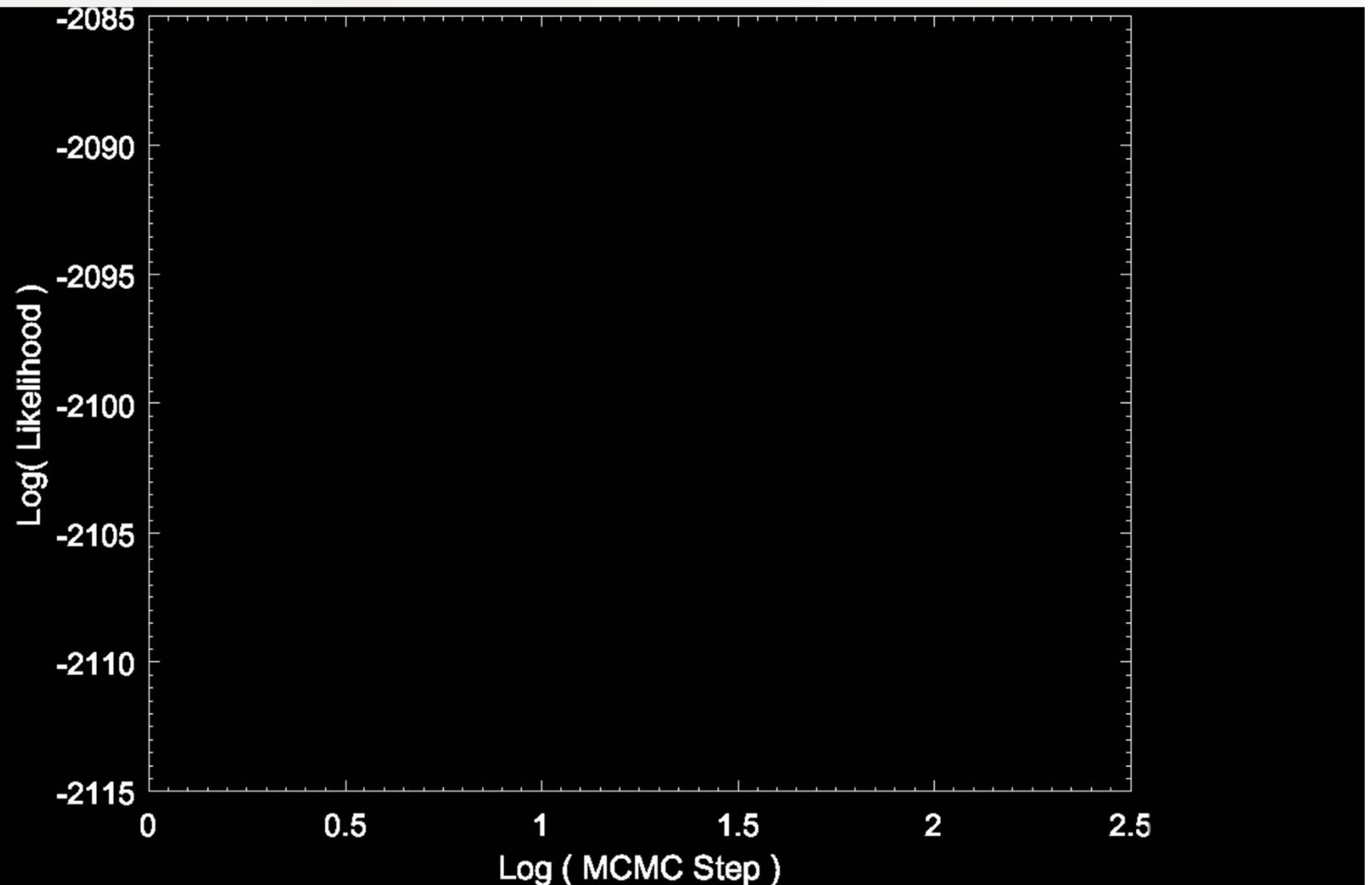
$$\underbrace{\mathcal{P}(\vec{\mu}, \Sigma | \mathcal{O})}_{P(A|B)} \propto \underbrace{\mathcal{P}(\vec{\mu}, \Sigma)}_{P(A)} \times \underbrace{\mathcal{L}(\mathcal{O} | \vec{\mu}, \Sigma)}_{P(B|A)}$$

The 16-D parameter posterior density is sampled via an Adaptive Metropolis-Hastings Markov Chain Monte Carlo algorithm

