

Linked List 2



Agenda

- 1. Revision Quizzes
- 2. Find Middle of linkedlist
- 3. Merge Two Sorted linkedlist
- 4. Sort the given linkedlist (MergeSort)
- 5. Google Maps got your back
- 6. Detect Cycle in the linkedlist
- 7. Starting point of cycle



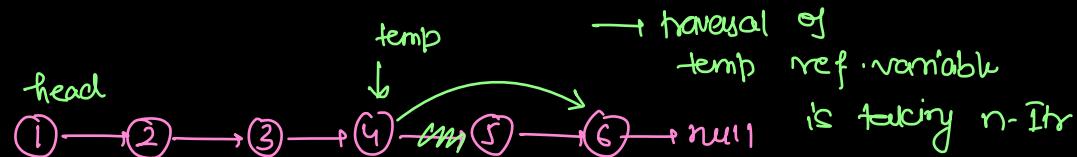
Hello Everyone

Very Special Good Evening

to all of you 😊😊😊

We will start session
from 9:06 PM

Revision Quizzes



Quiz 1:

What is the time complexity needed to delete a node from a linked list?

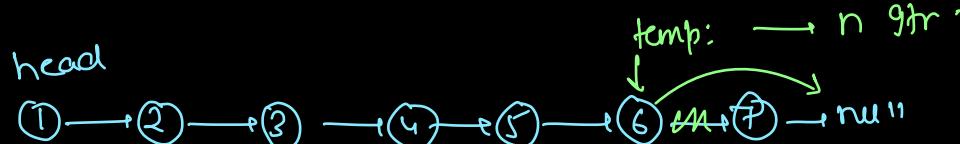
- [] $O(1)$
- [] $O(N)$
- [] $O(\log(N))$
- [] $O(N^2)$



Quiz 2:

What is the time complexity needed to insert a node as the head of a linked list?

- [] $O(1)$
- [] $O(N)$
- [] $O(\log(N))$
- [] $O(N^2)$



Quiz 3:

What is the time complexity needed to delete the last node from a linked list?

- [] $O(1)$
- [] $O(N)$
- [] $O(\log(N))$
- [] $O(N^2)$

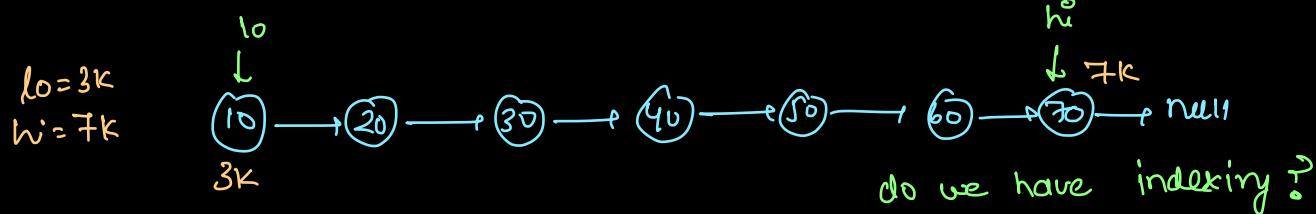
Quiz 4:

Can we do Binary Search in a sorted Linked List?

[] Yes

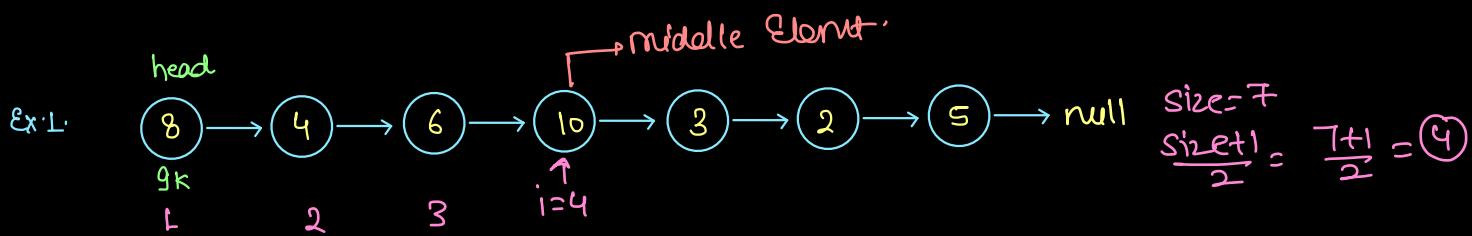
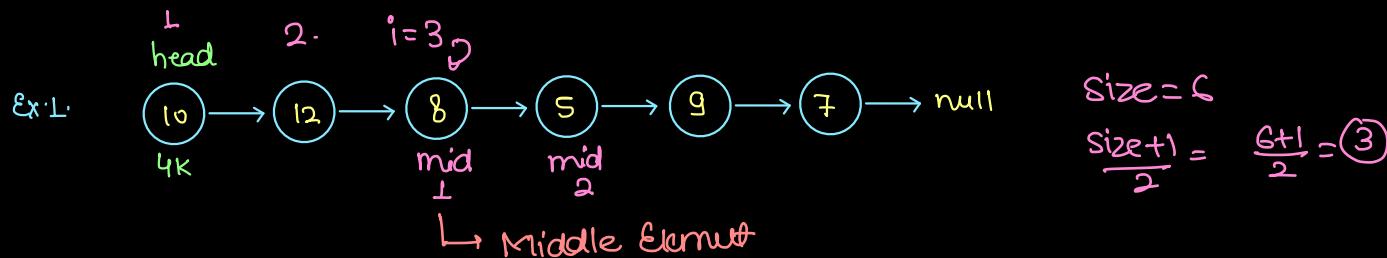
[] No

$$\text{mid} = \frac{l_0 + h}{2}$$



Find Middle of linkedlist

Given a Linked List, Find the middle element.



Idea 0: Brute force Approach:

1. calculate size of the linkedlist from head pointer.
2. iterate from 1 to $\frac{\text{size}+1}{2}$ to find middle of LL.

