Educational Worksheet

Answer Key: Organizing and Presenting Data

Grade 7 Mathematics - Hard Difficulty

Total Marks: 100

Section A: Theoretical Understanding

1. Data Representation Theory (7 marks)

<u>a) Why pie chart over histogram (3 marks):</u> - Pie charts show parts of a whole/categorical data ✓ - Histogram shows frequency distribution of continuous data ✓ - Subject preferences are categorical, not continuous measurements ✓

b) Pie chart angles (4 marks): - Mathematics: $(125/500) \times 360^{\circ} = 90^{\circ}$ ✓ - Science: $(100/500) \times 360^{\circ} = 72^{\circ}$ ✓ - English: $(75/500) \times 360^{\circ} = 54^{\circ}$ ✓ - History: $(50/500) \times 360^{\circ} = 36^{\circ}$ ✓ - Art: $(75/500) \times 360^{\circ} = 54^{\circ}$ ✓ - PE: $(75/500) \times 360^{\circ} = 54^{\circ}$ ✓ (Total should equal 360°)

2. Waffle Diagram Analysis (4 marks)

<u>a) Percentages (2 marks):</u> - Excellent: 23% ✓ - Good: 45% ✓ - Satisfactory: 27% ✓ - Needs Improvement: 5% ✓

b) Advantage of waffle diagram (2 marks): Accept any valid advantage such as: - Easier to read exact percentages ✓ - Better for audiences who struggle with angles ✓ - More intuitive visual representation ✓

Section B: Data Interpretation Puzzles

3. Scatter Diagram Mystery (5 marks)

a) Explanation for contradiction (3 marks): Accept reasonable explanations such as: - Different

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b) Additional data question (2 marks): Accept relevant questions such as: - "What study methods did you use?" ✓ - "How many hours of sleep did you get?" ✓ - "Did you have any distractions while studying?" ✓

4. Histogram Frequency Puzzle (8 marks)

a) Correct drawing analysis (4 marks): - Bar height should be proportional to frequency \checkmark - 155-159 cm has frequency 12, 150-154 cm has frequency 8 \checkmark - Ratio should be 12:8 = 1.5:1 \checkmark - The histogram IS correctly drawn \checkmark

<u>b) Symmetric distribution frequencies (4 marks):</u> If symmetric with total 40: - Possible pattern: 4, 8, 12, 12, $4 \checkmark \checkmark$ - Or: 2, 8, 20, 8, $2 \checkmark \checkmark$ - Must show working and total = $40 \checkmark \checkmark$

Section C: Complex Problem Solving

5. Multi-representation Challenge (10 marks)

<u>a) Calculations (4 marks): Pie chart angles:</u> - Car: $(96/240) \times 360^{\circ} = 144^{\circ}$ ✓ - Public Transport: $(72/240) \times 360^{\circ} = 108^{\circ}$ ✓ - Walking: $(48/240) \times 360^{\circ} = 72^{\circ}$ ✓ - Cycling: $(24/240) \times 360^{\circ} = 36^{\circ}$ ✓

Waffle diagram: - Car: 40 squares, Public Transport: 30 squares ✓ - Walking: 20 squares, Cycling: 10 squares ✓

<u>b) Audience-appropriate representations (6 marks):</u> - <u>City planners</u>: Bar chart or histogram for clear comparison of usage numbers ✓ ✓ - <u>Environmental activists</u>: Pie chart to emphasize proportion using cars vs. eco-friendly options ✓ ✓ - <u>School children</u>: Waffle diagram for easy visual understanding ✓ ✓

6. Data Detective (6 marks)

a) Error identification (4 marks): - Check pie chart: $90^{\circ} + 135^{\circ} + 90^{\circ} + 45^{\circ} = 360^{\circ} \checkmark$ - Check percentages: $25\% + 37.5\% + 25\% + 12.5\% = 100\% \checkmark$ - Check bar chart with table: If total = 80, then A should be 20, B should be 30, C should be 20, D should be $10 \checkmark$ - ERROR in table: Shows A=25% of $80 = 20 \checkmark$ but percentages don't match frequencies

