

Chapter-3

3.3

0101111011010100

The attraction is that each hex digit contains one of 16 different characters. (0-9, A-F). Since, with 4 binary bits you can represent 16 different patterns, in hex each digit requires exactly 4 binary bits.

3.12 62x12

Step	Action	Multiplier	Multiplicand	Product
0	Initial values	001 010	000 000 110 010	0000 0000 0000
1	lsb=0, no op Left meand Rshift mplier	000 101	000 001 100 100	000 0000 0000
2.	Prod = Prod + Meand Lshift meand Rshift mplier	000 010	000 011 001 000	000 001 100 100
3.	lsb=0, no op Lshift meand Rshift mplier	000 001	000 110 010 000	000 001 100 100
4.	Prod = Prod + Meand Lshift meand Rshift mplier	000 000	000 1 100 100 000	000 111 110 100
5.	lsb=0, no op Lshift meand Rshift mplier	000 000	011 001 000 000	000 111 110 100
6	lsb=0, no op Lshift meand Rshift mplier	000 000	110 010 000 000	000 111 110 100

$$3 \times 7 \rightarrow (0011)_2 \times (0111)_2$$

Iteration	Step	Multiplier	Multiplicand	Product
0	Initial values	0111	0000 0011	0000 0000
1	1a: $1 \Rightarrow \text{Prod} = \text{Prod} + \text{Meand}$ 2: Shift left multiplicand 3: Shift right multiplier	0111 0111 0011	0000 0011 0000 0110 0000 0110	0000 0011 0000 0011 0000 0011
2	1a: $1 \Rightarrow \text{Prod} = \text{Prod} + \text{Meand}$ 2: Shift left multiplicand 3: Shift right multiplier	0011 0011 0001	0000 0110 0000 1100 0000 1100	0000 1001 0000 1001 0000 1001
3	1a: $1 \Rightarrow \text{Prod} = \text{Prod} + \text{Meand}$ 2: Shift left multiplicand 3: Shift right multiplier	0001 0001 0000	0000 1100 0000 1000 0001 1000	0000 0101 0001 0101 0001 0101

$$\underline{3.15} \\ \# 2 \times 4 \rightarrow (0010)_2 \times (0100)_2$$

Iteration	Step	Multiplier	Multiplicand	Product
0	Initial values	0100	0000 0010	0000 0000
1	1a: $1 \Rightarrow \text{Prod} = \text{Prod} + \text{Meand}$ 2: Shift left multiplicand 3: Shift right multiplier	0100 0100 0010	0000 0010 0000 0100 0000 0100	0000 0010 0000 0010 0000 0010
2	1a: $1 \Rightarrow \text{Prod} = \text{Prod} + \text{Meand}$ 2: Shift left multiplicand 3: Shift right multiplier	0010 0010 0001	0000 0100 0000 1000 0000 1000	0000 0110 0000 0110 0000 0110
3	1a: $1 \Rightarrow \text{Prod} = \text{Prod} + \text{Meand}$ 2: Shift left multiplicand 3: Shift right multiplier	0001 0001 0000	0000 1000 0000 0000 0001 0000	0000 1010 0000 1110 0000 1110
4				

Division

$$7 \div 2$$

$$2(1110) \times 5(1100) \leftarrow 5 \times 2$$

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Iteration	Step	Quotient	Divisor	Remainder
0	Initial value	0000	0010 0000	0000 0111
1	1a: Rem = Rem - Div 2b: Rem < 0 \Rightarrow +Div, set Q, Q0 = 0 3: Shift Div Right	0000 01000 01000	0010 0000 0010 0000 0001 0000	0110 0111 0000 0111 0000 0111
2	1: Rem = Rem - Div 2b: Rem < 0 \Rightarrow +Div, set Q, Q0 = 0 3: Shift Div Right	0000 0000 01000	0001 0000 0001 0000 0000 1000	0111 0111 0000 0111 0000 0111
3	1: Rem = Rem - Div 2b: Rem < 0 \Rightarrow +Div, set Q, Q0 = 0 3: Shift Div Right	0000 0000 0000	0000 1000 0000 1000 0000 0100	1111 1111 0000 0111 0000 0111
4	1: Rem = Rem - Div 2: Rem ≥ 0 , set Q, Q0 = 1 3: Shift Div Right	0000 0001 0001	0000 0100 0000 0100 0000 0010	0000 0011 0000 0011 0000 0011
5	1: Rem = Rem - Div 2: Rem ≥ 0 , set Q, Q0 = 1 3: Shift Div Right	0001 0011 0011	0000 0010 0000 0010 0010 0001	0000 0001 0000 0001 0000 0001

#3.22

~~#3.22~~

L-1029010

Iteration	Step	Quotient	Divisor	Remainder
0	Initial value PC0	0000	0010 0000	0000 0011
1	1: Rem = Rem - Div 2b: Rem < 0 \Rightarrow + Div, all Q, Q=0 3: Shift div right	0000 0000 0000	0010 0000 0010 0000 0001 0000	①110 0011 0000 0011 0000 0011
2	1: Rem = Rem - Div 2b: Rem < 0 \Rightarrow + Div, all Q, Q=0 3: Shift div right	0000 0000 0000	0001 0000 0001 0000 0000 1000	①111 0011 0000 0011 0000 1001
3	1: Rem = Rem - Div 2b: Rem < 0 \Rightarrow + Div, all Q, Q=0 3: Shift div right	0000 0000 0000	0000 1000 0000 1000 0000 0100	①111 1011 0000 0011 0000 0011
4	1: Rem = Rem - Div 2b: Rem < 0 \Rightarrow + Div, all Q, Q=0 3: Shift div right	0000 0000 0000	0000 0100 0000 0100 0000 0010	①111 1111 0000 0011 0000 0011
5	1: Rem = Rem - Div 2b: Rem > 0; all Q, Q=1 3: Shift div right	0000 0001 0001	0000 0010 0000 0010 0000 0001	①000 0001 0000 0001 0000 0001

$$0.1 \times 8.1 = \frac{0.1 \times 8.1}{8.1} = 0.1 \text{ - } 0.1 \text{ - } 0.1 \text{ - } 0.1 \text{ - } 0.1$$

3.22

8. 101. 1010

$$0 \times 0 \text{e} 000000 = 0000 \ 1100 \ 0000 \ 0000 \ 0000 \ 0000 \ 0000 \ 0000$$
$$= 0 \ 0001 \ 1000 \ 0000 \ 0000 \ 0000 \ 0000 \ 0000$$

sign is positive

$$\text{exp} = 0 \times 18$$

$$= 24 - 127$$

$$= -103$$

there is a hidden 1

$$\text{mantissa} = 0$$

$$\text{answer} = 1.0 \times 2^{-103}$$