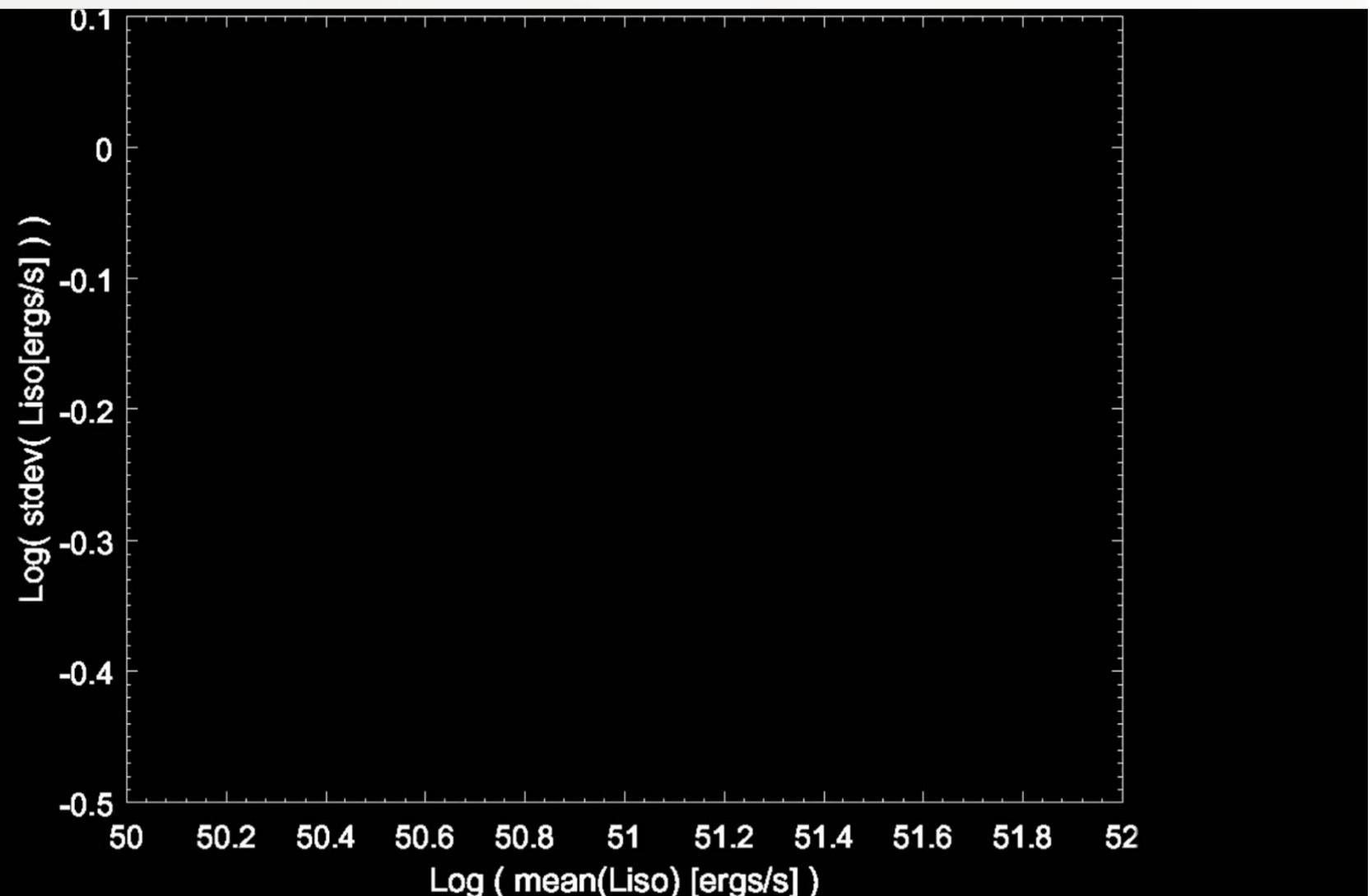
https://github.com/shahmoradi/grb_world



The posterior probability density of model parameters can be obtained from Bayes rule



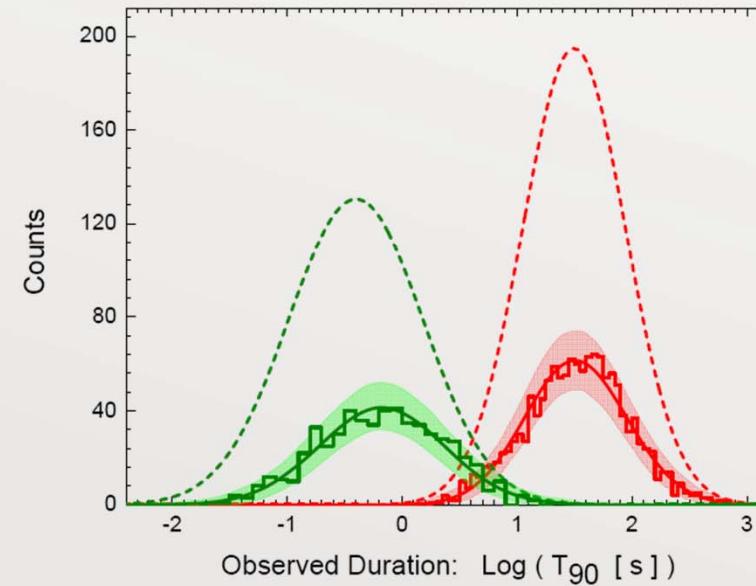
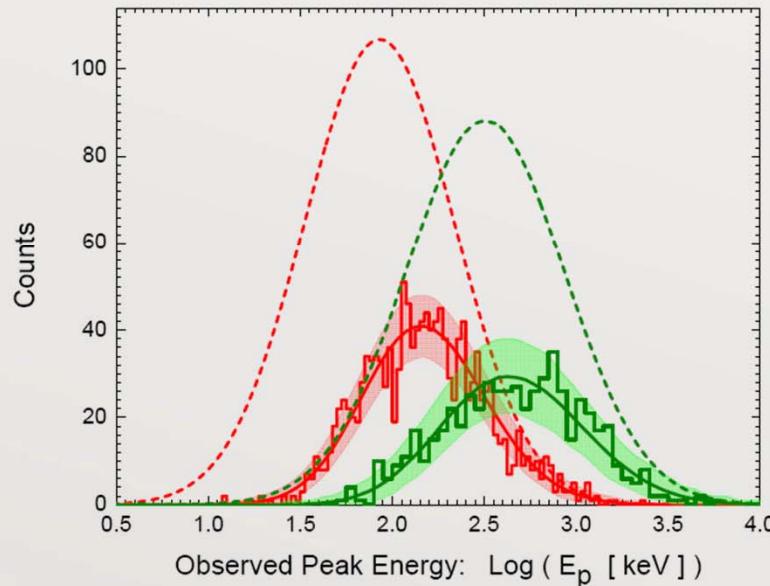
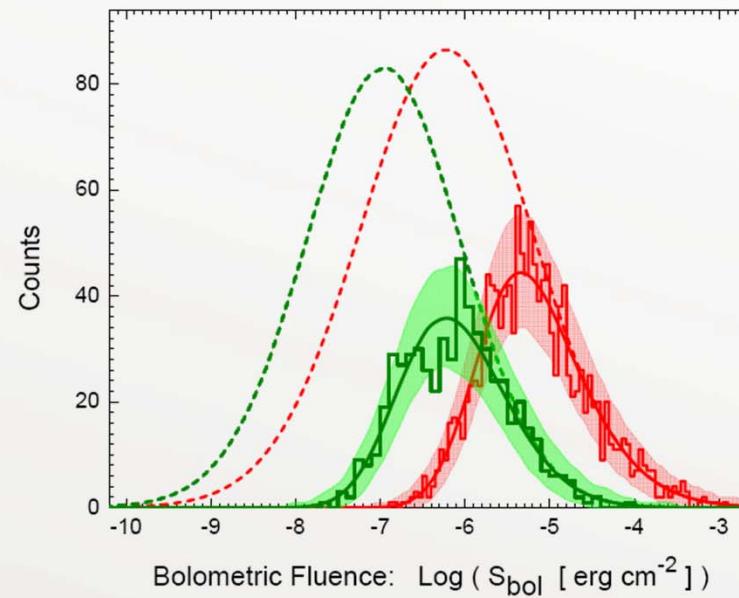
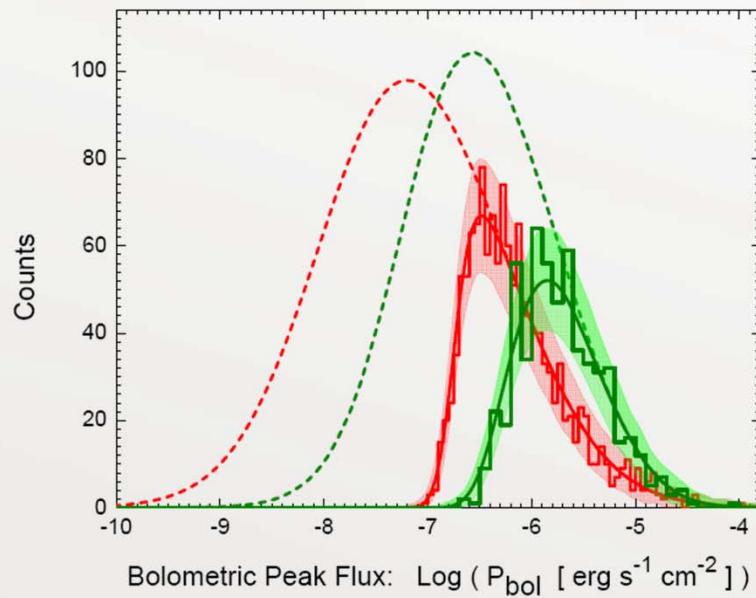
The posterior probability density of model parameters can be obtained from Bayes rule