Pseudo:

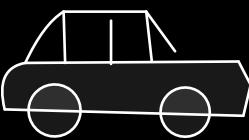
```

Node middleElement( Node head) {
    // calculate size           → n - Iterate
    // iterate from i=1 to i <  $\frac{\text{size}+1}{2}$  to find middle →  $\frac{n}{2}$  for
}
Total time = n +  $\frac{n}{2}$  =  $\frac{3n}{2}$ 
T.C: O(n)
S.C: O(1)

```

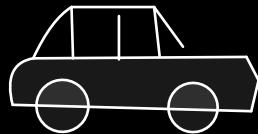
Idea 1: slow and fast pointers:

1. slow
2. fast



speed of corr = x
(slow)

$$d_{\text{slow}} = x * T = xT$$

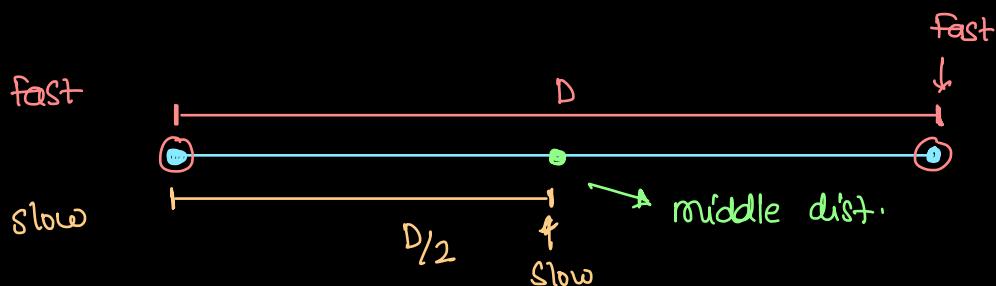


speed of corr = $2x$
(fast)

$$d_{\text{fast}} = 2x * T = 2xT$$

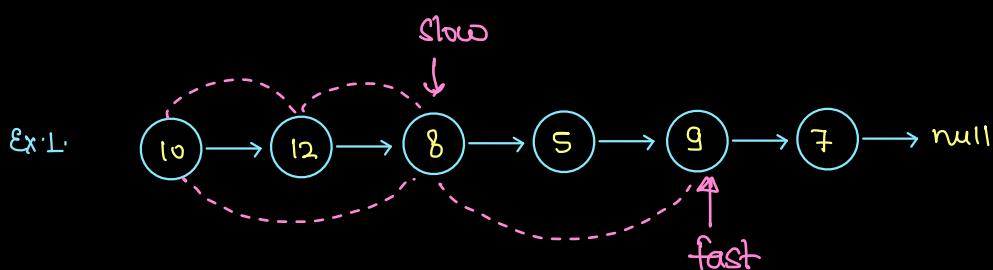
$$\text{dist(fast)} = 2 * \text{dist(slow)}$$

$$\Rightarrow \text{dist(slow)} = \frac{\text{dist(fast)}}{2}$$



Conclusion:

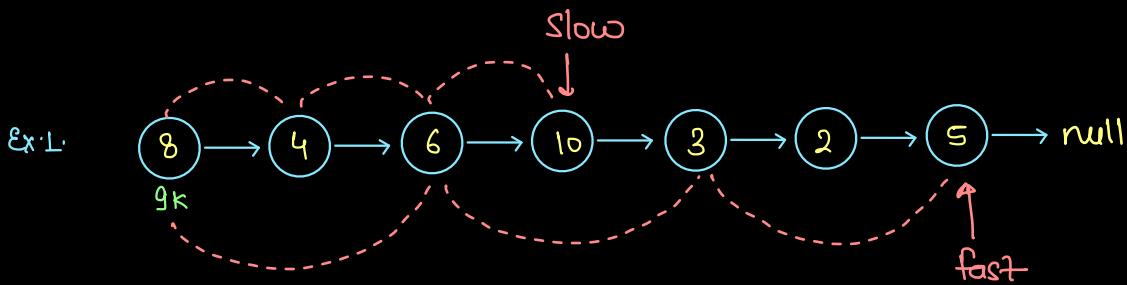
- * Start slow & fast from same point
- * When fast reaches at end position of slow is mid pos.



Stop condition $\Rightarrow \text{fast} \cdot \text{next} \cdot \text{next} == \text{null}$

Running condition $\Rightarrow \text{fast} \cdot \text{next} \cdot \text{next} != \text{null} \rightarrow$ keep going

①



Stop condition \rightarrow $\text{fast} \cdot \text{next} == \text{null}$

Running cond. \rightarrow $\text{fast} \cdot \text{next} != \text{null}$ \longrightarrow keep gtr ②

How to unite both condition together \rightarrow

Condition 1 \rightarrow $\text{fast} \cdot \text{next} \cdot \text{next} == \text{null}$

Condition 2 \rightarrow $\text{fast} \cdot \text{next} != \text{null}$

Final cond. \longrightarrow Condition 2 $\&\&$ Condition 1

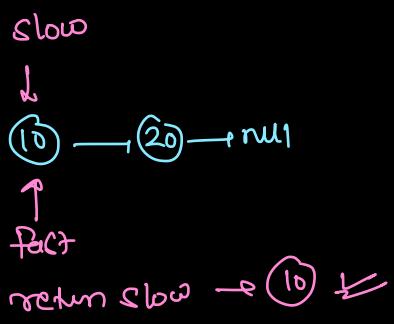
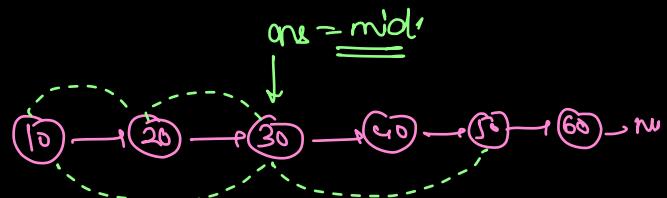
Pseudo code:

```
Node middleNode( Node head) {
    Node slow = head;
    Node fast = head;

    while( fast != null && fast.next != null) {
        slow = slow.next;
        fast = fast.next.next;
    }
}
```

