

# Unfolding Technique for Manifold in complex plane

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# Unfolding Technique for a Manifold in complex plane

## Abstract

In This paper we introduce new unfolding technique for manifolds in complex plane Using basic features from complex plane. During this Technique exploration we will introduce a general visual explanation for Zeta function Zeros. Finally, we will see a visualization for the sign oscillations issue at [6] and a visualization for natural numbers re-synchronization on steady bases almost equal to [12.5].

**Keywords:** zeta function, Riemann hypothesis, complex plane, none-trivial zeros, critical strip

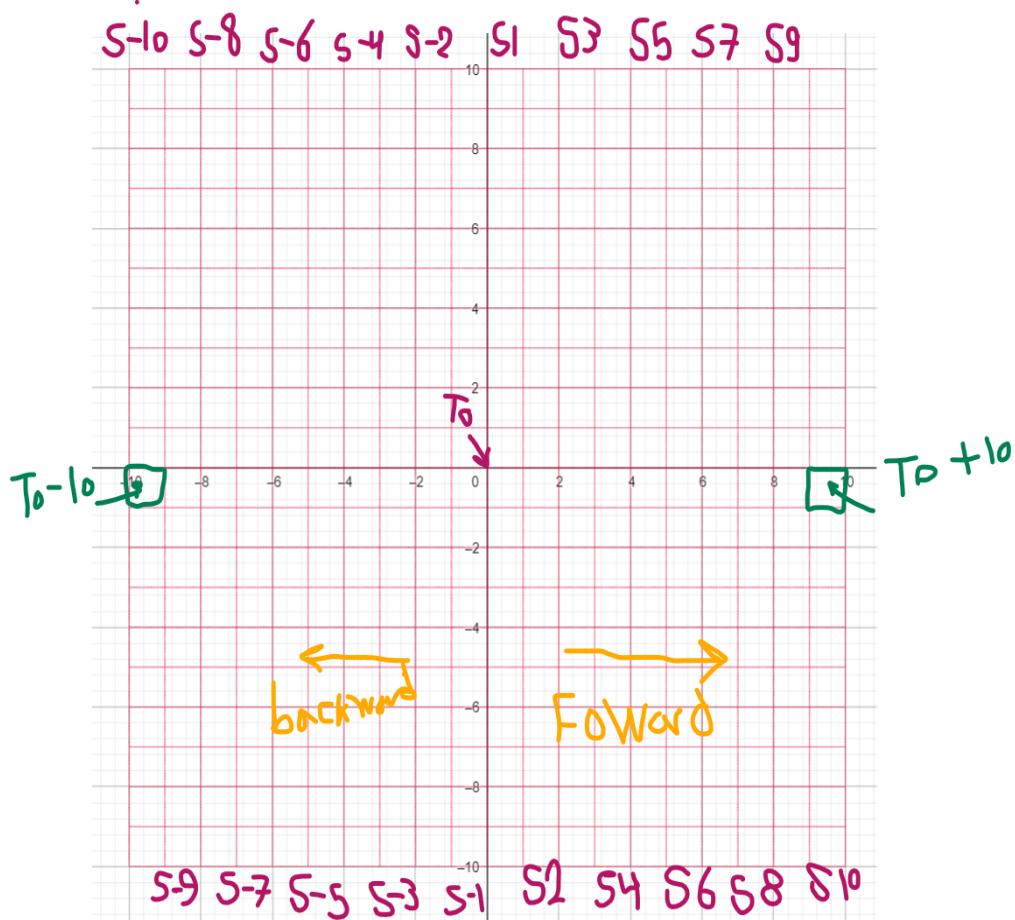
## 1. Introduction

$$\text{Frame of reference} = i * x$$

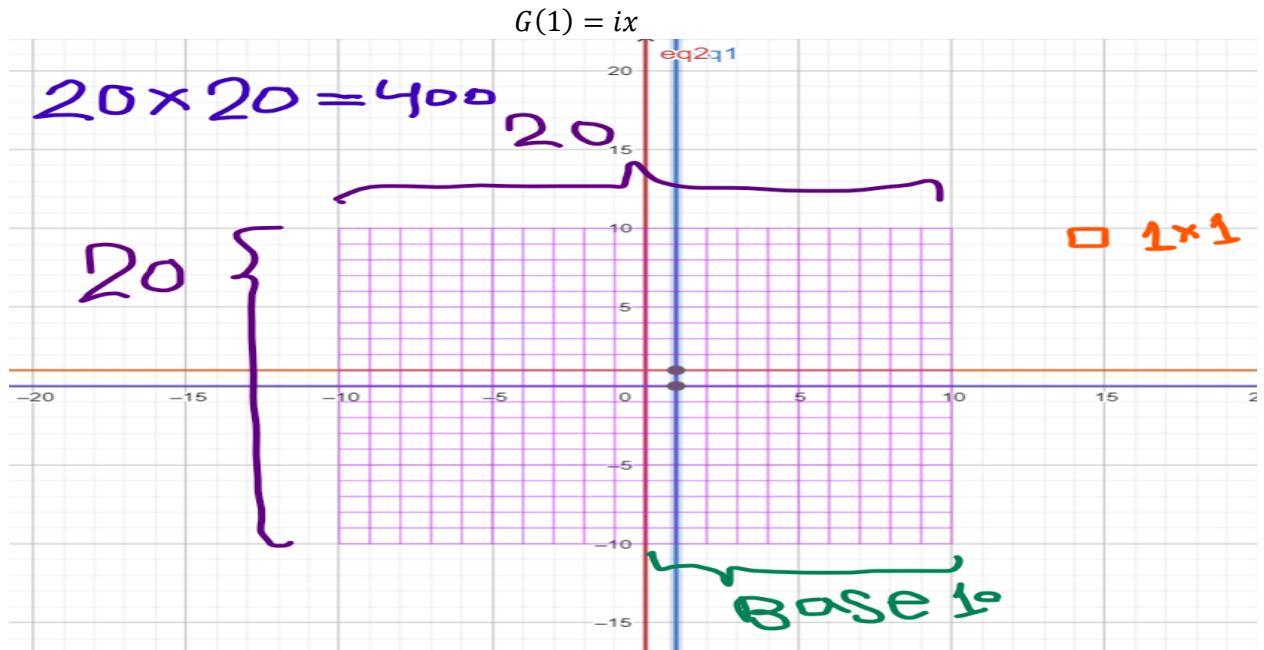
Complex plane frame of reference represents all basic natural numbers from [0,10]

It contains 400-unit squares, square unit area is 1.

If our observation point ( $T_0$ ) was at center point at the origin (0,0), Each unit square represents [+1] one step towards future from current point ( $T_0$ ). and each unit square before our [-1] observation point ( $T_0$ ) represents one step backwards from our observation point ( $T_0$ ).



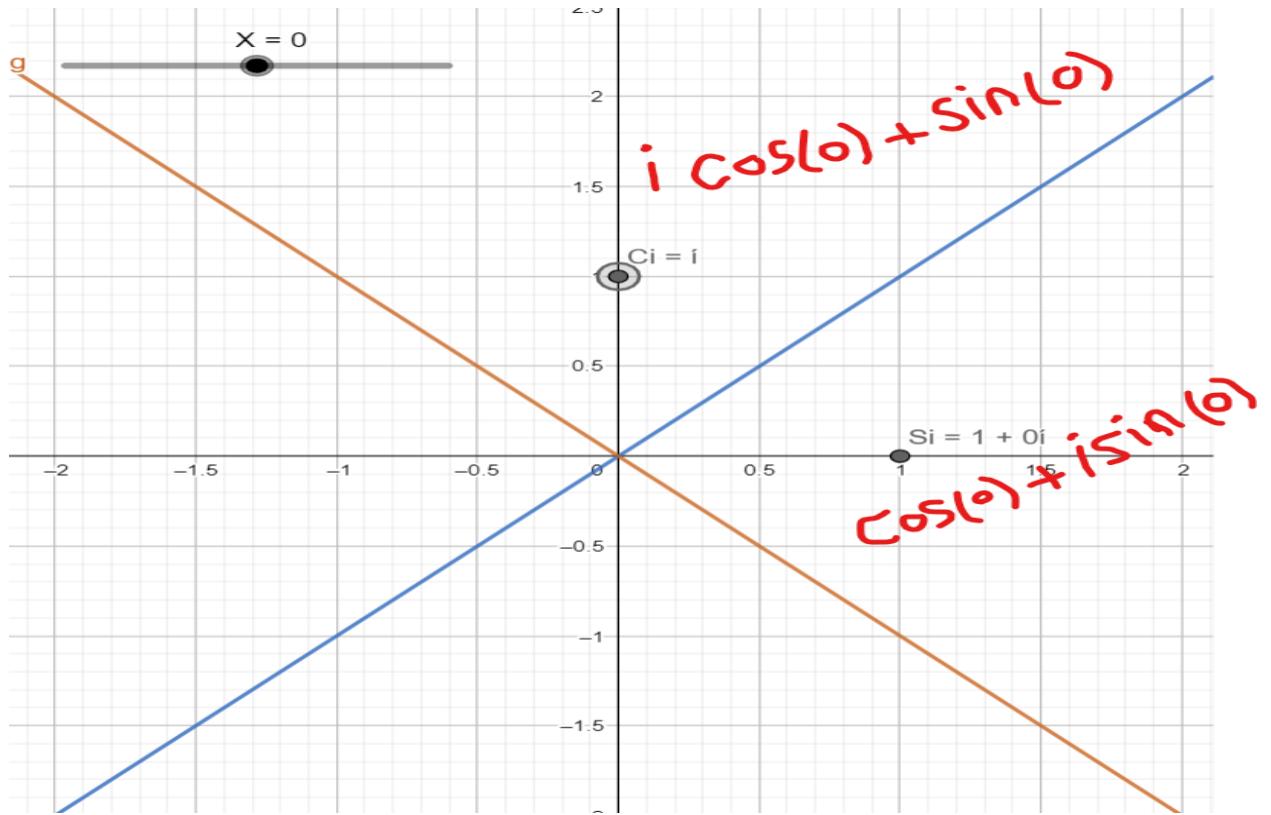
1- Complex plane Frame of reference



2- In complex plane we are going to represent its units in term of [Sin] and [Cos]

$$Si = 1 = \cos(0) + i \sin(0)$$

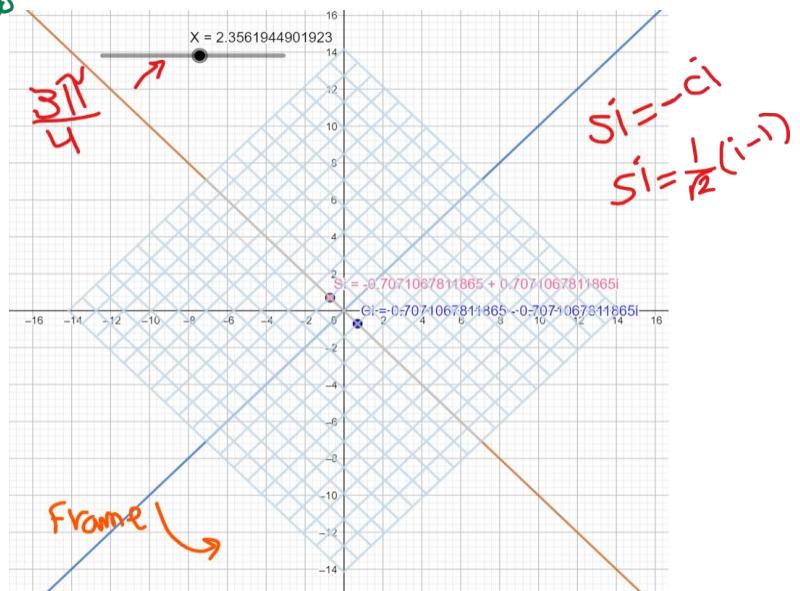
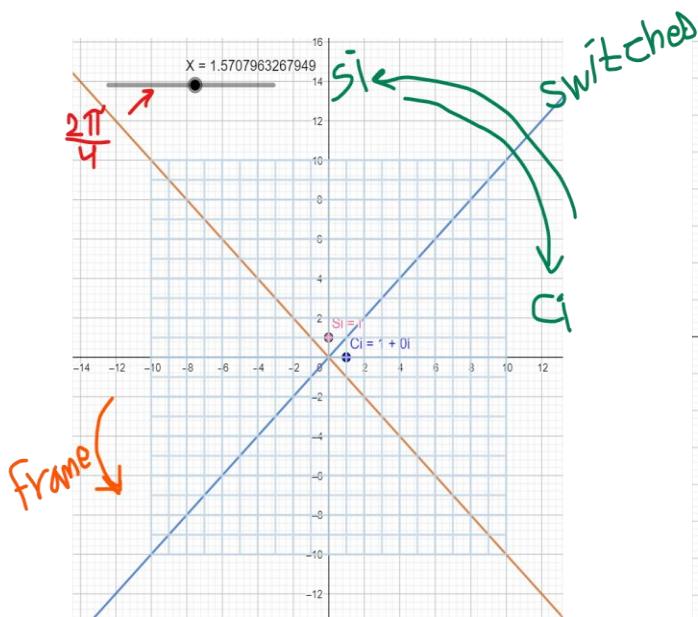
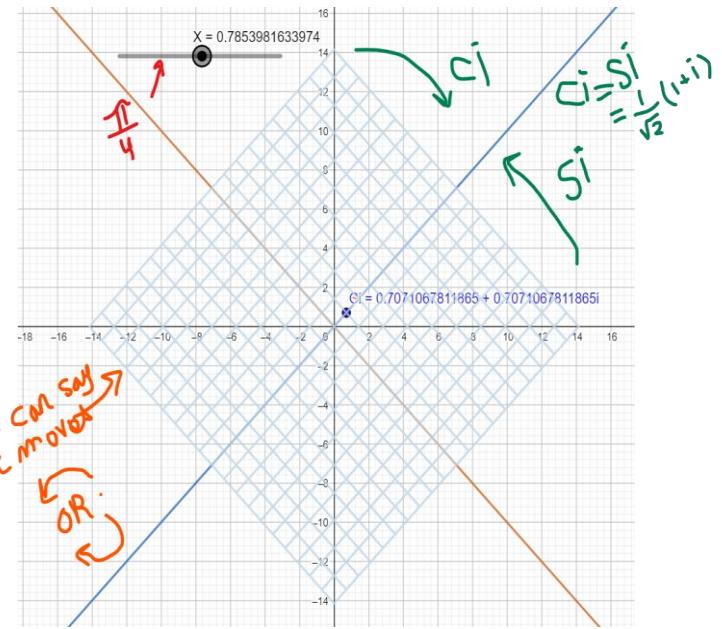
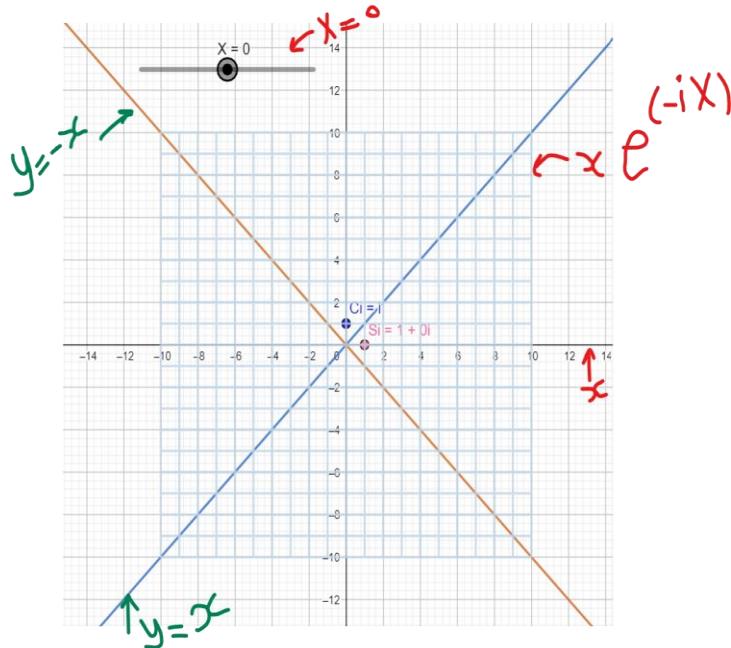
$$Ci = i = i * \cos(0) + \sin(0)$$

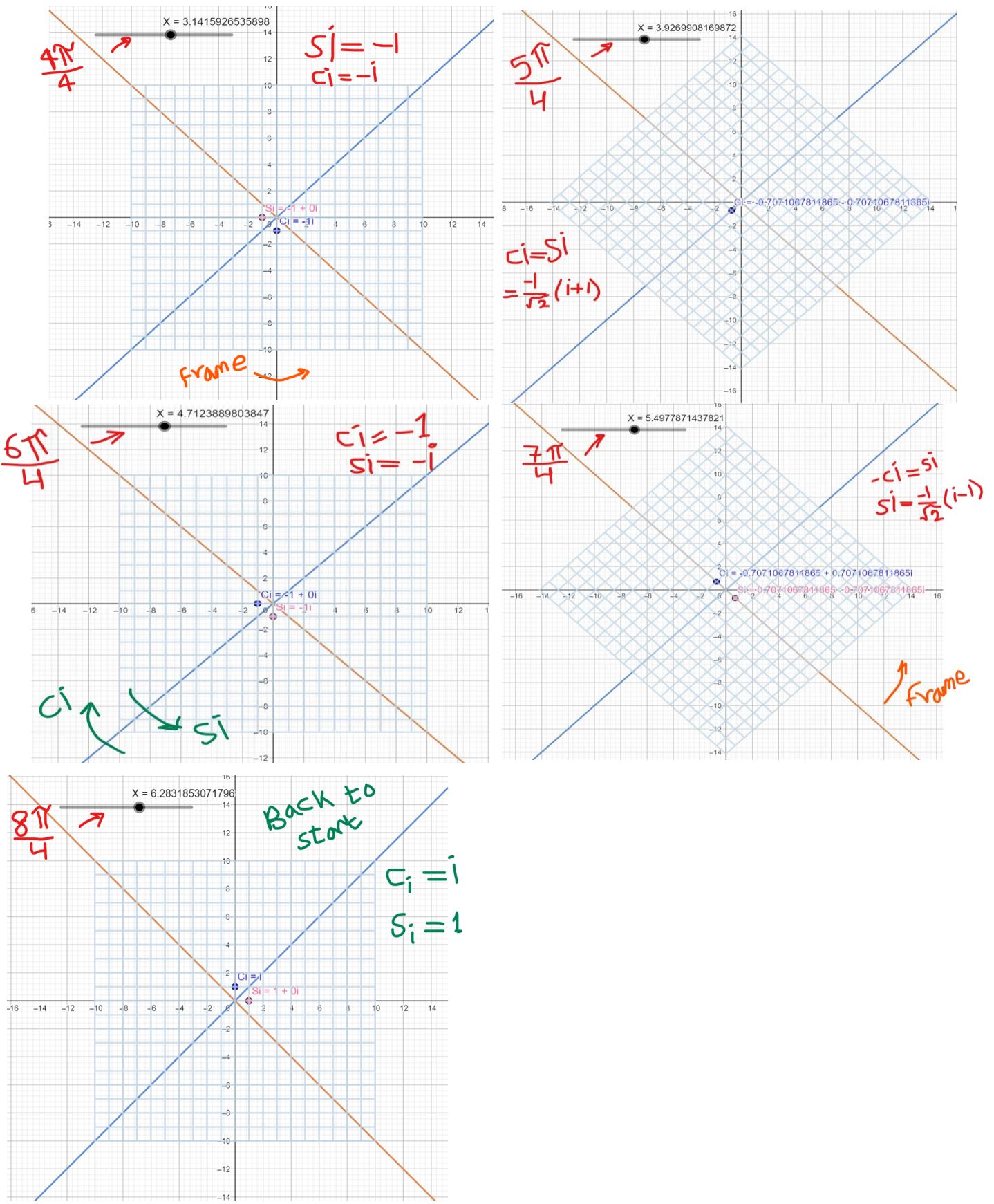


### 3- Complex plane axis rotation with frame of reference

$C_i$  and  $S_i$  will move in opposite directions of each other.

