

# Collatz conjecture and Prime Numbers Distribution

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# Collatz Conjecture and Prime Numbers Distribution

## Abstract

This paper introduces a proof for Collatz Conjecture based on the distribution of Prime numbers and its composites. Then, we will introduce a formula that includes Collatz function main Cycle (1,2,4) that evaluate to value = 1 for any Natural Number. Also, we will introduce other formulas that evaluates to value [0] or value [1/2] for any real number. Also, we introduced a flipping point formula that will reverse the +ev and -ev numbers on the line number for any Natural number N.


**Keywords:** Collatz Conjecture, Prime Number, Distribution,  $3x+1$  problem.

## 1. Introduction

### 1.1 Pyramid distribution.

Stratring from Natural number 7 we can generate any Prime number and its composite that is  $> 7$

Just by a series of adding fours and two to natural number 7.



The diagram shows a sequence of numbers starting from 7. Red arrows indicate the increments: a horizontal arrow labeled '+4' from 7 to 11, and a diagonal arrow labeled '+2' from 11 to 13. This pattern continues for the rest of the sequence.

7	
7	11
13	17
19	23
25	29
31	35
37	41
43	47
49	53
55	59
61	65
67	71
73	77
79	83
85	89
91	95
97	101
103	107
109	113
115	119
121	125
127	131
133	137
139	143
145	149
151	155
157	161
163	167
169	173
175	179
181	185
187	191
193	197

And once we reached [7] in Collatz conjecture its odd then adding one it goes to 8 and then 4 and then 2 and then 1.

Therefore, any prime number and its composites will go eventually to 1.

Therefore; for any natural number  $N$  ;

$$7 + 1 * 4 * N + 1 * 2 * N = 7 + 6 * N$$

$$7 + \left(\frac{7-1}{6}\right) * 4 * N + \left(\frac{7-1}{6}\right) * 2 * N = M$$

$$M - 7 = 6 * N$$

$M$  is Prime number or composite prime

$$M = 6 * N + 7$$

Therefore, for each Prime number or composite number  $M$  there will be Natural number  $N$  that its multiple of 6 will be exactly different away from the prime number by 7.

$$M - 6 * N = 7$$

$$\begin{aligned} m_1 &= 7 + \frac{7-1}{6} \cdot 4 \cdot 4 + \frac{7-1}{6} \cdot 2 \cdot 4 + \left(\frac{7-1}{6} - 1\right) \cdot 6 \\ &= 31 \end{aligned}$$

$$\begin{aligned} n_1 &= 7 + \frac{7-1}{6} \cdot 4 \cdot 3 + \frac{7-1}{6} \cdot 2 \cdot 3 + \left(\frac{7-1}{6} - 1\right) \cdot 6 \\ &= 25 \end{aligned}$$

$$\begin{aligned} o_1 &= 7 + \frac{7-1}{6} \cdot 4 \cdot 2 + \frac{7-1}{6} \cdot 2 \cdot 2 + \left(\frac{7-1}{6} - 1\right) \cdot 6 \\ &= 19 \end{aligned}$$

$$\begin{aligned} p_1 &= 7 + \frac{7-1}{6} \cdot 4 \cdot 1 + \frac{7-1}{6} \cdot 2 \cdot 1 + \left(\frac{7-1}{6} - 1\right) \cdot 6 \\ &= 13 \end{aligned}$$

$$\begin{aligned} q_1 &= 7 + \frac{7-1}{6} \cdot 4 \cdot 0 + \frac{7-1}{6} \cdot 2 \cdot 0 + \left(\frac{7-1}{6} - 1\right) \cdot 6 \\ &= 7 \end{aligned}$$

Any natural number  $N \leq 7$  already satisfies Collatz conjecture

For any Natural number  $N > 7$  and any  $S = \left\{ \dots, -\frac{3}{2}, -1, -\frac{1}{2}, 0, \frac{1}{2}, 1, \frac{3}{2}, 2, \frac{5}{2}, 3, \frac{7}{2}, 4, \frac{9}{2}, 5, \dots \right\}$  there will be some number  $M$  that satisfies this formula

$$7 + 1 * 4 * S + 1 * 2 * S = M$$

$$7 + \left(\frac{7-1}{6}\right) * 4 * S + \left(\frac{7-1}{6}\right) * 2 * S = M$$