3

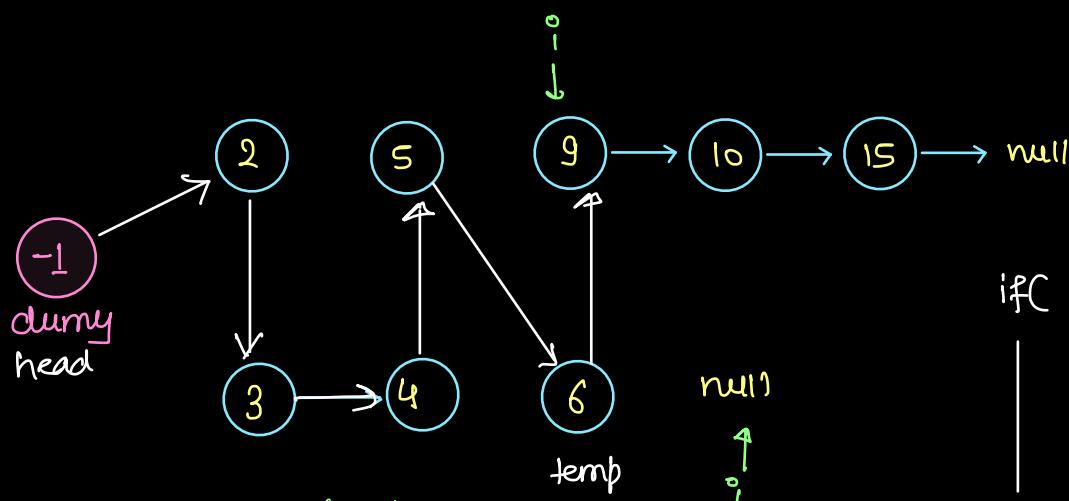
```
slow
↓
(8) → null
↑
fast
return slow
```



$$\text{gtr} = \frac{n}{2}. \quad \text{T.C: } O(n)$$

Merge Two Sorted linkedlist

Given two sorted Linked Lists, Merge them into a single sorted linked list.



if i is exhausted, 'j' available.
temp.next = j;

if j is exhausted, 'i' is avl.
temp.next = i;

ans → dummyhead.next;

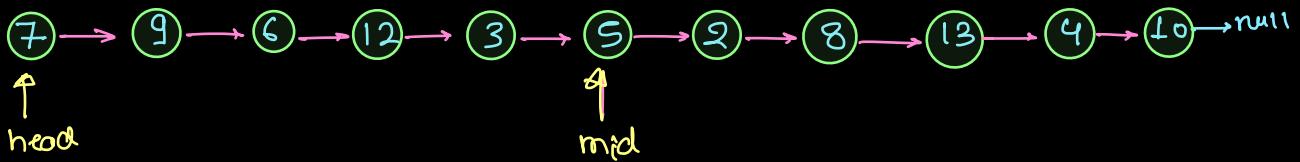
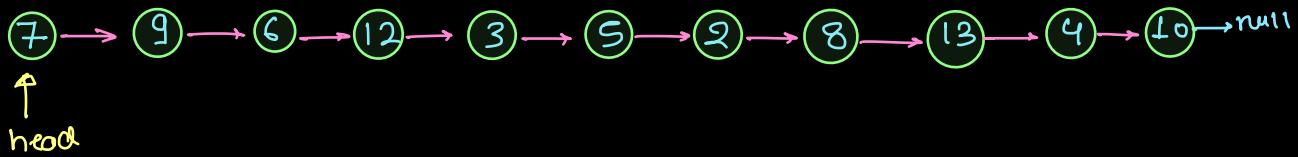
```
if(i.data < j.data){  
    temp.next = i;  
    temp = temp.next;  
    i = i.next;  
}  
else{  
    temp.next = j;  
    temp = temp.next;  
    j = j.next;  
}
```

Pseudo code:

```
Node mergeTwoSorted( Node head1, Node head2 ) {  
    Node dummyHead = new Node(-1);  
    temp = dummyHead, i = head1, j = head2;  
    while( i != null && j != null ) {  
        if( i.data <= j.data ) {  
            temp.next = i;  
            i = i.next;  
        } else {  
            temp.next = j;  
            j = j.next;  
        }  
        temp = temp.next;  
    }  
    if( i != null ) temp.next = i;  
    if( j != null ) temp.next = j;  
    return dummyHead.next;  
}
```

Sort the given linkedlist (MergeSort)

A Linked List is given, Sort the Linked list using merge sort.



① Given head

② find middle node .

