New Riemann’s Functional Equation for Odd Numbers

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New Riemann’s Functional Equation for Odd Numbers

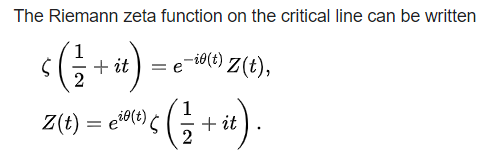
**Abstract**

This paper introduces a new functional form for Zeta function to proof Zeta function will converge to Zero at S = S+ 0.5 for any odd number using this new derived formula from Riemann’s functional equation. By breaking down gamma function into Euler formula.

**Keywords:** zeta function, Riemann hypothesis, complex plane, none-trivial zeros, critical strip

**1. Introduction**

Riemann's functional equation



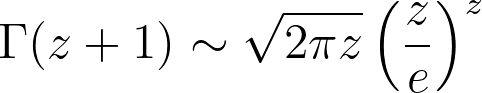
We can generalize this formula in a conceptual form.

Where this constant is the evaluation result for the rest of the terms in the Zeta functional formula regardless of its value.

Therefore, we only need to study these two terms, [ ], and their effect on the result of any complex number.

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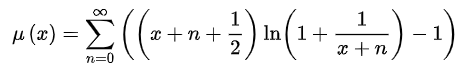
And based on Stirling’s formula we can replace gamma function with Euler formula as Stirling’s formula states that there is relation between gamma function and factorials in general.





where?

�(�)=∑�=0∞((�+�+12)ln⁡(1+1�+�)−1).



So, we can replace gamma function in the zeta functional form by Euler’s formula multiply some constant.



At S = S +1/2

And because

Therefore. For any odd natural number S at S = S +1/2 zeta function = 0

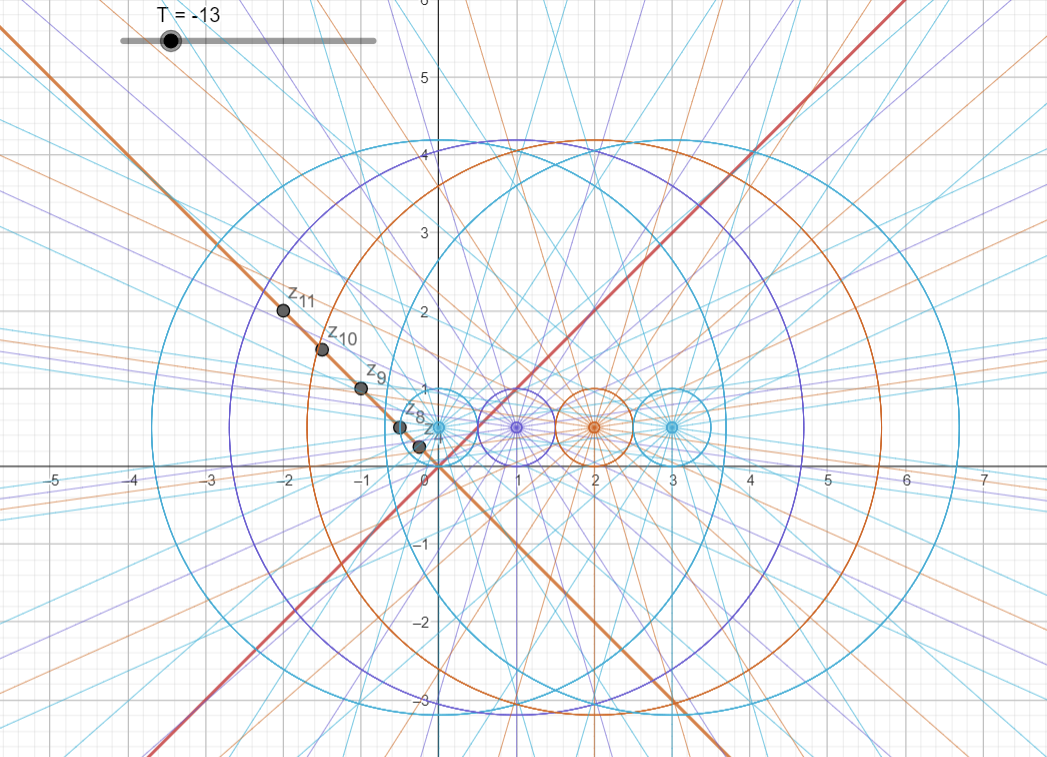
Therefore, also we can write Zeta function at S = S +1/2 as