$$7 + \left(\frac{6}{3}\right) * 2 * S + \left(\frac{6}{3}\right) * 1 * S = M$$

$$7 + 2 * 2 * S + 2 * 1 * S = M$$

$$7 + 6 * S = M$$

$$\text{at } S = -\frac{3}{2}; M = -2; \text{because } 7 + 1 * 4 * -\frac{3}{2} + 1 * 2 * -\frac{3}{2} = -2$$

$$\text{at } S = -1; M = 1; \text{because } 7 + 1 * 4 * -1 + 1 * 2 * -1 = 1$$

$$\text{at } S = -\frac{1}{2}; M = 4; \text{because } 7 + 1 * 4 * -\frac{1}{2} + 1 * 2 * -\frac{1}{2} = 4$$

$$\text{at } S = 0; M = 7; \text{because } 7 + 1 * 4 * 0 + 1 * 2 * 0 = 7$$

$$\text{at } S = \frac{1}{2}; M = 10; \text{because } 7 + 1 * 4 * \frac{1}{2} + 1 * 2 * \frac{1}{2} = 10$$

$$\text{at } S = 1; M = 13; \text{because } 7 + 1 * 4 * 1 + 1 * 2 * 1 = 13$$

$$\text{at } S = \frac{3}{2}; M = 16; \text{because } 7 + 1 * 4 * \frac{3}{2} + 1 * 2 * \frac{3}{2} = 16$$

$$\text{at } S = 2; M = 19; \text{because } 7 + 1 * 4 * 2 + 1 * 2 * 2 = 19$$

$$7 + \left(\frac{7-5}{6}\right) * 4 * S + \left(\frac{7-5}{6}\right) * 2 * S = M$$

$$7 + \left(\frac{7-5}{6}\right) * 4 * -1 + \left(\frac{7-5}{6}\right) * 2 * -1 = 5$$

$$7 + \left(\frac{7-5}{6}\right) * 4 * -\frac{1}{2} + \left(\frac{7-5}{6}\right) * 2 * -\frac{1}{2} = 6$$

$$7 + \left(\frac{7-5}{6}\right) * 4 * 1 + \left(\frac{7-5}{6}\right) * 2 * 1 = 9$$

Similarly, the product of any two numbers can be represented as [7], which will fall into Collatz main cycle [4,2,1]

For any two natural number [m] and natural number [n] there will be a new number  $K = m * n$

Such that

$$7 + \left(\frac{m-1}{6}\right) * 4 * n + \left(\frac{m-1}{6}\right) * 2 * n + \left(\frac{n-1}{6} - 1\right) * 6 = m * n$$

$$7 + \left(\frac{m-1}{3}\right) * 2 * n + \left(\frac{m-1}{3}\right) * n + (n - 7) = m * n$$

$$7 = -\left(\frac{m-1}{3}\right) * 2 * n - \left(\frac{m-1}{3}\right) * n - (n - 7) + m * n$$

$$\begin{aligned} h_1 &= -\frac{67-1}{3} \cdot 2 \cdot 97 - \frac{67-1}{3} \cdot 97 - (97-7) + 67 \cdot 97 \\ &= 7 \end{aligned}$$

$$\begin{aligned} i_1 &= \frac{7+1}{2} \\ &= 4 \end{aligned}$$

$$\begin{aligned} j_1 &= \frac{4}{2} \\ &= 2 \end{aligned}$$

$$\begin{aligned} k_1 &= \frac{2}{2} \\ &= 1 \end{aligned}$$

## 2. Collatz Conjecture

### 2.1 Number line Flipping point Formula.

we can generalize the prime numbers distribution formula.

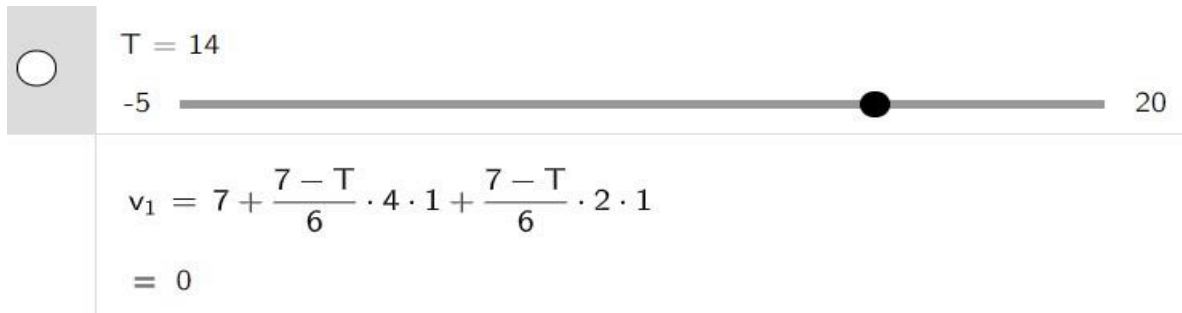
So using this genral formula we can represent any Natural number as  $\{7 + \text{some number}\}$

$$7 + \left(\frac{7-T}{6}\right) * 4 * 1 + \left(\frac{7-T}{6}\right) * 2 * 1 = L$$

