The effects of sock on the adjustment path: Autoregressive Process (Mathematical Structure)

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Note: 3

$$y_t = \rho y_{t-k} + v$$

$$v \sim N(0, \sigma_v^2)$$

$$f^{1}\left(t\right)=\left\{ y_{t}\in\mathbb{R}\mid\left(y_{t}\rightarrow\boldsymbol{y_{t-k}}\right)\mapsto\left(y_{t}\longrightarrow\left(\boldsymbol{\rho}\right)^{t}\times\boldsymbol{v}\right)\;where\;\left(t,\rho,\boldsymbol{v},\boldsymbol{k}\right)\in\mathbb{R}\;\&\;t\longrightarrow\infty,t>\boldsymbol{k}\right\}$$

$$y_t = \gamma e_{t-k} + \zeta$$

$$\zeta \sim N(0, \sigma_{\zeta}^2)$$

$$f^{2}\left(t\right)=\left\{ y_{t}\in\mathbb{R}\mid\left(y_{t}\rightarrow\boldsymbol{e_{t-k}}\right)\mapsto\left(y_{t}\longrightarrow\left(\boldsymbol{\gamma}\right)^{t}\times\boldsymbol{v}\right)\;where\;\left(t,\boldsymbol{\gamma},\boldsymbol{v},\boldsymbol{k}\right)\in\mathbb{R}\;\&\;t\longrightarrow\infty,t>\boldsymbol{k}\right\}$$

$$y_t = \delta \sigma_{t-k} + \eta$$

$$\eta \sim N(0,\sigma_\eta^2)$$

or,

$$\eta \sim G(0, \sigma_{\eta}^2)$$

or,

$$\eta \sim NG(0, \sigma_{\eta}^2)$$

$$f^{3}\left(t\right) = \left\{y_{t} \in \mathbb{R} \mid \left(y_{t} \to \boldsymbol{\sigma_{t-k}}\right) \mapsto \left(y_{t} \longrightarrow \left(\boldsymbol{\delta}\right)^{t} \times \sigma_{t} \times v\right) \text{ where } \left(t, \delta, v, k\right) \in \mathbb{R} \& t \longrightarrow \infty, t > k\right\}$$

References

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