$$\text{at } X = \frac{\pi}{4} \text{ and at } X = \frac{5\pi}{4}; \text{ both } C_i = S_i$$





4- In base  $e^i$  at initial it has its own transformation for complex plane axis and we need 6.2831853071793 steps to complete full 360 cycle

$$e^i = 0.5403023058681 + 0.8414709848079i$$

$$e^{1* i} = \cos(\theta) + i \sin(\theta)$$

$$\theta = \alpha = \cos^{-1}(0.5403023058681)$$

$$c = \frac{360}{57.295779513085} \quad \vdots$$

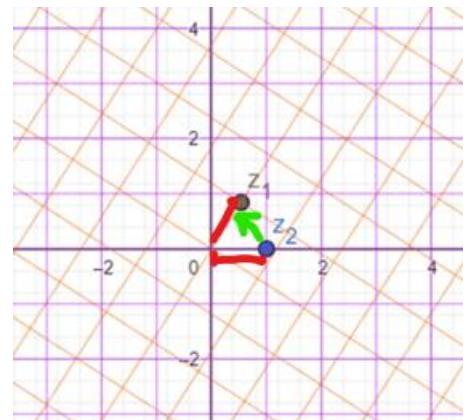
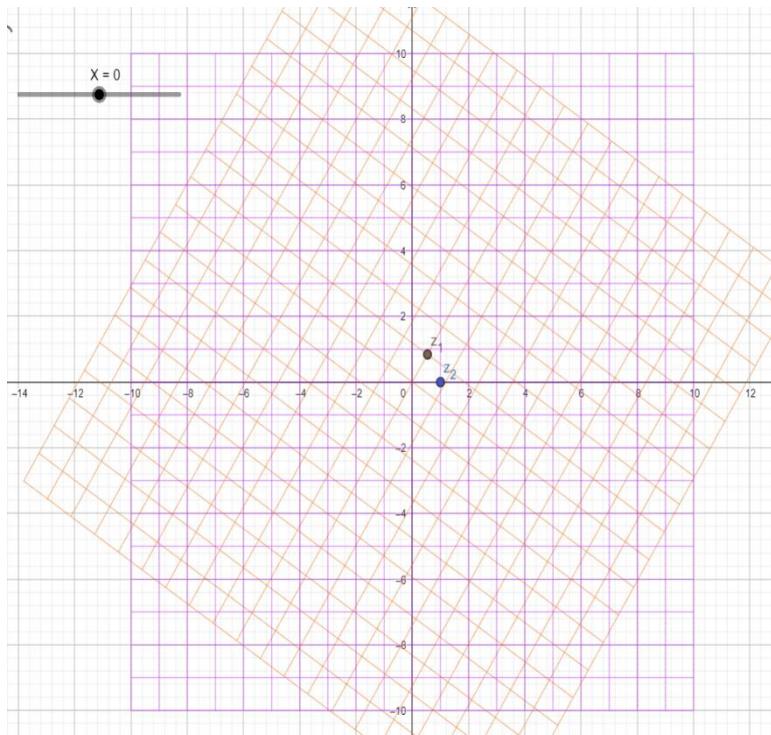
$$\rightarrow 6.2831853071793$$

$$\alpha = \cos^{-1}(0.5403023058681) \quad \vdots$$

$$z_1 = e^i$$

$$\rightarrow 57.295779513085^\circ$$

$$\rightarrow 0.5403023058681 + 0.8414709848079i$$



5- In Systems with base [e] there is already initial transformation for complex plane as we showed in point (4). In this system with base [e]

$$e = e^{\frac{1}{i} \cdot i} = \cos\left(\frac{1}{i}\right) + i \sin\left(\frac{1}{i}\right)$$

$$\frac{1}{i} = -i$$

$$e = \cos(-i) + i \sin(-i)$$

IF

$$z_2 = \cos(-i) + i \sin(-i)$$

$$\rightarrow 2.718281828459 + 0i$$

$$i = i \cos(0) + i \sin(0)$$

$$e = \cos(-(i \cos(0) + i \sin(0))) + i \sin(-(i \cos(0) + i \sin(0)))$$

IF



$$z_4 = \sin(\cos(0))$$

$$\rightarrow (0.8414709848079, 0)$$

$$d = \cos(\cos(0))$$

$$\rightarrow 0.5403023058681$$

AND



$$z_5 = e^i$$

$$\rightarrow 0.5403023058681 + 0.8414709848079i$$

THEN

$$e^i = \cos(\cos(0)) + i \sin(\cos(0))$$

And this  $\cos(0) = 1$

Note this one degree in the new system with base [e] not in the original complex plane axis.

6- Complex plane with base unit [ $e = 2.718281828459$ ]

$$i = e^{\pi i} = \cos(\pi) + i \sin(\pi)$$

$$1 = e^{0i} = \cos(0) + i \sin(0)$$

$$e = e^{\frac{1}{i}*i} = \cos\left(\frac{1}{i}\right) + i \sin\left(\frac{1}{i}\right) = \cos(-i) + i \sin(-i)$$

$$e = \cos(-i) + i \sin(-i)$$

We showed that.

$$i = i * \cos(0) + \sin(0)$$

$$1 = \cos(0) + i \sin(0)$$

$$\cos(\pi) + i \sin(\pi) = i * \cos(0) + \sin(0)$$

$$\cos(\pi) - \sin(0) = i * \cos(0) - i \sin(\pi)$$

$$i = \frac{\cos(\pi) - \sin(0)}{\cos(0) - \sin(\pi)} = -1$$

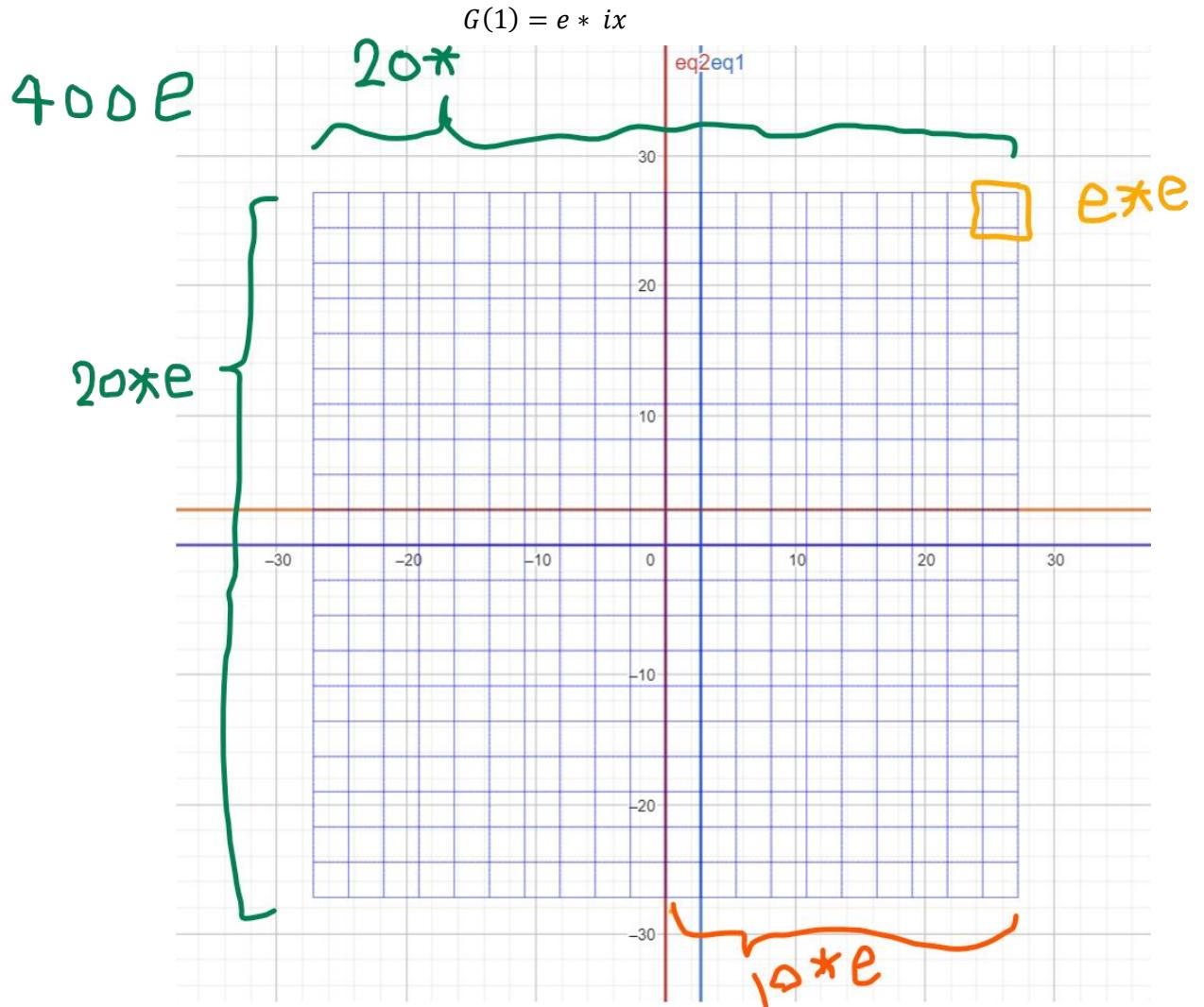
And

$$1 = \cos(0) + i \sin(0)$$

$$i = \frac{1 - \cos(0)}{\sin(0)} = \frac{0}{0} = 1$$

So, [i] has dual state in complex plane at  $\theta = \pi$

Here we are going to scale our frame of reference by  $[e]$  to convert our system to base  $[e]$  as  $[e^i]$  already has an initial transformation from the original complex plane.



First let us see what the effect on the frame of reference of applying powers of any base  $[A]$ . As  $e^{-i\omega t}$  is already Power function .

7- Power function using imaginary number and complex plane manifolding.

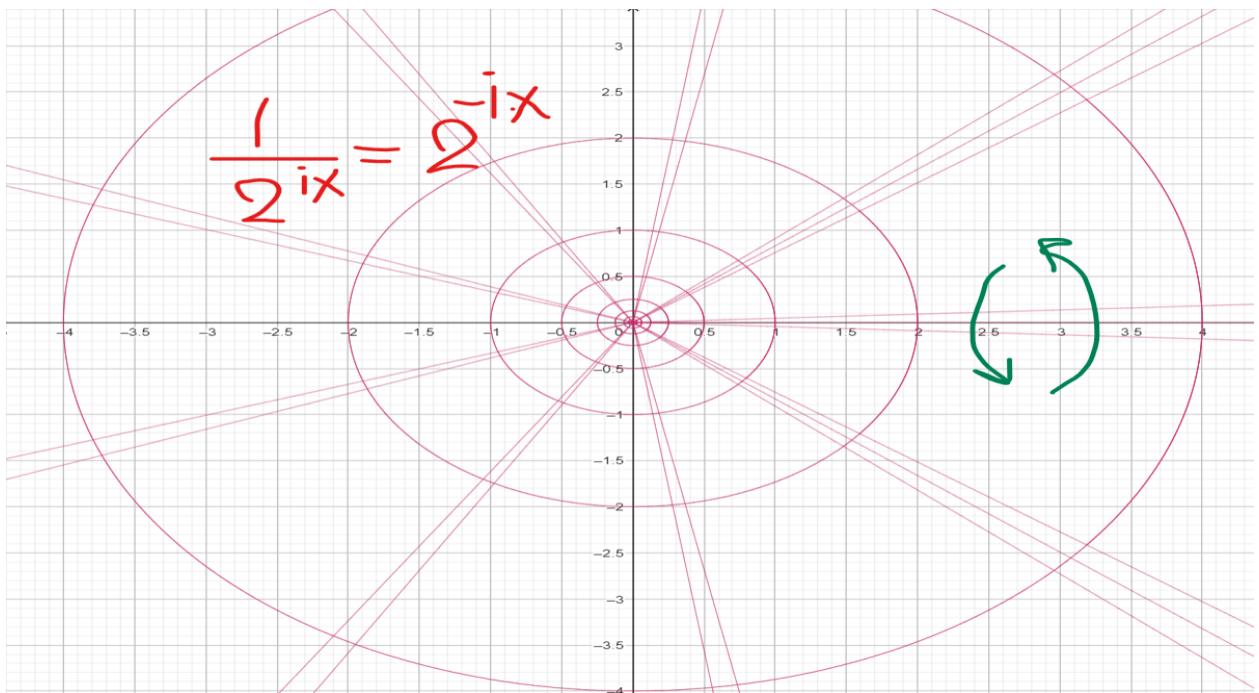
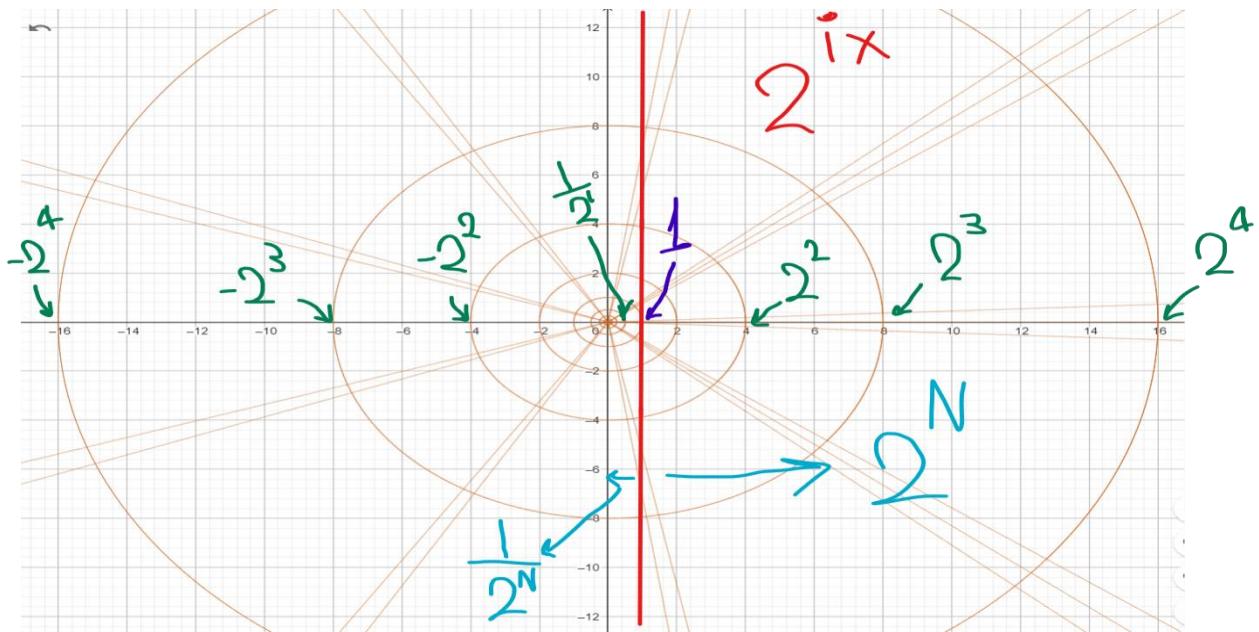
[i] has a unique feature of keeping steady vector length because it is the unit of a complex plane

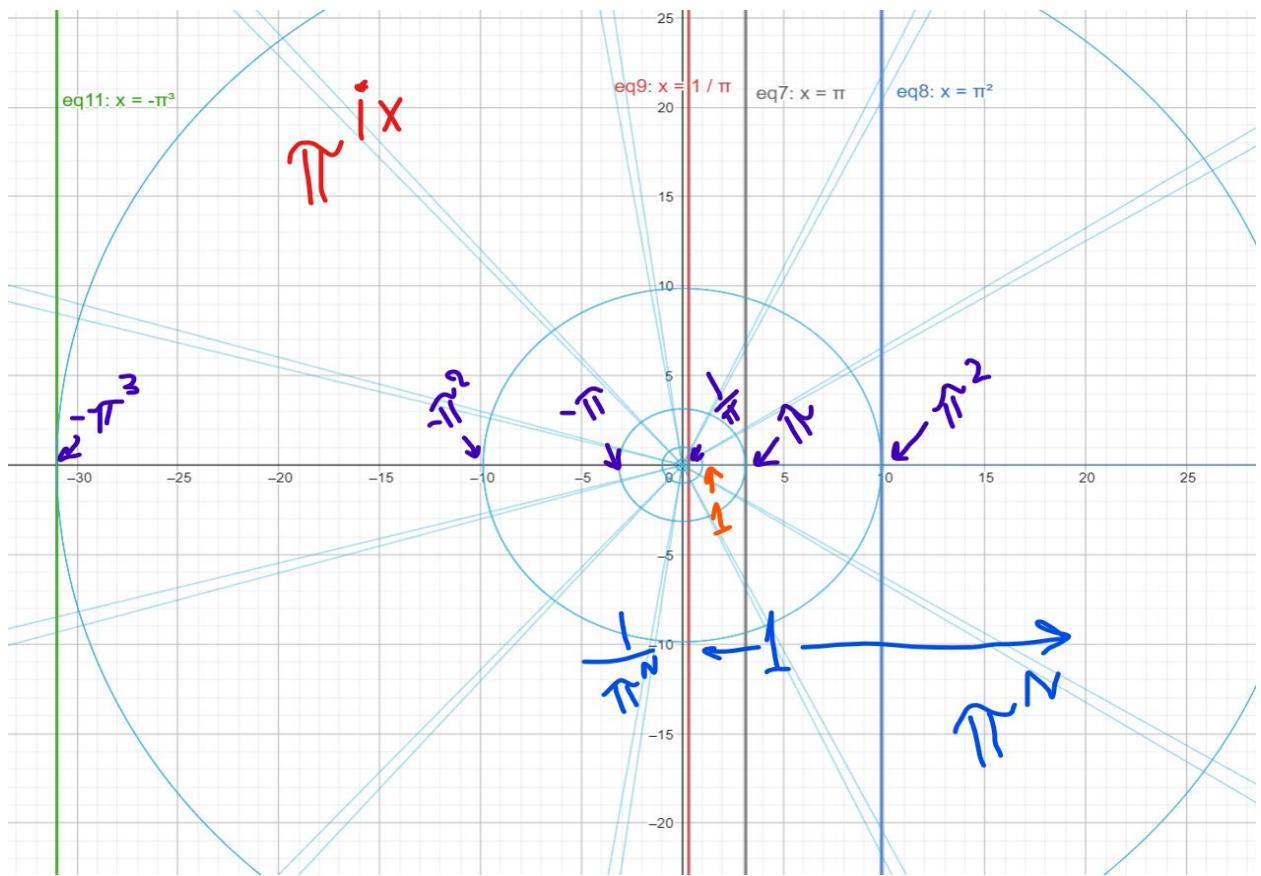
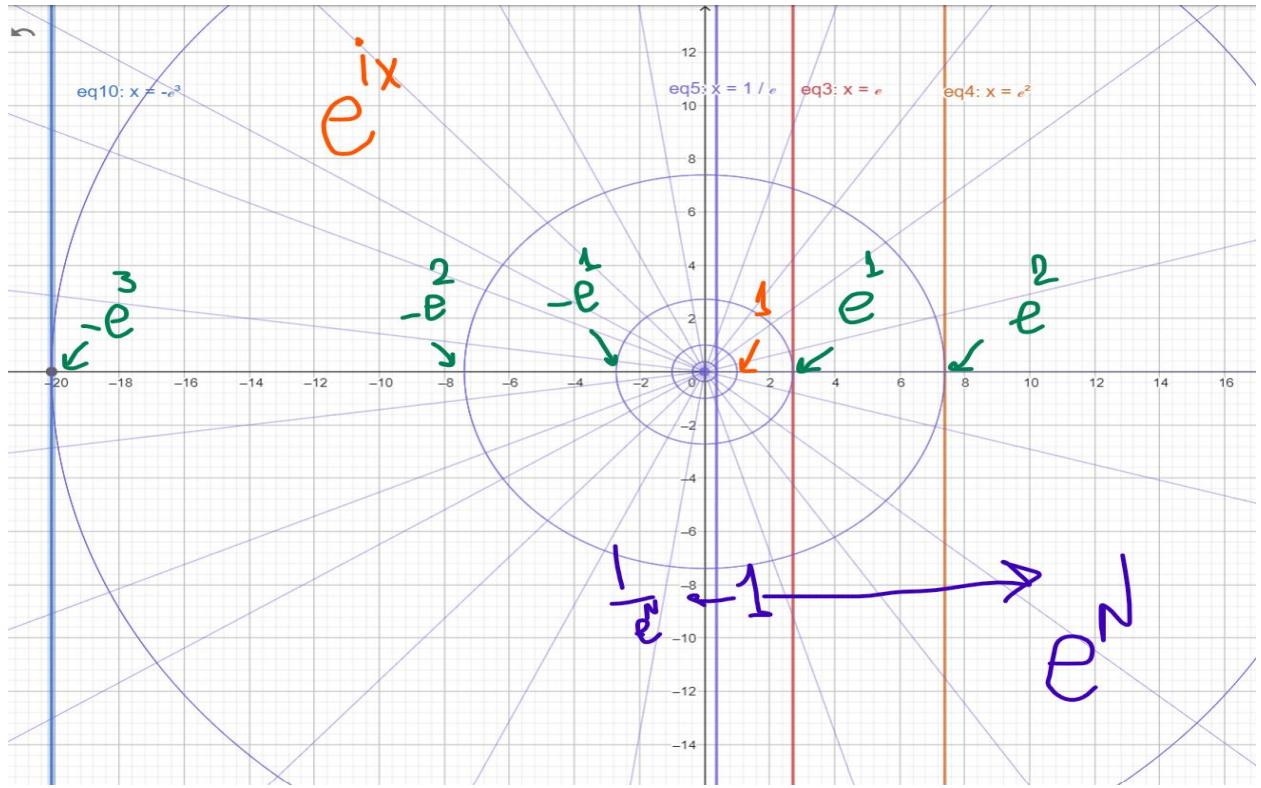
[i] is square root so it has  $\pm$  values, and also natural numbers have

