ST301_A1_S19_837

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Introduction to Insurance Claims Dataset

This report provides an overview of an insurance company's annual medical claims made by its customers. The dataset used in this analysis contains information on medical claims filed by customers over a certain period.

The dataset includes variables such as:

- age   : age of the policyholder
- gender   : the policyholder's gender - female,male
- bmi   : body mass index of the policyholder
- num_dependents : number of dependents covered by the health insurance(spouse and children below age 18)
- is_smoker   : smoking status of the policyholder - yes,no
- working_env   : working environment of the policyholder - construction site,factory,office
- tot_claims   : total amount ofclaims made by the policyholder

This report aims to explore and analyze patterns and develop a model to predict tha annual medical claims made by its customers within the data to gain insights into the company's medical claim records.

```r
#Install Packages
# install.packages("performance")
# install.packages("sp")
# install.packages("magrittr")
# install.packages("dplyr")
# install.packages("tinytex")
# install.packages("gridExtra")
# install.packages("MASS")
# install.packages("tidyverse")
# install.packages("corrplot")

library(MASS)
library(tidyverse)

## — Attaching core tidyverse packages ———————————————— tidyverse
2.0.0 —
## ✓ dplyr      1.1.4      ✓ readr      2.1.5
## ✓ forcats    1.0.0      ✓ stringr    1.5.1
## ✓ ggplot2    3.5.0      ✓ tibble     3.2.1
```

```
## ✓ lubridate 1.9.3       ✓ tidyr       1.3.1
## ✓ purrr       1.0.2
## — Conflicts ——————————————————————————————————————
tidyverse_conflicts() —
## X dplyr::filter() masks stats::filter()
## X dplyr::lag()     masks stats::lag()
## X dplyr::select() masks MASS::select()
## i Use the conflicted package (<http://conflicted.r-lib.org/>) to force all
conflicts to become errors

library(gridExtra)

##
## Attaching package: 'gridExtra'
##
## The following object is masked from 'package:dplyr':
##
##      combine

library(corrplot)

## corrplot 0.92 loaded

library(performance)
library(tinytex)
library(sp)
library(ggplot2)
library(gridExtra)

### Import the data set
insurance_data <- read.csv("insurance_claims.csv")
insurance_data

##      age    sex    bmi children is_smoker       working_env tot_claims
## 1    19 female 27.900        0       yes          factory 16884.924
## 2    18   male 33.770        1        no           office  1725.552
## 3    28   male 33.000        3        no           office  4449.462
## 4    33   male 22.705        0        no          factory 21984.471
## 5    32   male 28.880        0        no           office  3866.855
## 6    31 female 25.740        0        no           office  3756.622
## 7    46 female 33.440        1        no           office  8240.590
## 8    37 female 27.740        3        no           office  7281.506
## 9    37   male 29.830        2        no           office  6406.411
## 10   60 female 25.840        0        no          factory 28923.137
## 11   25   male 26.220        0        no           office  2721.321
## 12   62 female 26.290        0       yes          factory 27808.725
## 13   23   male 34.400        0        no           office  1826.843
## 14   56 female 39.820        0        no           office 11090.718
## 15   27   male 42.130        0       yes construction_site 39611.758
## 16   19   male 24.600        1        no           office  1837.237
## 17   52 female 30.780        1        no           office 10797.336
```

```
summary(insurance_data)

##      age              sex                 bmi             children
##  Min.   :18.00   Length:1338        Min.   :15.96   Min.   :0.000
##  1st Qu.:27.00   Class :character   1st Qu.:26.30   1st Qu.:0.000
##  Median :39.00   Mode  :character   Median :30.40   Median :1.000
##  Mean   :39.21                      Mean   :30.66   Mean   :1.095
##  3rd Qu.:51.00                      3rd Qu.:34.69   3rd Qu.:2.000
##  Max.   :64.00                      Max.   :53.13   Max.   :5.000
##   is_smoker          working_env           tot_claims
##  Length:1338        Length:1338        Min.   : 1122
##  Class :character   Class :character   1st Qu.: 4740
##  Mode  :character   Mode  :character   Median : 9382
##                                        Mean   :13270
##                                        3rd Qu.:16640
##                                        Max.   :63770

str(insurance_data)

## 'data.frame':    1338 obs. of  7 variables:
##  $ age        : int  19 18 28 33 32 31 46 37 37 60 ...
##  $ sex        : chr  "female" "male" "male" "male" ...
##  $ bmi        : num  27.9 33.8 33 22.7 28.9 ...
##  $ children   : int  0 1 3 0 0 0 1 3 2 0 ...
##  $ is_smoker  : chr  "yes" "no" "no" "no" ...
##  $ working_env: chr  "factory" "office" "office" "factory" ...
##  $ tot_claims : num  16885 1726 4449 21984 3867 ...
```

Note that, there are three categorical variables in the given data set. Such as, 'sex' , 'is_smoker' and 'working_env'