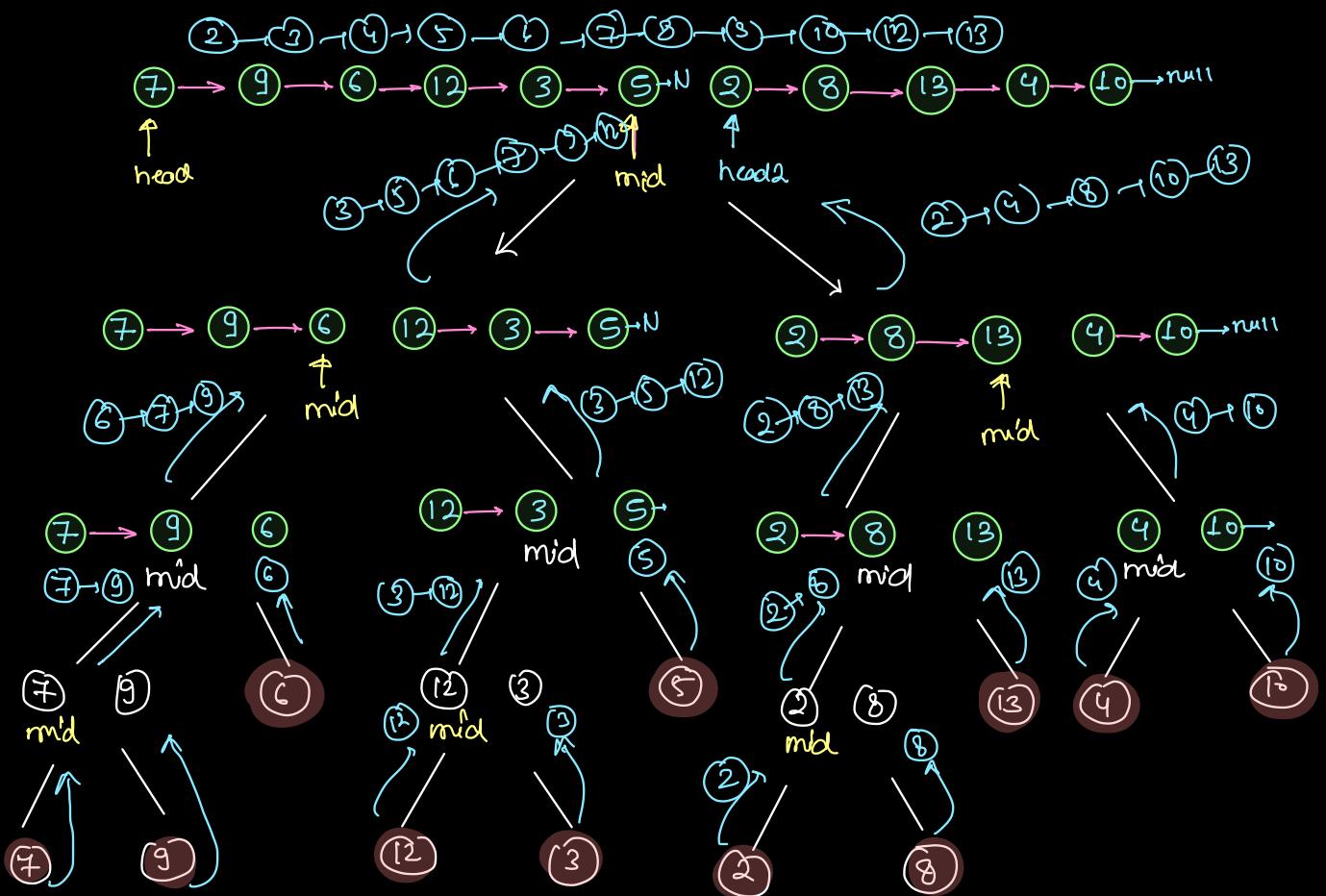
→ split the LL in two parts.

 head₁ → head to mid

 head₂ → mid.next to last

③ Ask from Recursion to sort both of the LL

④ Merge two sorted linkedlist. & return final head;



pseudo code:

```
Node mergeSort(Node head) { → T(n)
    if (head.next == null) {
        return head;
    }
    Node mid = middleNode(head); →  $\frac{n}{2}$ 
    Node head2 = mid.next;
    mid.next = null;

    Node left = mergeSort(head); →  $T(\frac{n}{2})$ 
    Node right = mergeSort(head2); →  $T(\frac{n}{2})$ 
    Node ans = mergeTwoSortedLL(left, right); → n
    return ans;
}
```

```
Node middleNode(Node head) {
    TODO
}
```

```
Node mergeTwoSortedLL(Node head1, Node head2) {
    TODO
}
```