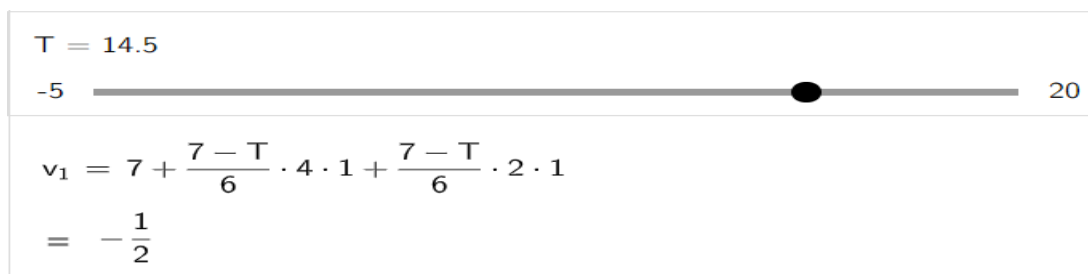
$$7 + \left(\frac{7-T}{6}\right) * 4 * 1 + \left(\frac{7-T}{6}\right) * 2 * 1 = \begin{cases} -ev \text{ number At } T > 14 \\ 0 \text{ At } T = 14 \\ +ev \text{ number at } T < 14 \end{cases}$$

Which is basically flipping the Line number (-ev and +ev) sides.