Exploratory Analysis

In this section, we explore the data to gain insights and identify patterns. Under the exploratory analysis, We have to look at the relationship between categorical variables and numerical variables. Also, want to look at the relationship between each and every variables with the response variable

```
# Plot Histogram using ggplot


p1 <- ggplot(data = insurance_data,aes(x = tot_claims)) + geom_histogram(col
= "black", fill = "skyblue",bins = 30) +
labs(x = "Total amount of Claims",title = "Histogram for Total amount of
Claims")+theme_bw()
```

```r
p2 <- ggplot(data = insurance_data,aes(x = log(tot_claims))) +
geom_histogram(col = "black", fill = "green",bins = 30) +
labs(x = "log(Total amount of Claims)",title = "Histogram for Log
transformed\n Total amount of Claims")+theme_bw()

grid.arrange(p1,p2, ncol = 2)
```
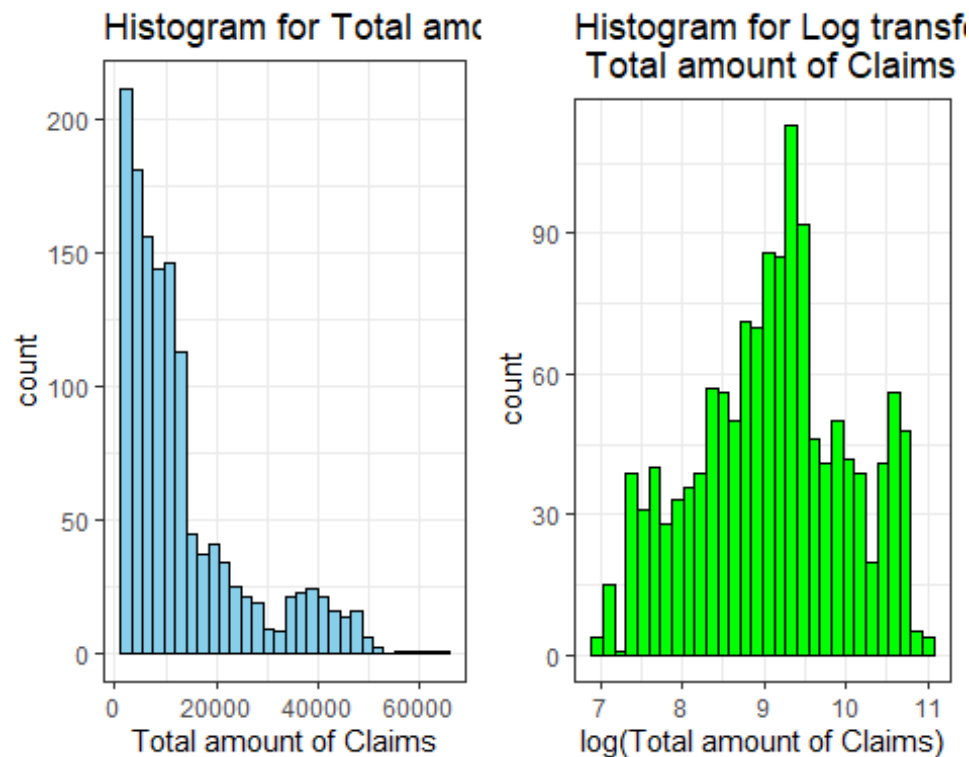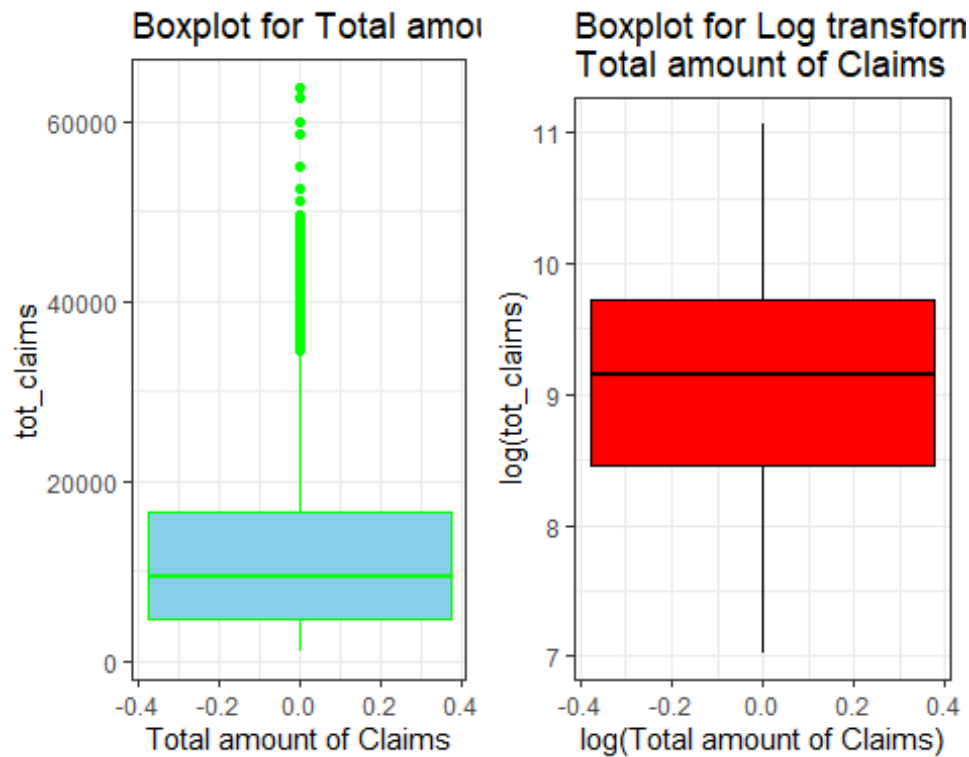


```r
# Plot boxplot using ggplot

p01 <- ggplot(data = insurance_data,aes(y = tot_claims)) + geom_boxplot(col =
"green", fill = "skyblue") + labs(x = "Total amount of Claims", title =
"Boxplot for Total amount of Claims") +
theme_bw()


p02 <- ggplot(data = insurance_data,aes(y = log(tot_claims))) +
geom_boxplot(col = "black", fill = "red") + labs(x = "log(Total amount of
Claims)",title = "Boxplot for Log transformed\nTotal amount of Claims") +
theme_bw()

grid.arrange(p01,p02, ncol = 2)
```

Boxplot for Total amount | Boxplot for Log transform Total amount of Claims

'tot_claims' variable is not normally distributed. Then I applied log transformation to the variable and it seems that, transformed variable is fairly normally distributed. So, we used log transformed variable for further analysis.

