

* Example 20:-

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a) Solution:-

$$A = \{1, 2, 3, \dots\}$$

$$A \times A = \{1, 2, 3, \dots\} \times \{1, 2, 3, \dots\}$$

$$R = \{(1,1), (1,2), (1,3), \dots, (2,1), (2,2), (2,3), \dots, (3,1), (3,2), (3,3), \dots\}$$

$$\text{Domain} = \{1, 2, 3, \dots\}$$

$$\text{Range} = \{1, 2, 3, \dots\}$$

$$\therefore \text{Dom } R = \text{Range } R = A$$

$$b) T = \{0, \pm 1, \pm 2\}$$

$$T \times T = \{0, 1, -1, 2, -2\} \times \{0, 1, -1, 2, -2\}$$

$$= \{(0,0), (0,1), (0,-1), (0,2), (0,-2), (1,0), (1,1), (1,-1), (1,2), (1,-2), (-1,0), (-1,1), (-1,-1), (-1,2), (-1,-2), (2,0), (2,1), (2,-1), (2,2), (2,-2), (-2,0), (-2,1), (-2,-1), (-2,2), (-2,-2)\}$$

$$R = \{(x,y), x \in T \wedge y \in T \wedge x+y=0\}$$

$$D = \{(0,0), (1,-1), (-1,1), (2,-2), (-2,2)\}$$

$$R_1 = \{(0,0), (1,-1), (-1,1), (2,-2), (-2,2)\}$$

$$\text{Dom } R_1 = \{0, \pm 1, \pm 2\}$$

$$\text{Range } R_1 = \{0, \pm 1, \pm 2\}$$

$$\text{Dom } R_1 = \text{Range } R_1 = \mathbb{T}$$

c) Solution:-

$$E = \{2, 4, 6\}, F = \{0, 1, 2\} \text{ and } R_2 = \{(x, y) |$$

$$x \in E, y \in F \wedge x+y=6\}$$

i) $E \times F$

$$E \times F = \{2, 4, 6\} \times \{0, 1, 2\}$$

$$= \{(2,0), (2,1), (2,2), (4,0), (4,1), (4,2), \\ (6,0), (6,1), (6,2)\}$$

ii) R_2 in tabular form:

$$R_2 = \{(4,2), (6,0)\}$$

iii) $\text{Dom } R_2 = \{4, 6\}$

$$\text{Range } R_2 = \{2, 0\}$$

* Example 21:-

$$A = \{0, 2, 3\}, B = \{0, 2, 4, 6, 9, 16\} \text{ and}$$

$A = \{0, 2, 3\}$, $B = \{0, 2, 4, 6, 9, 16\}$ and
 $R = \{(x, y) \mid x \in A \wedge y \in B \wedge x^2 = y\}$ Verify
 $\text{Dom } R^{-1} = \text{Range } R$ and $\text{Range } R^{-1} =$
 $\text{Dom } R$

Solution:-

$$A \times B = \{0, 2, 3\} \times \{0, 2, 4, 6, 9, 16\}$$

$$= \{(0, 0), (0, 2), (0, 4), (0, 6), (0, 9), (0, 16),$$

$$(2, 0), (2, 2), (2, 4), (2, 6), (2, 9), (2, 16),$$

$$(3, 0), (3, 2), (3, 4), (3, 6), (3, 9), (3, 16)\}$$

$$R = \{(0, 0), (2, 4), (3, 9)\}$$

$$\text{Dom } R = \{0, 2, 3\}, \text{ Range } R = \{0, 4, 9\}$$

$$R^{-1} = \{(0, 0), (4, 2), (9, 3)\}$$

$$\text{Dom } R^{-1} = \{0, 4, 9\}, \text{ Range } R^{-1} = \{0, 2, 3\}$$

$$*\text{Dom } R^{-1} = \{0, 4, 9\} = \text{Range } R$$

$$*\text{Range } R^{-1} = \{0, 2, 3\} = \text{Dom } R$$

* Ex # 3.4

$$(Q) (i) A = \{1, 3\}, B = \{0, 2, 4\}$$

Solution:-

$$n(A) = 2, n(B) = 3$$

No. of binary relations in $A \times B = 2^{n(A \times B)}$

$$n(A) = 2, \text{ thus } -$$

Number of binary relations in $A \times B = 2^{n(A \times B)}$

$$= 2^{2 \times 3}$$
$$= 2^6$$
$$= 64$$

(ii) $n(C) = 7$

Number of binary relations in $C \times C = 2^{n(C \times C)}$

$$= 2^{7 \times 7}$$
$$= 2^{49}$$

(iii) $D = \{1, 3, 5\}$

$$n(D) = 3$$

Number of binary relations in $D \times D = 2^{n(D \times D)}$

$$= 2^{(3 \times 3)}$$
$$= 2^9$$