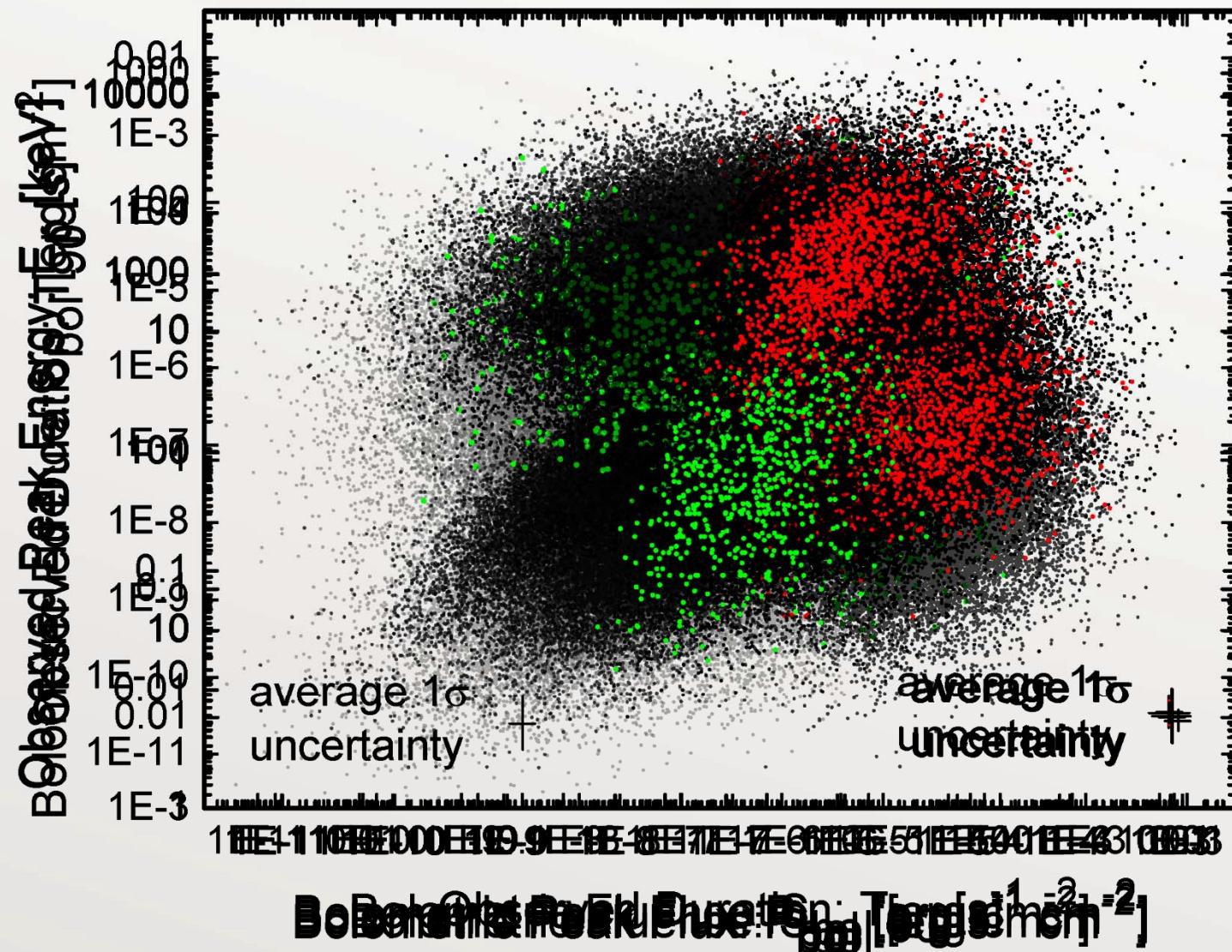
Colors bear the same meaning in all plots:

- BATSE SGRBs + model prediction
- BATSE LGRBs + model prediction

- - - predicted underlying population of SGRBs
- - - predicted underlying population of LGRBs

