

Enrollment No: \_\_\_\_\_

**FACULTY OF ENGINEERING**

**B.E. Sem - Mid Semester Examination Summer 2025**

**Subject Name: Mathematics-II**

**Subject Code: 2010200201**

**Date: 01/4/25**

**Time: 10:00 am to 11:30 am**

**Total Marks: 40**

**Instructions:**

1. Attempt any **FOUR** questions out of **FIVE** questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.

**Q.1 Answer the following.**

- (A) Find  $L(e^{-3t}t^4)$
- (B) Solve:  $y^{iv} - y = 0$
- (C) Solve:  $Y''' - 5Y'' + 6Y = e^{4x}$

$$L\{D^2 y\} = s^2 L\{y\} - s(y') - y(0)$$

$$L\{D y\} = s L\{y\} - y(0)$$

$$= s L\{y\} - y(0)$$

**Q.2 Answer the following.**

- (A) State convolution theorem for Laplace Transform (2)
- (B) Find  $L^{-1}\left\{\frac{1}{s(s+1)(s+2)}\right\}$  (3)
- (C) Solve  $\frac{d^4 x}{dy^2} + 5x^2 + 6x = e^{-t}$  given  $x(0)=0$  and  $x'(0)=-1$  (5)

**Q.3 Answer the following.**

- (A) Find the order and degree of the differential equation  

$$\left(\frac{d^2 y}{dx^2}\right)^4 = y + \left(\frac{dy}{dx}\right)^2$$
 (2)
- (B) Solve the following differential equation using the method of variation of parameters:  
 $y'' + y = \operatorname{cosec} x$  (3)

- (C) Solve  $y'' + 4y' + 4y = 0$ ,  $y(0)=1$ ,  $y'(0)=1$  (5)

$$s^2 + 4s + 4 = 0$$

$$s^2 + 3s + 2s + 4 = 0$$

$$s(s+3) + 2(s+2) = 0$$

**Q.4 Answer the following.**

- (A) State First Shifting Theorem (2)

(B) Find the Laplace transform of

$$f(t) = \begin{cases} 1 & 0 \leq t \leq a \\ -1 & a \leq t \leq 2a \end{cases} \quad \text{Also } f(t) \text{ is periodic} \quad (3)$$

with period  $2a$ .

(C) Apply Laplace Transform to Solve  $x'' + 9x = \cos 2t$  given  $x(0) = 1$  and  $x(\pi/2) = -1$  (5)

**Q.5 Answer the following.**

(A) Find  $L(\sin 4t)$  (2)

(B) Find Laplace transform of  $f(t) = \begin{cases} 0 & 0 < t < 3 \\ 4 & t \geq 3 \end{cases}$  (3)

(C)  $(x+1)^2 \frac{d^2y}{dx^2} + (x+1) \frac{dy}{dx} + y = 4 \cos(\log(1+x))$  (5)

\*\*\*\*\*Best of Luck\*\*\*\*\*

$\times \frac{0-20}{0-20}$

0 + 20