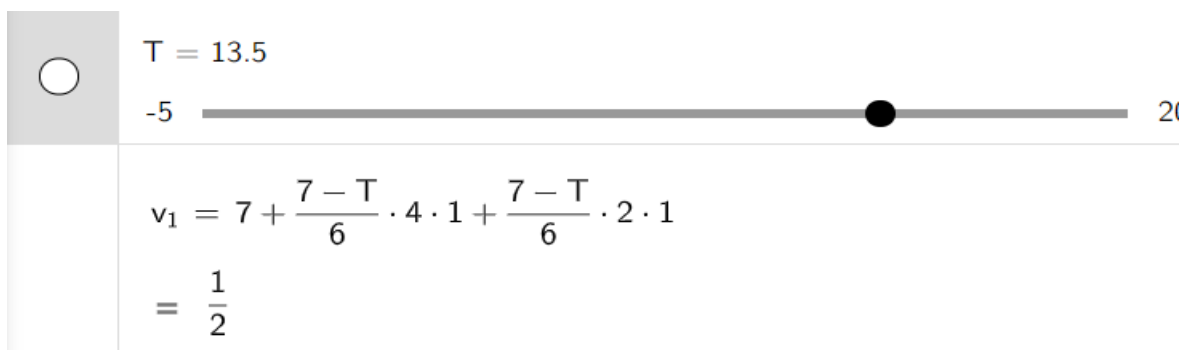
At  $T = 14$   $L = 0$







At  $T > 14$   $L$  is negative number



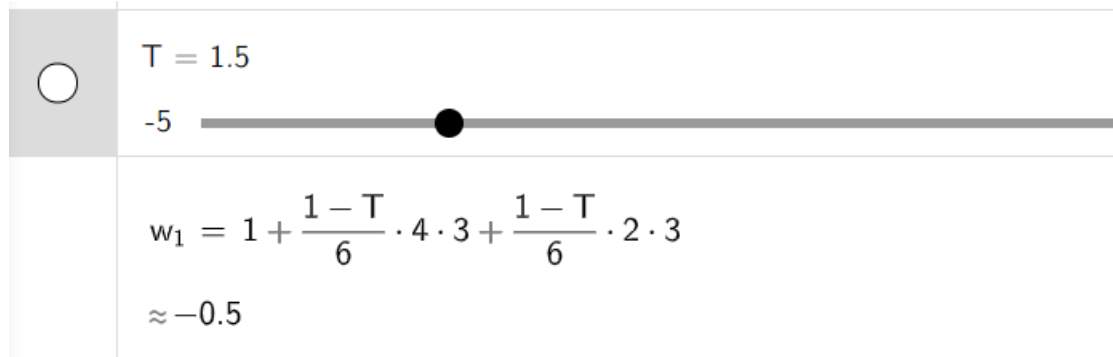
At  $T < 14$   $L$  is positive number



<input type="radio"/>	$T = 7.5$ 
	$v_1 = 7 + \frac{7-T}{6} \cdot 4 \cdot 12 + \frac{7-T}{6} \cdot 2 \cdot 24$ $= -1$
<input checked="" type="radio"/>	$T = 7$ 
	$v_1 = 7 + \frac{7-T}{6} \cdot 4 \cdot 12 + \frac{7-T}{6} \cdot 2 \cdot 24$ $= 7$
<input type="radio"/>	$T = 7$ 
	$v_1 = 7 + \frac{7-T}{6} \cdot 4 \cdot 24 + \frac{7-T}{6} \cdot 2 \cdot 24$ $= 7$
<input type="radio"/>	$T = 7.5$ 
	$v_1 = 7 + \frac{7-T}{6} \cdot 4 \cdot 12 + \frac{7-T}{6} \cdot 2 \cdot 12$ $= 1$

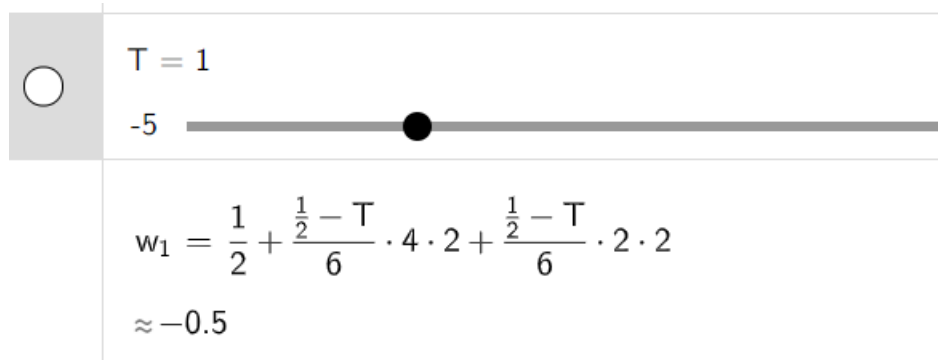
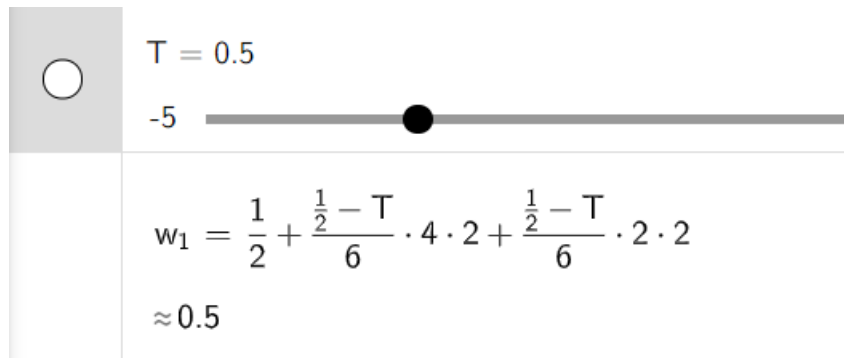
And to generalize this flipping formula more we can use any number including 1 instead of 7.

$$1 + \left(\frac{1-T}{6}\right) \cdot 4 \cdot 2 + \left(\frac{1-T}{6}\right) \cdot 2 \cdot 2 = \begin{cases} -ev \text{ number At } T > 1 \\ 1 \text{ At } T = 1 \\ +ev \text{ number at } T < 1 \end{cases}$$



So basically if we choose the flipping number to be A



$$A + \left( \frac{A-T}{6} \right) * 4 * 2 + \left( \frac{A-T}{6} \right) * 2 * 2 = \begin{cases} -ev \text{ number At } T > A \\ A \text{ At } T = A \\ +ev \text{ number at } T < A \end{cases}$$



And if the formula is

$$A + \left( \frac{A-T}{6} \right) * 4 * 1 + \left( \frac{A-T}{6} \right) * 2 * 1 = \begin{cases} -ev \text{ number At } T > A \\ 0 \text{ At } T = 2 * A \\ +ev \text{ number at } T < A \end{cases}$$