2.Relationship between Age and Total amount of claims

```r
p3 <- ggplot(data = insurance_data,aes(x = age,y = log(tot_claims))) +
geom_point(col = "black") +
labs(x = "Age",y = "log(Total amount of Claims)",
title = "Age vs Log transformed\nTotal amount of Claims") +
theme_bw()

p4 <- ggplot(data = insurance_data,aes(y = age)) +
geom_boxplot(col = "blue", fill = "skyblue") +
labs(x = "Age",
title = "Boxplot for Age") +
theme_bw()

grid.arrange(p3,p4, ncol = 2)
```
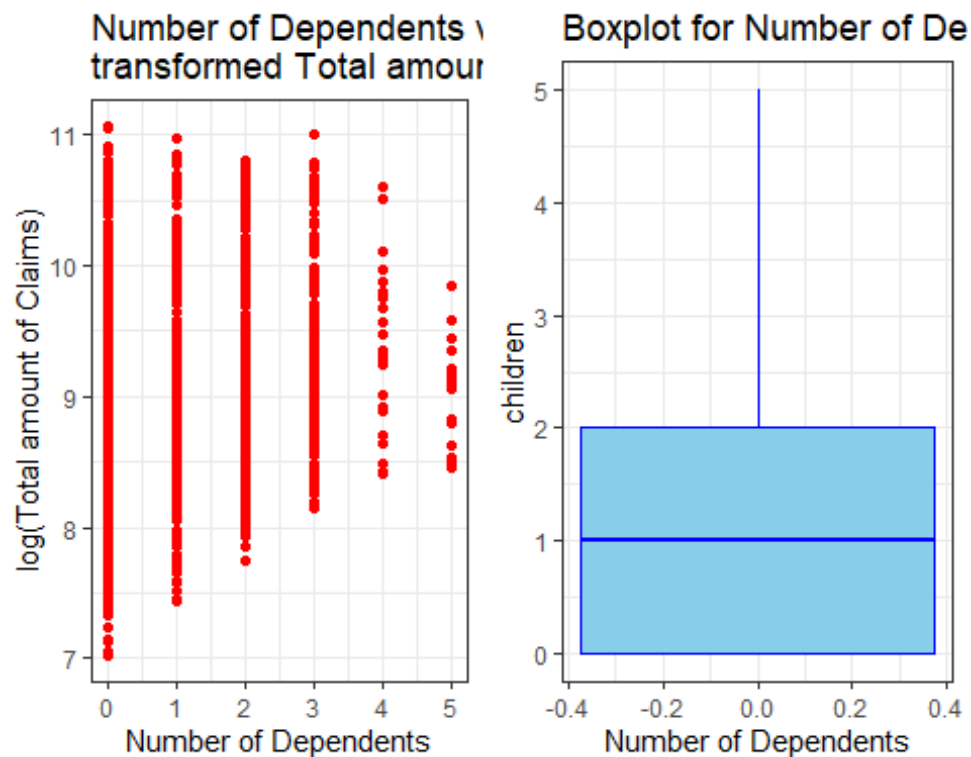
Age vs Log transformed Total amount of Claims / Boxplot for Age
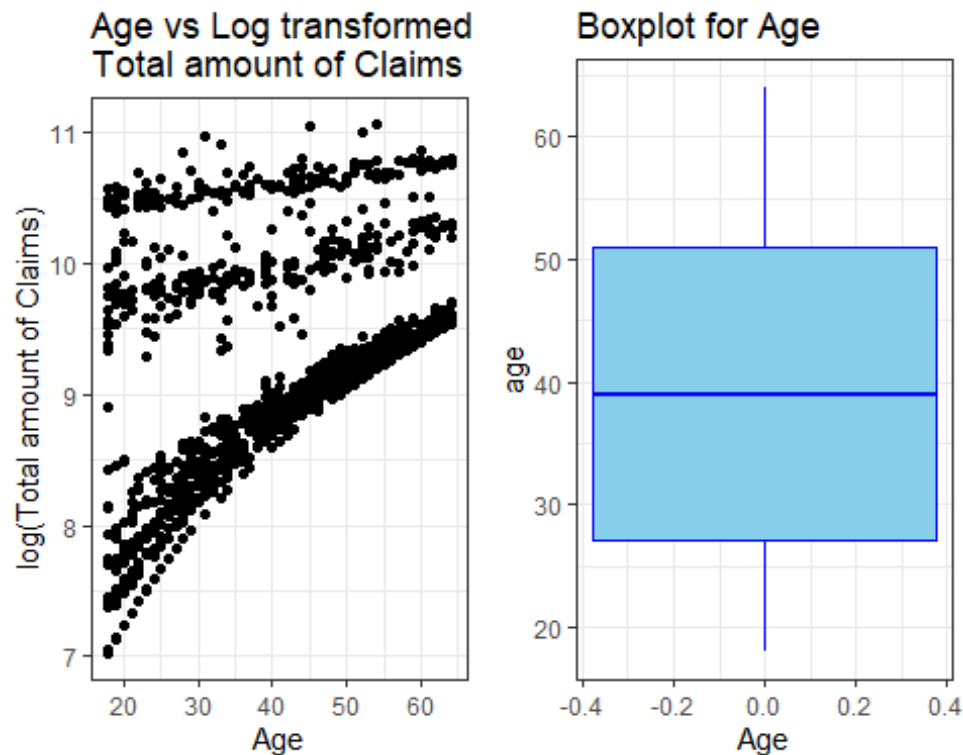
There is a moderately positive relationship between Age and log transformed variable. Age variable does not contain any outliers.

3. Relationship between BMI and Total amount of claims

```
p5 <-ggplot(data = insurance_data,aes(x = bmi,y = log(tot_claims)))
+geom_point(col = "blue") +labs(x = "BMI",y = "log(Total amount of
Claims)",title = "BMI vs Log transformed\nTotal amount of Claims") +
theme_bw()

p6 <- ggplot(data = insurance_data,aes(y = bmi)) +
geom_boxplot(col = "blue", fill = "skyblue") +
labs(x = "BMI",
title = "Boxplot for BMI") +
theme_bw()

grid.arrange(p5,p6, ncol = 2)
```

BMI vs Log transformed Total amount of Claims — Boxplot for BMI
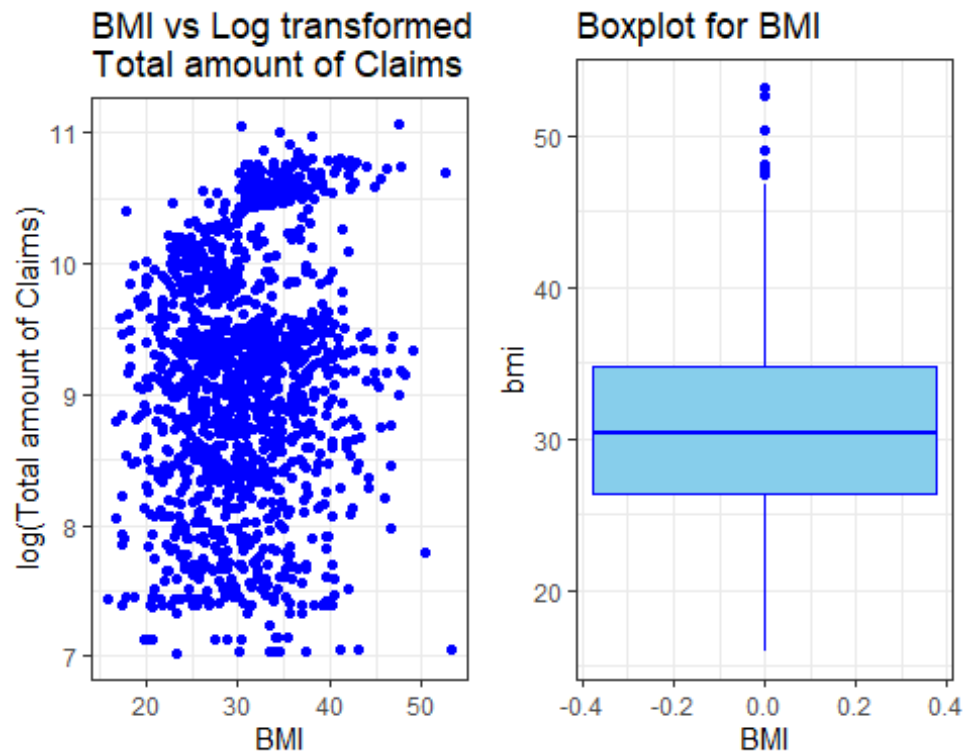
There is a very poor relationship between 'bmi' and log transformed variable. There are some outlires in "bmi" variable.