$\pm$  values which make 4 sides in complex plane

so any number [A] raised to power [i] will keep a power to base length [A]

$$\text{Power Function} = A^{ix}$$

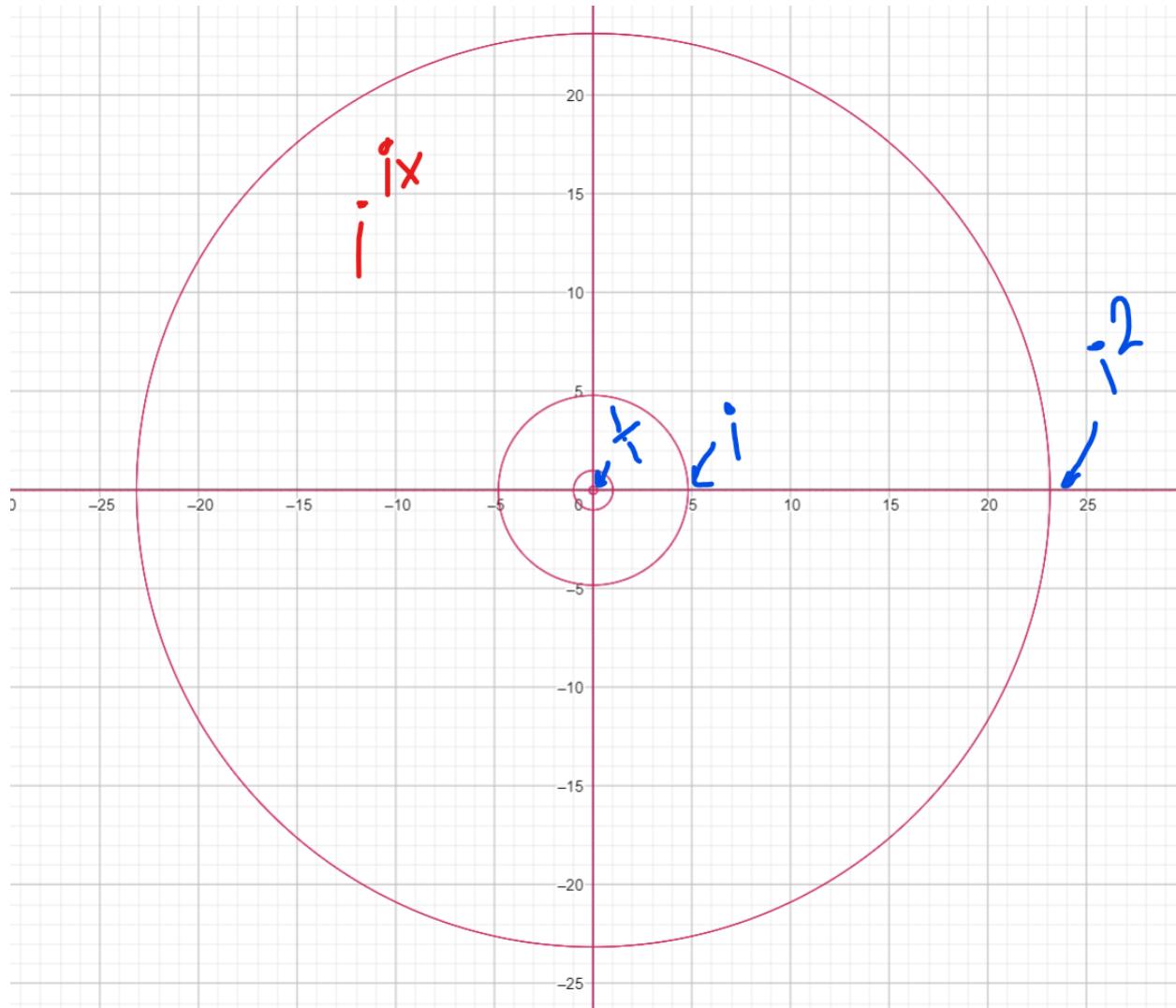




With the same concept we can say that is approximately = 5

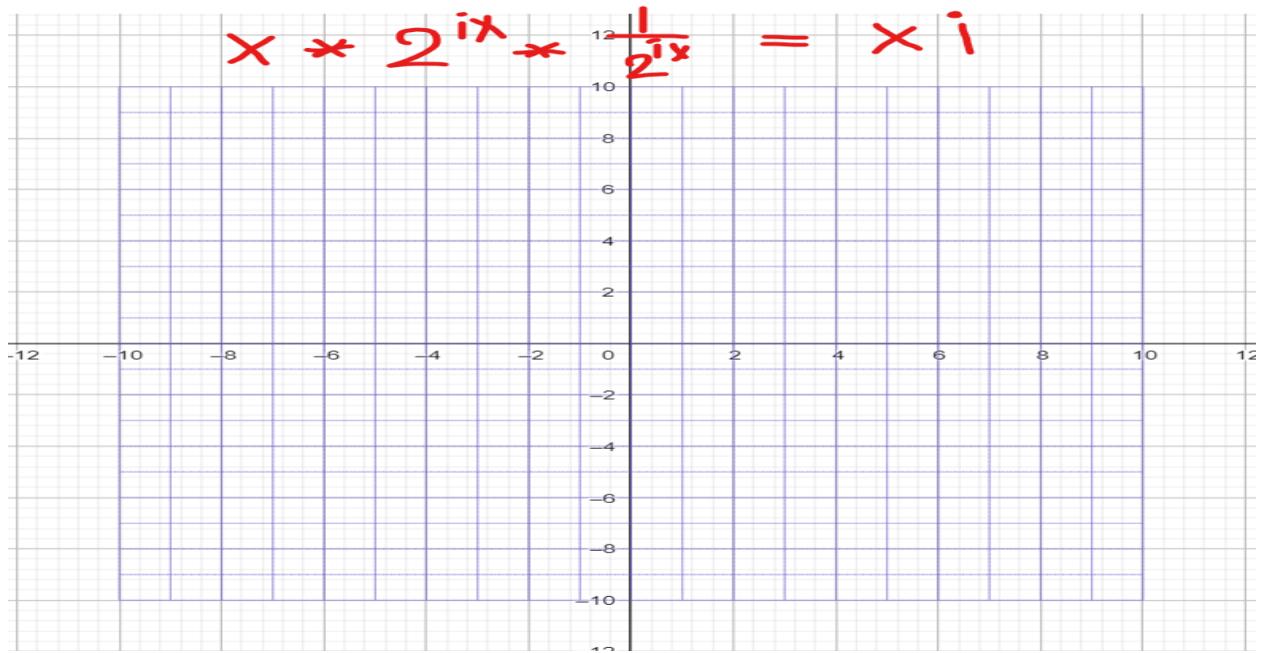
$$i = \frac{1}{0.207879}$$

$$\rightarrow 4.8104907181582$$

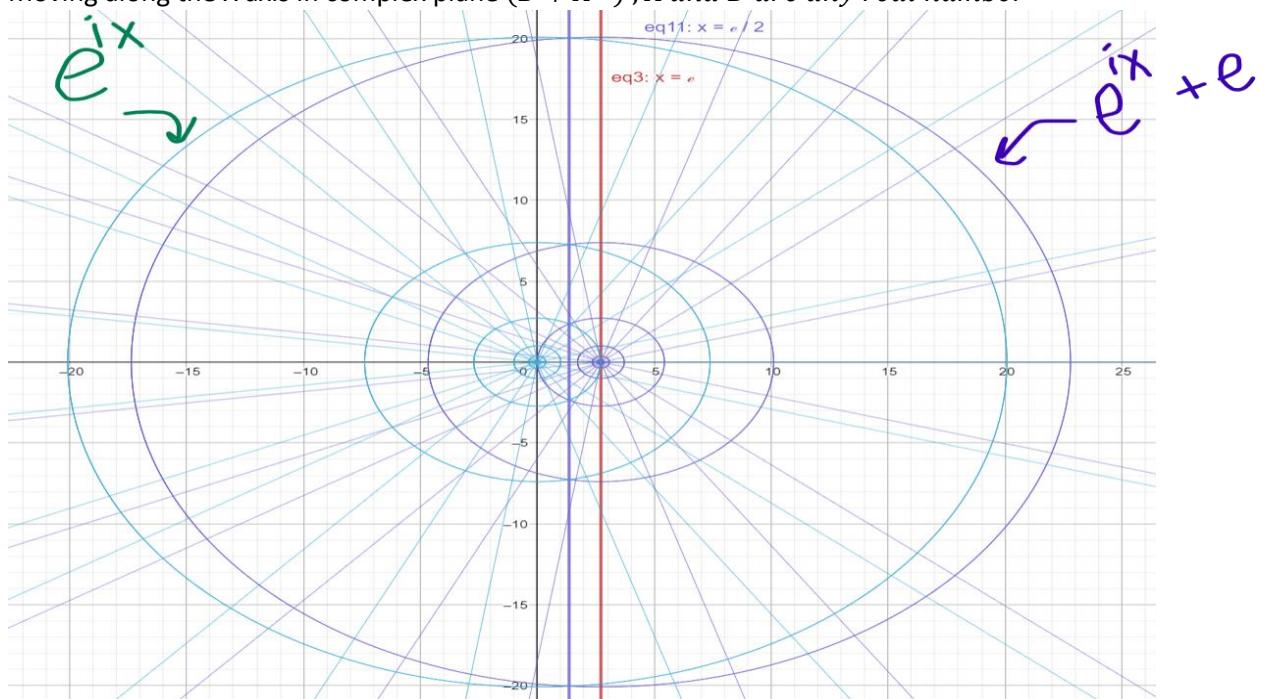


8- Reciprocal of number with base A=2

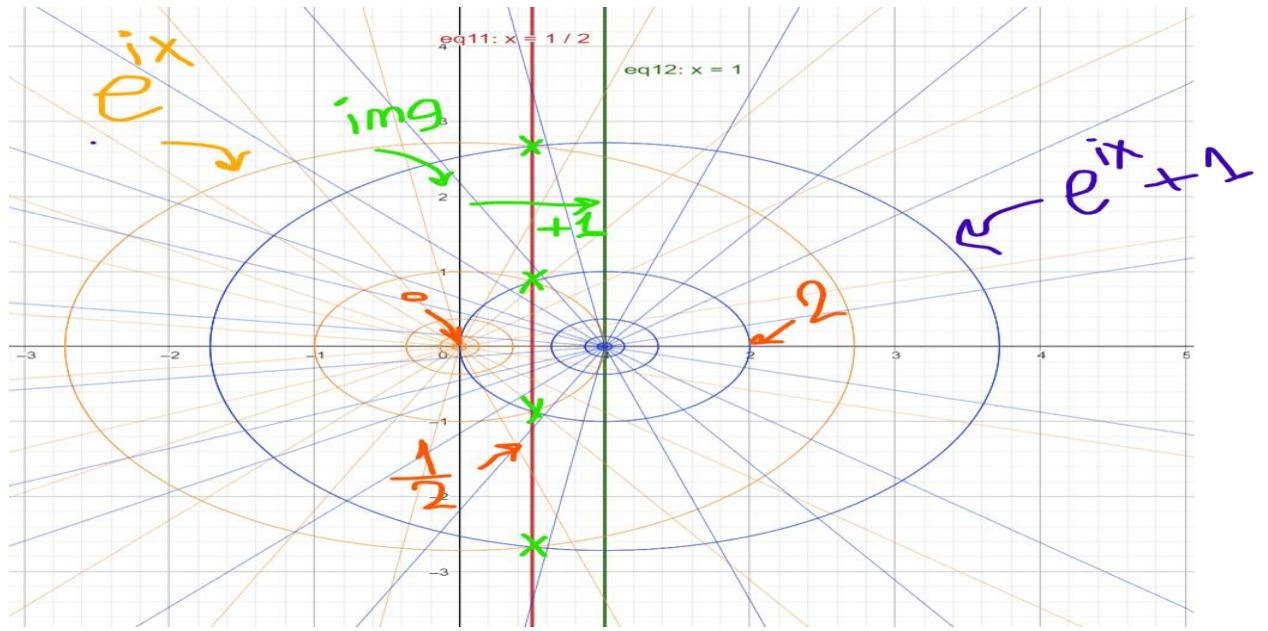
$$x * A^{ix} * \frac{1}{A^{ix}} = i * x$$



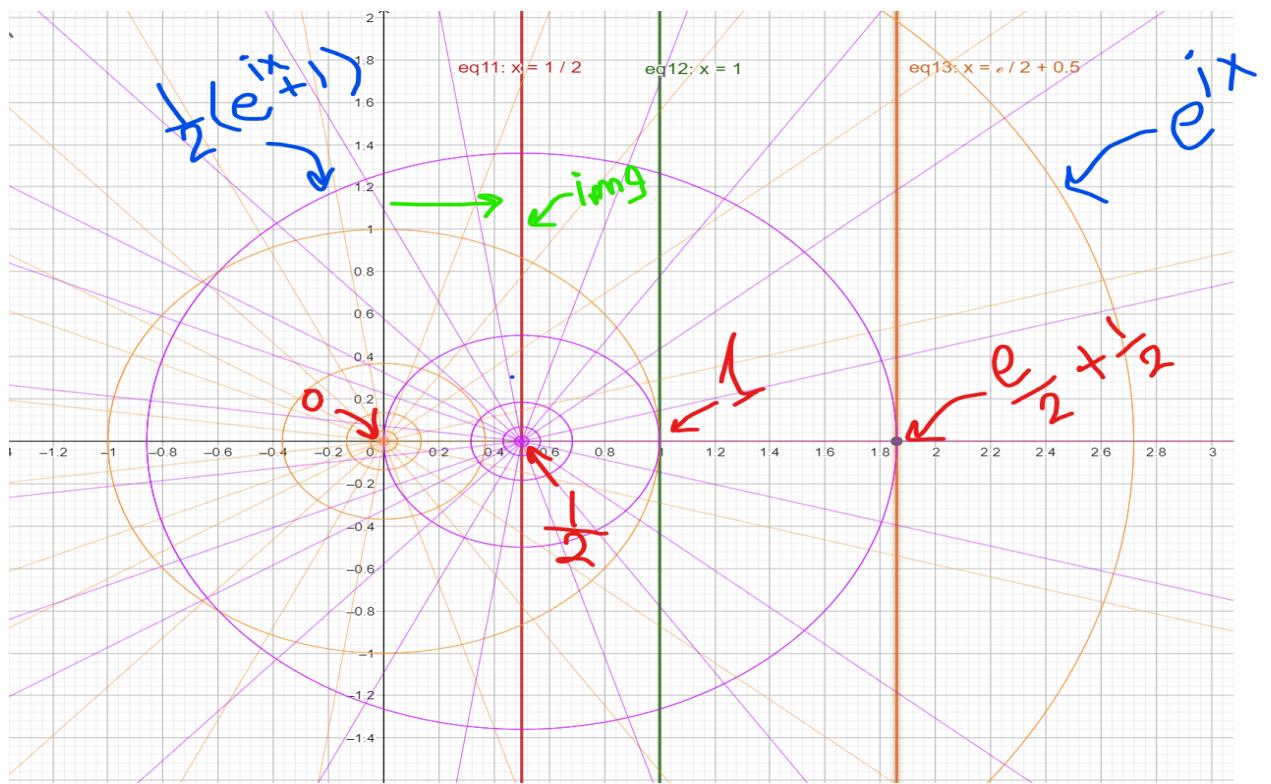
9- Moving along the X axis in complex plane ( $B + A^{ix}$ ) ; A and B are any real number



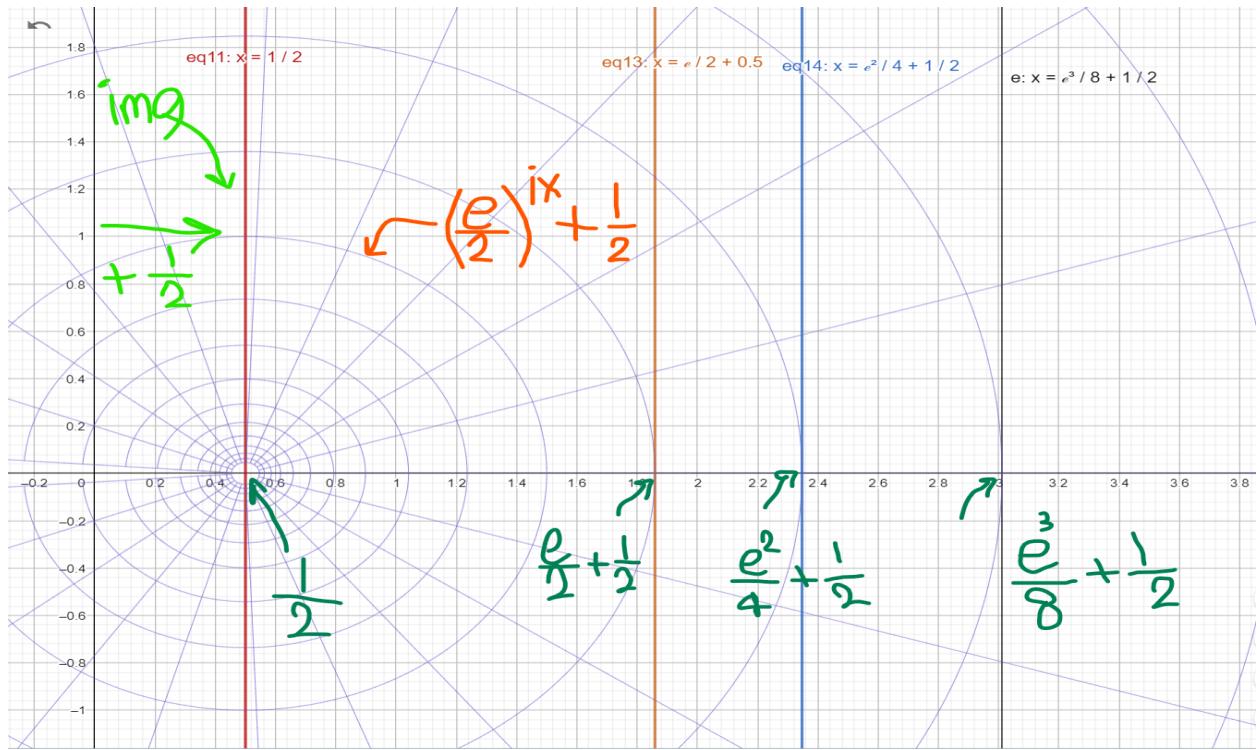
10- Moving along X axis in complex plane ( $B + A^{ix}$ ) ;  $A = e$  and  $B = 1$