As Term

And because

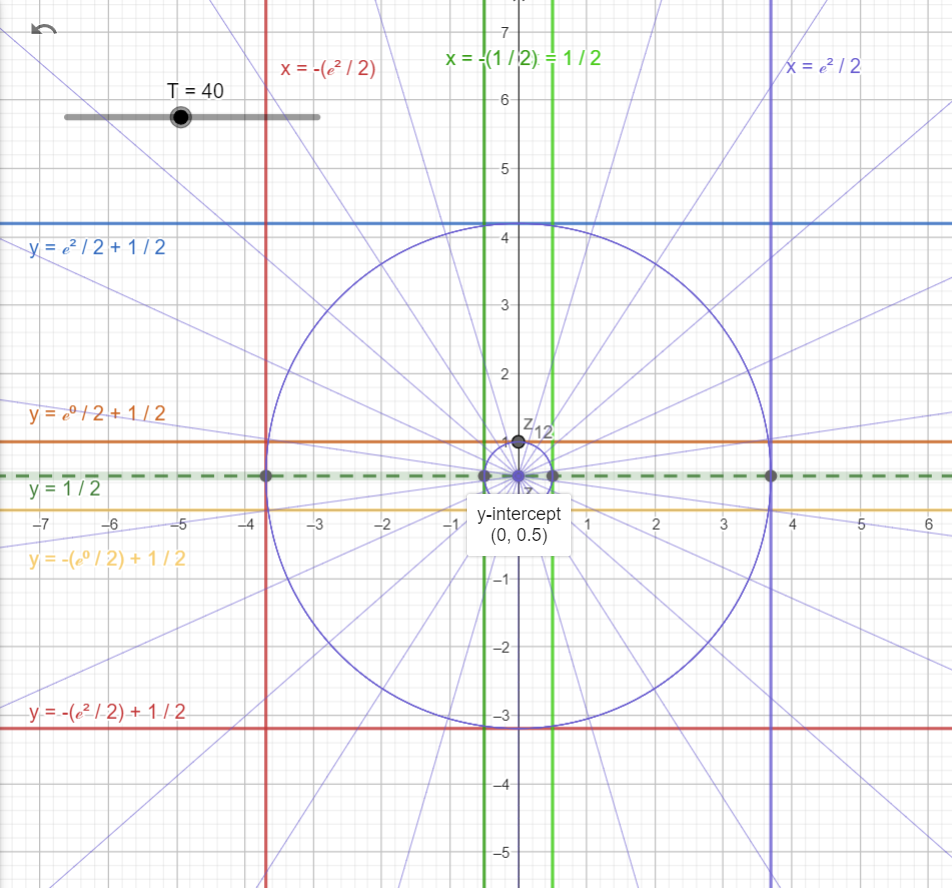
Based on the next analysis we will show that these two terms only; restrict the result of the Zeta function in a specific matter

1 - Multiplying [ by some constant will result in complex numbers on a line y =x with slope =1 or -1. Regardless of how the rest of the terms in the zeta function will evaluate to.

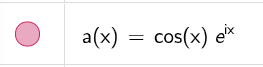


2- Multiplying [ is shifting our complex plane origin to the point (0,0.5) instead of (0.0) and the complex plane unit circle will be with radius =0.5.



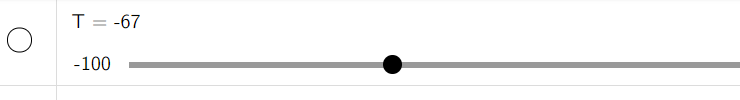


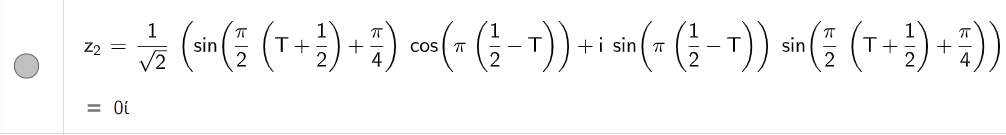
3- Multiplying [ is shifting our complex plane origin to the point (0.5,0) instead of (0.0) and the complex plane unit circle will be with radius =0.5.



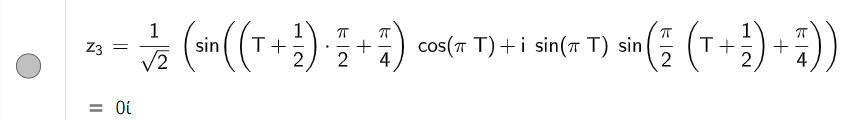


4- will give us more accurate exact value for 0.5 for any neutral number x



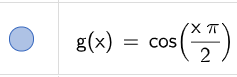


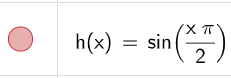




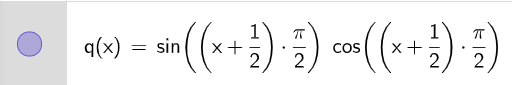
5- when using x = x+1/2 with and

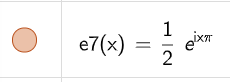
6-

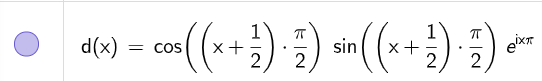
7-  Zero out all odd natural numbers

8-Zero out all even natural numbers

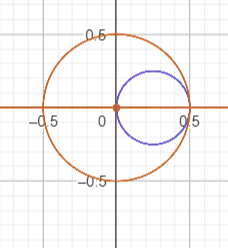
9-Zero out all Natural numbers and have only value = ½ at x = x+1/2

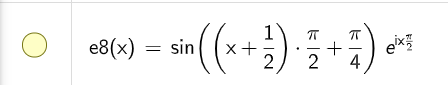
10-  ½ = at any natural number even x and = -1/2 at each odd natural number

11-  multiplying by ½ scale complex number unit circle to half its size therefore this function Zeros will be at ±0.5 and the complex plane imaginary unit will be = i/2

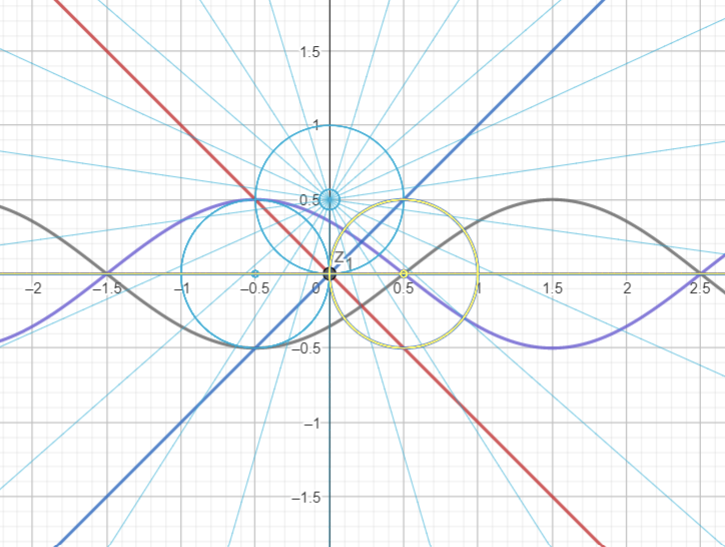
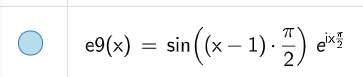
12-  multiplying by