4.Relationship between No.of Children and Total amount of claims

```
p7 <-ggplot(data = insurance_data,aes(x = children,y = log(tot_claims))) +
geom_point(col = "red") +
labs(x = "Number of Dependents",y = "log(Total amount of Claims)",
title = "Number of Dependents vs Log\ntransformed Total amount of Claims") +
theme_bw()

p8 <- ggplot(data = insurance_data,aes(y = children)) +
geom_boxplot(col = "blue", fill = "skyblue") +
labs(x = "Number of Dependents",
title = "Boxplot for Number of Dependents") +
theme_bw()

grid.arrange(p7,p8, ncol = 2)
```

Number of Dependents v transformed Total amour

Boxplot for Number of De

There is a poor relationship with 'children' and log transformed variable. But we can not detect any outlires in this variable.

5. <u>Total amount of claims across Gender</u>

```
p9 <- ggplot(data = insurance_data,aes(x = sex, y = tot_claims)) +
geom_boxplot(fill = "skyblue") +
labs(x = "Gender",y = "Total amount of Claims",
title = "Total amount of claims across\nGender") +
theme_bw()

p10 <-ggplot(data = insurance_data,aes(x = sex,y = log(tot_claims))) +
geom_boxplot(fill = "skyblue") +
labs(x = "Gender",y = "log(Total amount of Claims)",
title = "log(Total amount of claims) across\nGender") +
theme_bw()

grid.arrange(p9,p10, ncol = 2)
```
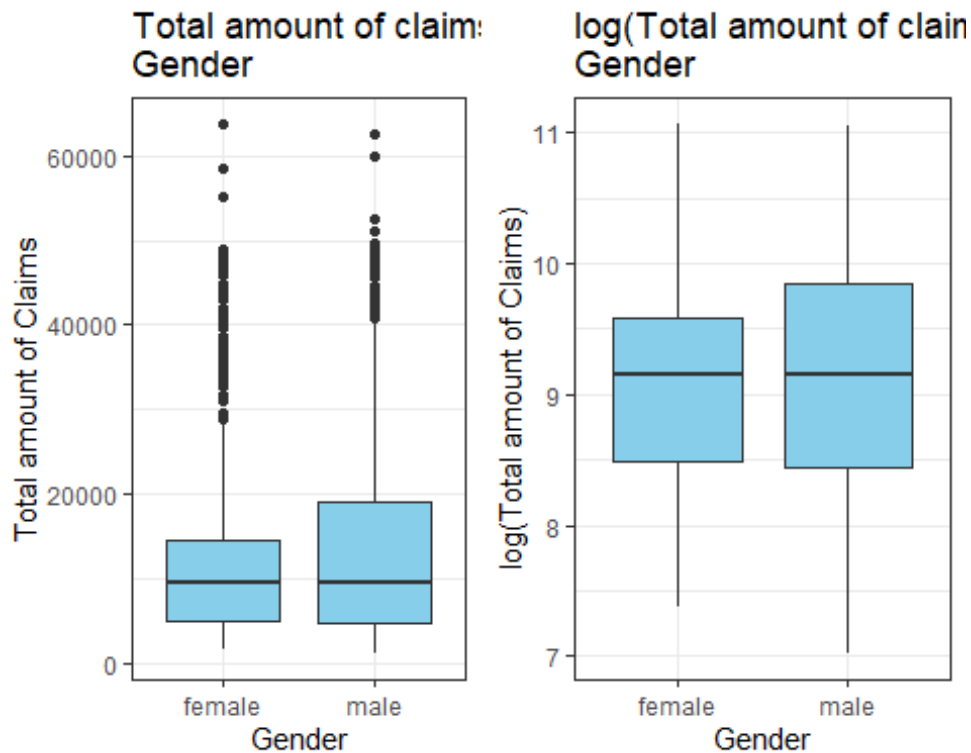
In this case there are outlires in the right side boxplot. But after applied the log transformation, we can not detect any outlires. Further, both distributions are fairly normally distributed because of both medians are approximately equal.

6. Total amount of claims across Smoking status

```
p11 <- ggplot(data = insurance_data,aes(x = is_smoker, y = tot_claims)) +
geom_boxplot(fill = "green") +
labs(x = "Smoking status",y = "Total amount of Claims",
title = "Total amount of claims across\nSmoking status") +
theme_bw()

p12 <- ggplot(data = insurance_data,aes(x = is_smoker,y = log(tot_claims))) +
geom_boxplot(fill = "red") +
labs(x = "Smoking status",y = "log(Total amount of Claims)",
title = "log(Total amount of claims) across\nSmoking status") +
theme_bw()

grid.arrange(p11,p12, ncol = 2)
```