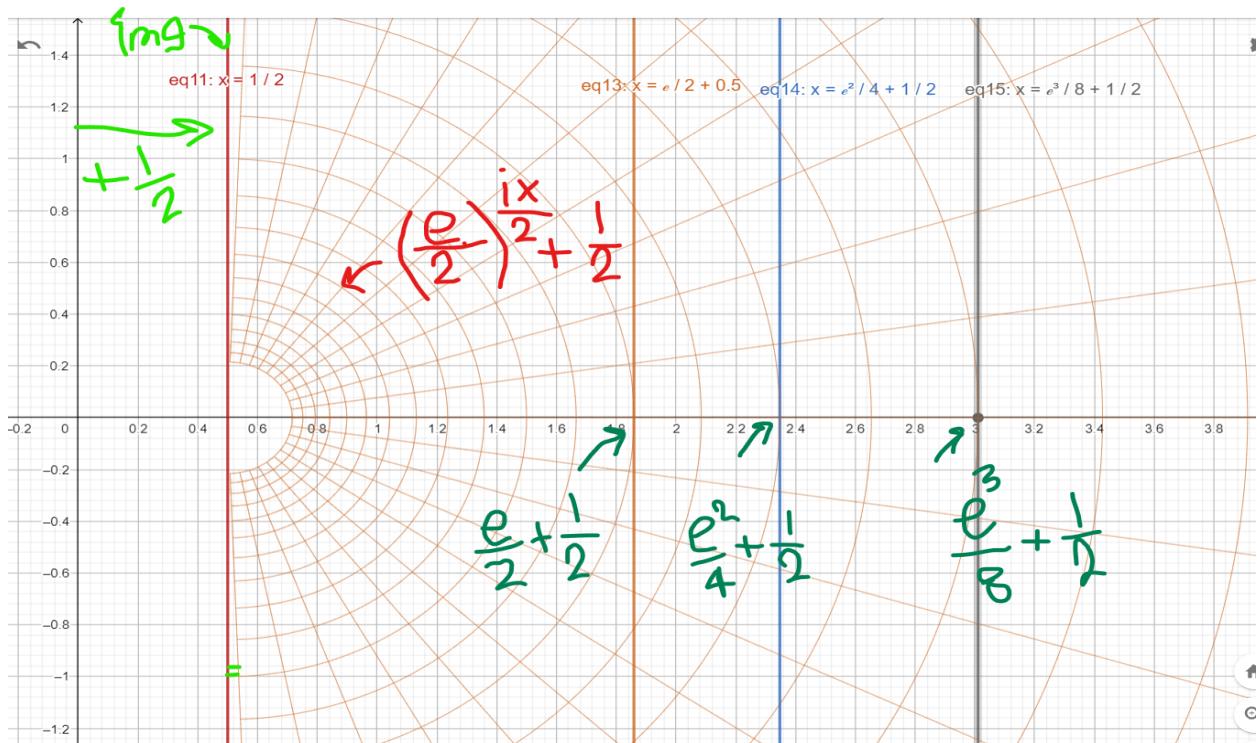
11- Moving along X axis in complex plane  $\frac{1}{2} * (B + A^{ix})$  ;  $A = e$  and  $B = 1$



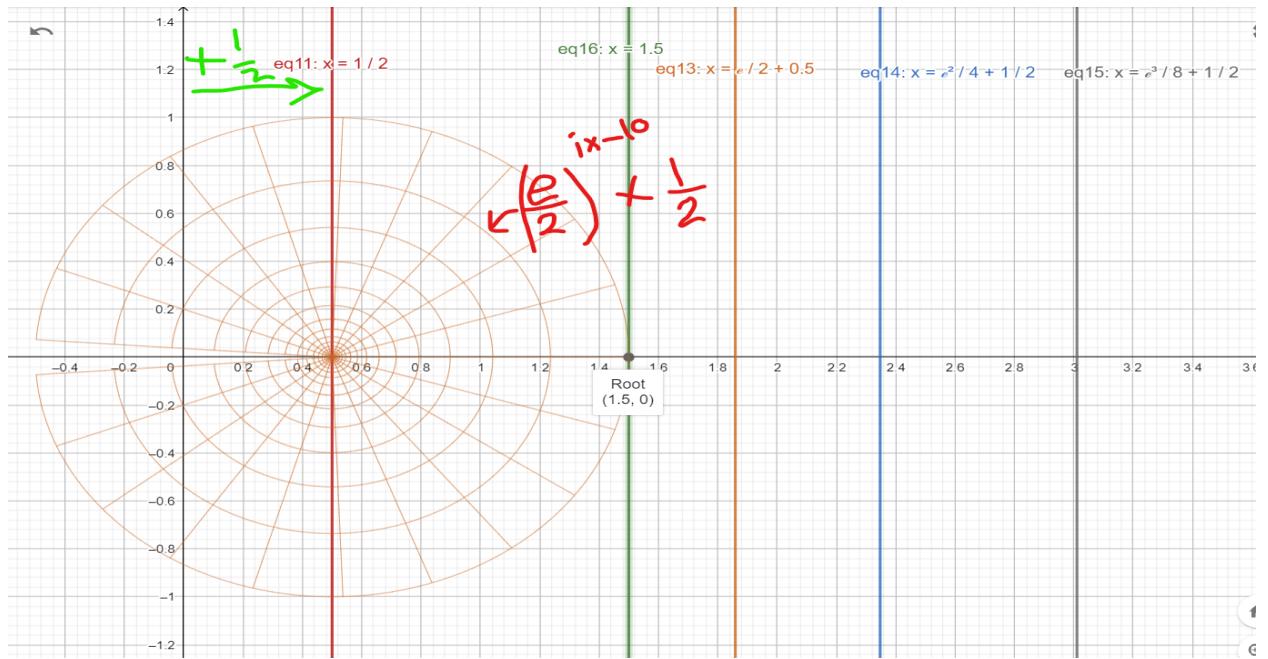
12- Moving along X axis in complex plane ( $B + A^{ix}$ ) ;  $A = \frac{e}{2}$  and  $B = \frac{1}{2}$



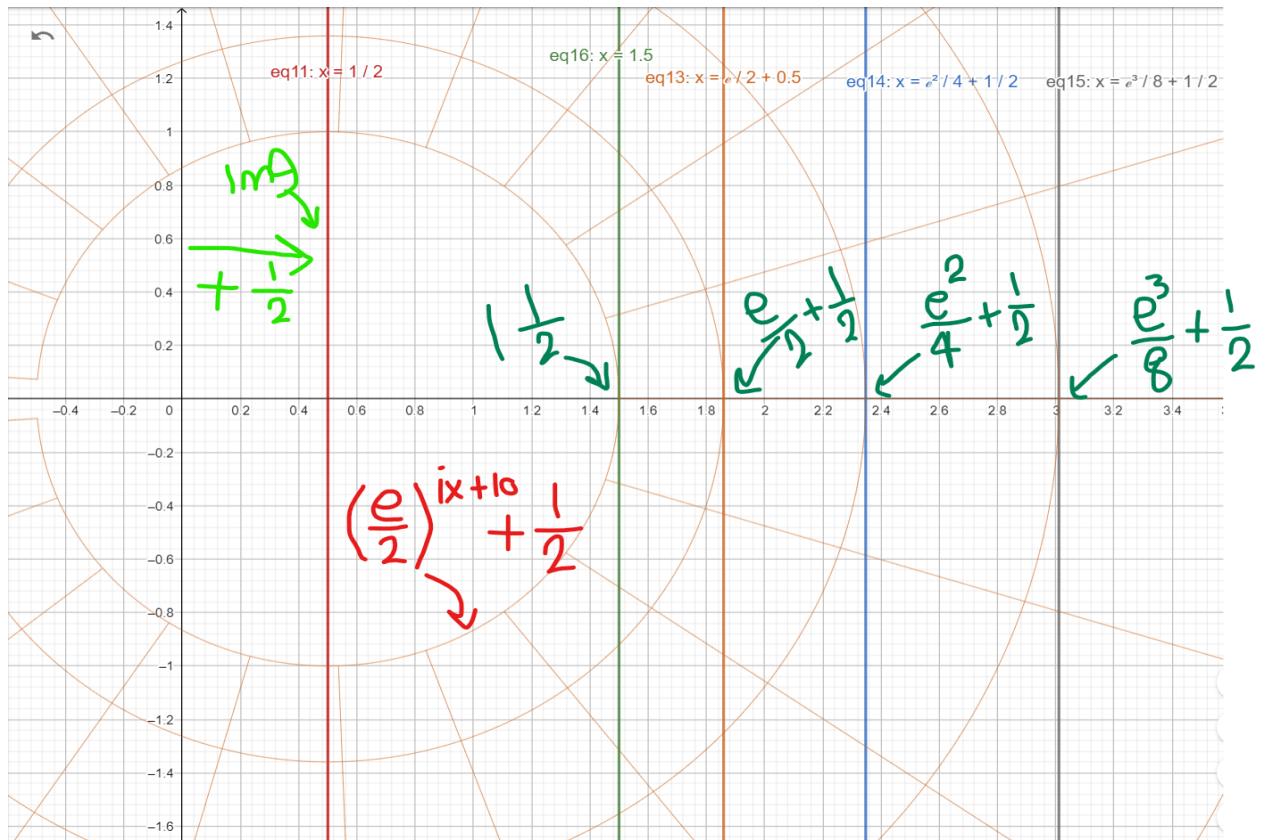
13- Moving along X axis in complex plane ( $B + A^{\frac{ix}{2}}$ ) ;  $A = \frac{e}{2}$  and  $B = \frac{1}{2}$



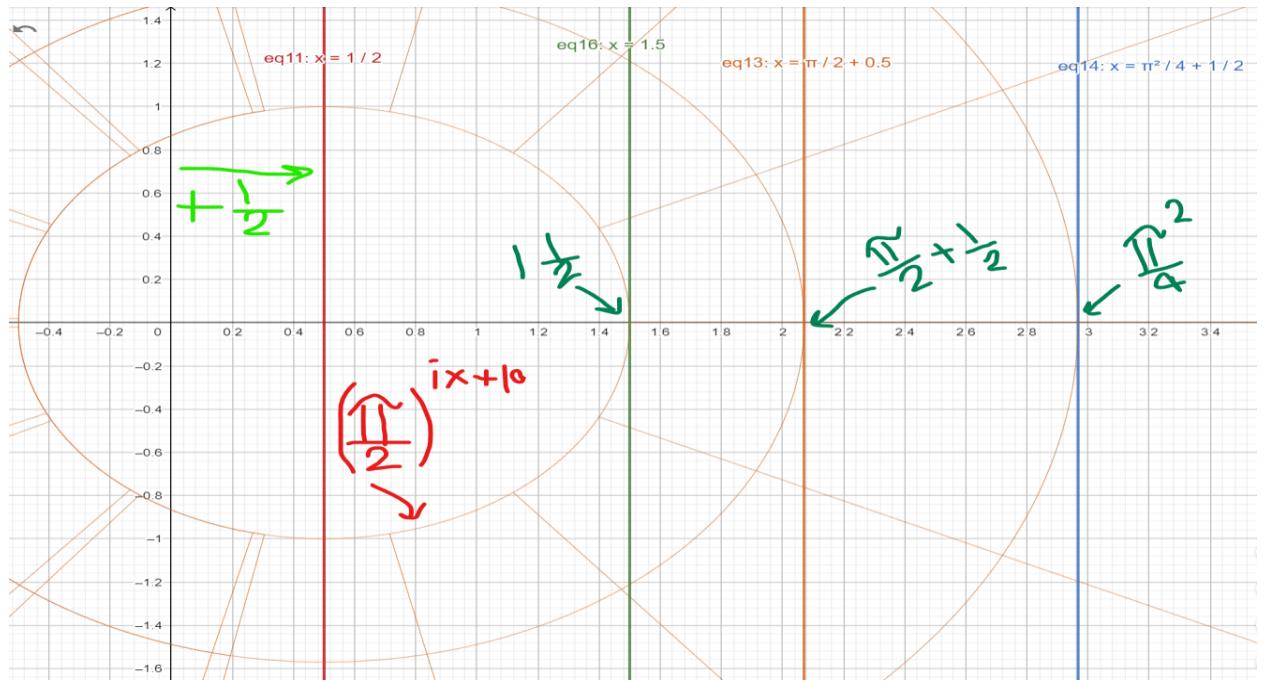
14- Moving along X axis in complex plane ( $B + A^{ix-10}$ ) ;  $A = \frac{e}{2}$  and  $B = \frac{1}{2}$



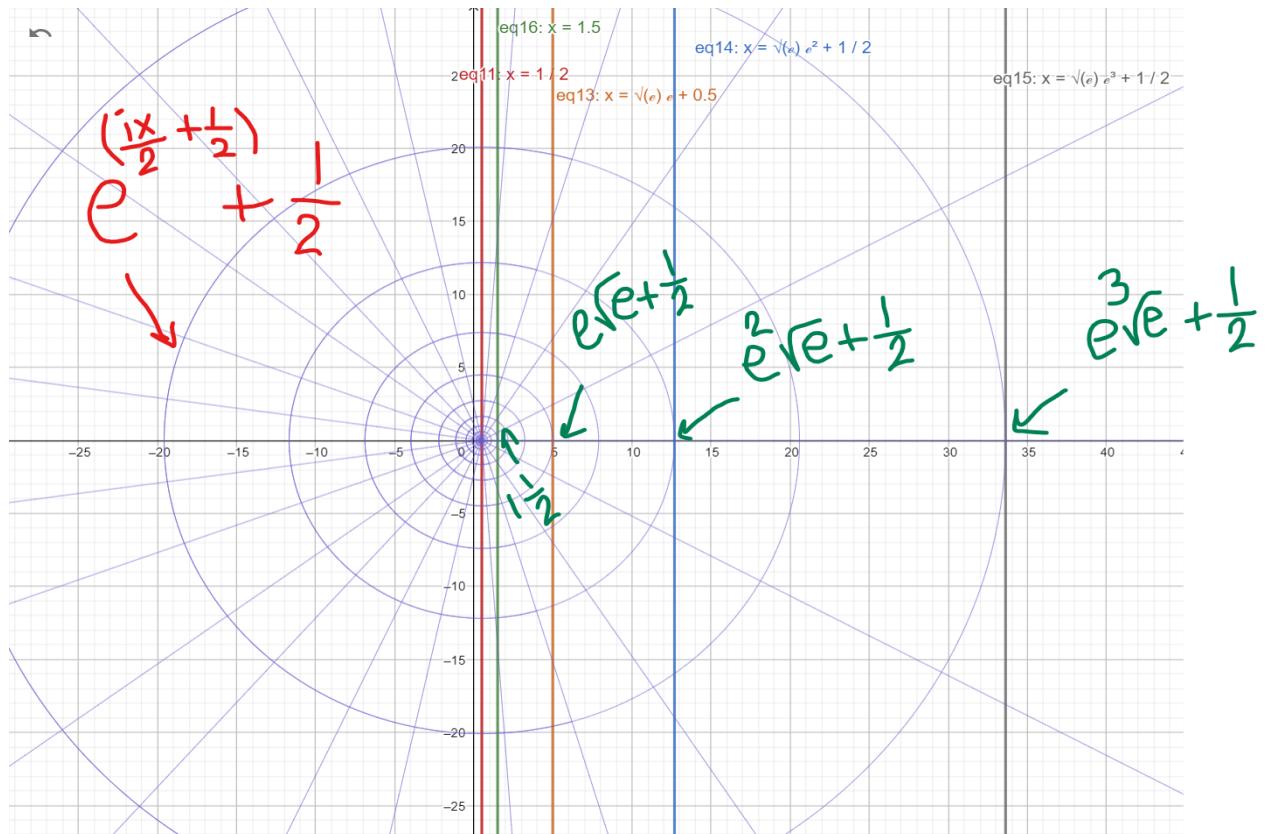
15- Moving along X axis in complex plane ( $B + A^{ix+10}$ ) ;  $A = \frac{e}{2}$  and  $B = \frac{1}{2}$



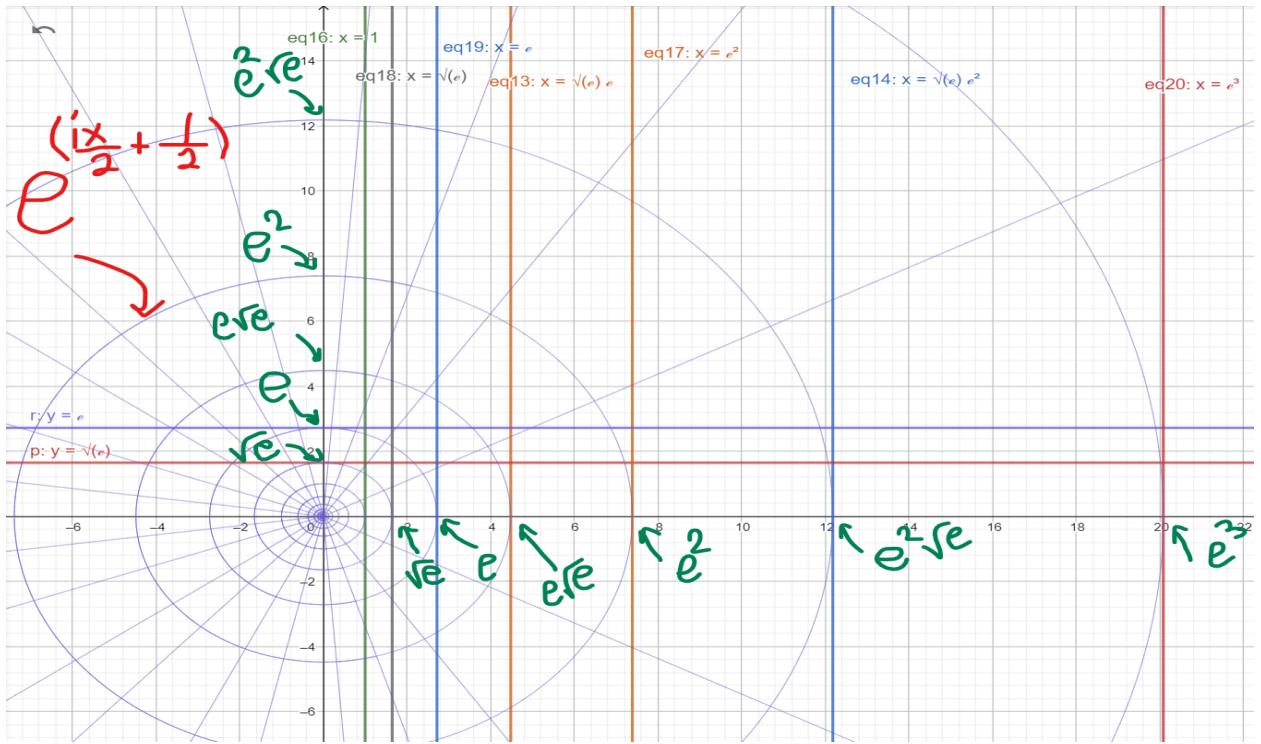
16- Moving along X axis in complex plane ( $B + A^{ix+10}$ ) ;  $A = \frac{\pi}{2}$  and  $B = \frac{1}{2}$