<input type="radio"/>	$T = 1$ 
	$w_1 = \frac{1}{2} + \frac{\frac{1}{2} - T}{6} \cdot 4 \cdot 1 + \frac{\frac{1}{2} - T}{6} \cdot 2 \cdot 1$ $= 0$
<input type="radio"/>	$T = 14$ 
	$v_1 = 7 + \frac{7 - T}{6} \cdot 4 \cdot 1 + \frac{7 - T}{6} \cdot 2 \cdot 1$ $= 0$

Based on this general formula any number will meet a flipping point once  $T = 2 \cdot A$ .

For any Natural number

And for  $A = 1/4$

<input type="radio"/>	$T = 0$ 
	$w_1 = \frac{1}{4} + \frac{\frac{1}{4} - T}{6} \cdot 4 \cdot 1 + \frac{\frac{1}{4} - T}{6} \cdot 2 \cdot 1$ $\approx 0.5$
<input type="radio"/>	$T = 0.5$ 
	$w_1 = \frac{1}{4} + \frac{\frac{1}{4} - T}{6} \cdot 4 \cdot 1 + \frac{\frac{1}{4} - T}{6} \cdot 2 \cdot 1$ $= 0$

To generalize this formula more

$$A + \left( \frac{A - T}{6} \right) * 4 * \frac{1}{B} + \left( \frac{A - T}{6} \right) * 2 * \frac{1}{B} = \begin{cases} -ev \text{ number At } T > A \\ A \text{ At } T = A \\ +ev \text{ number at } T < A \end{cases}$$



$$T = 1$$

-10



$$w_1 = \frac{1}{4} + \frac{\frac{1}{4} - T}{6} \cdot 4 \cdot \frac{1}{2} + \frac{\frac{1}{4} - T}{6} \cdot 2 \cdot \frac{1}{2}$$

$$\approx -0.125$$

$$v_1 = \frac{1}{4} + \frac{\frac{1}{4} - T}{6} \cdot 4 \cdot \frac{1}{3} + \frac{\frac{1}{4} - T}{6} \cdot 2 \cdot \frac{1}{3}$$

$$= 0$$



$$a_2 = \frac{1}{4} + \frac{\frac{1}{4} - T}{6} \cdot 4 \cdot \frac{1}{4} + \frac{\frac{1}{4} - T}{6} \cdot 2 \cdot \frac{1}{4}$$

$$= \frac{1}{16}$$

$$c_2 = \frac{1}{4} + \frac{\frac{1}{4} - T}{6} \cdot 4 \cdot \frac{1}{5} + \frac{\frac{1}{4} - T}{6} \cdot 2 \cdot \frac{1}{5}$$

$$= \frac{1}{10}$$

$$b_2 = \frac{1}{4} + \frac{\frac{1}{4} - T}{6} \cdot 4 \cdot \frac{1}{6} + \frac{\frac{1}{4} - T}{6} \cdot 2 \cdot \frac{1}{6}$$

$$= \frac{1}{8}$$

$$d_2 = \frac{1}{4} + \frac{\frac{1}{4} - T}{6} \cdot 4 \cdot \frac{1}{7} + \frac{\frac{1}{4} - T}{6} \cdot 2 \cdot \frac{1}{7}$$