$$T(n) = 2T\left(\frac{n}{2}\right) + k_1n + k_2 \rightarrow \text{Solve it}$$

⇒ T.C: $O(n \log n)$
S.C: $O(\log n)$

~~~~~ Google Maps got your back

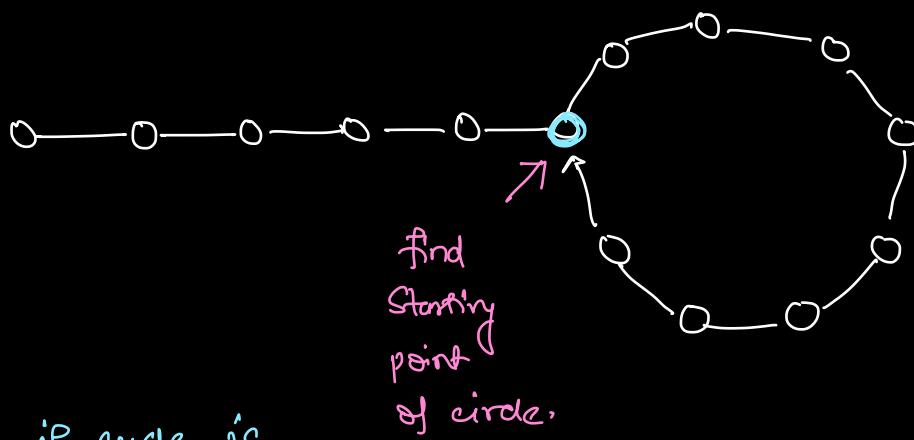
Scenerio

You are using Google Maps to help you find your way around a new place. But, you get lost and end up walking in a circle. Google Maps has a way to keep track of where you've been with the help of special sensors.

These sensors notice that you're walking in a loop, and now, Google wants to create a new feature to help you figure out exactly where you started going in circles.

Problem

You have a linked list that shows each step of your journey, like a chain of events. Some of these steps have accidentally led you back to a place you've already been, making you walk in a loop. The goal is to find out the exact point where you first started walking in this loop.



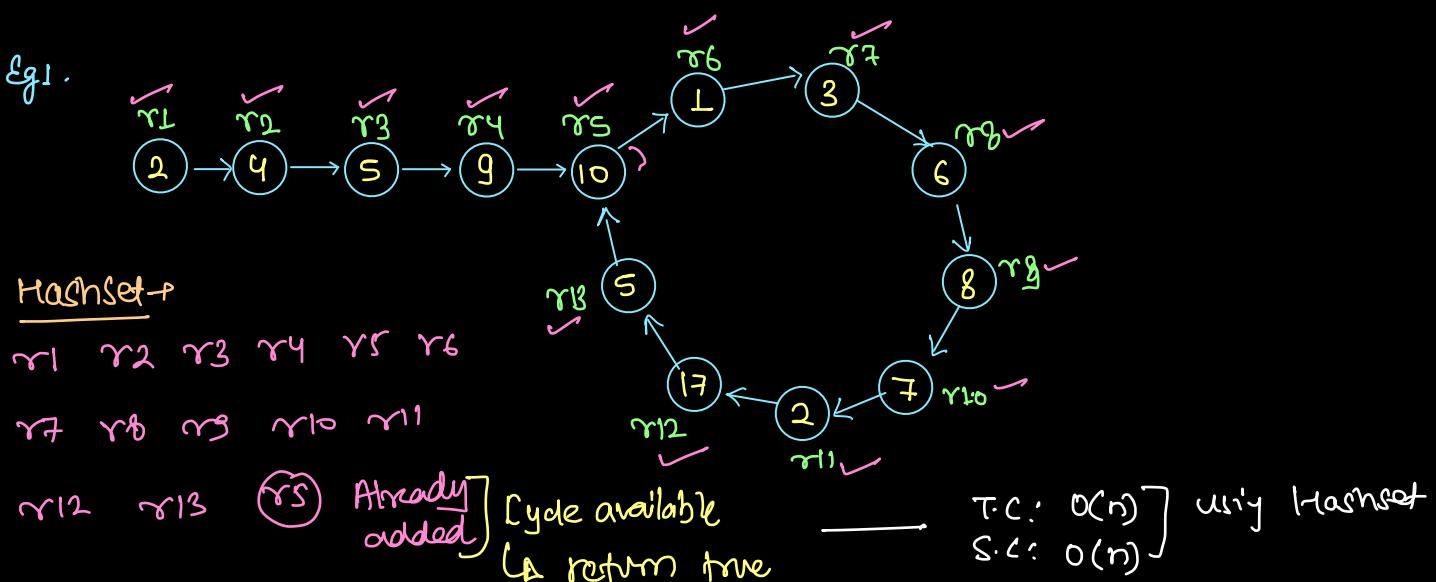
- * Check if cycle is actually present.
- * find starting point of cycle
- * Remove cycle from the linked list

10:36 - 10:46 PM
~~~~~  
Break

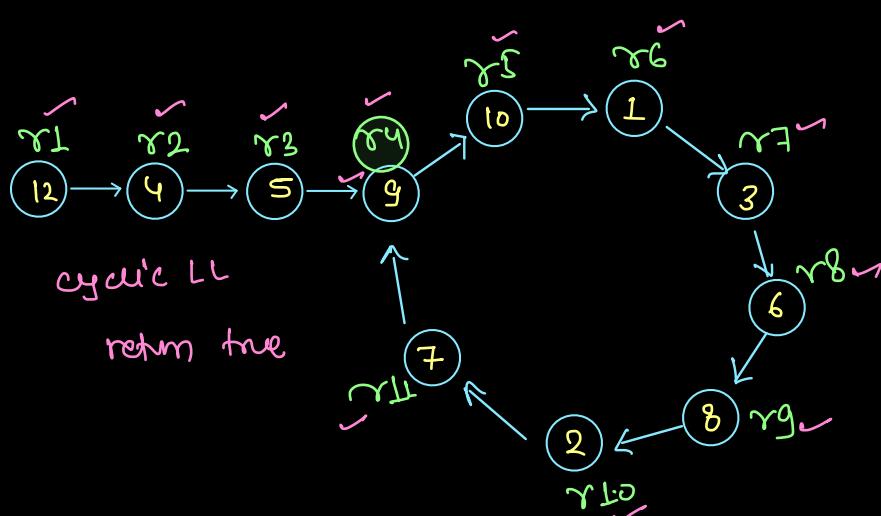
## Detect Cycle in the linkedlist

Given a Linked List, Find whether it contains a cycle.

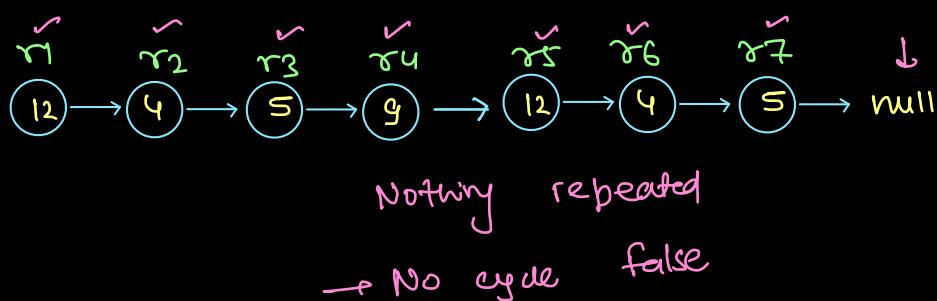
Eg1.



Eg2.



Eg3.