Total amount of claims / Smoking status — log(Total amount of claims) / Smoking status
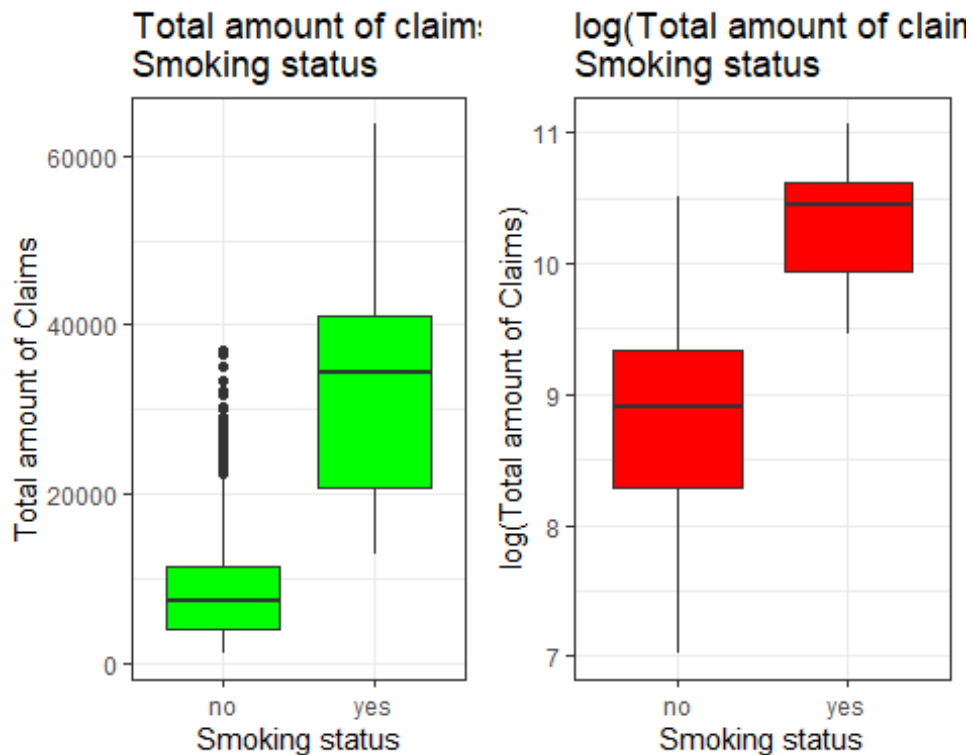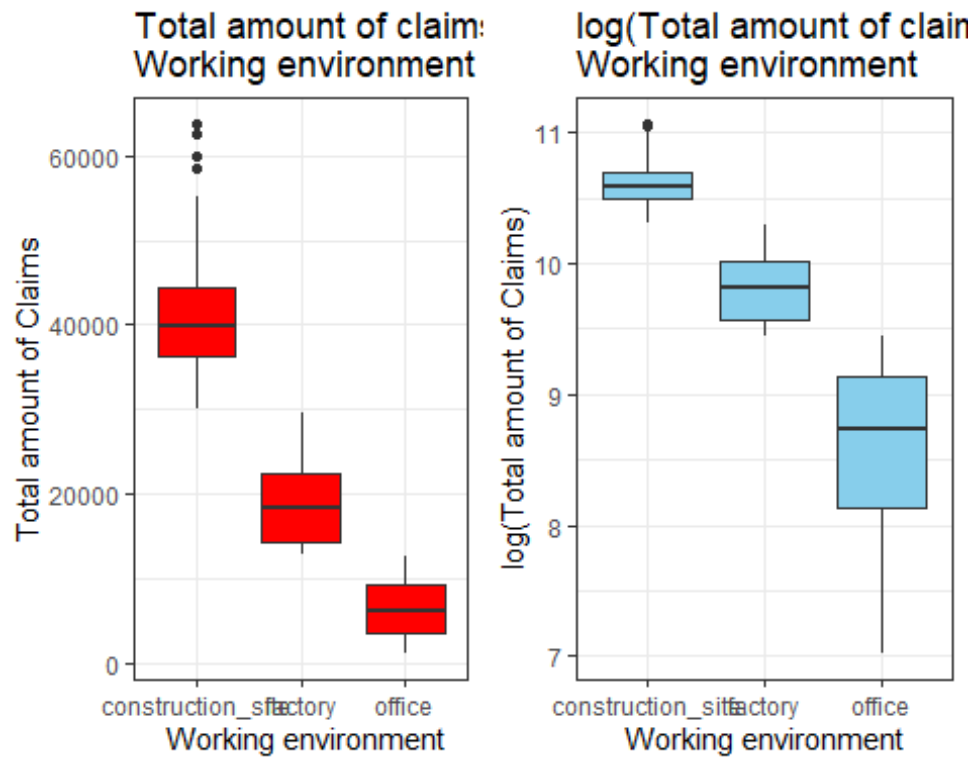
 In this case there are outlires in the right side boxplot. But after transformed, we can not detect any outliers and both distributions are fairly normally distributed. In 'yes' category has significantly higher median than 'no' category. So, it seems that 'is_smoker' variable has an effect on 'tot_claims' variable

7. Total amount of claims across working environment

```
p13 <- ggplot(data = insurance_data,aes(x = working_env, y = tot_claims)) +
geom_boxplot(fill = "red") +
labs(x = " Working environment",y = "Total amount of Claims",
title = "Total amount of claims across\nWorking environment") +
theme_bw()

p14 <-ggplot(data = insurance_data,aes(x = working_env,y = log(tot_claims)))
+
geom_boxplot(fill = "skyblue") +
labs(x = "Working environment",y = "log(Total amount of Claims)",
title = "log(Total amount of claims) across\nWorking environment") +
theme_bw()

grid.arrange(p13,p14, ncol = 2)
```

Total amount of claims / Working environment

log(Total amount of claims) / Working environment

 In this case We can see that there are outlires in the right side boxplots. In 'construction_site' category has significantly higher median than other categories. So, it seems 'working_env' variable has an effect on 'tot_claims' variable.

Correlation between Age, BMI and No.of Children

```
corrplot(cor(insurance_data[,c("age","bmi","children")]),method = 'square')
```
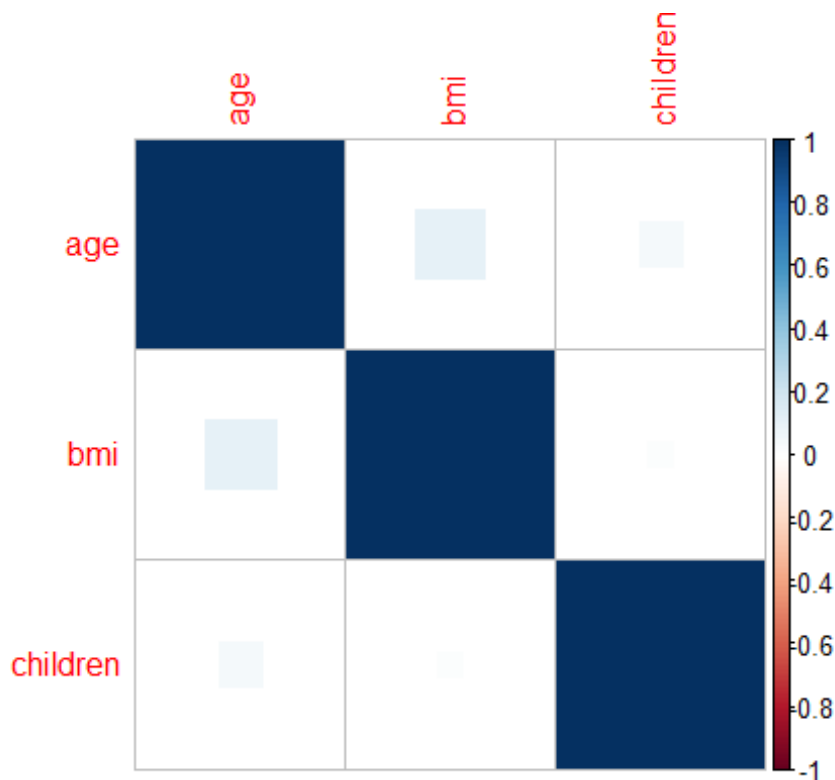
 There is a very poor correlation between 'bmi and 'age'. Also, there is no relationship between other pairs in the plot