Is Like limiting our range from 0 to +∞ instead of original range from -∞ to +∞



13 - these are the terms in Zeta function

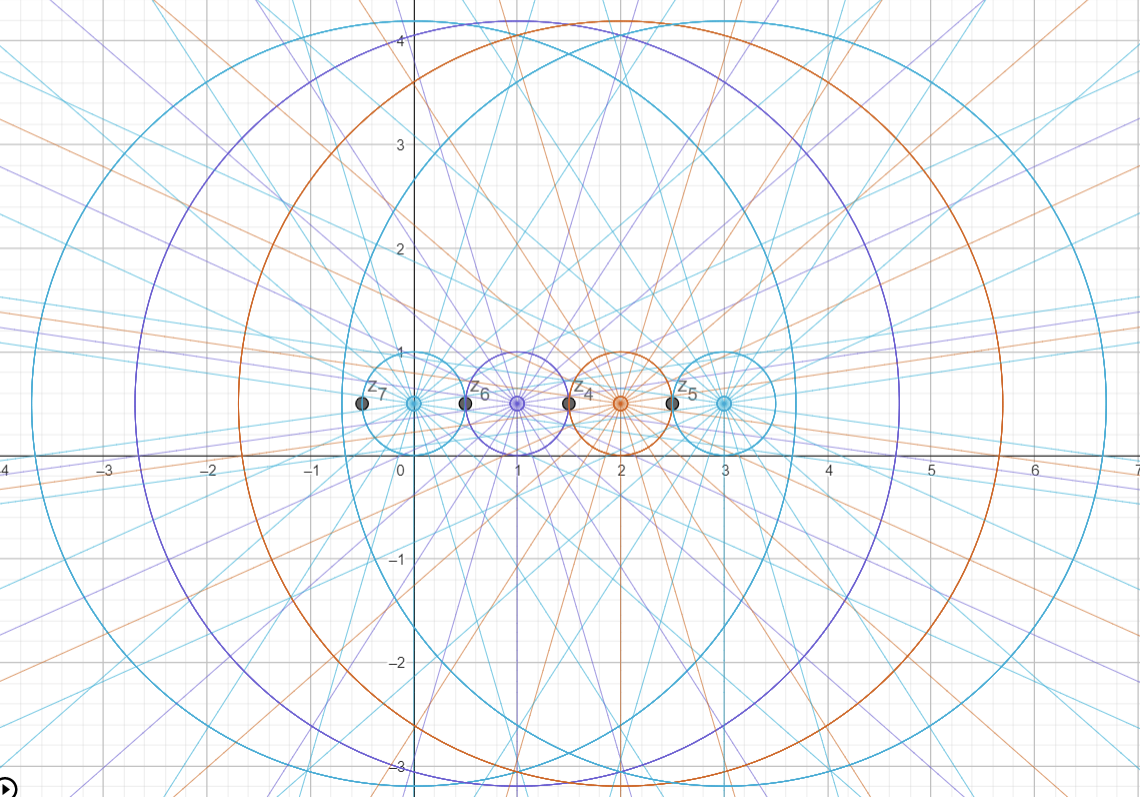
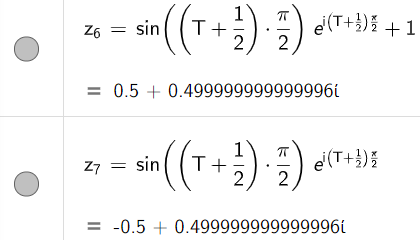
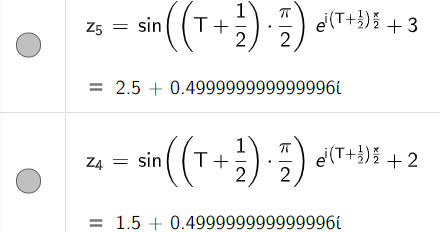
= 0 for any X odd natural number and = 1 for any X even number



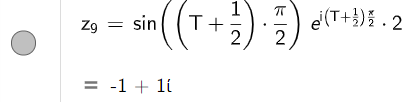
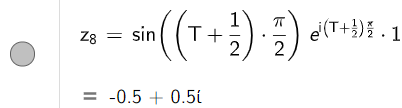
Therefore if

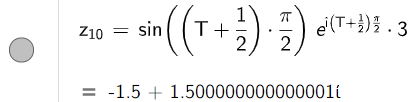
And if

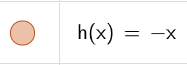
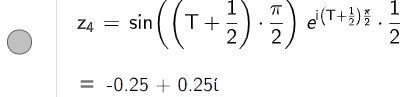
Adding any number to f(x) will not going to change the final value of the complex number it will remain carrying this 0.5 along any coming number in the Zeta functional formula represented by Z(S±1).