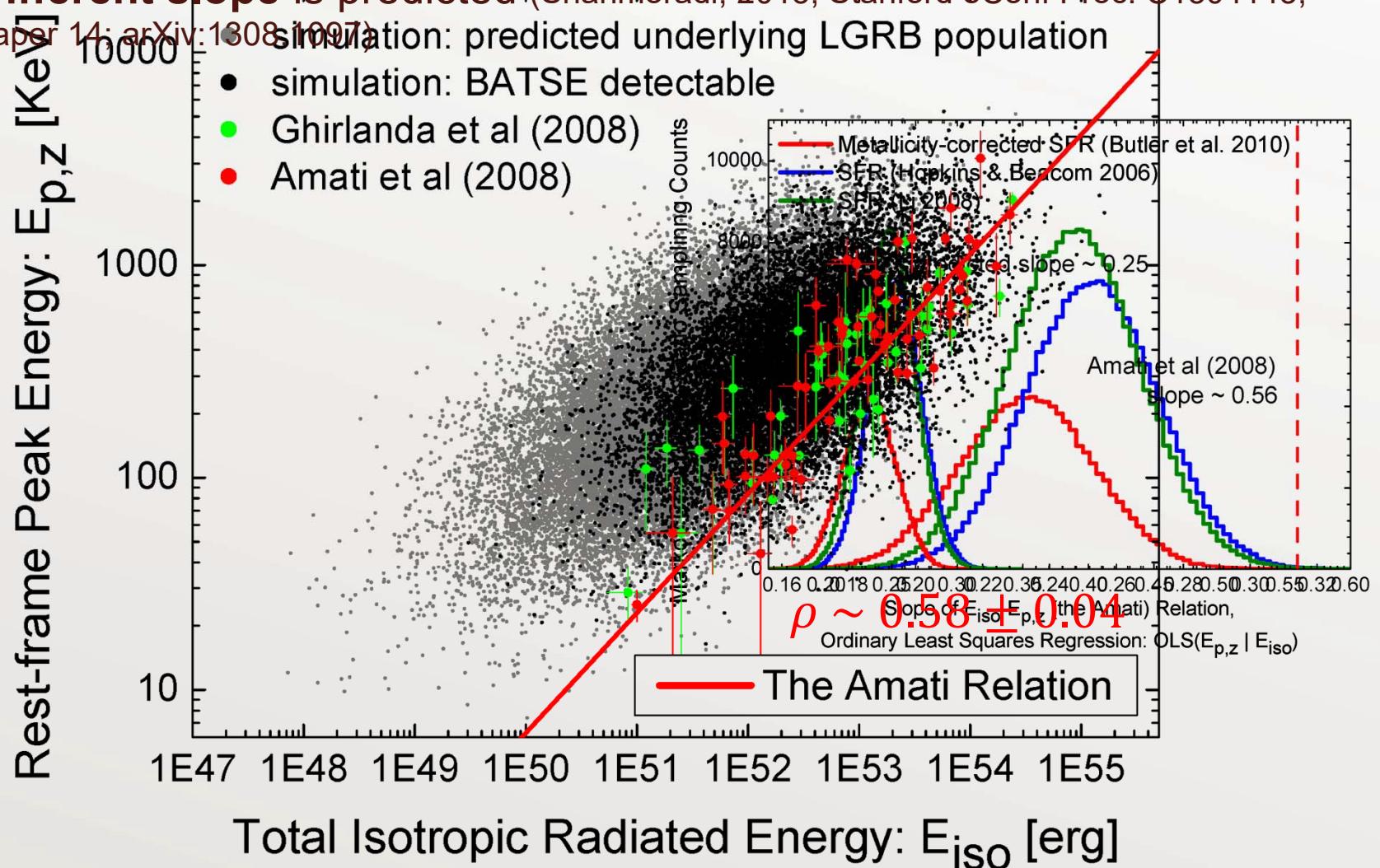


- Colors bear the same meaning in all plots:
- simulation: predicted underlying LGRB population
 - simulation: predicted underlying SGRB population
- 1366 BATSE LGRBs detected
 - 600 BATSE SGRBs detected
 - simulation: BATSE detectable

