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# Assignment : DAA.

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1. Solve The following.

$$T(n) = T(n-1) + 5 \quad \text{for } n > 1 \quad T(1) = 0.$$

$$\text{at } n=1; \quad T(1) = 0$$

$$\begin{aligned} n=2; \quad T(2) &= T(2-1) + 5 \\ &= 0 + 5 = 5 \end{aligned}$$

$$\begin{aligned} T=4; \quad T(4) &= T(3) + 5 \\ &= 15 \end{aligned}$$

$$T(n) = T(1) + (n-1) \cdot 5$$

$$T(n) = 5(n-1)$$

$$\begin{aligned} T(3) &= n(3-1) + 5 \\ &= n(2) + 5 \\ &= 10. \end{aligned}$$

$T(n)$  is +5 for each increment.

B.  $T(n) = 3T(n-1)$  for  $n > 1$   $T(1) = 4$ ,

$$n=1; \quad T(1) = 4 \quad (\text{Given})$$

$$n=2; \quad T(2) = 3T(2-1)$$

$$= 3T(1)$$

$$= 3 \times 4 = 12$$

$$n=4; \quad T(4) = 3T(4-1)$$

$$= 3(36)$$

$$= 108.$$

$$\begin{aligned} n=3; \quad T(3) &= 3T(3-1) \\ &= 3T(2) \end{aligned}$$

$$= 3 \times 12$$

$$T(3) = 36$$

$(T(n))$  is obtained

$$\therefore T(n) = 4 \times 3^{n-1}$$

C).  $T(n) = T(n/2) + n$  for  $n > 1$   $T(1) = 1$

Solve  $n=2^k$

$$n=2^k$$

$$n=1; \quad T(1) = 1$$

$$n=2; \quad T(2) = T(2/2) + n$$

$$= 1 + 2 = 3$$

$$n=4; \quad T(4) = T(4/2) + 4$$

$$= T(2) + 4$$

$$= 7.$$

$$n=8; \quad T(8/2)+8$$

$$= T(4)+8$$

$$= 7+8=15$$

$$n=16; \quad T(8)+16$$

$$= 15+16=31$$

$$T(2^k) = T(2^{k-1}) + 2^k$$

$$T(2^k) = 2^{k+1} - 1$$

$$2^k = n$$

$$T(n) = T(2^k) = 2^{(\log_2 n)+1} - 1$$

$$= 2 \cdot 2^{\log_2 n} - 1$$

$$= 2n - 1$$

d).  $T(n) = T(n/3) + 1 \quad n > 1 \quad T(1) = 1 \quad \text{Solve } n=27$

$$T(1) = 1$$

$$T(3) = T(1) + 1 = 2$$

$$T(9) = T(3) + 1 = 3$$

$$T(27) = T(9) + 1 = 4$$

$$T(n) = 1 + \log_3 n$$

Evaluate The following.

i.  $T(n) = T(n/2) + 1$ ; where  $n=2^k$  for all  $k \geq 0$ .

Assume  $n=2^k$  i.e.  $k = \log n$ .

$$T(2^k) = T\left(\frac{2^k}{2}\right) + 1$$

$$= T(2^{k-1}) + 1$$

$$T(2^k) = T(2^{k-1}) + 2$$

$$T(2^k) = T(2^{k-1}) + 3$$

$$T(2^k) = T(2^{k-k}) + k = T(2^0) + k = T(1) + k.$$

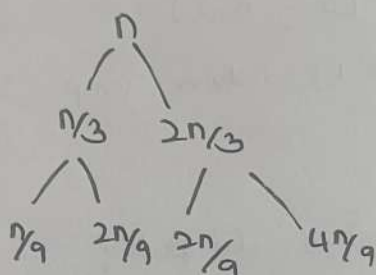
$$T(1) = 1$$

$$T(2^k) = k+1$$

$$\text{i.e. } T(n) = \log n + 1.$$

$$T(n) = (\log n)$$

ii  $T(n) = T(n/3) + T(2n/3) + cn$ , where  $c$  is constant.



$T(n) =$  Sum of all numbers.

$$\text{length} = \log_{3/2} n.$$

$$T(n) > n \log_{3/2} n$$

$\therefore T$  is  $\Omega(n \log n)$

$$\text{depth} = \log_{3/2} n$$

$$T(n) \leq n \log_{3/2} n.$$

analyse the order of growth.

P.  $f(n) = 2n^2 + 5$  &  $g(n) = 7n$ . use the  $\Omega g(n)$ .

$$f(n) = 2n^2 + 5 > c \cdot g(n). \quad f(n) \geq c \cdot g(n)$$

$$\text{if } n=1; \quad 7 = 7$$

$$n=2; \quad 13 = 14$$

$$n=3; \quad 23 = 21$$

$$n=4: 37 > 28$$

$$n=5, 55 > 35$$

$f(n)$  is greater

$$f(n) \geq g(n).$$

3). Consider The following.

$\min [A[0] \dots n-1]$ .

if  $n=1$  return  $A[0]$

else  $\text{Temp} = \min A[0 \dots n-2]$

if  $\text{Temp} < A[n-1]$  return  $\text{Temp}$

else

return  $A[n-1]$

Q]. What does this algorithm compute?

returns min value in array A.

! Best case ( $n=1$ )

if  $n=1$ , only one element. It returns the  $A[0]$  and its min value in a single element array.

2. Recursive case:

if  $n > 1$ , create the Temp

call recursively ( $A[0 \dots n-2]$ ) = first  $n-1$  element.

Comparing Temp with last element ( $A[n-1]$ )

if  $\text{Temp} < A[n-1]$

return Temp

else

return  $A[n-1]$ .

8 Set up a recurrence relation for the algorithm's basic operation count & solve it.

Base case:  $T(1) = C_1$  [constant  $C_1$ ]

recursive case:  $T(n) = T(n-1) + C_2$  [ $C_2 \rightarrow$  constant]

Final Solution:-

$$T(n) = C_2 * n^2 + (C_1 - C_2)$$

$$T(n) = O(n^2).$$