Idea 0: Using HashSet →

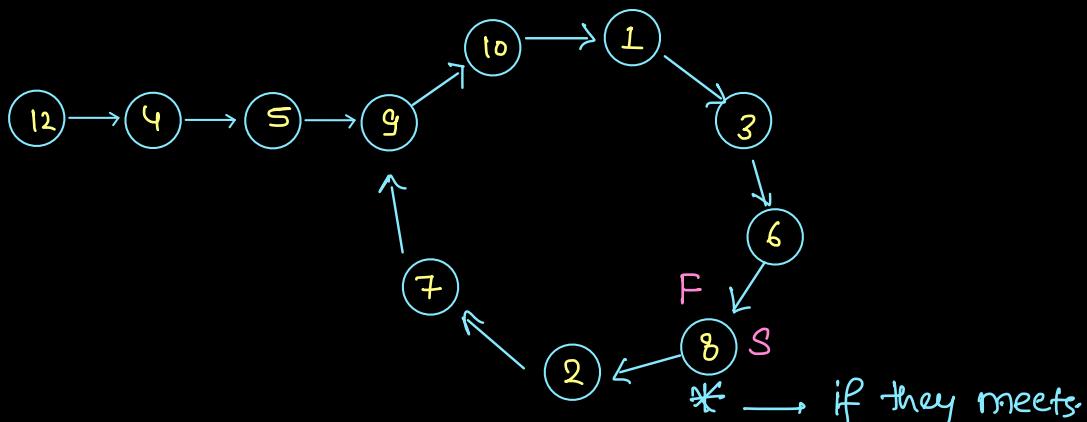
HashSet < Node >

T.C.:  $O(n)$

S.C.:  $O(n)$

Ques 1: without using extra space

Floyd Cycle Detection technique



Steps:

- ① slow = head, fast = head;
- ② slow = slow.next at  $\alpha$  speed  
fast = fast.next.next at  $2\alpha$  speed.
- ③ if cycle present, slow & fast will definitely enter in cycle.  
& if they enter in cycle, they will cross path again
- ④ If they meet at any point, tract may LL is cyclic.

pseudo code:

```
boolean isCyclic(Node head){  
    Node slow = head;  
    Node fast = head;  
    boolean isCycle = false;  
    while(fast.next != null && fast.next.next != null) {  
        slow = slow.next;  
        fast = fast.next.next;  
        if(slow == fast) {  
            isCycle = true;  
            break;  
        }  
    }  
    return isCycle;
```

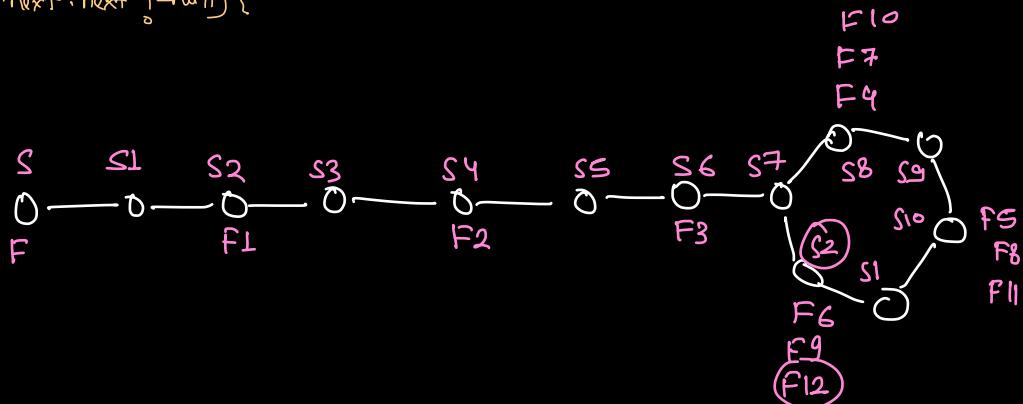
```

boolean isCyclic(Node head) {
    Node slow = head;
    Node fast = head;
    boolean isCycle = false;
    while(fast.next != null && fast.next.next != null) {
        slow = slow.next;
        fast = fast.next.next;
        if(slow == fast) {
            isCycle = true;
            break;
        }
    }
    return isCycle;
}

```

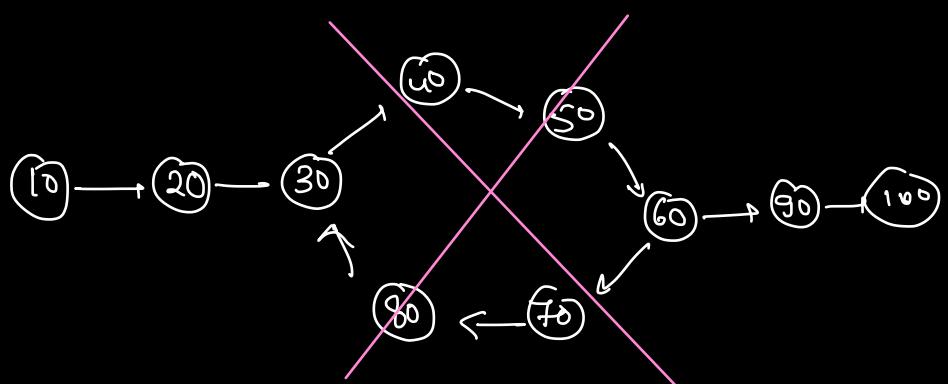
true.

is Cycle = false  
true



$T.C: O(n)$   
 $S.C: O(1)$

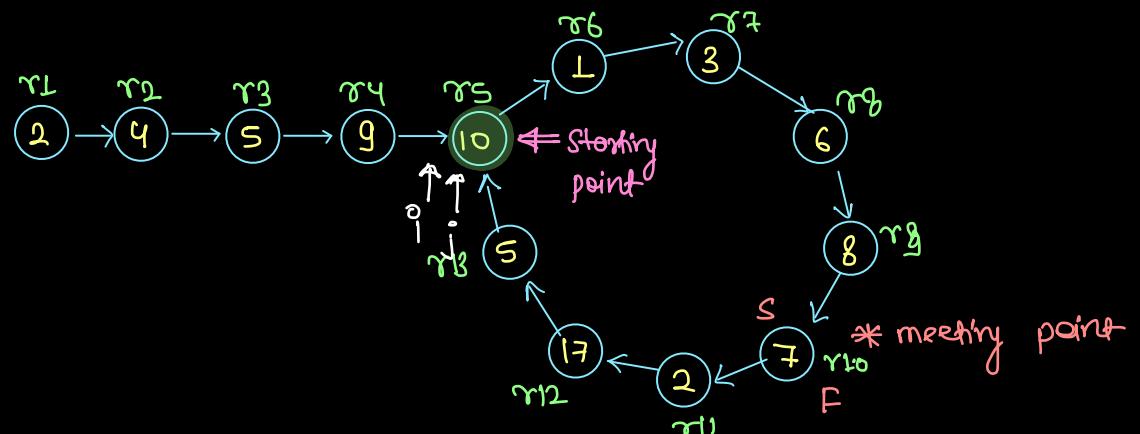
floyd cycle Detection Algorithm.