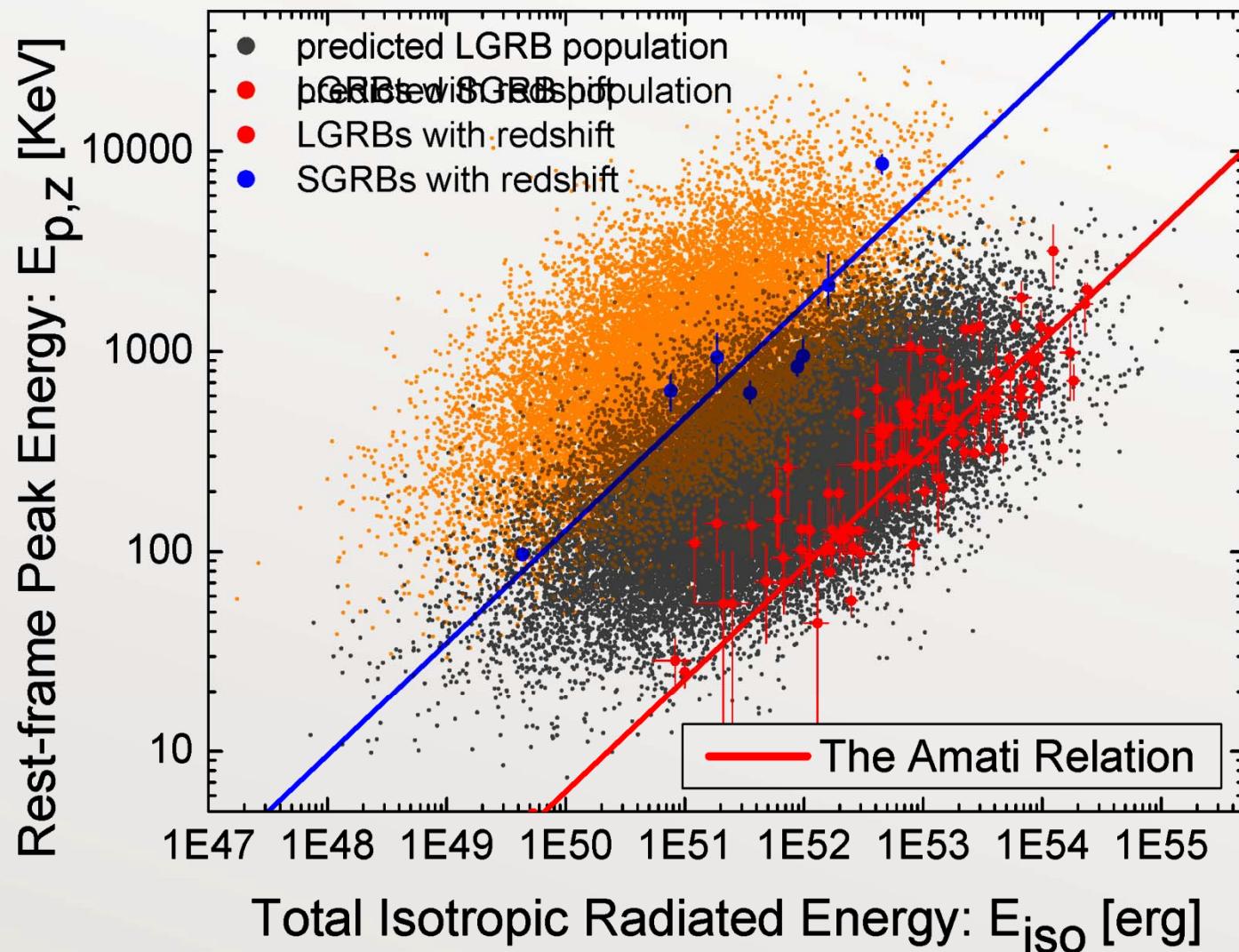


The Amati relation

- Larger dispersion is predicted (Shahmoradi, 2013, ApJ, 766, 111)
- Different slope is predicted (Shahmoradi, 2013, Stanford eConf Proc. C1304143, paper 14; arXiv:1308.1097)



Short and long GRBs exhibit similar prompt correlations



Summary for GRB astronomers

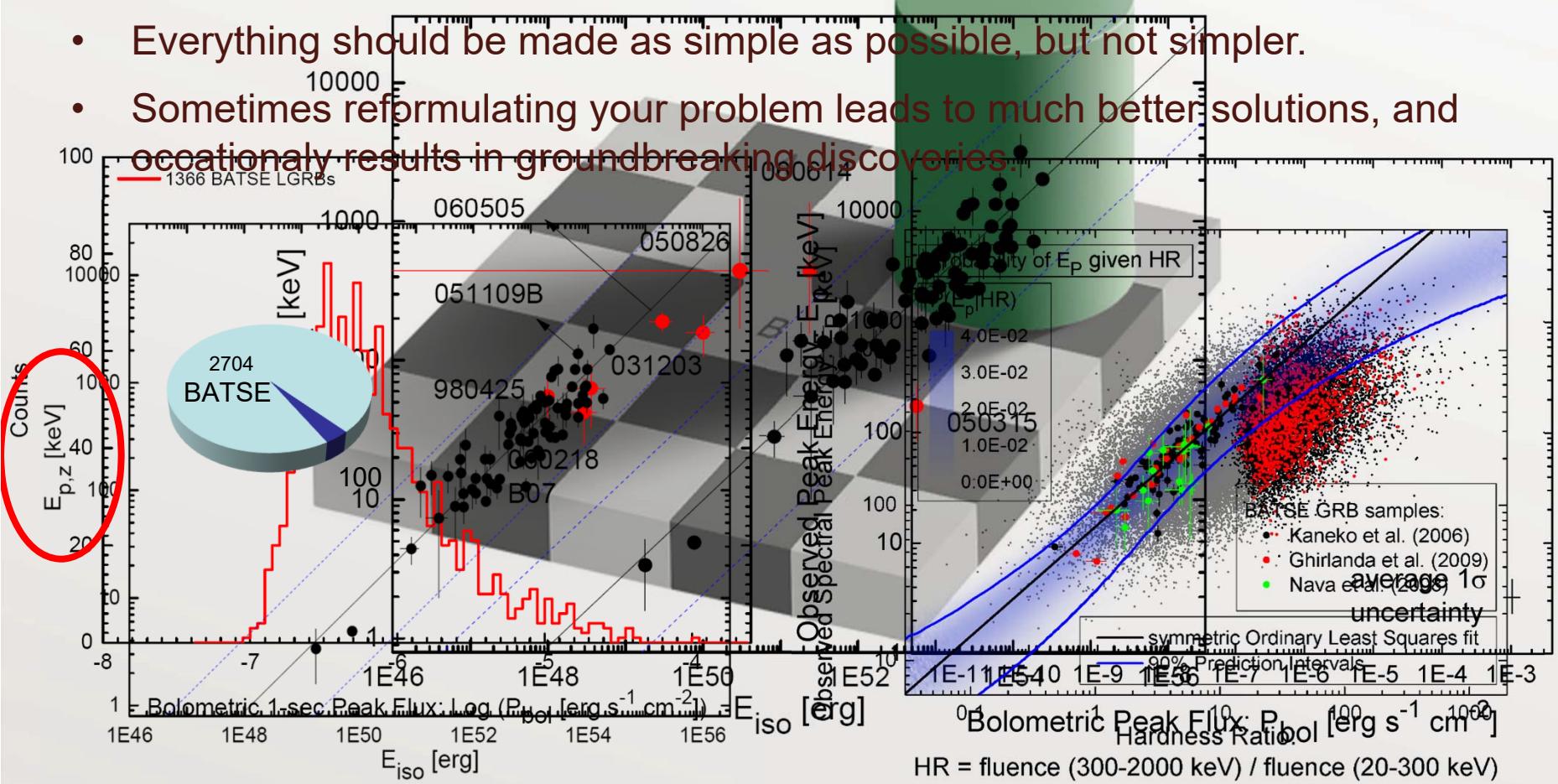
- Multivariate log-normal distribution provides good fit to BATSE short and long GRB prompt emission data (*peak luminosity, isotropic emission, intrinsic peak energy, intrinsic duration*).
- The Amati (E_{iso} - $E_{P,Z}$) relation is confirmed, but with significantly **higher dispersion** and **shallower slope** of the regression line (0.25 vs. 0.55).
- Short GRBs exhibit very similar prompt emission correlations to long GRBs prompt correlations.
- BATSE Long GRBs data favor, though do not necessitate, a cosmic rate tracing metallicity evolution consistent with a cutoff $Z/Z_{\odot} \sim 0.2\text{--}0.5$, assuming no luminosity–redshift evolution.
- The proposed method provides the most accurate, as of today, method of GRB classification based on prompt emission data.

