

Given a positive integer  $n$  and two distinct prime numbers  $p_1$  and  $p_2$ , where  $p_1 < p_2$ , we call the two prime numbers “rhyming primes” with respect to  $n$  if both prime numbers have the same distance to  $n$  (distance means the number of integers in between two numbers), that is if  $n - p_1 = p_2 - n$ . For example, there 3 rhyming prime pairs with respect to  $n = 20$  as (3, 37), (11, 29) and (23, 17).

Develop a Python program to compute the number of rhyming prime pairs for a given positive integer  $n$ . The input to the program is the name of a file that contains several  $n$ , one in each line. The number of rhyming prime pairs for each  $n$  in the input should be output to the screen and to a file named “Output.txt”.

**Special requirement:** You must define at least 2 functions and use them in your code.

**Format:**

Input: input\_file  
(Each line of the input file will contain a positive integer  $n$ )

Output: Display on screen and write to the output file named “Output.txt”, in each line in the output, the number of rhyming prime pairs for each  $n$  in the input.

**Sample:**

Case 1

Input: test\_data1.txt  
Content: 20  
1000

Output: On screen and in output file  
Content: 3  
37