<u>b) Correction (2 marks):</u> - Correct frequencies: A=20, B=30, C=20, D=10 (total=80) ✓ - Correct percentages: A=25%, B=37.5%, C=25%, D=12.5% ✓

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7. Scatter Diagram Construction (6 marks)

- <u>a) Correlation prediction (3 marks):</u> Strong positive correlation expected \checkmark As temperature increases, ice cream sales increase \checkmark Logical reasoning based on real-world experience \checkmark
- <u>b) Sales estimation for 26°C (3 marks):</u> Method: interpolation between 25°C (75 units) and 28°C (88 units) ✓ Calculation: approximately 79-82 units ✓ Justification of interpolation method ✓

8. Histogram Intervals Decision (8 marks)

<u>a) Interval comparison (4 marks):</u> 5% intervals: - Advantages: More detailed view, better for large datasets ✓ - Disadvantages: Too many bars, harder to see overall pattern ✓

<u>10% intervals:</u> - Advantages: Clearer overall pattern, easier to read ✓ - Disadvantages: Less detail, might miss important features ✓

b) Recommendation (4 marks): - Recommend 10% or 20% intervals ✓ - Reasoning: Current data naturally clusters in these ranges ✓ - Suggested intervals: 20-39%, 40-59%, 60-79%, 80-89%, 90%+ ✓ - Justification based on data distribution ✓

9. Critical Analysis (6 marks)

- <u>a) Missing information (3 marks):</u> Accept any three of: Sample size ✓ Comparison data (before/after) ✓ Response rate ✓ How satisfaction was measured ✓ Time period of survey ✓ Demographics of respondents ✓
- b) Better evidence suggestions (3 marks): Scatter diagram: Customer satisfaction vs. time since product launch ✓ Histogram: Distribution of satisfaction scores over time ✓ Show trend data rather than single snapshot ✓

10. Data Transformation Challenge (6 marks)

- <u>a) Pie chart calculations (3 marks):</u> Total frequency = 50 ✓ Angles: 0-19: 21.6° , 20-39: 50.4° , 40-59: 108° , 60-79: 144° , 80-100: 36° ✓ Show working: (frequency/total) × 360° ✓
- <u>b) Waffle diagram challenges (3 marks):</u> Challenge: 50 total doesn't divide evenly into 100 squares
 ✓ Modification: Use 50 squares (each = 1 student) or multiply all by 2 ✓ Alternative: Use percentages and round to nearest whole square ✓

Teaching Notes

Common Mistakes to Watch For:

- Pie chart calculations: Students often forget to multiply by 360° or use wrong total
- <u>Correlation confusion</u>: Assuming correlation implies causation
- **<u>Histogram vs. bar chart</u>**: Using gaps when data is continuous
- Scale misunderstanding: Not considering sample size when interpreting percentages

Extension Activities:

- Real data collection: Have students survey classmates and create multiple representations
- Media analysis: Find examples of misleading data presentations in newspapers/online
- <u>Technology integration</u>: Use spreadsheet software to create different chart types
- Cross-curricular connections: Apply to science experiments or social studies surveys

Assessment Criteria:

- Excellent (90-100 marks): Demonstrates deep understanding of when and why to use different representations, shows sophisticated reasoning, makes connections between concepts
- <u>Good (75-89 marks)</u>: Shows solid understanding with minor gaps, can solve most problems with appropriate methods
- <u>Satisfactory (60-74 marks)</u>: Basic understanding of data representations, can complete routine calculations with some support
- Needs Support (<60 marks): Requires significant support with concept understanding and application

Differentiation Strategies:

• For struggling learners: Provide step-by-step templates for calculations
• <u>Visual learners</u> : Use actual manipulatives or online interactive tools
• Kinesthetic learners: Have them physically sort data or create human bar charts
This answer key corresponds to: organizing-presenting-data.md
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