$$= \frac{1}{7}$$

For A = 1/4

$T = 0.5$	$g_2 = \frac{1}{4} + \frac{\frac{1}{4} - T}{6} \cdot 4 \cdot \frac{1}{1} + \frac{\frac{1}{4} - T}{6} \cdot 2 \cdot \frac{1}{1}$ $= 0$	<b>B = 1</b>
$T = -\frac{1}{4}$ $\approx -0.25$	$j_2 = \frac{1}{4} + \frac{\frac{1}{4} - T}{6} \cdot 4 \cdot \frac{-1}{2} + \frac{\frac{1}{4} - T}{6} \cdot 2 \cdot \frac{-1}{2}$ $= 0$	<b>B = -0.5</b>
$T = -\frac{1}{2}$ $\approx -0.5$	$k_2 = \frac{1}{4} + \frac{\frac{1}{4} - T}{6} \cdot 4 \cdot \frac{-1}{3} + \frac{\frac{1}{4} - T}{6} \cdot 2 \cdot \frac{-1}{3}$ $= 0$	<b>B = -1/3</b>
$T = 1$	$v_1 = \frac{1}{4} + \frac{\frac{1}{4} - T}{6} \cdot 4 \cdot \frac{1}{3} + \frac{\frac{1}{4} - T}{6} \cdot 2 \cdot \frac{1}{3}$ $= 0$	<b>B = 1/3</b>
$T = 1.5$	$c_2 = \frac{1}{4} + \frac{\frac{1}{4} - T}{6} \cdot 4 \cdot \frac{1}{5} + \frac{\frac{1}{4} - T}{6} \cdot 2 \cdot \frac{1}{5}$ $= 0$	<b>B = 1/5</b>
$T = 2$	$d_2 = \frac{1}{4} + \frac{\frac{1}{4} - T}{6} \cdot 4 \cdot \frac{1}{7} + \frac{\frac{1}{4} - T}{6} \cdot 2 \cdot \frac{1}{7}$ $= 0$	<b>B = 1/7</b>
$T = 2.5$	$f_2 = \frac{1}{4} + \frac{\frac{1}{4} - T}{6} \cdot 4 \cdot \frac{1}{9} + \frac{\frac{1}{4} - T}{6} \cdot 2 \cdot \frac{1}{9}$ $= 0$	<b>B = 1/9</b>
$T = 3$	$e_2 = \frac{1}{4} + \frac{\frac{1}{4} - T}{6} \cdot 4 \cdot \frac{1}{11} + \frac{\frac{1}{4} - T}{6} \cdot 2 \cdot \frac{1}{11}$ $= 0$	<b>B = 1/11</b>

For A = 1/2

$T = -0.5$	$j_2 = \frac{1}{2} + \frac{\frac{1}{2} - T}{6} \cdot 4 \cdot \frac{-1}{2} + \frac{\frac{1}{2} - T}{6} \cdot 2 \cdot \frac{-1}{2}$ $= 0$	<b>B = -2   1/B = -1/2</b>
$T = 1$	$g_2 = \frac{1}{2} + \frac{\frac{1}{2} - T}{6} \cdot 4 \cdot \frac{1}{1} + \frac{\frac{1}{2} - T}{6} \cdot 2 \cdot \frac{1}{1}$ $= 0$	<b>B = 1   1/B = 1</b>
$T = 1.5$	$w_1 = \frac{1}{2} + \frac{\frac{1}{2} - T}{6} \cdot 4 \cdot \frac{1}{2} + \frac{\frac{1}{2} - T}{6} \cdot 2 \cdot \frac{1}{2}$ $= 0$	<b>B = 2   1/B = 1/2</b>
$T = 2$	$v_1 = \frac{1}{2} + \frac{\frac{1}{2} - T}{6} \cdot 4 \cdot \frac{1}{3} + \frac{\frac{1}{2} - T}{6} \cdot 2 \cdot \frac{1}{3}$ $= 0$	<b>B = 3   1/B = 1/3</b>
$T = 2.5$	$a_2 = \frac{1}{2} + \frac{\frac{1}{2} - T}{6} \cdot 4 \cdot \frac{1}{4} + \frac{\frac{1}{2} - T}{6} \cdot 2 \cdot \frac{1}{4}$ $= 0$	<b>B = 4   1/B = 1/4</b>
$T = 3$	$c_2 = \frac{1}{2} + \frac{\frac{1}{2} - T}{6} \cdot 4 \cdot \frac{1}{5} + \frac{\frac{1}{2} - T}{6} \cdot 2 \cdot \frac{1}{5}$ $= 0$	<b>B = 5   1/B = 1/5</b>
$T = 3.5$	$b_2 = \frac{1}{2} + \frac{\frac{1}{2} - T}{6} \cdot 4 \cdot \frac{1}{6} + \frac{\frac{1}{2} - T}{6} \cdot 2 \cdot \frac{1}{6}$ $= 0$	<b>B = 6   1/B = 1/6</b>
$T = 4$	$d_2 = \frac{1}{2} + \frac{\frac{1}{2} - T}{6} \cdot 4 \cdot \frac{1}{7} + \frac{\frac{1}{2} - T}{6} \cdot 2 \cdot \frac{1}{7}$ $= 0$	<b>B = 7   1/B = 1/7</b>

## 2.2 Collatz Conjecture.

The generalization for the prime number distributions or more accurately the Flipping point Formula.