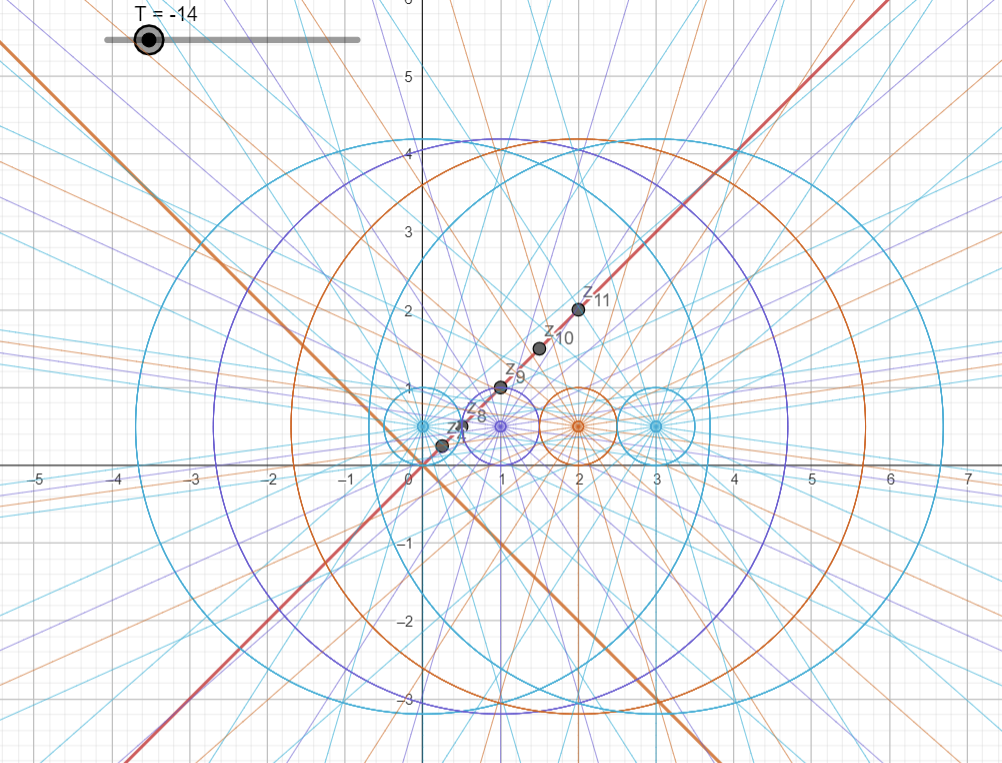


Therefor multiply [ by some constant which will be the value of the rets of terms in Zeta function; result complex numbers on a line y =x with slope =1 or -1. Regardless of the value of the rets of the terms in the zeta function will evaluates to.