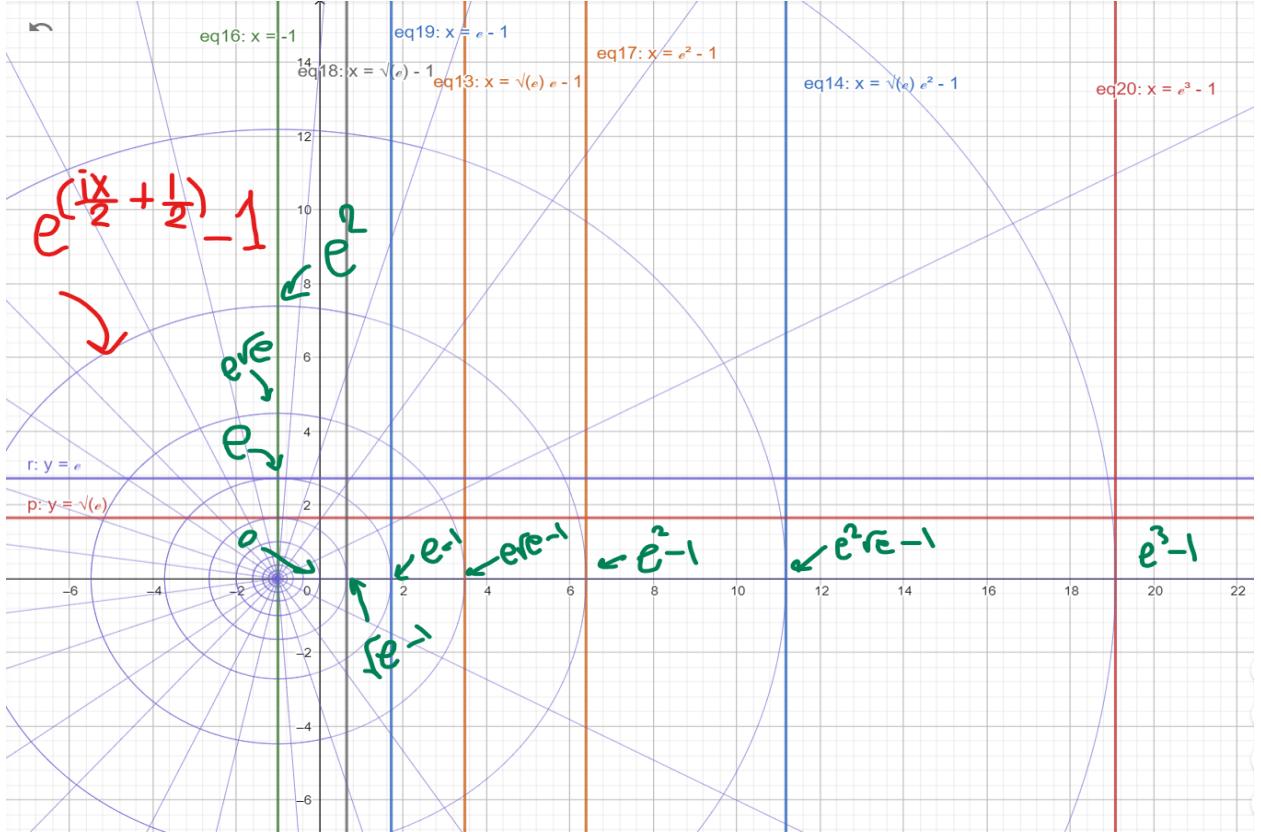
17- Moving along X axis in complex plane ( $B + A^{(\frac{ix}{2} + \frac{1}{2})}$ ) ;  $A = e$  and  $B = \frac{1}{2}$



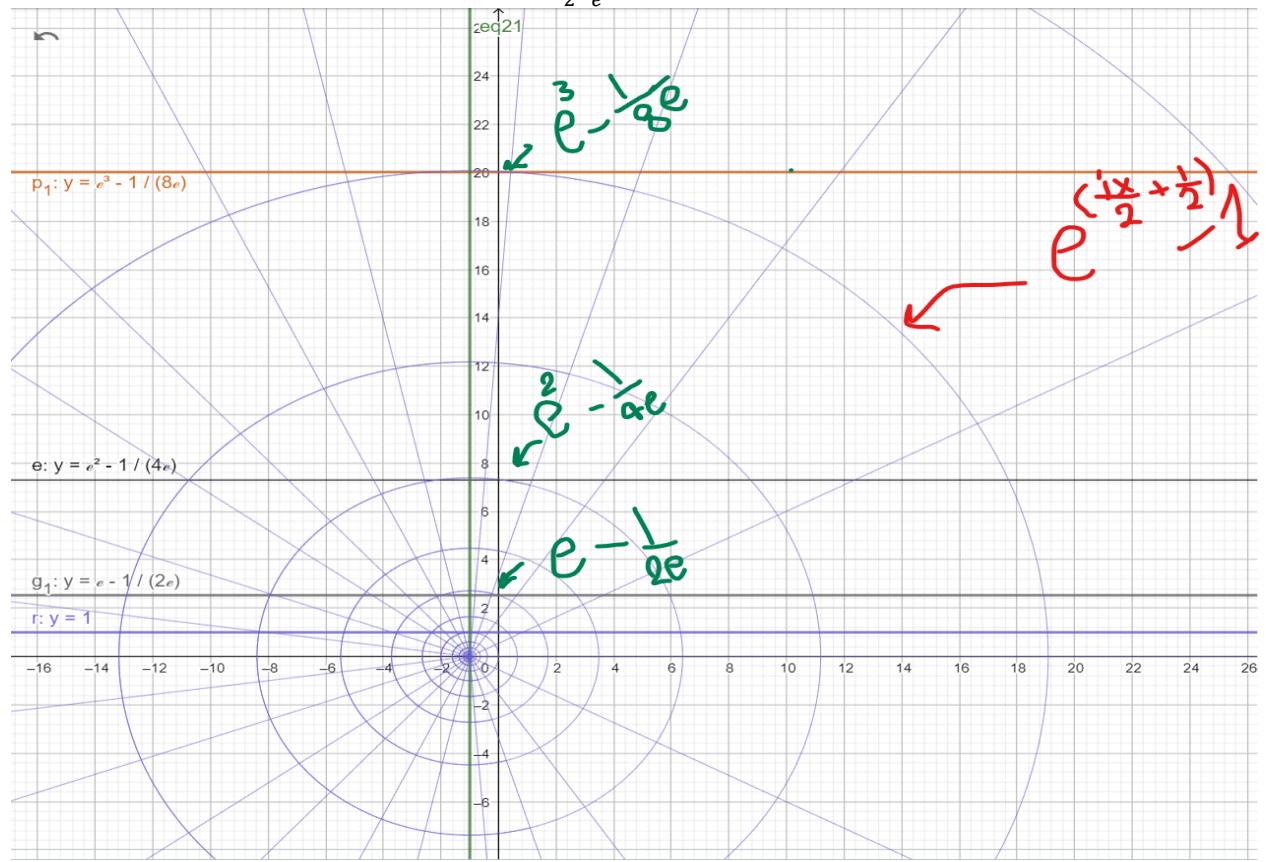
18- Moving along X axis in complex plane ( $B + A(\frac{ix}{2} + \frac{1}{2})$ ) ;  $A = e$  and  $B = 0$



19- Moving along X axis in complex plane ( $B + A(\frac{ix}{2} + \frac{1}{2})$ ) ;  $A = e$  and  $B = -1$



Values at Imaginary axis approximate to  $e^N - \frac{1}{2^N e}; N \geq 1$

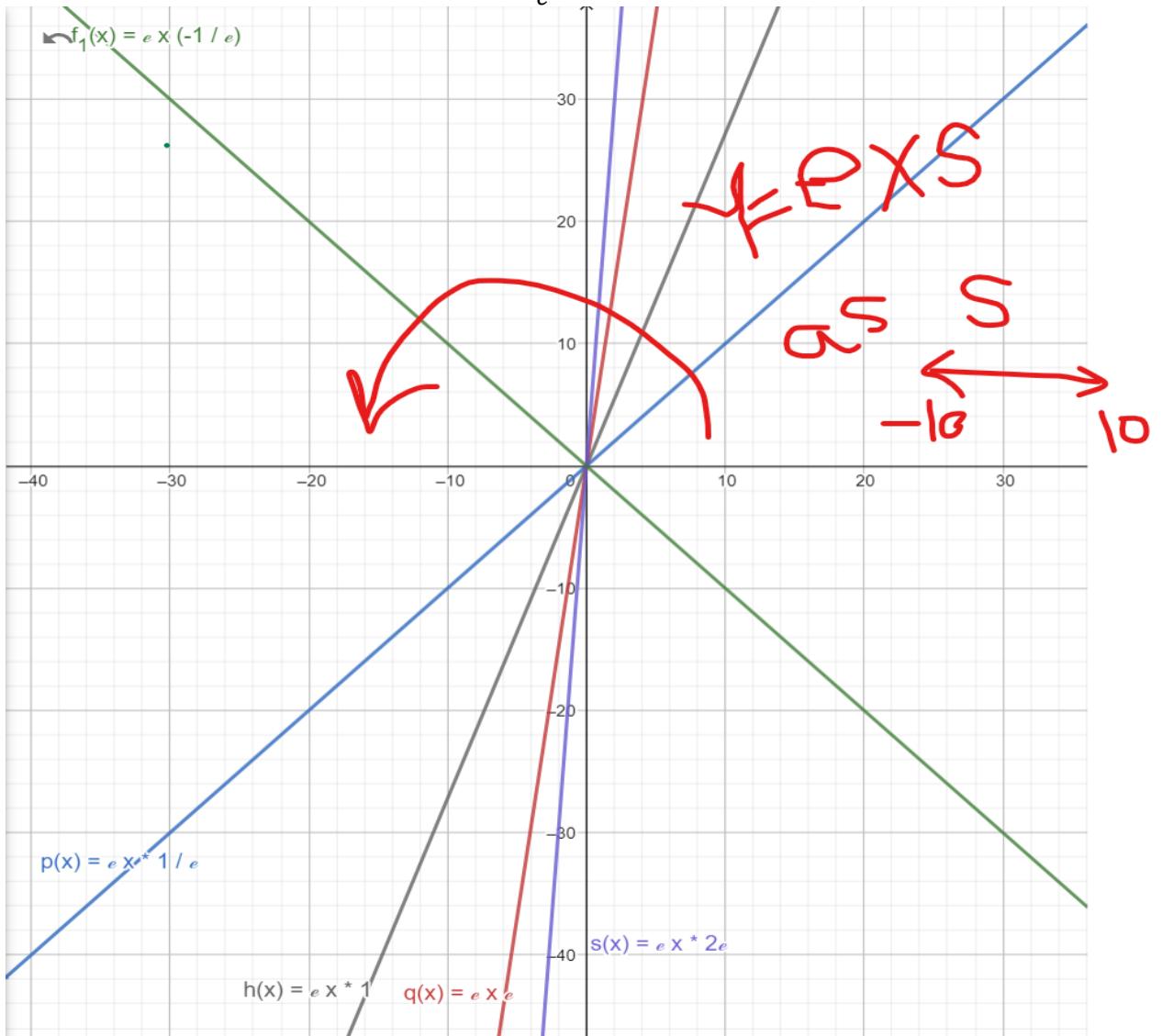


20-  $Y = X$  in complex plane  $Y = (e * x * A)$ ; for  $A = \text{any real value}$   
 multiply  $e$

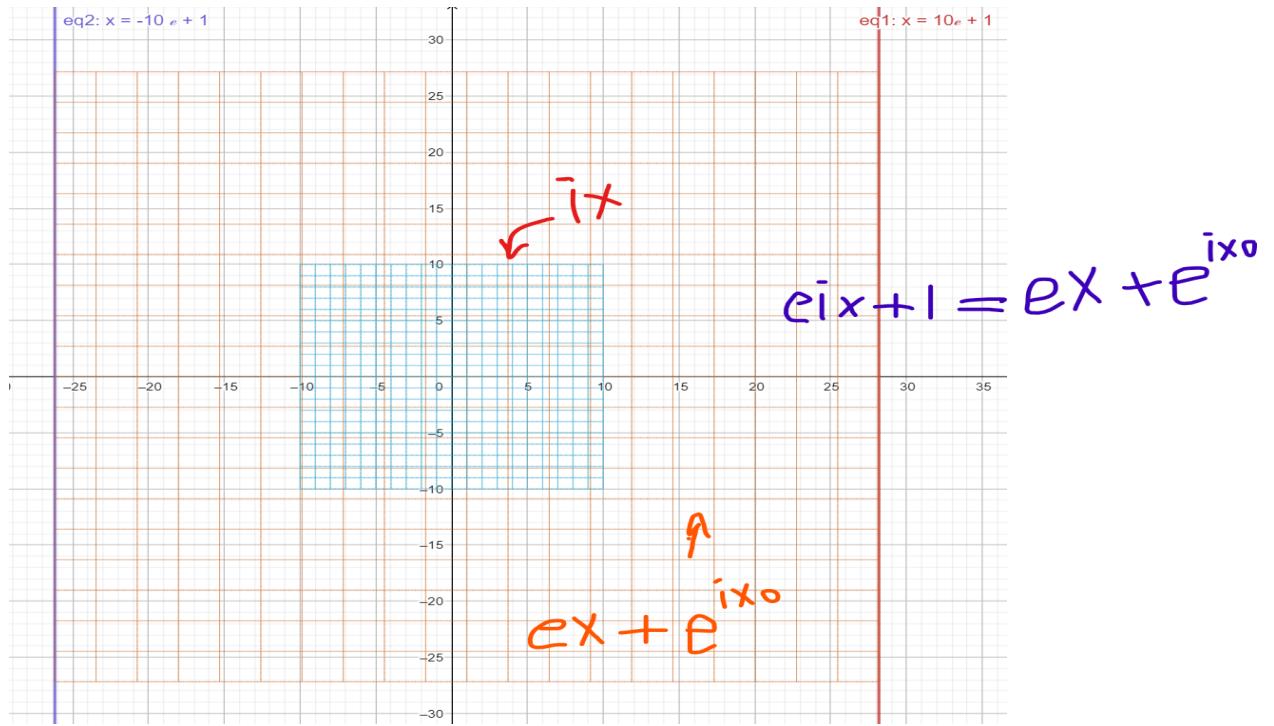
\*  $x$  by any function  $[A]$  keeps the function signature and add rotation effect to the function  $[A]$