$$A + \left( \frac{A-T}{6} \right) * 4 * \frac{1}{B} + \left( \frac{A-T}{6} \right) * 2 * \frac{1}{B} = \begin{cases} -ev \text{ number At } T > \frac{B+1}{2} \text{ and } A = \frac{1}{2} \\ 0 \text{ At } T = \frac{B+1}{2} \text{ and } A = \frac{1}{2} \\ +ev \text{ number at } T < \frac{B+1}{2} \text{ and } A = \frac{1}{2} \end{cases}$$

*This means we will have a flipping point when  $A = \frac{1}{2}$  ;*

*and  $T = \frac{B+1}{2}$  for any natrual value of B*

And if B = 1; this general formula will be.

$$A + \left( \frac{A-T}{6} \right) * 4 * 1 + \left( \frac{A-T}{6} \right) * 2 * 1 = \begin{cases} -ev \text{ number At } T > A \\ 0 \text{ At } T = 2 * A \\ +ev \text{ number at } T < A \end{cases}$$

Another point sum of each two consequence [B] numbers

$$\begin{aligned} & \left( \frac{1}{2} + \left( \frac{\frac{1}{2}-T}{6} \right) * 4 * 1 + \left( \frac{\frac{1}{2}-T}{6} \right) * 2 * 1 \right) + \left( 1 + \left( \frac{1-T}{6} \right) * 4 * (B-1) + \left( \frac{1-T}{6} \right) * 2 * (B-1) \right) \\ & = \left( 1 + \left( \frac{1-T}{6} \right) * 4 * B + \left( \frac{1-T}{6} \right) * 2 * B \right) \end{aligned}$$

This means for each number [B] can be written in this formula.  $\left( 1 + \left( \frac{1-T}{6} \right) * 4 * B + \left( \frac{1-T}{6} \right) * 2 * B \right)$

And can be represented as sum of two number the number before it (B -1) + the formula when A = ½ and B = 1. For any value T. as shown in previous equation.

$u_2 = \frac{1}{2} + \frac{\frac{1}{2} - F}{6} \cdot 4 \cdot 1 + \frac{\frac{1}{2} - F}{6} \cdot 2 \cdot 1$ $= -2$	$F = 3$ $B = 1 ; A = 1/2$
$t_2 = 1 + \frac{1 - F}{6} \cdot 4 \cdot 6 + \frac{1 - F}{6} \cdot 2 \cdot 6$ $= -11$	$B - 1 = 7 - 1 = 6$
$s_2 = 1 + \frac{1 - F}{6} \cdot 4 \cdot 7 + \frac{1 - F}{6} \cdot 2 \cdot 7$ $= -13$	$B = 7$

$$S_2 = t_2 + u_2 = -11 - 2 = -13$$

*Or in other words we can say that if  $A = 1$  the difference between each two consequence numbers  $[B]$  in the same formula = the value of the formula at  $A = \frac{1}{2}$  and  $B = 1$ .*

*And this is because*

$$T - 1 = \left( \frac{1}{2} + \left( \frac{\frac{1}{2} - T}{6} \right) * 4 * 1 + \left( \frac{\frac{1}{2} - T}{6} \right) * 2 * 1 \right) ; \text{for any natural value of } T$$

And

$$2 - T = \left( 1 + \left( \frac{1 - T}{6} \right) * 4 * 1 + \left( \frac{1 - T}{6} \right) * 2 * 1 \right) ; \text{for any natural value of } T$$

And as these are two consequence numbers then.

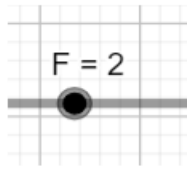
$$2 - T - 1 = T - 1$$

$$1 - T = T - 1$$

As the flipping point is at  $T = 2 * A = 1$ . And this is the point reach Zero.

So, we have two flipping points for each number  $T$ .

- 1) When  $A = \frac{1}{2}$  then  $T = 2 * A = 1$  then  $T - 1 = 0$  reach Zero at  $T = 1$ .
- 2) When  $A = 1$  then  $T = 2 * A = 2$  then  $2 - T = 0$  reach Zero at  $T = 2$ .