Further results on GRB energetics & correlations

- Shahmoradi, 2013, ApJ, **766**, 111
- Shahmoradi, 2013, Stanford eConf Proc. C1304143, paper 14; arXiv:1308.1097
- Shahmoradi & Nemiroff, 2010, MNRAS, **407**, 2075–2090
- Shahmoradi & Nemiroff, 2011, MNRAS, **411**, 1843–1856
- Shahmoradi & Nemiroff, 2009, AIP Conf Proc, **1133**, 425

Summary: Lessons learned for everyday life (scientific & non-scientific)

- Never underestimate human cognitive biases in scientific research and life in general
- If you obtain new data in your research that does not match your prior belief, do not discard it as bad-quality data.
- Everything should be made as simple as possible, but not simpler.
- Sometimes reformulating your problem leads to much better solutions, and occasionally results in groundbreaking discoveries.



What if there are better models of GRB rate than multivariate log-normal?

$$P(M_k|D) = \frac{P(D|M_k)P(M_k)}{\sum_k P(D|M_k)P(M_k)}$$

Marginal likelihood (evidence)

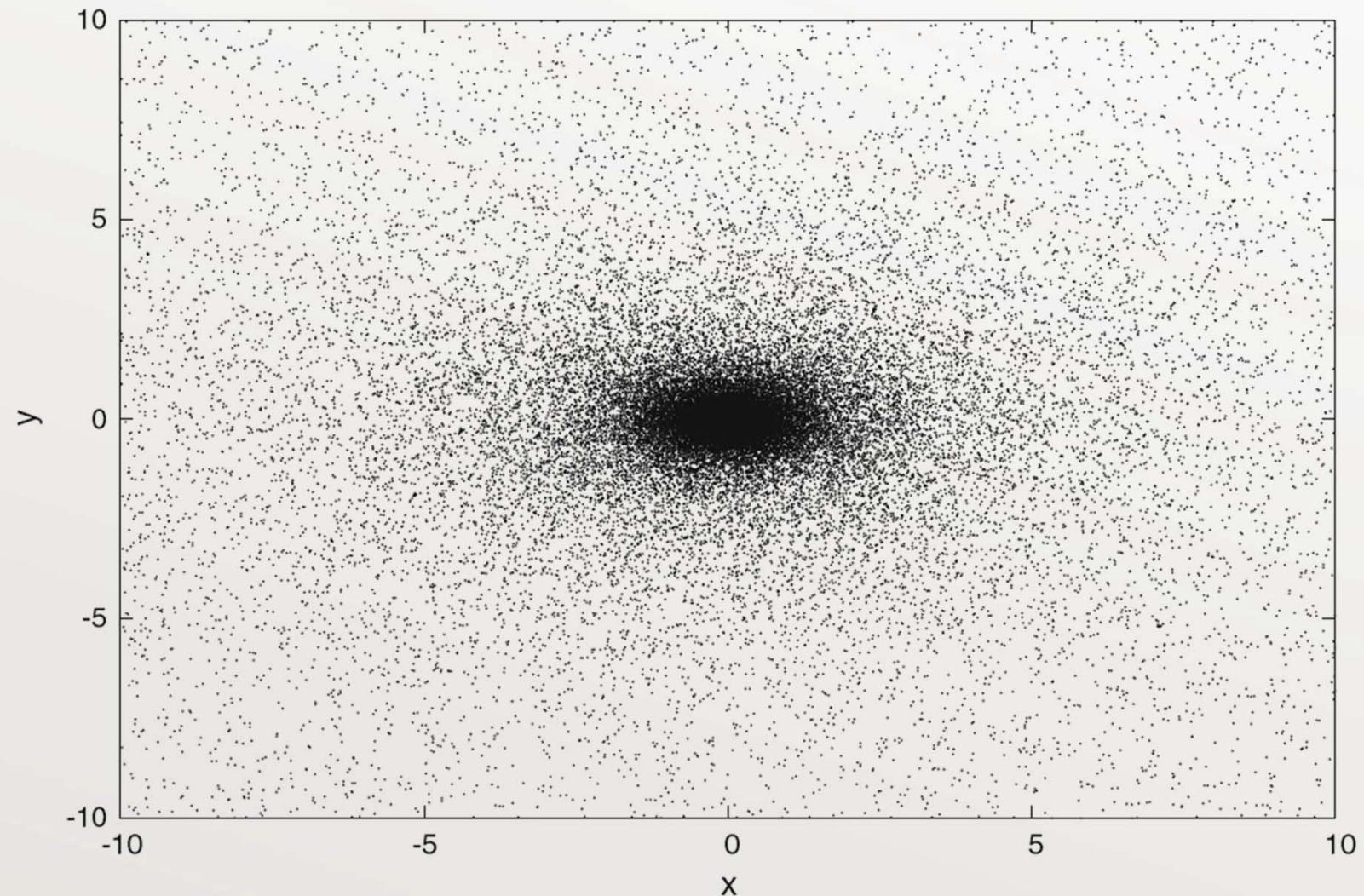
$$P(D|M_k) = \int P(D|\boldsymbol{\theta}, M_k)P(\boldsymbol{\theta}|M_k)d\boldsymbol{\theta}$$

$$\frac{P(M_1|D)}{P(M_2|D)} = \frac{P(D|M_1)}{P(D|M_2)} \times \frac{P(M_1)}{P(M_2)}$$