for example when  $A = \frac{1}{e}$  then we get  $y = X$

for example when  $A = \frac{-1}{e}$  then we get  $y = -X$

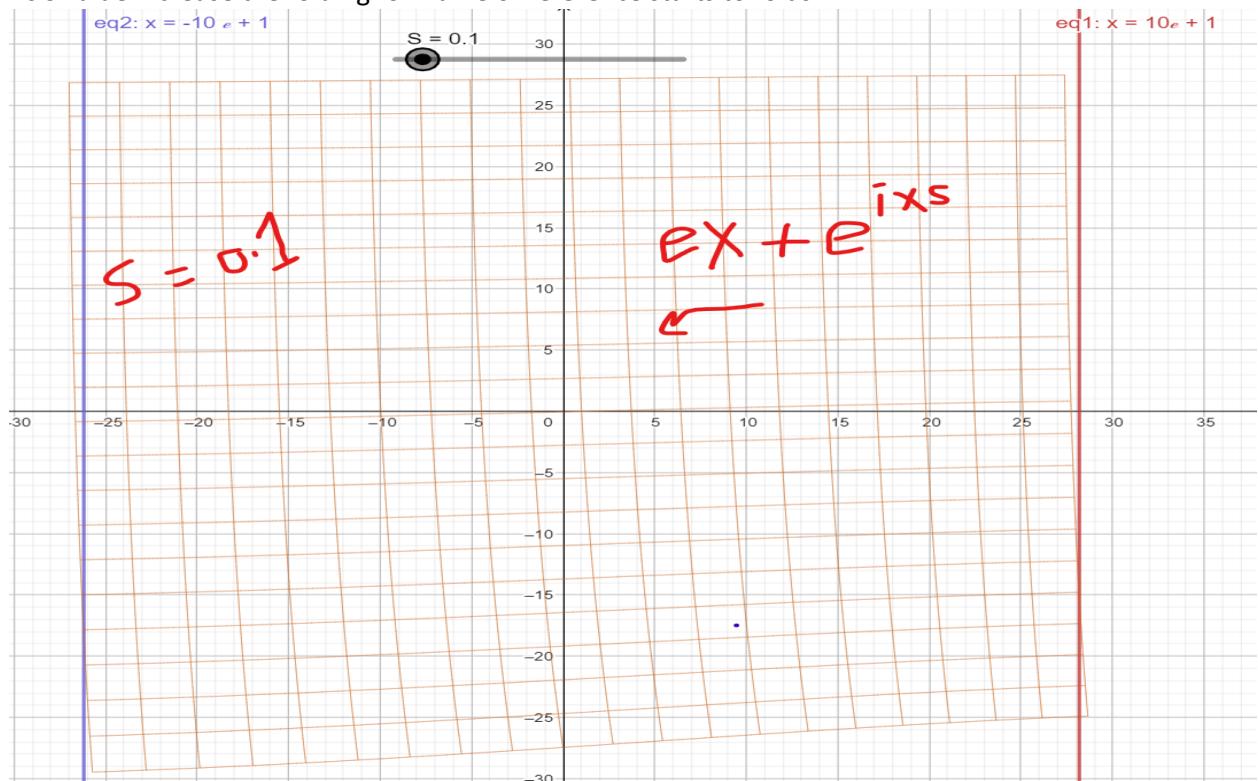


$$21- (i * e * x + 1 = e * x + e^{i*x*0});$$



$$22- (e * x + e^{i*x*S}); S = 0.1$$

As S value increase the folding for frame of reference starts to folds

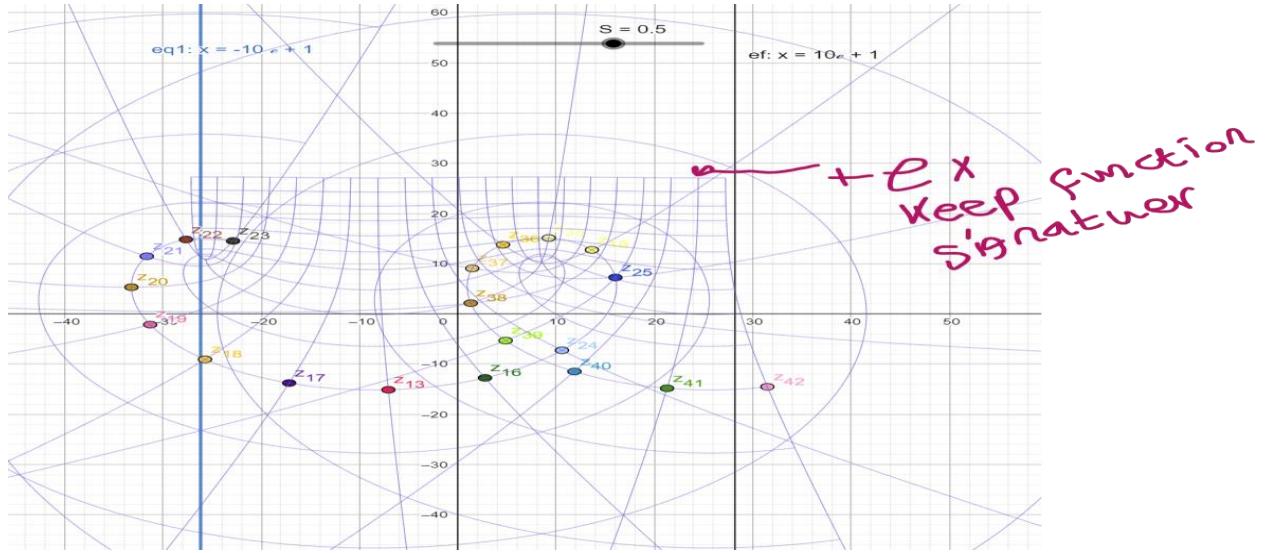


$$23- (-e * x + e^{-(i*x*S-e)}); S = 0.5$$

First Fold at S = 0.5

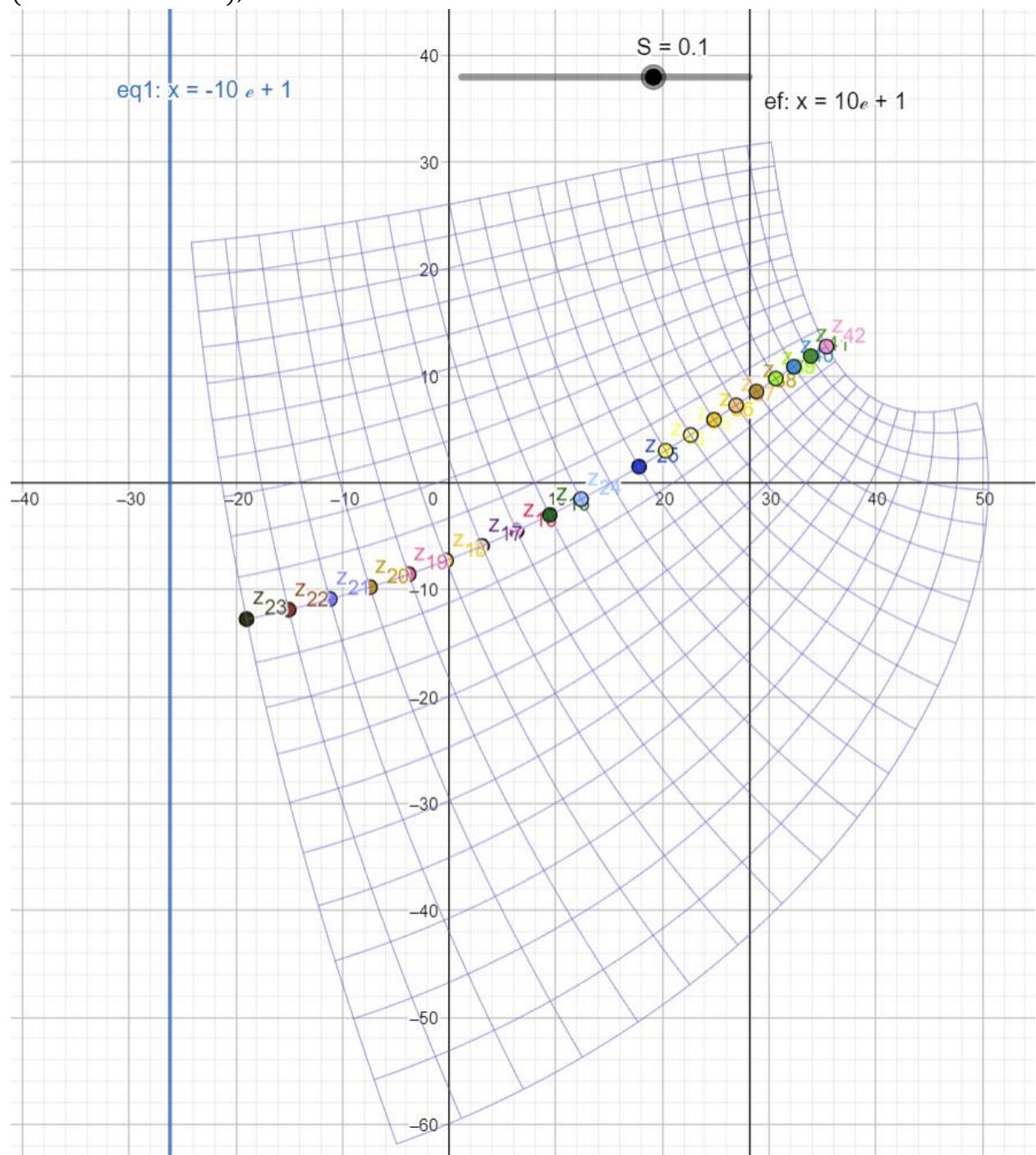
$$e = \cos(-i) + i \sin(-i)$$

Adding  $[-e x]$  and in the same time moving forward or backwards, is doing normalizing using  $1/e$  for the transformation back to the normal frame of reference . so, half frame of reference looks the same

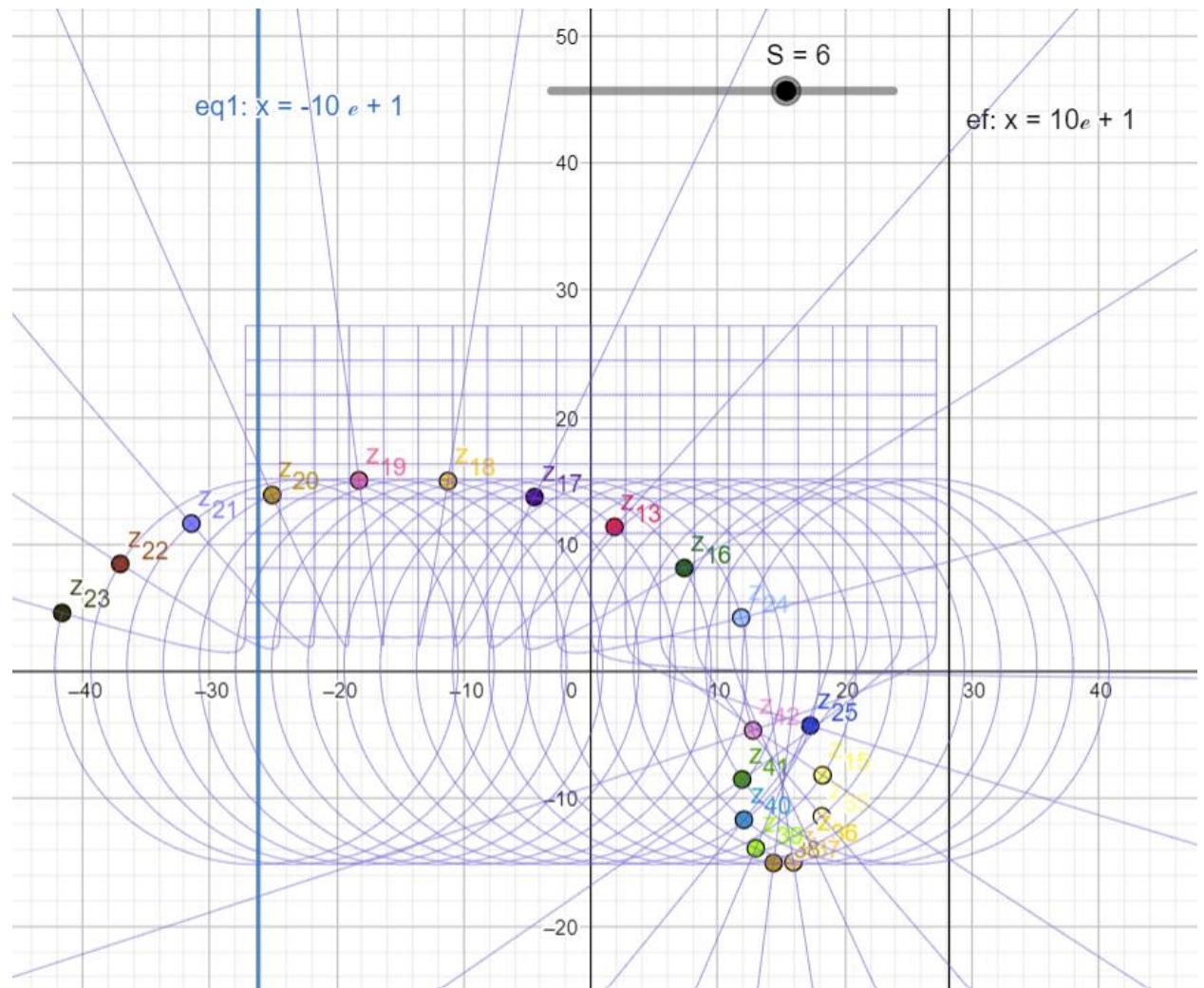


	$eq(x) = -e x + e^{-(xSi-e)}$	⋮		$z_{25} = e + e^{Si+e}$	⋮
	$z_{13} = -3 e + e^{-(3Si-e)}$ → $-7.0828753810764 - 15.1163006115587i$	⋮		$z_{15} = 2 e + e^{2Si+e}$ → $13.6244464897198 + 12.7518719723747i$	⋮
	$z_{16} = -2 e + e^{-(2Si-e)}$ → $2.7513191758836 - 12.7518719723747i$	⋮		$z_{35} = 3 e + e^{3Si+e}$ → $9.2268155896779 + 15.1163006115587i$	⋮
	$z_{17} = -4 e + e^{-(4Si-e)}$ → $-17.1795256058336 - 13.7797316616187i$	⋮		$z_{36} = 4 e + e^{4Si+e}$ → $4.5667290218388 + 13.7797316616187i$	⋮
	$z_{18} = -5 e + e^{-(5Si-e)}$ → $-25.7321495853803 - 9.0694038159717i$	⋮		$z_{37} = 5 e + e^{5Si+e}$ → $1.4506686992101 + 9.0694038159717i$	⋮
	$z_{19} = -6 e + e^{-(6Si-e)}$ → $-31.3122968813342 - 2.1385696096589i$	⋮		$z_{38} = 6 e + e^{6Si+e}$ → $1.3070850601744 + 2.1385696096589i$	⋮
	$z_{20} = -7 e + e^{-(7Si-e)}$ → $-33.219283016205 + 5.315861022321i$	⋮		$z_{39} = 7 e + e^{7Si+e}$ → $4.8366625822216 - 5.315861022321i$	⋮
	$z_{21} = -8 e + e^{-(8Si-e)}$ → $-31.6517414707096 + 11.4687834789022i$	⋮		$z_{40} = 8 e + e^{8Si+e}$ → $11.8407677846351 - 11.4687834789022i$	⋮
	$z_{22} = -9 e + e^{-(9Si-e)}$ → $-27.6589912801077 + 14.813747752041i$	⋮		$z_{41} = 9 e + e^{9Si+e}$ → $21.2700816321551 - 14.813747752041i$	⋮
	$z_{23} = -10 e + e^{-(10Si-e)}$ → $-22.8841271380896 + 14.5317899279655i$	⋮		$z_{42} = 10 e + e^{10Si+e}$ → $31.4815094310913 - 14.5317899279655i$	⋮
	$z_{24} = -1 e + e^{-(1Si-e)}$ → $10.5808344529769 - 7.2653403372705i$	⋮			⋮

$$24- (-e * x + e^{-(i*x*S-e)}); \ S = 0.1$$



25-  $(-e * x + e^{-(i*x*S-e)})$ ; S = 6 First Synchronization visual point between all events



26-  $(-e * x + e^{-(i*x*S-e)})$ ;  $S = 6.285$  First Synchronization point between all numbers  
 after this point the sign will be reversed and this what cause sign change in i  
 Which also can be calculated

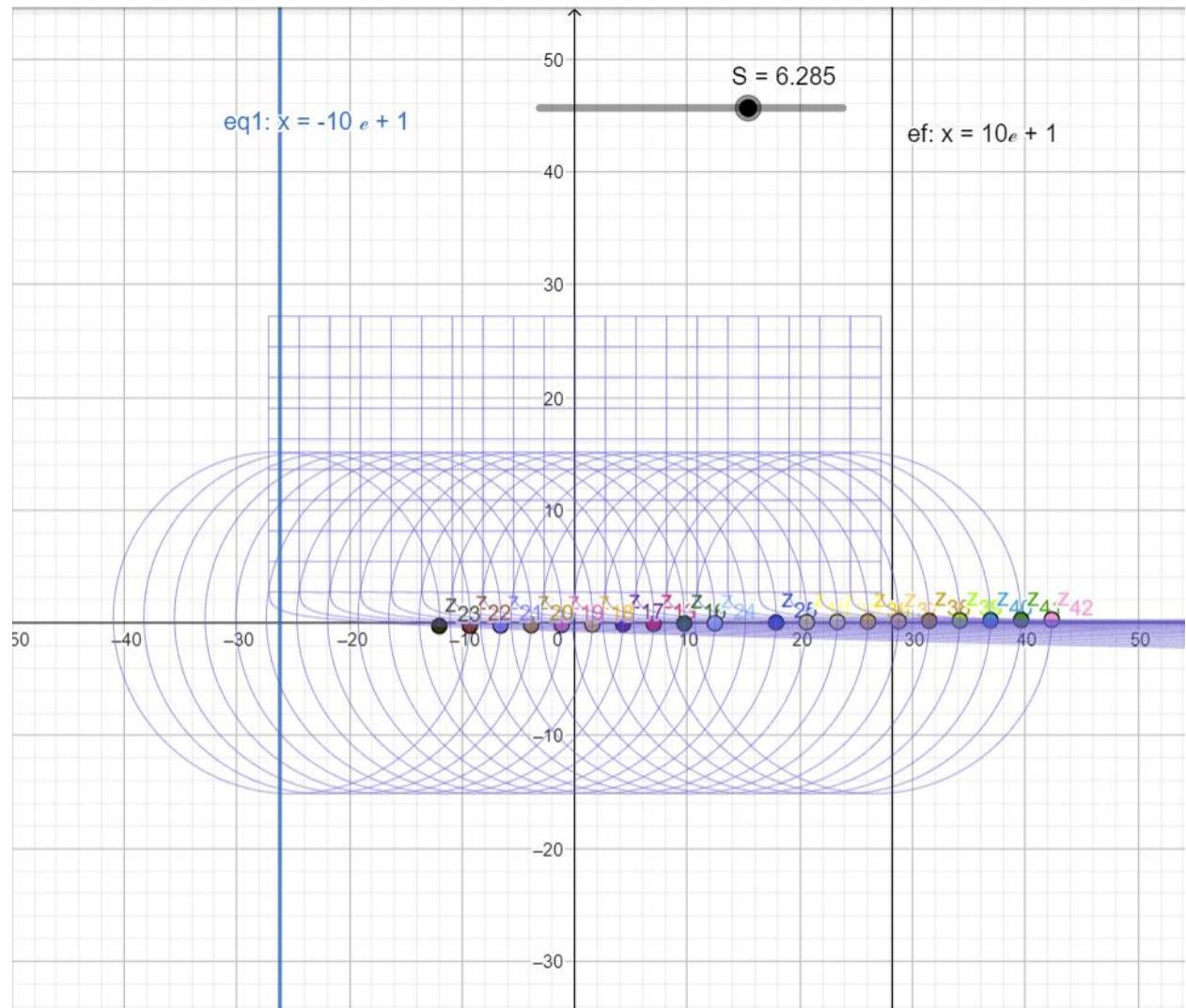
$$e^i = 0.5403023058681 + 0.8414709848079i$$

$$c = \frac{360}{57.295779513085} \quad \vdots$$

$$\rightarrow 6.2831853071793$$

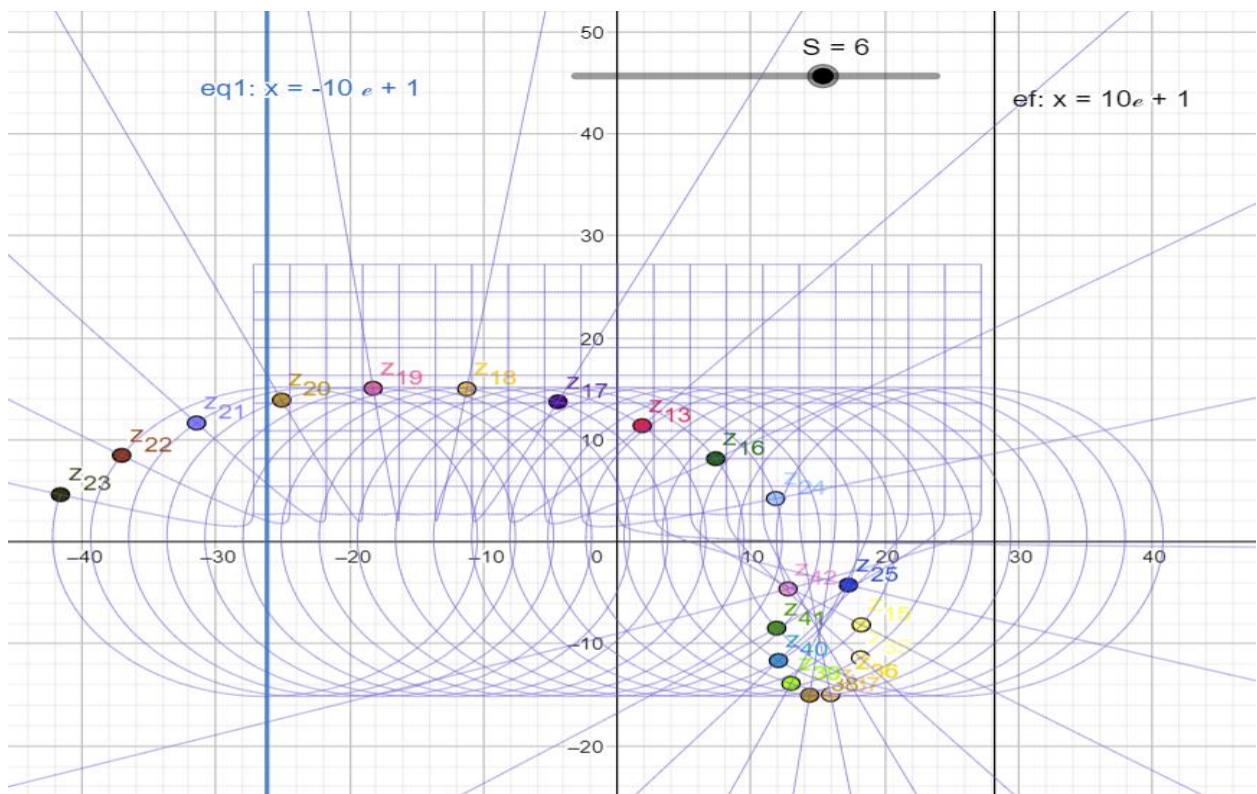
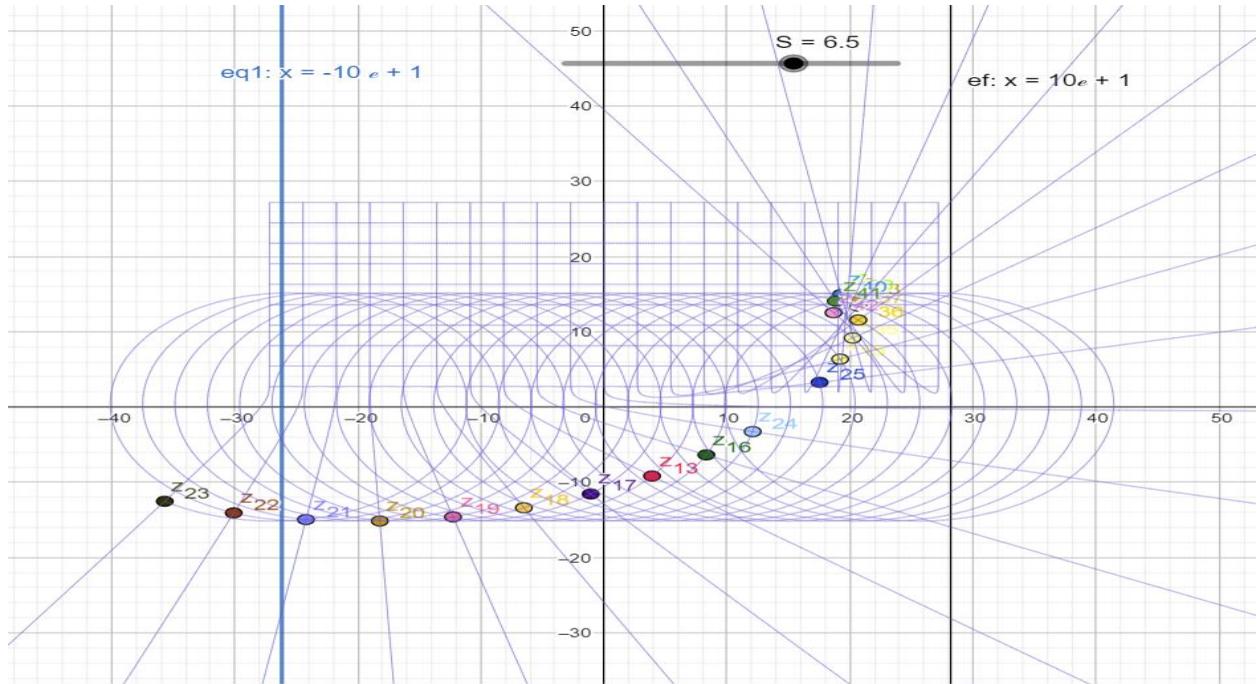
$$\alpha = \cos^{-1}(0.5403023058681) \quad \vdots$$