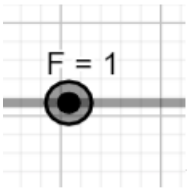
$$b_3 = 1 + \frac{1-F}{6} \cdot 4 \cdot 1 + \frac{1-F}{6} \cdot 2 \cdot 1$$

$$= 0$$

$$c_3 = 2 - F$$

$$= 0$$

First  
Flipping  
Point



$$e_3 = \frac{1}{2} + \frac{\frac{1}{2}-F}{6} \cdot 4 \cdot 1 + \frac{\frac{1}{2}-F}{6} \cdot 2 \cdot 1$$

$$= 0$$

$$d_3 = F - 1$$

$$= 0$$

Second  
Flipping  
Point

For any Real number  $T \neq 0$  this Formula = Zero.

$$0 = \frac{1}{2} + \frac{\frac{1}{2}-T}{6} \cdot 4 \cdot \frac{1}{T} + \frac{\frac{1}{2}-T}{6} \cdot 2 \cdot \frac{1}{T} + \left( \frac{\frac{T}{2}-\frac{1}{2}}{T} \right)$$

$$\frac{1}{2} + \frac{\frac{1}{2}-T}{6} \cdot 4 \cdot \frac{1}{T} + \frac{\frac{1}{2}-T}{6} \cdot 2 \cdot \frac{1}{T} = - \left( \frac{\frac{T}{2}-\frac{1}{2}}{T} \right)$$

$$\frac{T}{2} + \frac{\frac{1}{2}-T}{6} \cdot 4 + \frac{\frac{1}{2}-T}{6} \cdot 2 = - \left( \frac{T}{2} - \frac{1}{2} \right)$$

$$T + \frac{\frac{1}{2}-T}{6} \cdot 4 + \frac{\frac{1}{2}-T}{6} \cdot 2 = \frac{1}{2}$$

For any Natural number  $T$  we can make it equal to  $\frac{1}{2}$  using this formula

And this also can be written as for any real value  $T$  including  $T=0$ .

$$T + \frac{1}{2} + \frac{\frac{1}{2}-T}{6} \cdot 4 + \frac{\frac{1}{2}-T}{6} \cdot 2 = 1$$

Which conclude Collatz conjecture each number will reach 1.

$$T + \frac{1}{2} + \frac{\frac{1}{2} - T}{6} * 4 + \frac{\frac{1}{2} - T}{6} * 2 = 1 ; \text{for any real value } T$$

And not only for  $\frac{1}{2}$  but also for any value A any Number T can be converted to  $2 * A$  using this formula.

$$T + \frac{A - T}{6} * 4 + \frac{A - T}{6} * 2 + A = 2 * A ; \text{for any real value } T$$

If any sequence of operations applied on any number N will make sure this number will be natural number as if it even will be divided by 2 and if odd, we will add one and then divide by 2 again.

So, any number in Collatz sequence will be natural number and using our formula it can reach 1. As it is clear the formula doing the same as Collatz function also include factors of 2 and adding  $\frac{1}{2}$  as in the odd case  $[(3n + 1)/2]$

And if this formula can be considered as a sequence of adding 4 and adding 2 to a Number T; we can say that no matter the value of several collatz sequence eventually will reach to this formula and then will reach [1] eventually for any [T].

As long the Collatz function collectively between its operation steps reverse the operation that is done in previous steps.

We do not care how many times Collatz function will be applied if there is a formula that brings back any number to [1] and this what Collatz conjecture states. And this is what we showed here there is a formula that includes Collatz function and brings any Number [T] to [1].

$$T + \frac{1}{2} + \frac{\frac{1}{2} - T}{6} * 4 + \frac{\frac{1}{2} - T}{6} * 2 = 1 ; \text{for any real value } T$$

And to elaborate more on Collatz function and this formula any number T can reach [Zero] using this formula.

$$0 = \frac{1}{2} + \frac{\frac{1}{2} - T}{6} * 4 * \frac{1}{T} + \frac{\frac{1}{2} - T}{6} * 2 * \frac{1}{T} + \left( \frac{\frac{T}{2} - \frac{1}{2}}{T} \right) \text{for any } T \neq 0$$

For example, if T = 274133054632352106267

This formula will equal [0].



## Conclusion

First, we showed the prime numbers and its composite distribution formula. Then we showed how this formula can be generalized and showed the concept of the number line flipping points formula for any natural number. Then we showed how this formula includes Collatz function main Cycle (1,2,4) that evaluates to value = 1 for any Natural.

Finally, we similarly showed formulas that have Collatz function main Cycle [1,2,4] and evaluates to value [0] or value [1/2] for any real number. Which gives a logical proof and formula from Riemann hypothesis as well.

## References

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