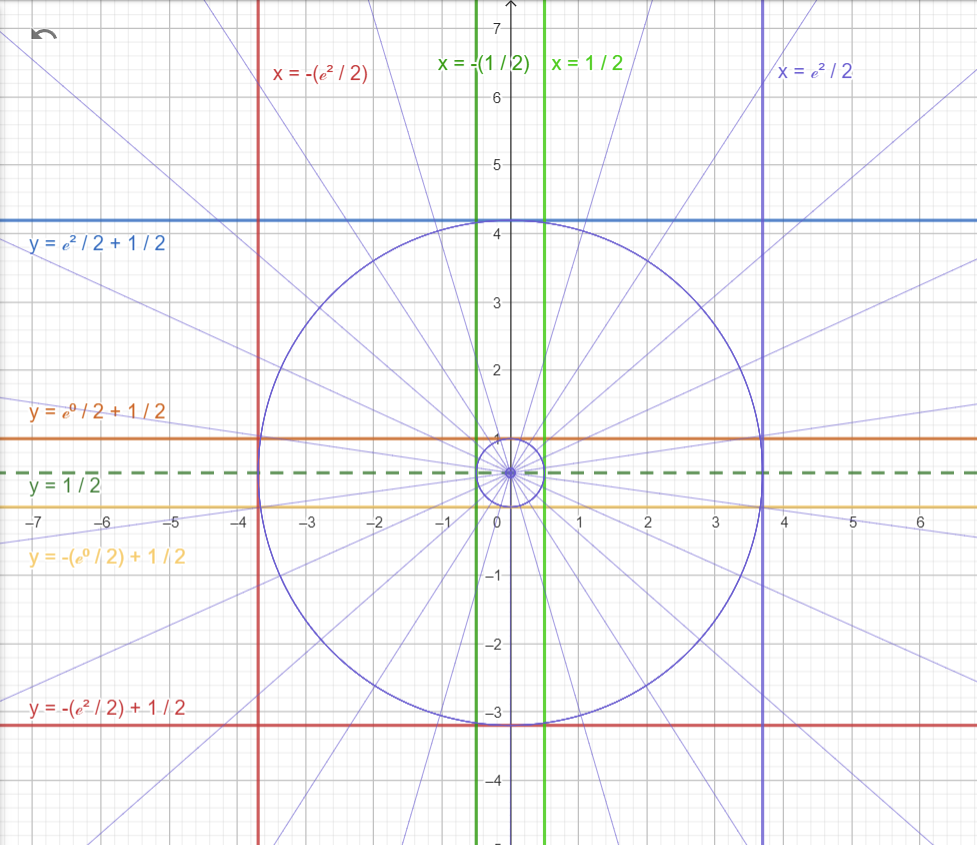




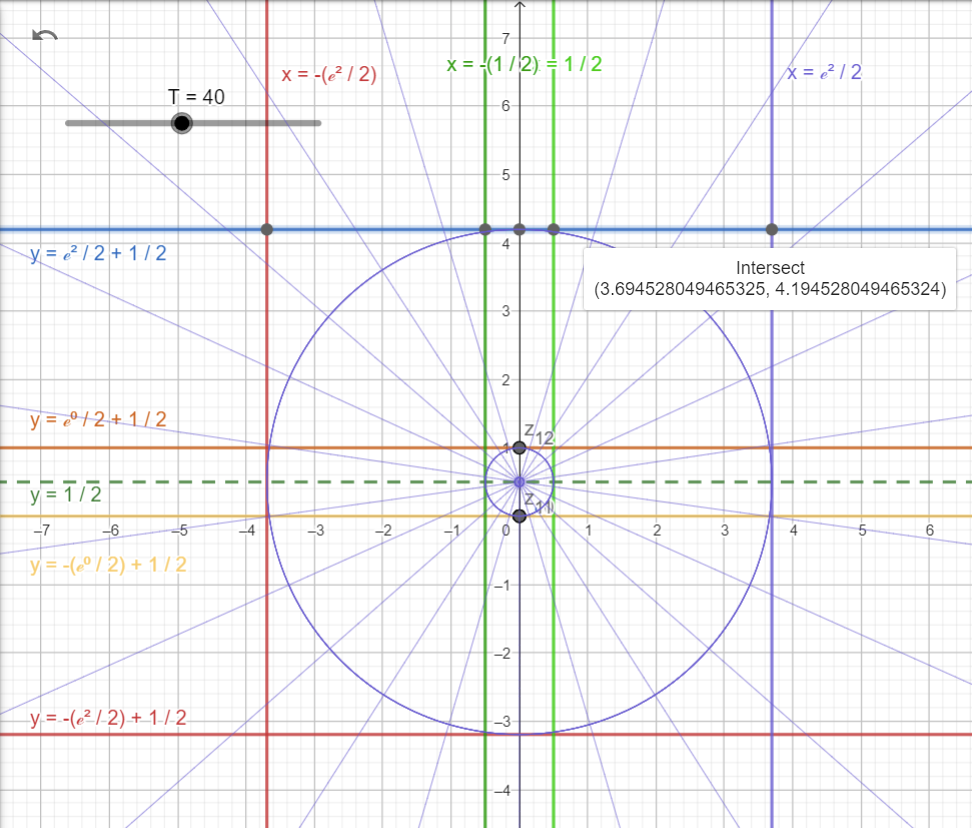


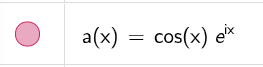
When T is even number all complex numbers will be distributed on the linear relation y = x. and when T odd all complex numbers will be distributed on the linear relation y = -x.