Handle the categorical variables

To create best regression model Here, we have to covert all the categorical variables as numeric.

```
insurance_data$sex <- as.numeric(factor(insurance_data$sex , labels =
c("male" , "female")))
insurance_data$is_smoker <- as.numeric(factor(insurance_data$is_smoker ,
labels = c("yes" , "no")))
insurance_data$working_env <- as.numeric(factor(insurance_data$working_env ,
labels = c("factory" ,"office","construction_site")))

str(insurance_data)

## 'data.frame':    1338 obs. of  7 variables:
##  $ age        : int  19 18 28 33 32 31 46 37 37 60 ...
##  $ sex        : num  1 2 2 2 2 1 1 1 2 1 ...
##  $ bmi        : num  27.9 33.8 33 22.7 28.9 ...
##  $ children   : int  0 1 3 0 0 0 1 3 2 0 ...
##  $ is_smoker  : num  2 1 1 1 1 1 1 1 1 1 ...
##  $ working_env: num  2 3 3 2 3 3 3 3 3 2 ...
##  $ tot_claims : num  16885 1726 4449 21984 3867 ...

head(insurance_data)
```

```
##    age sex      bmi children is_smoker working_env tot_claims
## 1   19   1 27.900        0         2           2  16884.924
## 2   18   2 33.770        1         1           3   1725.552
## 3   28   2 33.000        3         1           3   4449.462
## 4   33   2 22.705        0         1           2  21984.471
## 5   32   2 28.880        0         1           3   3866.855
## 6   31   1 25.740        0         1           3   3756.622
```

Model Fitting

For the purpose of model fitting, I have used the forward selection method based on Adjusted R-squared values to select the significance variables.

Iteration 01

```
fit1 <- lm(tot_claims ~ age,data = insurance_data)
fit2 <- lm(tot_claims ~ sex,data = insurance_data)
fit3 <- lm(tot_claims ~ bmi,data = insurance_data)
fit4 <- lm(tot_claims ~ children,data = insurance_data)
fit5 <- lm(tot_claims ~ is_smoker,data = insurance_data)
fit6 <- lm(tot_claims ~ working_env,data = insurance_data)

### using adjusted R squre to select the best model
summary(fit1)$adj.r.square

## [1] 0.08872432

summary(fit2)$adj.r.square

## [1] 0.002536334

summary(fit3)$adj.r.square

## [1] 0.03862008

summary(fit4)$adj.r.square

## [1] 0.003878717

summary(fit5)$adj.r.square

## [1] 0.6194802

summary(fit6)$adj.r.square

## [1] 0.8614734
```

Since 'working_env' variable has the largest adjusted R-squared value as 0.8614734, that variable is included to the model

Iteration 02

```
#working_env is add
fit1 <- lm(tot_claims ~ working_env + age ,data = insurance_data)
fit2 <- lm(tot_claims ~ working_env + sex ,data = insurance_data)
fit3 <- lm(tot_claims ~ working_env + bmi ,data = insurance_data)
fit4 <- lm(tot_claims ~ working_env + children ,data = insurance_data)
fit5 <- lm(tot_claims ~ working_env + is_smoker ,data = insurance_data)

### using adjusted R squre to select the best model
summary(fit1)$adj.r.square

## [1] 0.886051

summary(fit2)$adj.r.square

## [1] 0.8614025

summary(fit3)$adj.r.square

## [1] 0.865276

summary(fit4)$adj.r.square

## [1] 0.8643907

summary(fit5)$adj.r.square

## [1] 0.8679371
```

Here 'age' variable has the highest adjusted R-squared value as 0.886051. Therefore, 'age' is added to the model.

Iteration 03

```
#age is added

fit1 <- lm(tot_claims ~ working_env + age + sex ,data = insurance_data)
fit2 <- lm(tot_claims ~ working_env + age + bmi ,data = insurance_data)
fit3 <- lm(tot_claims ~ working_env + age + children ,data = insurance_data)
fit4 <- lm(tot_claims ~ working_env + age + is_smoker ,data = insurance_data)

### using adjusted R squre to select the best model
summary(fit1)$adj.r.square

## [1] 0.8859661

summary(fit2)$adj.r.square

## [1] 0.888348

summary(fit3)$adj.r.square

## [1] 0.8883291
```

```
summary(fit4)$adj.r.square
```

```
## [1] 0.9013036
```

Note that, 'is_smoker' variable has largest adjusted R-squared value as 0.9013036. So, this variable is also added to the model.

Iteration 04
```
# is_smoker is add
```

```
fit1 <- lm(tot_claims ~ working_env + age + is_smoker + sex ,data =
insurance_data)
fit2 <- lm(tot_claims ~ working_env + age + is_smoker + bmi ,data =
insurance_data)
fit3 <- lm(tot_claims ~ working_env + age + is_smoker + children ,data =
insurance_data)
```

```
### using adjusted R squre to select the best model
summary(fit1)$adj.r.square
```

```
## [1] 0.9012491
```

```
summary(fit2)$adj.r.square
```

```
## [1] 0.9063182
```

```
summary(fit3)$adj.r.square
```

```
## [1] 0.903542
```

Since 'bmi' variable has largest adjusted R-squared as 0.9063182. 'bmi' variable is included to the model.

Iteration 05

```
#bmi add
```

```
fit1 <- lm(tot_claims ~ working_env + age + is_smoker + bmi + sex ,data =
insurance_data)
fit2 <- lm(tot_claims ~ working_env + age + is_smoker + bmi + children ,data
= insurance_data)
```

```
### using adjusted R squre to select the best model
summary(fit1)$adj.r.square
```

```
## [1] 0.9063071
```

```
summary(fit2)$adj.r.square
```

```
## [1] 0.9085069
```

Here 'children' variable has highest adjusted R-squared value as 0.9085069. So, this variable is also in the model.

