



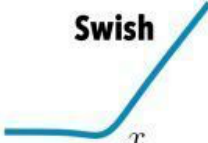




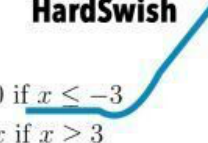
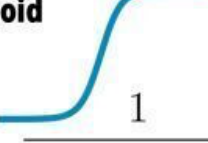
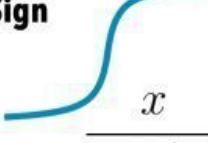

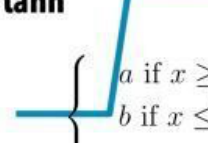
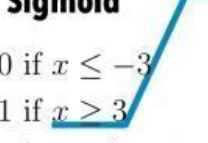

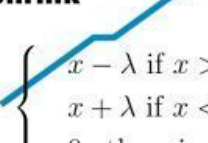
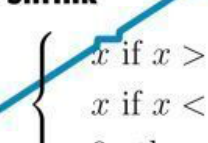


Neural Network Activation Functions: a small subset!

ReLU  $\max(0, x)$	GELU  $\frac{x}{2} \left(1 + \tanh \left(\sqrt{\frac{2}{\pi}} (x + ax^3) \right) \right)$	PReLU  $\max(0, x)$
ELU  $\begin{cases} x & \text{if } x > 0 \\ \alpha(x \exp x - 1) & \text{if } x < 0 \end{cases}$	Swish  $\frac{x}{1 + \exp -x}$	SELU  $\alpha(\max(0, x) + \min(0, \beta(\exp x - 1)))$
SoftPlus  $\frac{1}{\beta} \log(1 + \exp(\beta x))$	Mish  $x \tanh \left(\frac{1}{\beta} \log(1 + \exp(\beta x)) \right)$	RReLU  $\begin{cases} x & \text{if } x \geq 0 \\ ax & \text{if } x < 0 \text{ with } a \sim \mathcal{R}(l, u) \end{cases}$
HardSwish  $\begin{cases} 0 & \text{if } x \leq -3 \\ x & \text{if } x \geq 3 \\ x(x+3)/6 & \text{otherwise} \end{cases}$	Sigmoid  $\frac{1}{1 + \exp(-x)}$	SoftSign  $\frac{x}{1 + x }$
Tanh  $\tanh(x)$	Hard tanh  $\begin{cases} a & \text{if } x \geq a \\ b & \text{if } x \leq b \\ x & \text{otherwise} \end{cases}$	Hard Sigmoid  $\begin{cases} 0 & \text{if } x \leq -3 \\ 1 & \text{if } x \geq 3 \\ x/6 + 1/2 & \text{otherwise} \end{cases}$
Tanh Shrink  $x - \tanh(x)$	Soft Shrink  $\begin{cases} x - \lambda & \text{if } x > \lambda \\ x + \lambda & \text{if } x < -\lambda \\ 0 & \text{otherwise} \end{cases}$	Hard Shrink  $\begin{cases} x & \text{if } x > \lambda \\ x & \text{if } x < -\lambda \\ 0 & \text{otherwise} \end{cases}$

Neural Network Activation Functions:

1 ReLU (Rectified Linear Unit):

Formula: $f(x) = \max(0, x)$

Pros: Simple, computationally efficient, helps mitigate the vanishing gradient problem.

Cons: Can lead to "dying ReLUs" where neurons become inactive and stop learning.

2 GELU (Gaussian Error Linear Unit):

Formula: $f(x) = x * P(X \leq x)$, where P is the cumulative distribution function of the standard normal distribution.

Pros: Smooth, differentiable, combines properties of ReLU and dropout, improves performance in NLP tasks.

Cons: Computationally more intensive compared to ReLU.

3 Sigmoid:

Formula: $f(x) = 1 / (1 + \exp(-x))$

Pros: Outputs probabilities, useful for binary classification.

Cons: Prone to vanishing gradient problem, slow convergence.

4 Tanh (Hyperbolic Tangent):

Formula: $f(x) = (\exp(x) - \exp(-x)) / (\exp(x) + \exp(-x))$

Pros: Zero-centered, less likely to saturate than sigmoid.

Cons: Still suffers from vanishing gradients, slower training.

5 Leaky ReLU:

Formula: $f(x) = x$ if $x > 0$ else $\alpha * x$

Pros: Addresses the "dying ReLU" problem, allows a small gradient when inactive.

Cons: Introduces a small negative slope, which may not always be optimal.

6 ELU (Exponential Linear Unit):

Formula: $f(x) = x$ if $x > 0$ else $\alpha * (\exp(x) - 1)$

Pros: Smooth, reduces the bias shift by pushing mean activations closer to zero.

Cons: More computationally intensive than ReLU, introduces an additional hyperparameter.

7 Swish:

Formula: $f(x) = x / (1 + \exp(-x))$

Pros: Smooth, differentiable, improves performance in deep networks.

Cons: More computationally intensive than ReLU.

8 Softplus:

Formula: $f(x) = \log(1 + \exp(x))$

Pros: Smooth, always positive, avoids the problem of zero gradients.

Cons: Computationally intensive, can lead to vanishing gradients for large negative inputs.

Choosing the right activation function can significantly impact your model's performance.