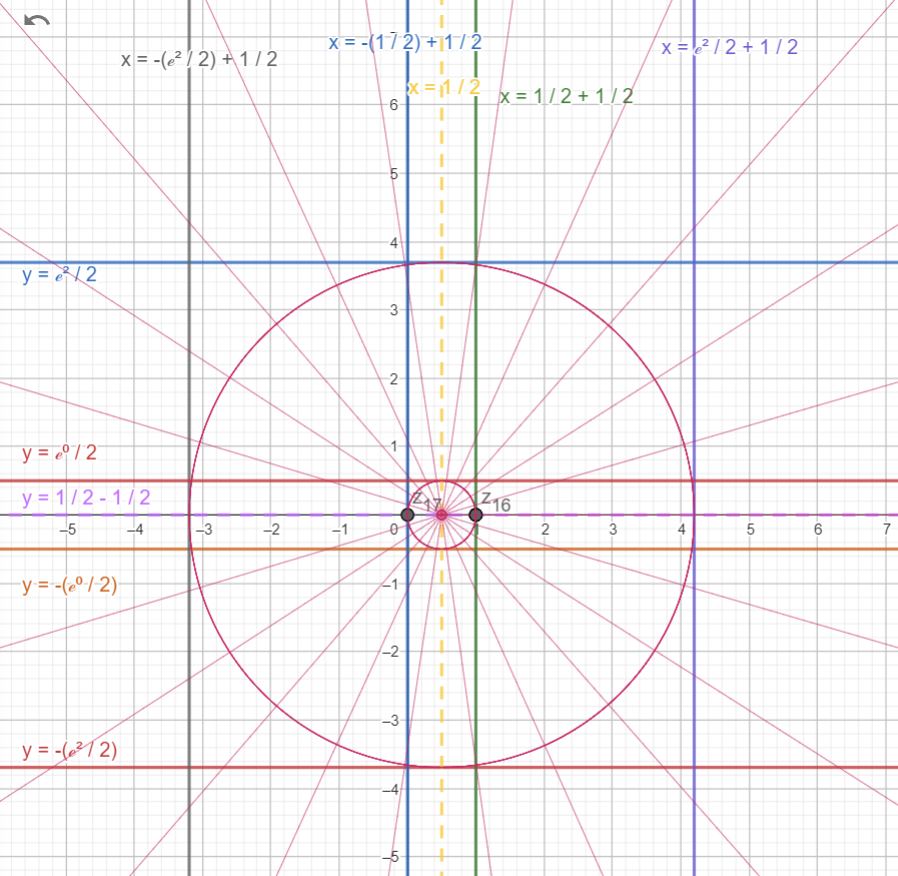


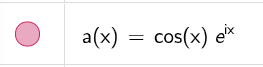


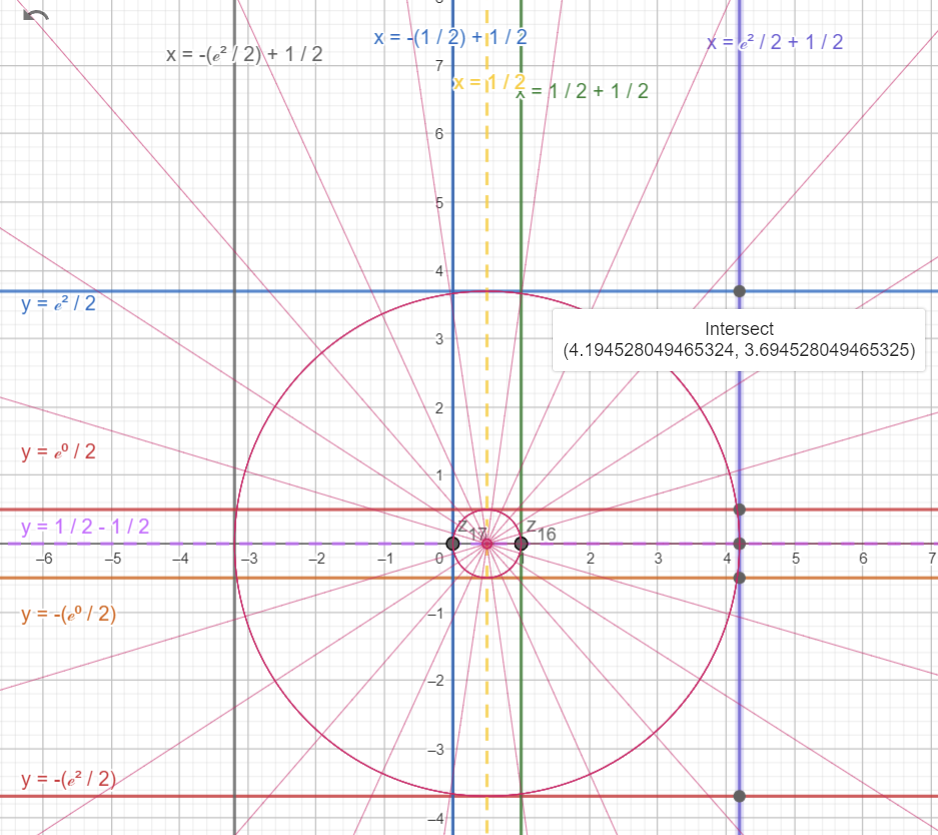


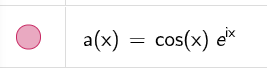
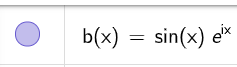


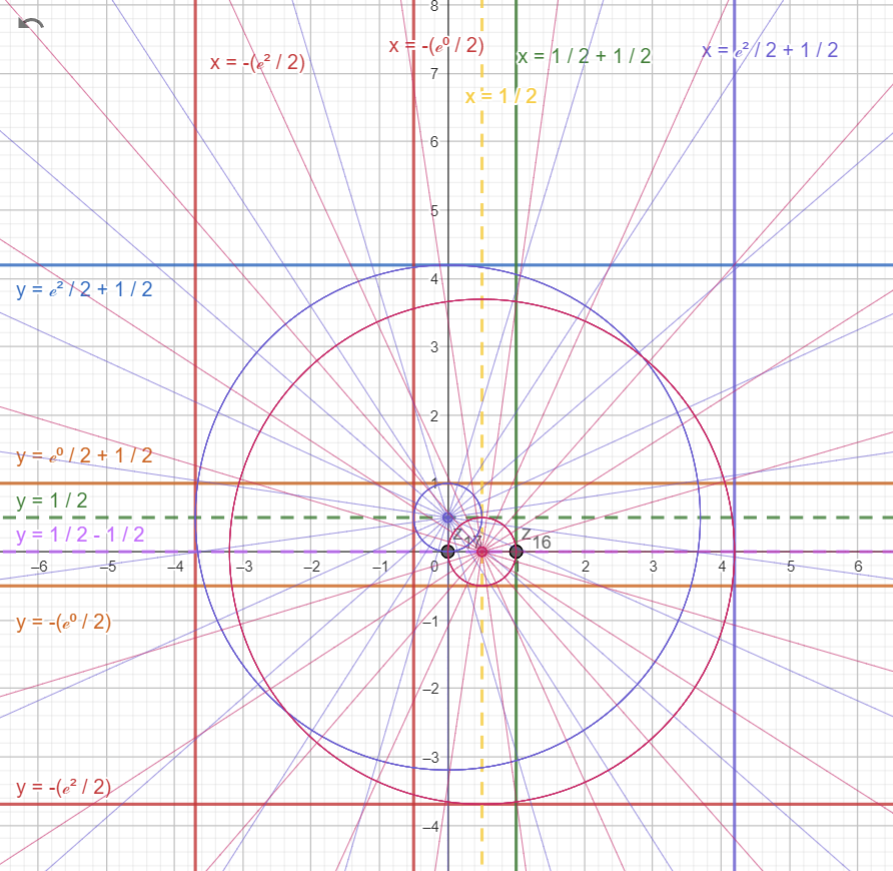


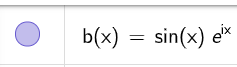
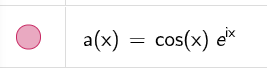