<u>Iteration 06</u>

```
#children add
fit1 <- lm(tot_claims ~ working_env + age + is_smoker + bmi + children+sex
,data = insurance_data)

### using adjusted R squre to select the best model
summary(fit1)$adj.r.square

## [1] 0.9085106
```

Note that, when the 'sex' variable is added to the model there is no any significance change in adjusted R-squared value. Based on that reason, we cannot include the 'sex' variable for the above fitted model.

plot all iteration Adjusted R-squared

```
plot(c(1,2,3,4,5,6),c(0.8614734,0.886051,0.9013036,0.9063182,0.9085069,
0.9085106),
xlab = "Number of variables in the model", ylab ="Adjusted R-squared",
type="o")
```
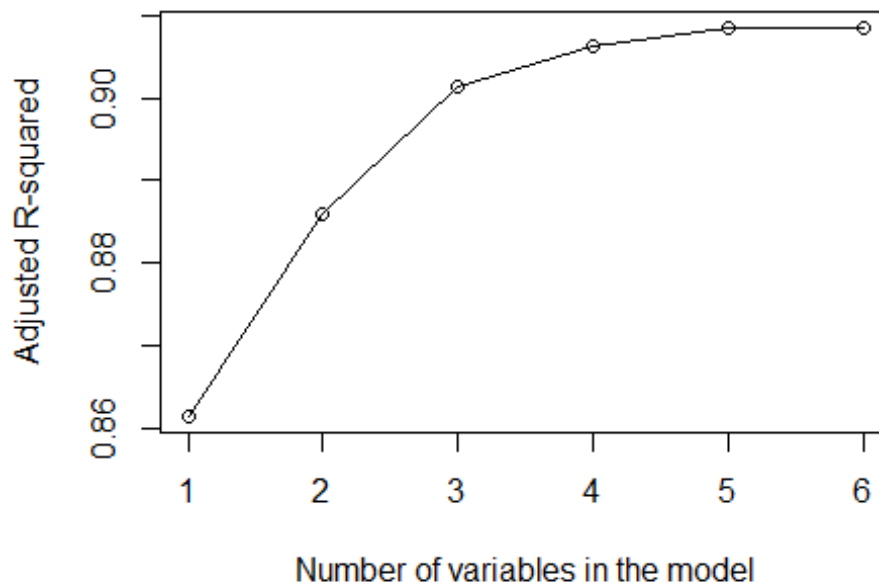

According to the above plot, we have to include the following variables in order to obtain the best fitted model. • age • bmi • children • is_smoker •working_env

Full model

Obtained the full model by including all the variables as follows.

```
full_model <- lm(tot_claims ~ . , data = insurance_data)
drop1(full_model, test = "F")

## Single term deletions
##
## Model:
## tot_claims ~ age + sex + bmi + children + is_smoker + working_env
##             Df  Sum of Sq        RSS    AIC   F value    Pr(>F)
## <none>                    1.7858e+10 21966
## age          1 6.1495e+09 2.4008e+10 22360  458.3293 < 2.2e-16 ***
## sex          1 1.4141e+07 1.7872e+10 21965    1.0539    0.3048
## bmi          1 9.9272e+08 1.8851e+10 22037   73.9888 < 2.2e-16 ***
## children     1 4.4385e+08 1.8302e+10 21997   33.0808 1.095e-08 ***
## is_smoker    1 3.5266e+09 2.1385e+10 22205  262.8435 < 2.2e-16 ***
## working_env  1 3.1215e+10 4.9073e+10 23317 2326.4839 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

summary(full_model)

##
## Call:
## lm(formula = tot_claims ~ ., data = insurance_data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -11247.0  -1187.3    184.6   1669.3  24756.6
##
## Coefficients:
##                Estimate Std. Error t value Pr(>|t|)
## (Intercept)   24886.835   1435.366  17.338  < 2e-16 ***
## age             159.817      7.465  21.409  < 2e-16 ***
## sex            -206.535    201.182  -1.027    0.305
## bmi             145.770     16.947   8.602  < 2e-16 ***
## children        478.491     83.193   5.752  1.1e-08 ***
## is_smoker      6958.673    429.218  16.212  < 2e-16 ***
## working_env  -12172.133    252.358 -48.234  < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 3663 on 1331 degrees of freedom
## Multiple R-squared:  0.9089, Adjusted R-squared:  0.9085
## F-statistic:  2214 on 6 and 1331 DF,  p-value: < 2.2e-16
```

According to the above results, we have to exclude the 'sex' variable as it is not significant to the fitted model. Further, it has high p value of 0.305 (>0.05) than the other variables

Reduced model

Obtained the reduced model by dropping 'sex' variable from the full_model.

```
reduced_model <- lm(tot_claims ~ age + bmi + children + is_smoker +
working_env , data = insurance_data)
summary(reduced_model)

##
## Call:
## lm(formula = tot_claims ~ age + bmi + children + is_smoker +
##      working_env, data = insurance_data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -11334.8  -1162.1    182.1   1684.2  24667.6
##
## Coefficients:
##                Estimate Std. Error t value Pr(>|t|)
## (Intercept)   24608.441   1409.546  17.458  < 2e-16 ***
## age             160.017      7.463  21.442  < 2e-16 ***
## bmi             144.977     16.929   8.564  < 2e-16 ***
## children        477.031     83.182   5.735 1.21e-08 ***
## is_smoker      6942.301    428.930  16.185  < 2e-16 ***
## working_env  -12170.053    252.355 -48.226  < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 3663 on 1332 degrees of freedom
## Multiple R-squared:  0.9088, Adjusted R-squared:  0.9085
## F-statistic:  2656 on 5 and 1332 DF,  p-value: < 2.2e-16
```

Validation of the model

Here, I have used Partial F Test to check the adequacy of the reduced model. • null hypothesis : Reduced model is adequate vs • alternative : Reduced model is not adequate

```
anova(full_model,reduced_model)

## Analysis of Variance Table
##
## Model 1: tot_claims ~ age + sex + bmi + children + is_smoker + working_env
## Model 2: tot_claims ~ age + bmi + children + is_smoker + working_env
##   Res.Df        RSS Df Sum of Sq      F Pr(>F)
## 1   1331 1.7858e+10
## 2   1332 1.7872e+10 -1 -14140693 1.0539 0.3048
```