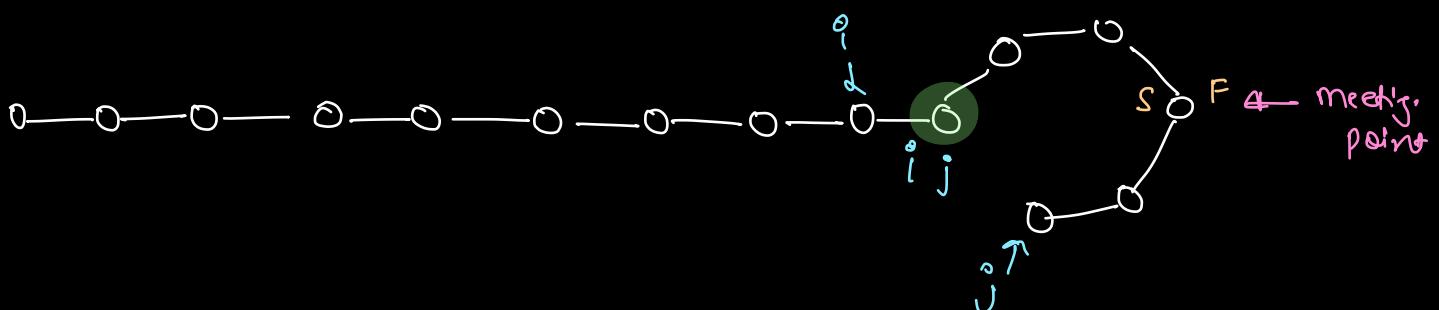
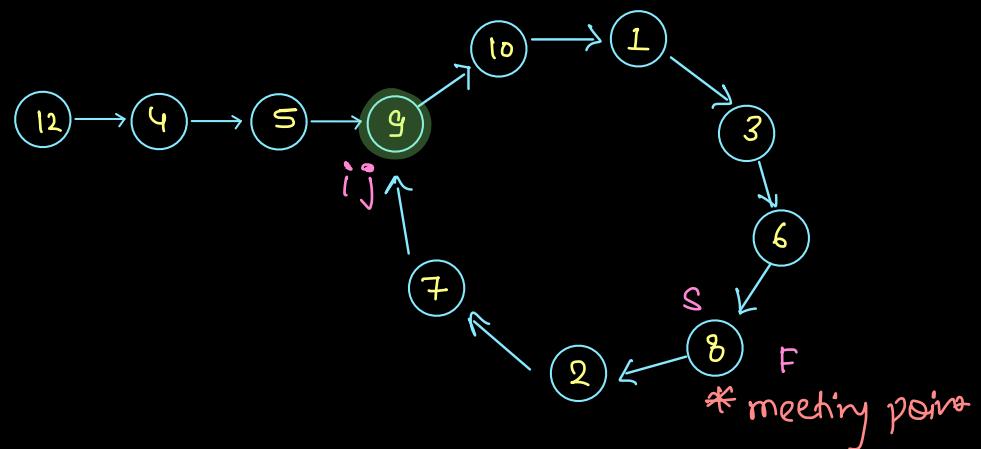
## ~~~~~ Starting point of cycle

Given a Linked List which contains a cycle , Find the start point of the cycle.

Eg 1.



Eg 2.



## Pseudo code:

```
Node startingOfCycle(Node head) {
    Node slow = head;
    Node fast = head;
    boolean isCycle = false;

    while(fast.next != null && fast.next.next != null) {
        slow = slow.next;
        fast = fast.next.next;
        if(slow == fast) {
            isCycle = true;
            break;
        }
    }

    if(isCycle == false) {
        // Do it according to problem statement
        // for now, we are assuming, we have to return null
        return null;
    }

    Node i = head;
    Node j = slow; // meeting point

    while(i != j) {
        i = i.next;
        j = j.next;
    }

    return i;
}
```

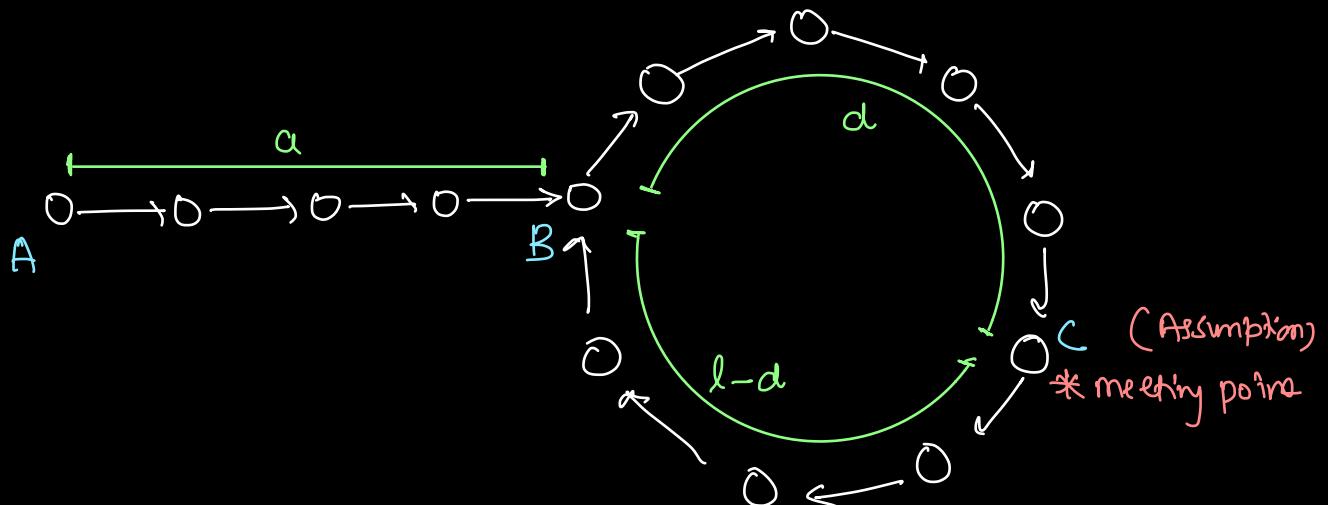
T.C: O(n)  
S.C: O(1)