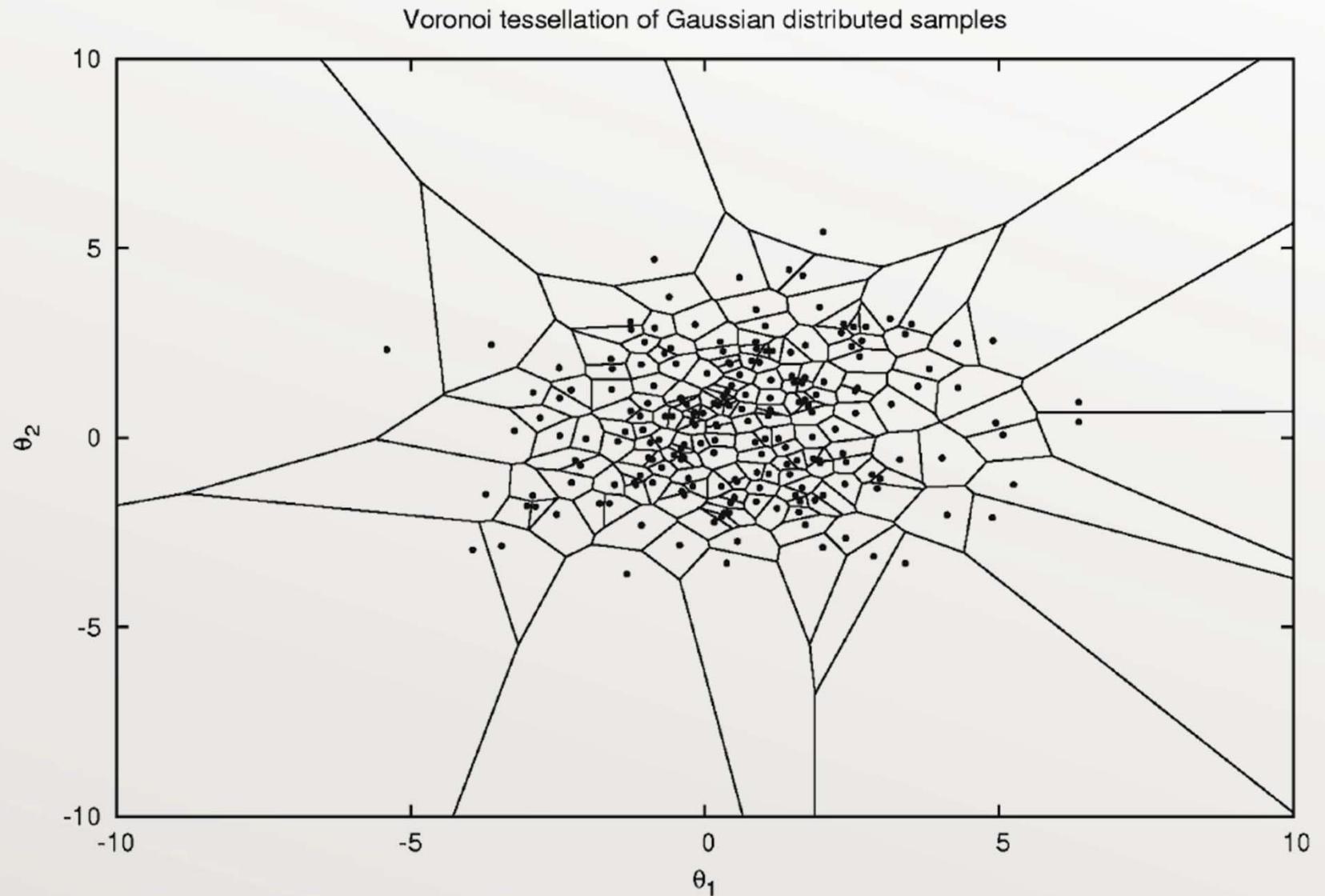


Bayes factor

How to calculate evidence?



How to calculate evidence?



How do astronomers measure the expansion rate of the universe?

Recipe for measuring the expansion rate of the universe:

1. Assume a cosmological model.
2. Find a celestial object that has a known fixed luminosity (a **standard candle**) and measure its distance according to,

$$D_{L,obs} = \sqrt{\frac{1}{4\pi} \frac{\text{Intrinsic brightness}}{\text{observed brightness}}}$$

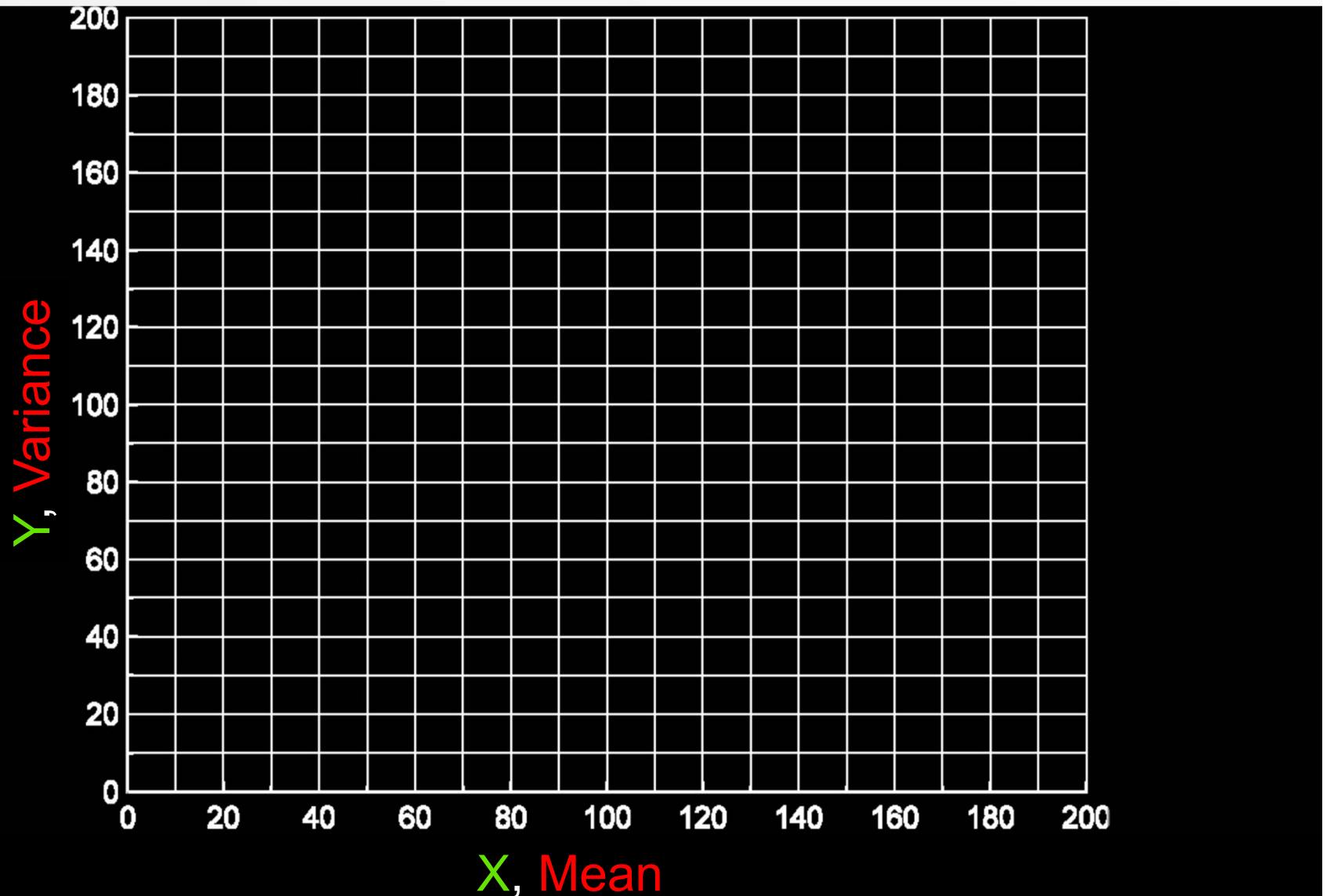


3. Somehow magically measure the redshift (z) of the standard candle. Then calculate,

$$D_{L,theory} = \frac{c}{H_0} (1 + z) \int_0^z \frac{dz'}{\sqrt{(1 + z')^3 \Omega_M(z') + \Omega_\Lambda(z')}}$$