$$\rightarrow 57.295779513085^\circ$$

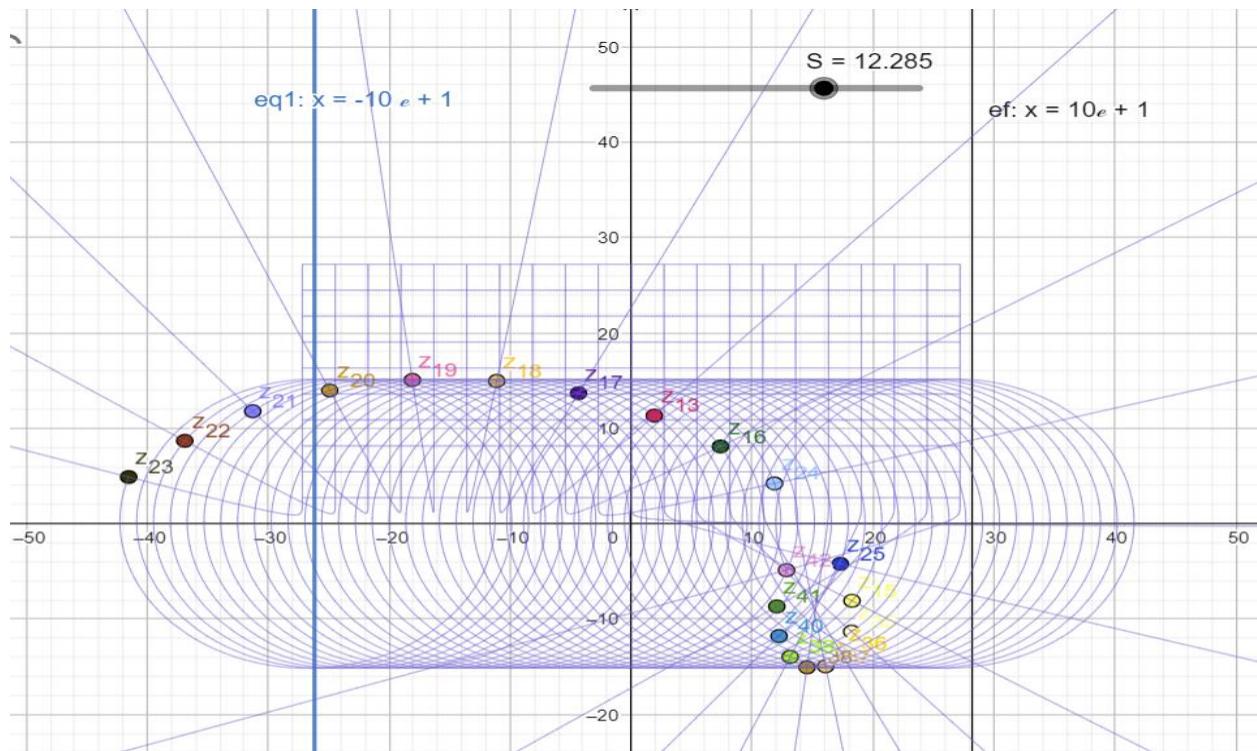


23 – Flipping Signs at [S] approximate to 6.5

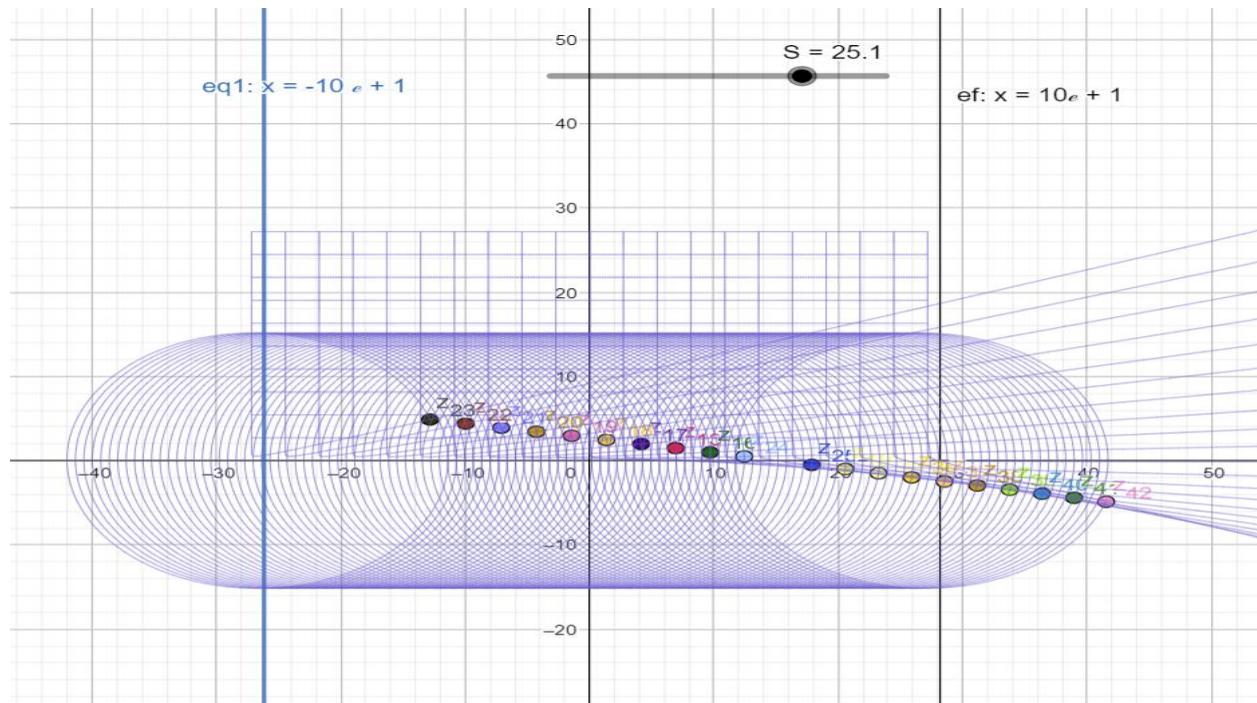
$(-e * x + e^{-(i*x*S-e)})$ ;  $S = 6.5$  Sign opposite of the sign at  $S = 6$



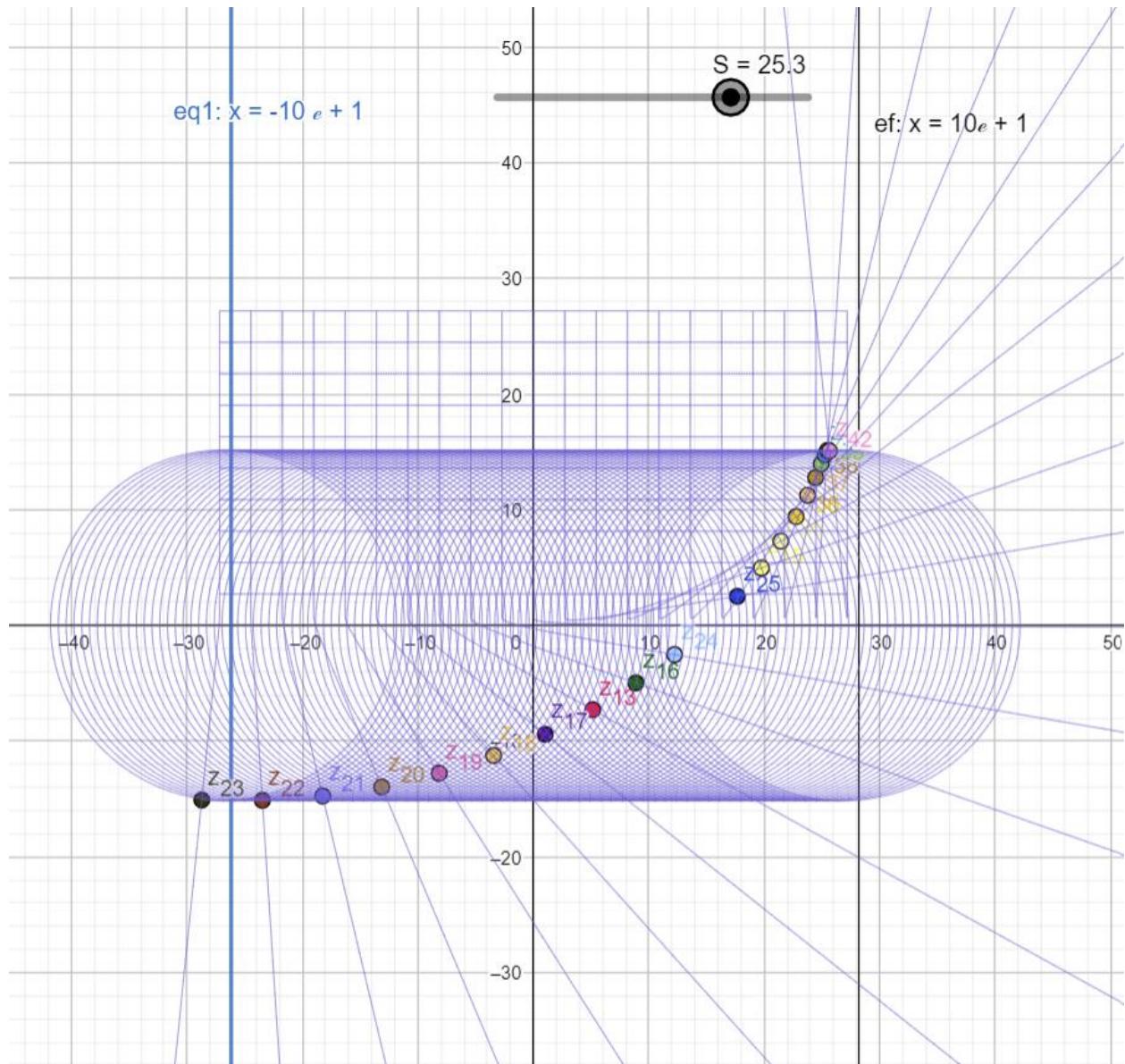
$24 - (-e * x + e^{-(i*x*S-e)})$ ;  $S = 12.285$  Second Synchronization point between all numbers



$25 - (-e * x + e^{-(i*x*S-e)})$ ;  $S > 25.1$  third Synchronization Flip point between all numbers

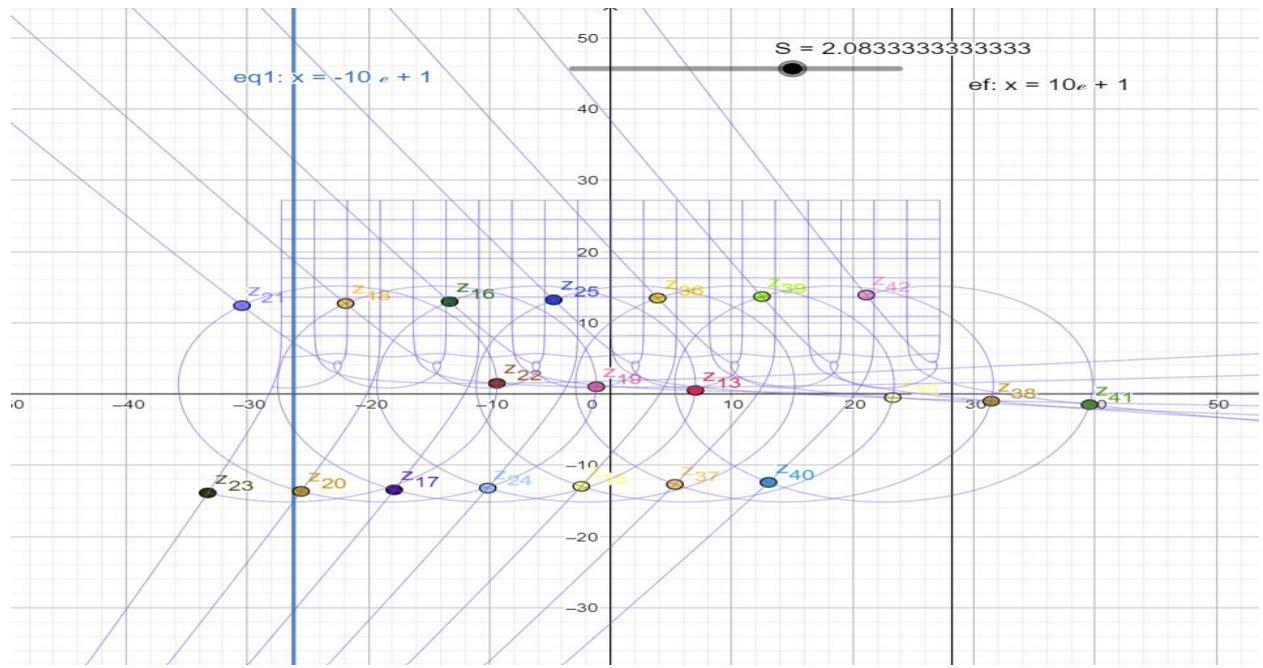


$25 - (-e * x + e^{-(i*x*S-e)})$ ;  $S = 25.3$  third Synchronization point between all numbers

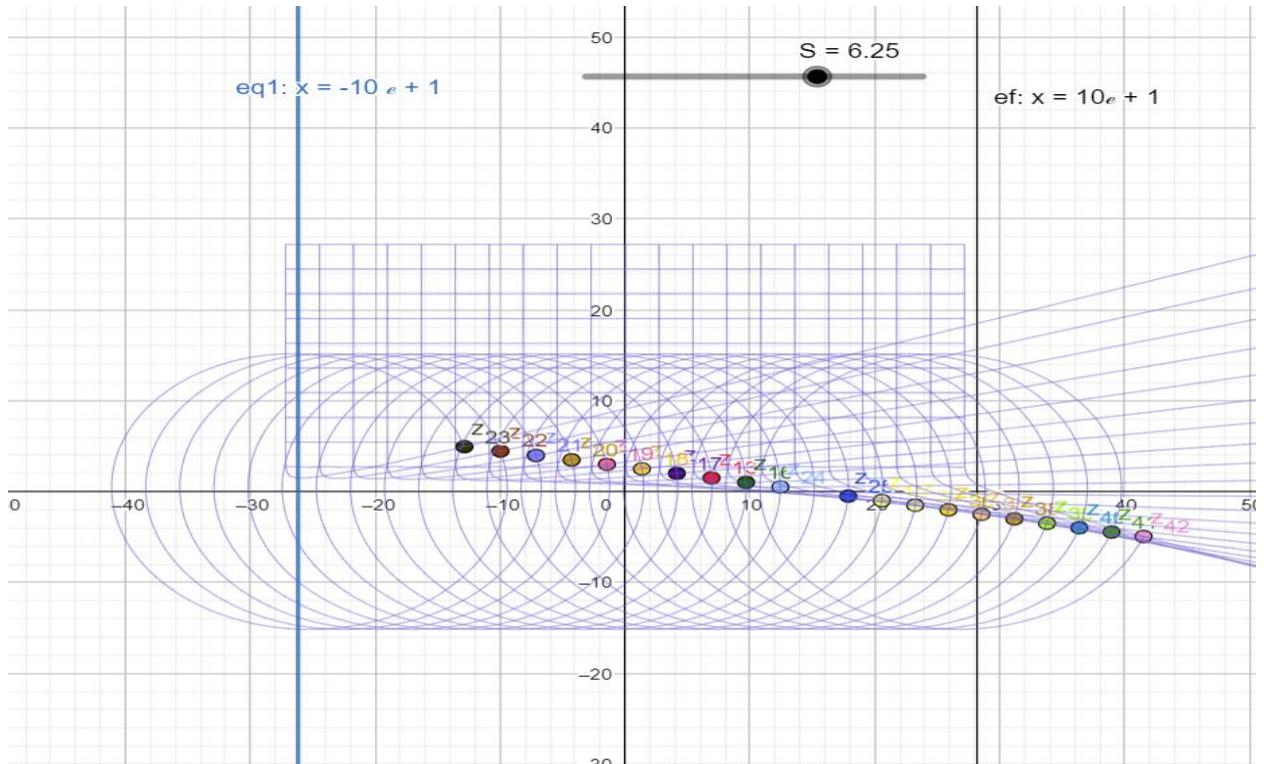


## 26 – Synchronization formula (with Seed 12.5)

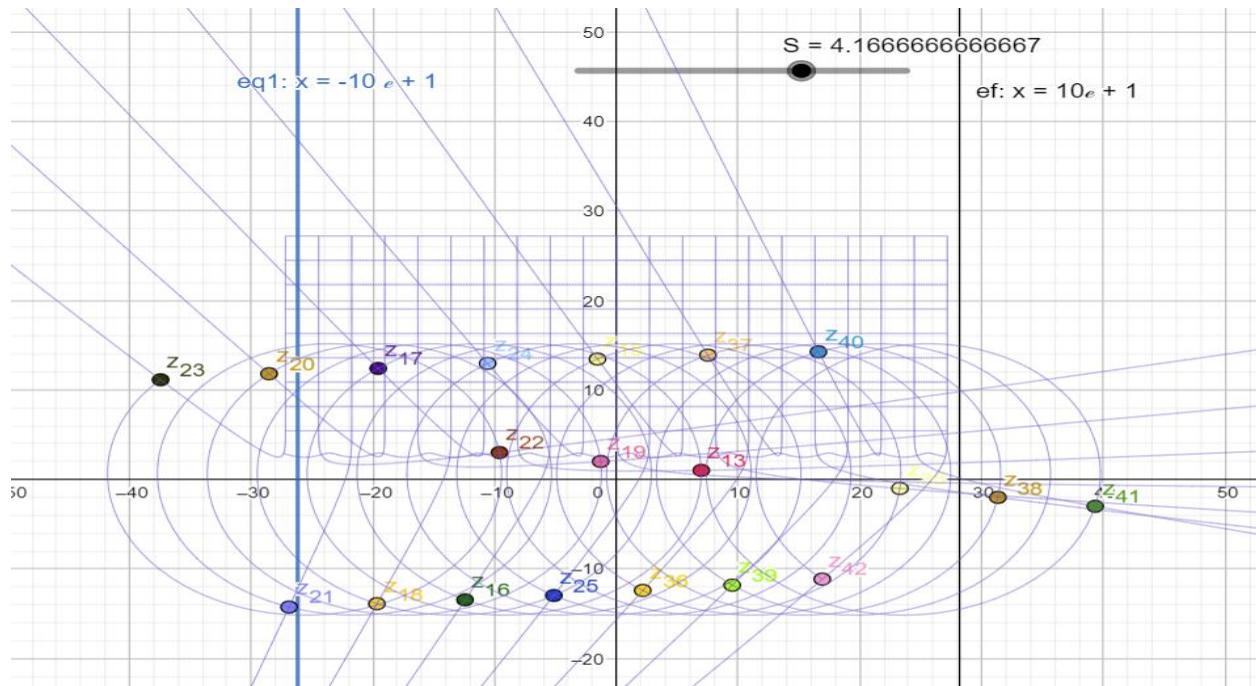
$$(-e * x + e^{-(i*x*S-e)}); \quad S = \frac{12.5}{6} = 2 + \frac{1}{12} = 2.083333333333333$$