think about it ?? TODO

if you have to break the cycle

```
while(i.next != j.next) {
    keep iterating
}
After loop:
j.next = null
```

Proof of starting point:



Distance b/w A to B = 'a'

length of complete cycle is = 'l'

Dist. b/w  $\overset{\curvearrowright}{BC} = d'$

Dist. b/w  $\underset{\curvearrowleft}{BC} = 'l-d'$

To prove  $\Rightarrow$

$$a = k * l + 'l-d'$$

dist. travelled by slow ptr = 'a+d'

dist. travelled by fast ptr = "a + x \* l + d" [x. is rotation taken by fast]

$$d_s = D$$

$$d_f = 2D$$

$\Rightarrow d_f = 2 * d_s$ , put the values.

$$a + x * l + d = 2(a+d)$$

$$a + xl + d = 2a + 2d$$

$$xl = a+d$$

$$a = xl - d$$

Add and subtract  $\ell$  in RHS.

$$\Rightarrow a = xl - d + l - l$$

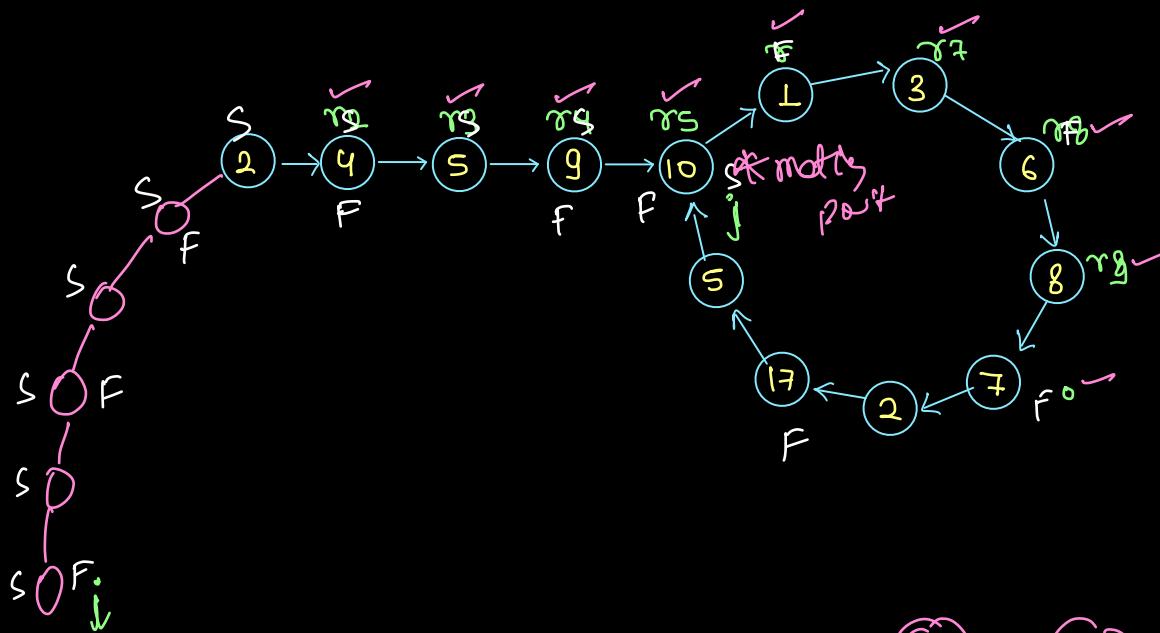
$$\Rightarrow a = xl - l + l - d$$

$$\Rightarrow a = l[x-1] + l-d$$

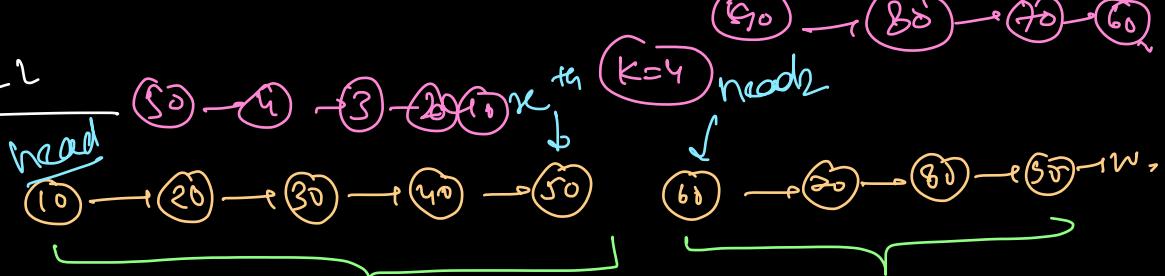
$$\Rightarrow Q = K l + l-d$$

proved<sup>1</sup>

doubt Session:



K-Rotate in LL



(\*) Calculated total size, n=9

④ find  $(n - k - 1)^{\text{th}}$  node (indexing is 0 based)  $\rightarrow$   $k^{\text{th}}$  node

 `head2 = x.next; x.next = null`