4. Now compare $D_{L,obs}$ with $D_{L,theory}$.

Hallmark of Poisson Stochastic Process: Equal mean and variance of sample



References

1. Shahmoradi, Amir and Nemiroff, Robert J, 2015, MNRAS, **451**, 126-143
2. Shahmoradi, Amir, 2013, The Astrophysical Journal (ApJ), **766**, 111
3. Shahmoradi, Amir, 2013, Stanford eConf Proc. C1304143, paper 14; arXiv:1308.1097
4. Shahmoradi, Amir and Nemiroff, Robert J, 2010, MNRAS, **407**, 2075–2090
5. Shahmoradi, Amir and Nemiroff, Robert J, 2011, MNRAS, **411**, 1843–1856
6. Shahmoradi, Amir and Nemiroff, Robert J, 2009, AIP Conf Proc, **1133**, 425
7. Shahmoradi, Amir and Nemiroff, Robert J, 2009, AIP Conf Proc, **1133**, 323

References

```
@article{shahmoradi2015short,
  title={Short versus long gamma-ray bursts: a comprehensive study of energetics and prompt gamma-ray correlations},
  author={Shahmoradi, Amir and Nemiroff, Robert J},
  journal={Monthly Notices of the Royal Astronomical Society},
  volume={451},
  number={1},
  pages={126--143},
  year={2015},
  publisher={Oxford University Press}
}

@inproceedings{shahmoradi2014similarities,
  title={On the similarities of the prompt gamma-ray emissions in Short and Long Gamma-Ray Busts},
  author={Shahmoradi, Amir},
  booktitle={APS April Meeting Abstracts},
  year={2014}
}
```

References

```
@inproceedings{nemiroff2009causes,  
    title={What Causes GRB Time Dilation?},  
    author={Nemiroff, Robert and Shahmoradi, Amir},  
    booktitle={AIP Conference Proceedings},  
    volume={1133},  
    number={1},  
    pages={323--327},  
    year={2009},  
    organization={AIP}  
}
```

```
@inproceedings{shahmoradi2009real,  
    title={How Real detector thresholds create false standard candles},  
    author={Shahmoradi, Amir and Nemiroff, Robert},  
    booktitle={AIP Conference Proceedings},  
    volume={1133},  
    number={1},  
    pages={425--427},  
    year={2009},  
    organization={AIP}  
}
```

References

```
@inproceedings{nemiroff2010detection,  
    title={Detection Threshold Effects on GRBs as a Cosmological Standard Candle},  
    author={Nemiroff, Robert J and Shahmoradi, A},  
    booktitle={Bulletin of the American Astronomical Society},  
    volume={42},  
    pages={228},  
    year={2010}  
}  
  
@article{shahmoradi2010hardness,  
    title={Hardness as a spectral peak estimator for gamma-ray bursts},  
    author={Shahmoradi, Amir and Nemiroff, Robert J},  
    journal={Monthly Notices of the Royal Astronomical Society},  
    volume={407},  
    number={4},  
    pages={2075--2090},  
    year={2010},  
    publisher={Blackwell Publishing Ltd Oxford, UK}  
}
```

References

```
@inproceedings{miller2011quantifying,  
    title={Quantifying GRB Pulse Shape Evolution to Study the Pulse Scale Conjecture},  
    author={Miller, Daniel and Nemiroff, RJ and Holmes, J and Shahmoradi, A},  
    booktitle={Bulletin of the American Astronomical Society},  
    volume={43},  
    year={2011}  
}  
  
@inproceedings{shahmoradi2011cosmological,  
    title={A Cosmological Discriminator Designed to Avoid Selection Bias},  
    author={Shahmoradi, Amir and Nemiroff, RJ},  
    booktitle={Bulletin of the American Astronomical Society},  
    volume={43},  
    year={2011}  
}
```

References

```
@article{shahmoradi2011vizier,
  title={VizieR Online Data Catalog: Gamma-ray bursts spectral peak estimator (Shahmoradi+, 2010)},
  author={Shahmoradi, A and Nemiroff, RJ},
  journal={VizieR Online Data Catalog},
  volume={740},
  year={2011}
}

@article{shahmoradi2011possible,
  title={The possible impact of gamma-ray burst detector thresholds on cosmological standard candles},
  author={Shahmoradi, A and Nemiroff, RJ},
  journal={Monthly Notices of the Royal Astronomical Society},
  volume={411},
  number={3},
  pages={1843--1856},
  year={2011},
  publisher={Blackwell Publishing Ltd}
}
```

References

```
@article{shahmoradi2013multivariate,
  title={A Multivariate Fit Luminosity Function and World Model for Long Gamma-Ray Bursts},
  author={Shahmoradi, Amir},
  journal={The Astrophysical Journal},
  volume={766},
  number={2},
  pages={111},
  year={2013},
  publisher={IOP Publishing}
}

@article{shahmoradi2013gamma,
  title={Gamma-Ray bursts: Energetics and Prompt Correlations},
  author={Shahmoradi, Amir},
  journal={arXiv preprint arXiv:1308.1097},
  year={2013}
}

@inproceedings{shahmoradi2014classification,
  title={Classification and Energetics of Cosmological Gamma-Ray Bursts},
  author={Shahmoradi, Amir and Nemiroff, RJ},
  booktitle={American Astronomical Society Meeting Abstracts\# 223},
  volume={223},
  year={2014}
}
```