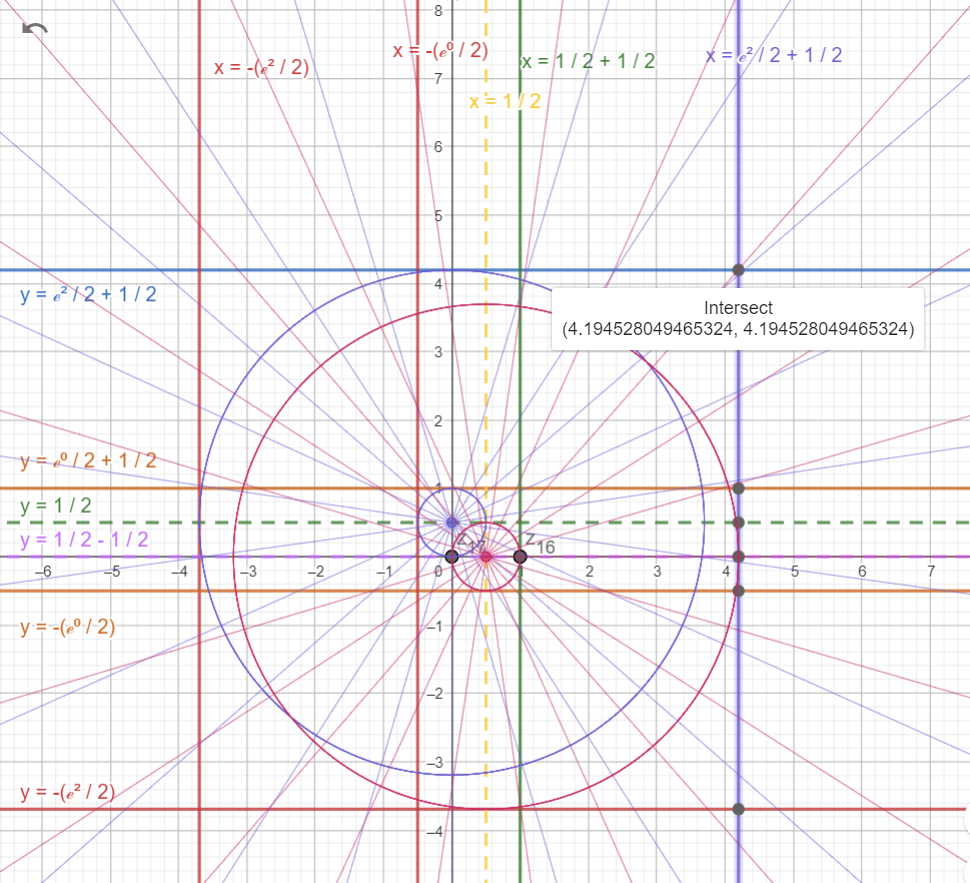




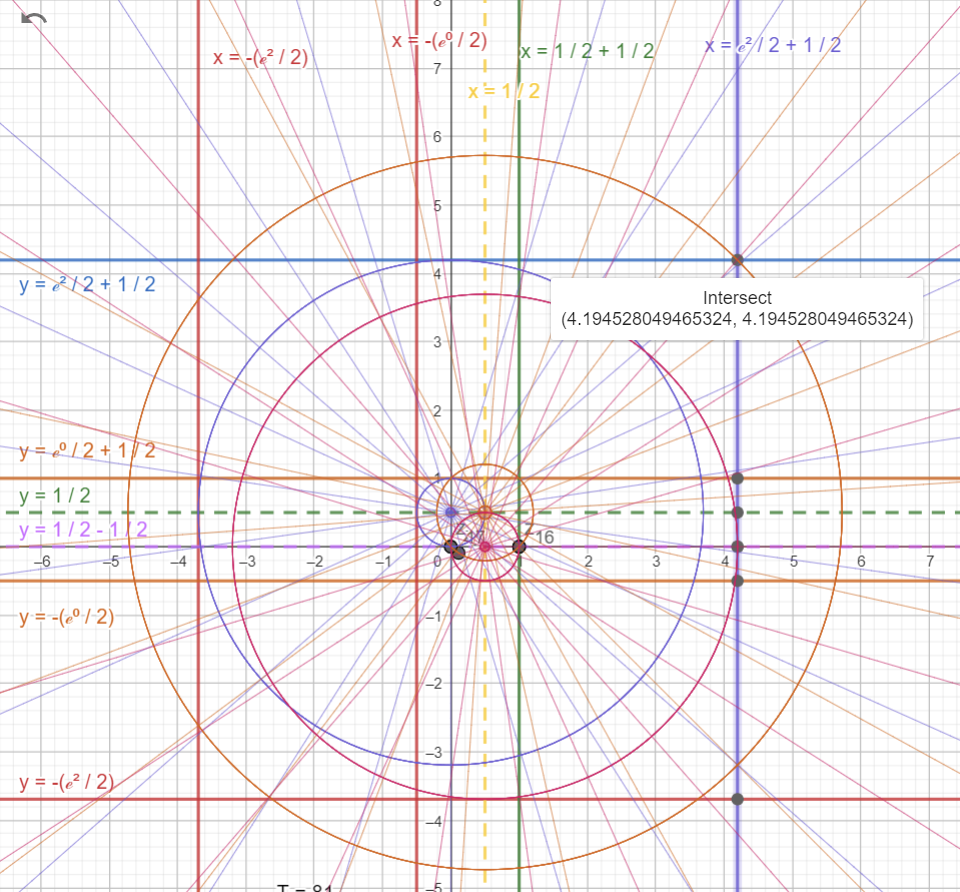


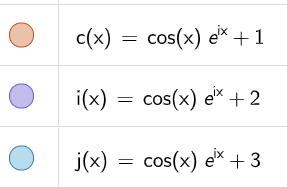


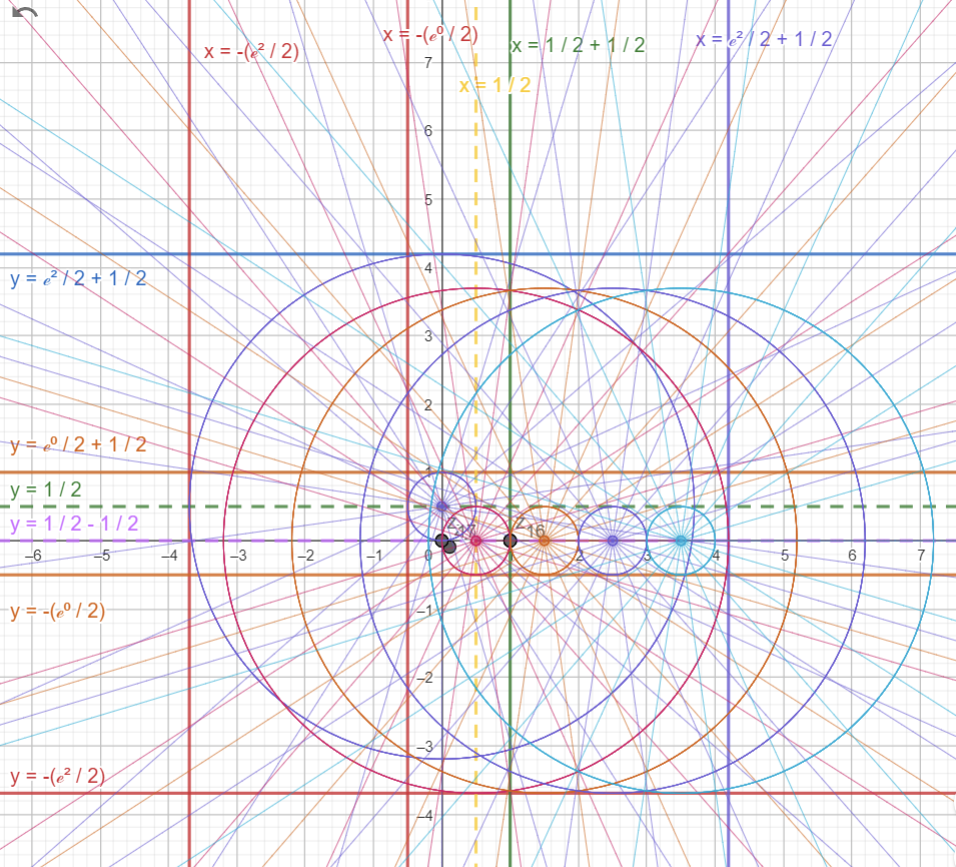


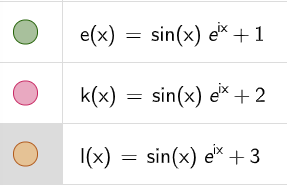


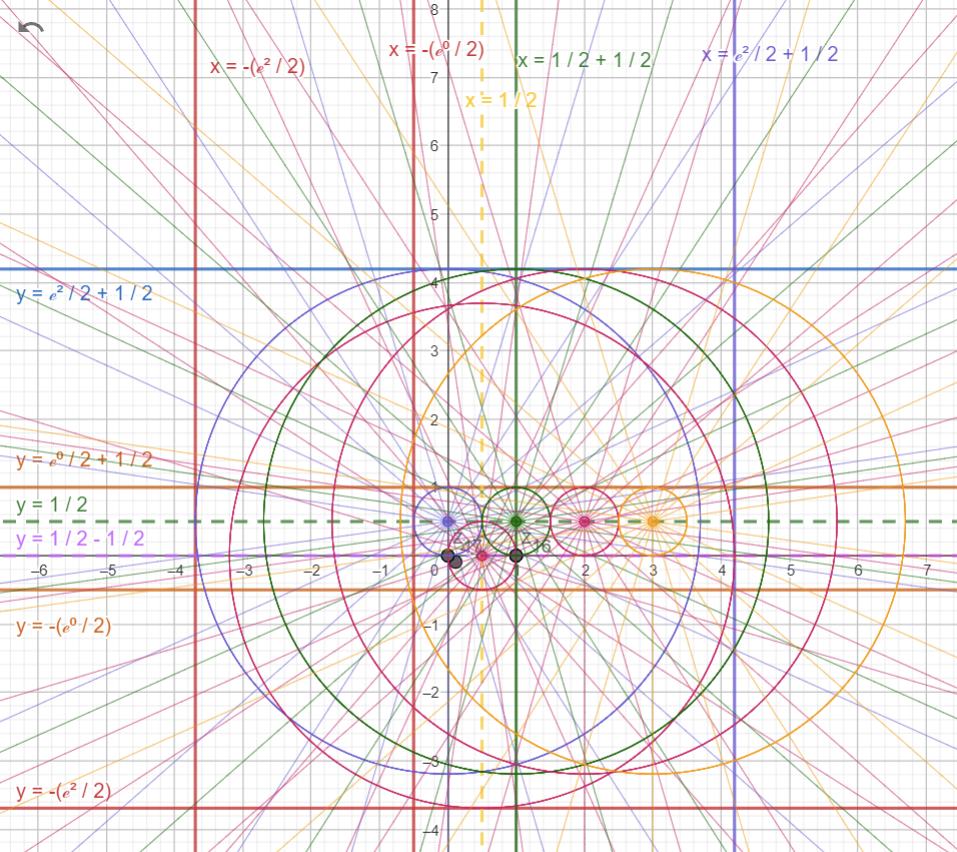












**Conclusion**

This paper we studied zeta functional in theoretical and abstract way then we derived new functional form by breaking down the gamma function in Riemann’s functional equation into Euler formula.

In this new functional Equation Zeta function converges to 0 at S = S +0.5. for any odd natural number.

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