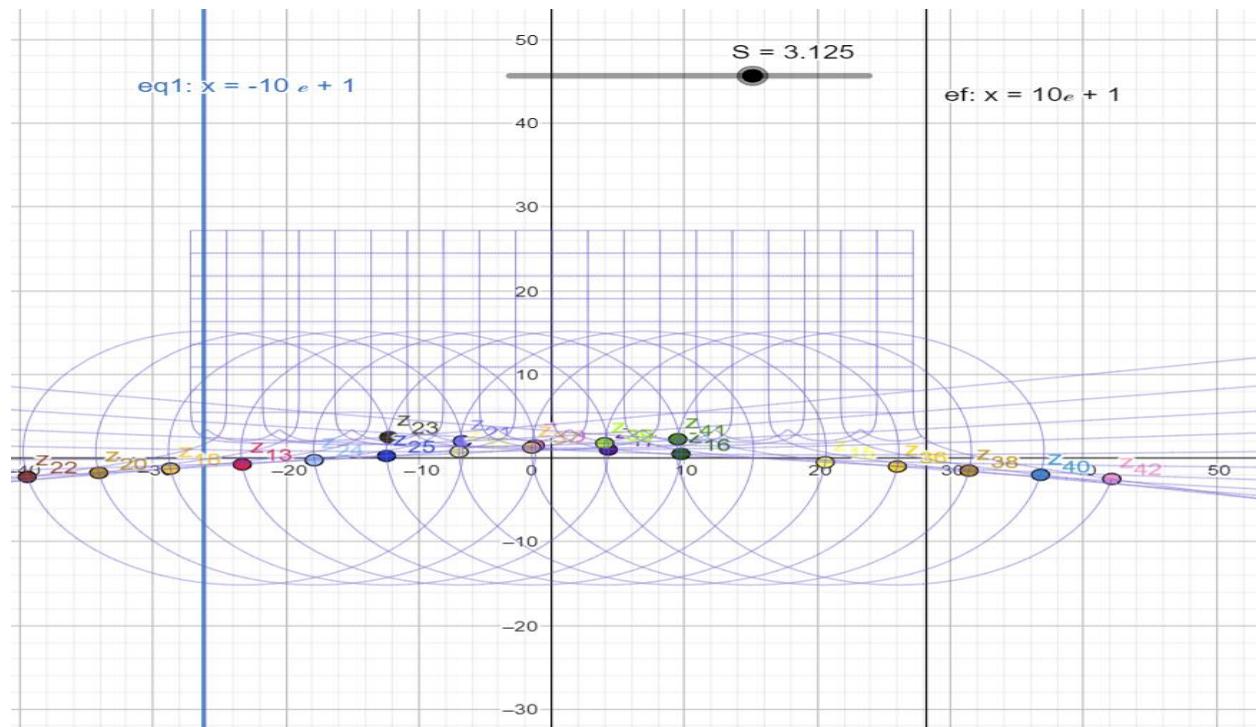
$$(-e * x + e^{-(i*x*S-e)}); \quad S = \frac{12.5}{2} = 6 + \frac{1}{4} = 6.25$$



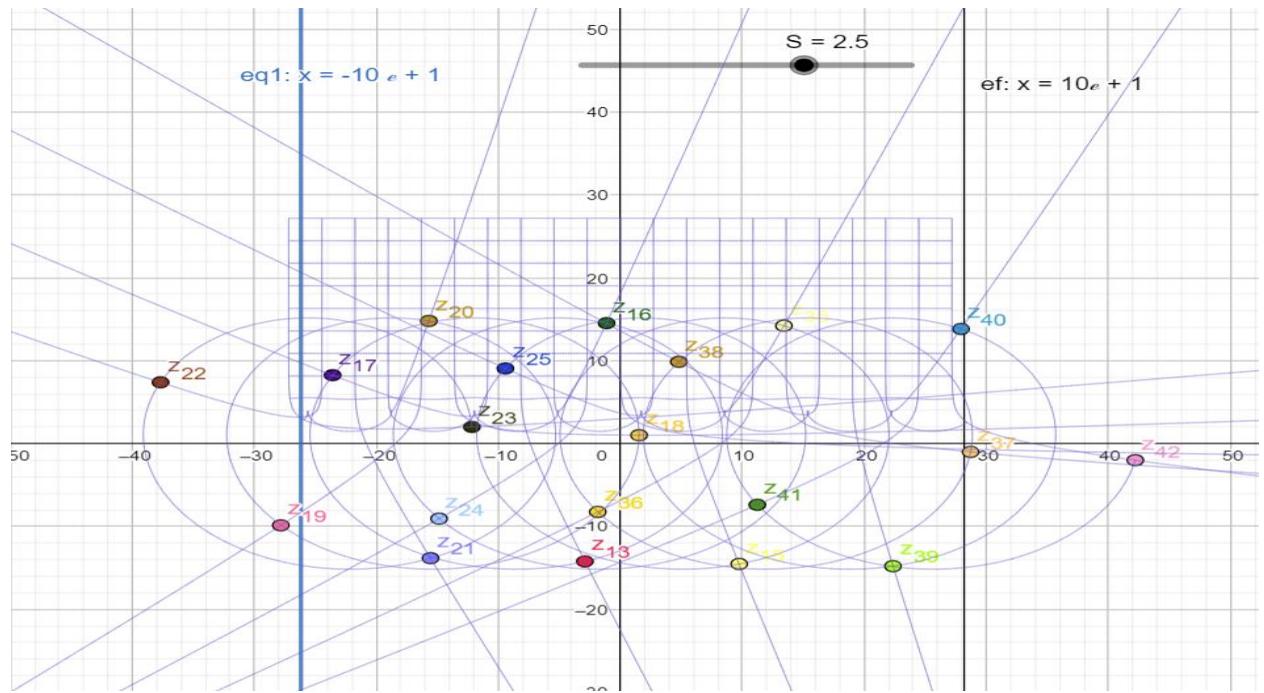
$$(-e * x + e^{-(i*x*S-e)}); \quad S = \frac{12.5}{3} = 4 + \frac{1}{6} = 4.1666666666667$$



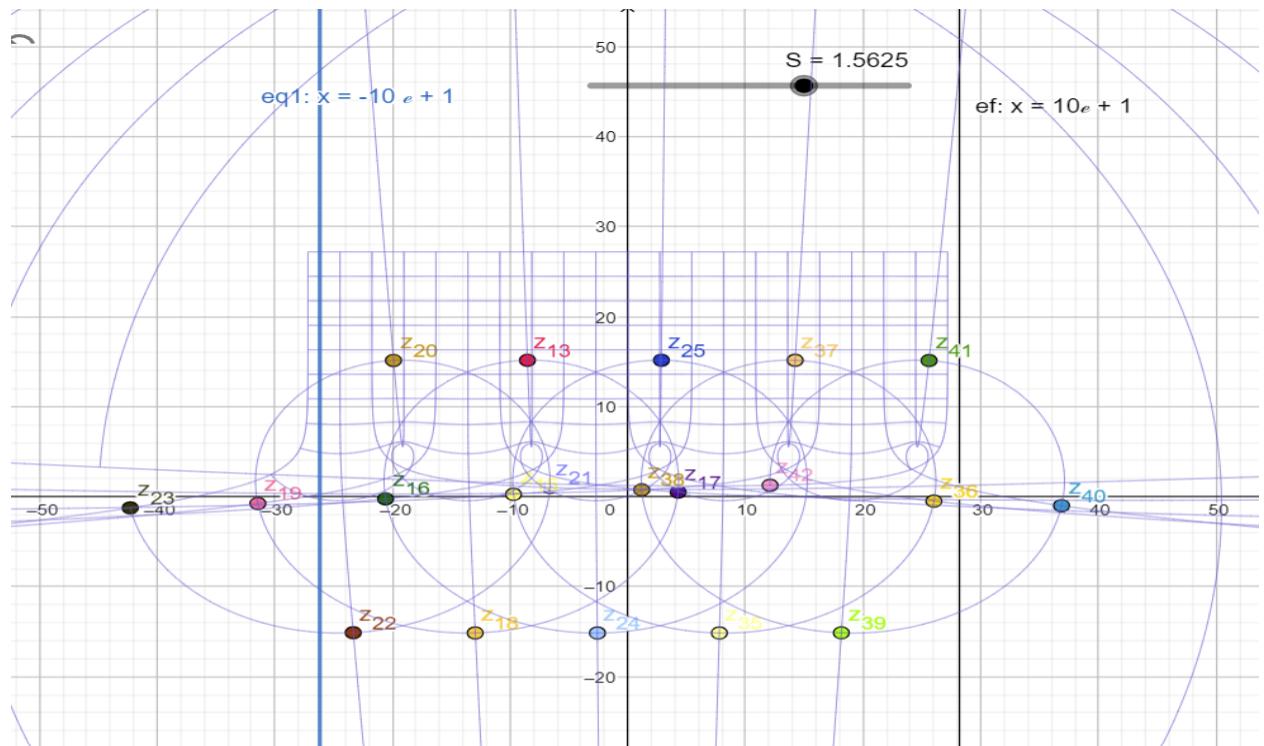
$$(-e * x + e^{-(i*x*S-e)}); \quad S = \frac{12.5}{4} = 3 + \frac{1}{8} = 3.125$$



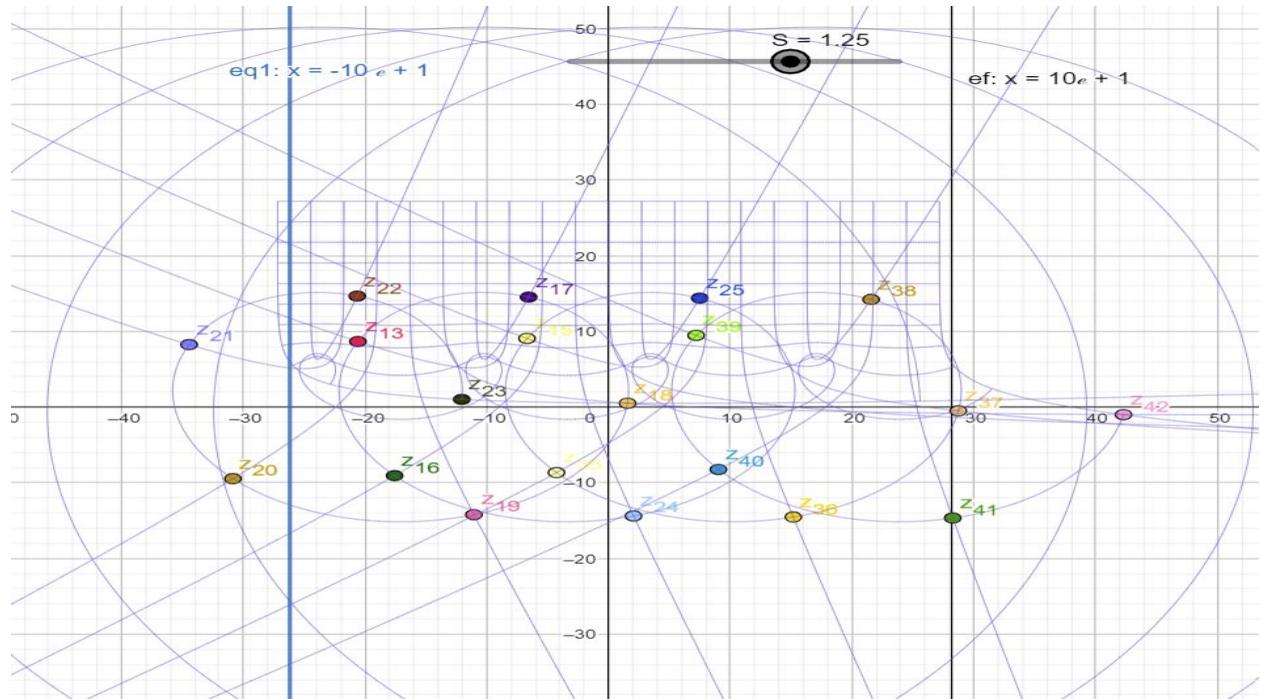
$$(-e * x + e^{-(i*x*s-e)}); \quad S = \frac{12.5}{5} = 2 + \frac{1}{2} = 2.5$$



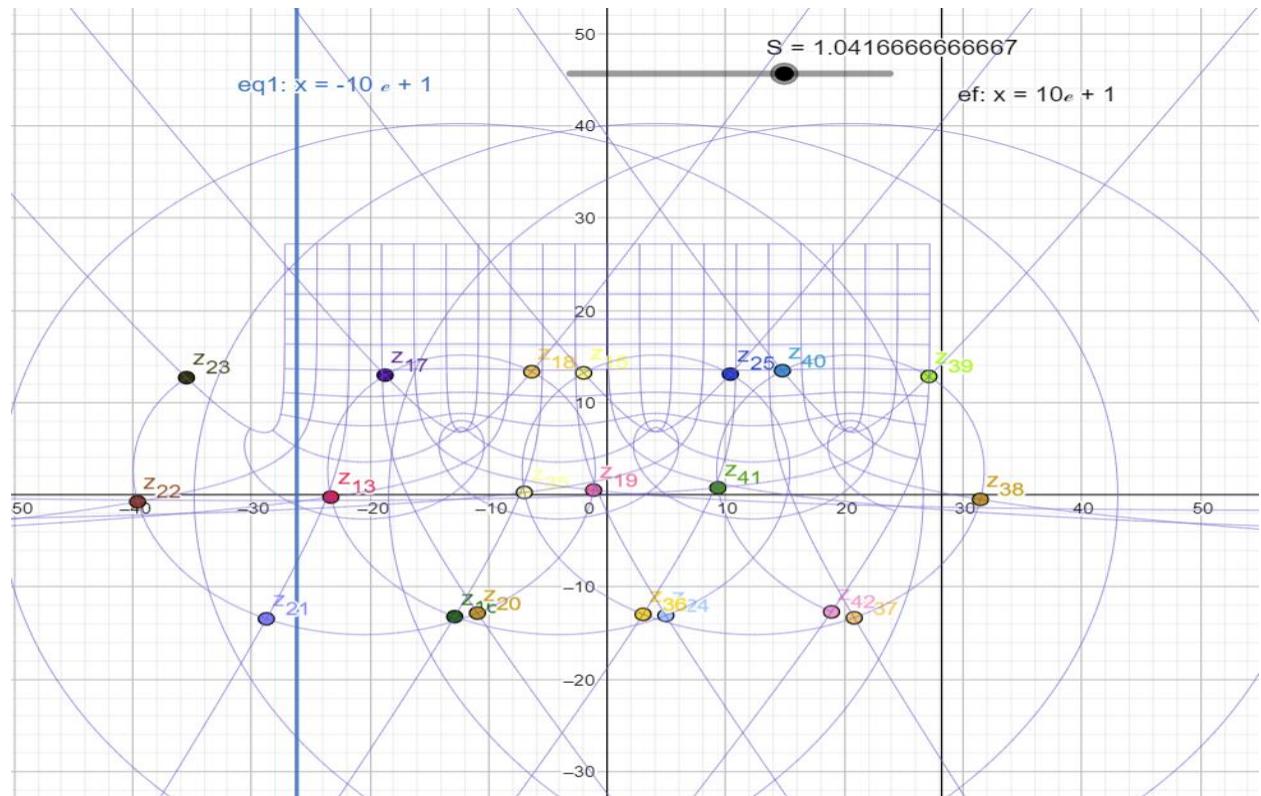
$$(-e * x + e^{-(i*x*s-e)}); \quad S = \frac{12.5}{8} = 1 + \frac{1}{2} + \frac{1}{16} = 1.5625$$



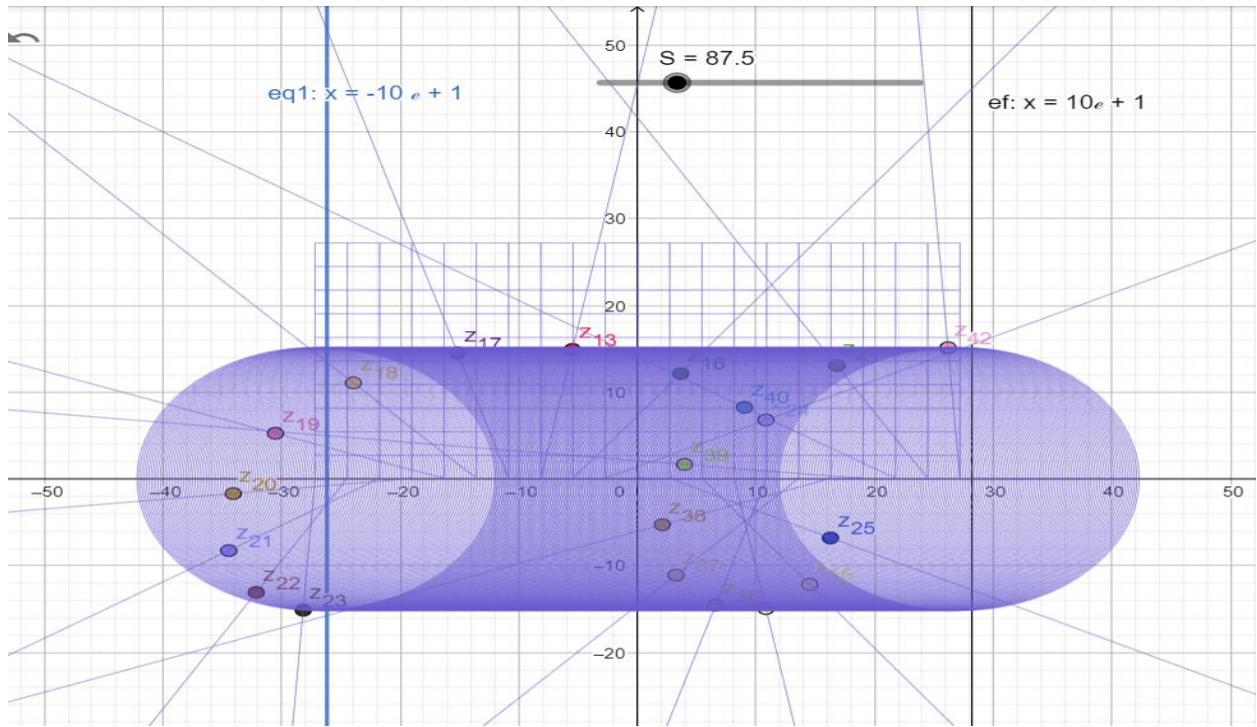
$$(-e * x + e^{-(i*x*S-e)}); S = \frac{12.5}{10} = 1 + \frac{1}{4} = 1.25$$



$$(-e * x + e^{-(i*x*S-e)}); S = \frac{12.5}{12} = 1 + \frac{1}{24} = 1.04166666667$$



$$S = 12.5 * \text{Odd number} = \text{Odd number} + 0.5$$



### 3. Results

In This paper we studied the power function first in a small field  $\varphi(i)$ ; a filed that includes mainly the imaginary number  $[i]$ .during this step we got through the complex plane imaginary axis is a projection for the square roots of all natural numbers. Then we increased our field domain for the power function to include  $[e]$  and studied the new field  $\varphi(i, e)$ . We also got through some number distributions using complex numbers and complex plane.

Then we increased our field domain for the power function again to include  $[\pi]$  and studied the new field  $\varphi(i, e, \pi)$ . Using these fields breakdown, we proofed Riemann hypothesis that says, all none-trivial zeros for Zeta function will have only imaginary part at the stripe line at [0.5].

### References

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Mathematics for Machine Learning: Linear Algebra; by Imperial College London; Taught by: David Dye, Professor of Metallurgy Department of Materials

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