By looking at the ANOVA table, we can detect that the p-value (0.3048) is greater than 0.05 at 5% significance level. That means we don't have enough evidence to reject null hypothesis at 5% significance level. Moreover, we can conclude that the reduced model is adequate.

```
check_model(reduced_model, check =
c("linearity","homogeneity","qq","outliers"))
```
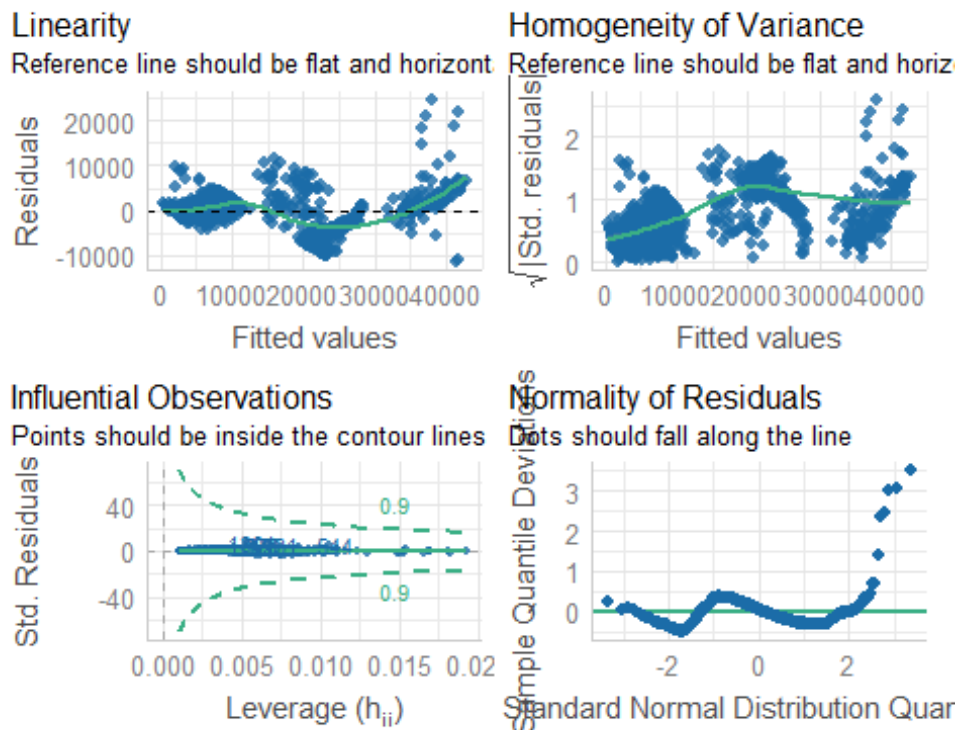


```
check_normality(reduced_model)

## Warning: Non-normality of residuals detected (p < .001).

check_heteroskedasticity(reduced_model)

## Warning: Heteroscedasticity (non-constant error variance) detected (p <
.001).

check_outliers(reduced_model)

## OK: No outliers detected.
## - Based on the following method and threshold: cook (0.9).
## - For variable: (Whole model)

check_autocorrelation(reduced_model)

## OK: Residuals appear to be independent and not autocorrelated (p = 0.946).
```
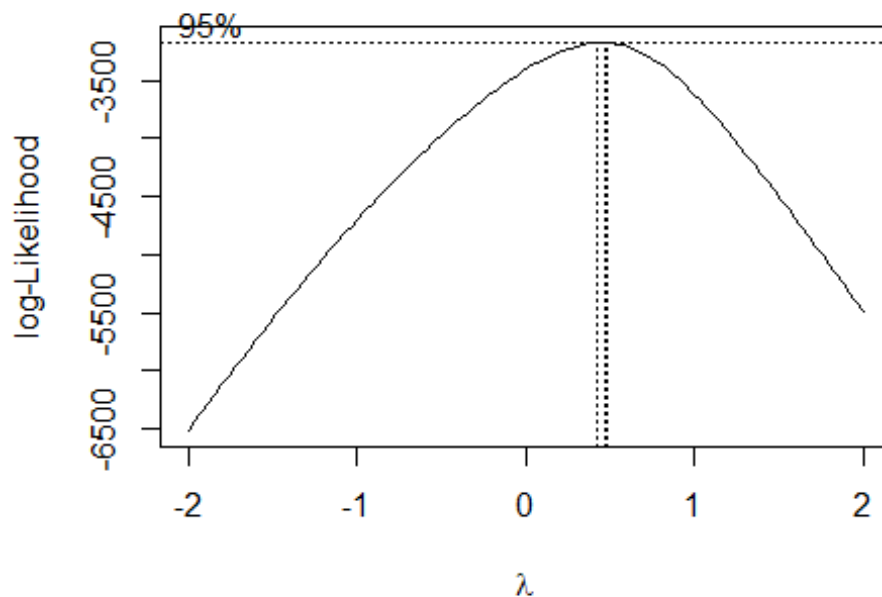
By looking at the above plot and results that we obtained, we can detect that the normality of residuals and heteroskedasticity is violated. So, we have to use the transformation method to correct those violation.

BOX - COX transformation

```
box_trans <- boxcox(reduced_model)
```

```
(lambda <- box_trans$x[which.max(box_trans$y)])

## [1] 0.4646465

fit_model <- lm(((tot_claims^lambda-1)/lambda) ~ working_env + is_smoker +
bmi + children + age, data = insurance_data)
summary(fit_model)

##
## Call:
## lm(formula = ((tot_claims^lambda - 1)/lambda) ~ working_env +
##      is_smoker + bmi + children + age, data = insurance_data)
##
## Residuals:
##     Min      1Q  Median      3Q     Max
## -71.549 -10.617  -0.124  10.492  90.610
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 193.97208    7.75948  24.998  < 2e-16 ***
## working_env -63.40573    1.38920 -45.642  < 2e-16 ***
## is_smoker    40.89734    2.36124  17.320  < 2e-16 ***
## bmi           0.37064    0.09320   3.977 7.36e-05 ***
## children      4.84877    0.45792  10.589  < 2e-16 ***
## age           1.54199    0.04108  37.535  < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
## 
## Residual standard error: 20.16 on 1332 degrees of freedom
## Multiple R-squared:  0.9132, Adjusted R-squared:  0.9129
## F-statistic:  2802 on 5 and 1332 DF,  p-value: < 2.2e-16
```

Check the model assumption

```
check_model(fit_model, check = c("qq", "linearity",
"homogeneity","outliers"))
```



```
check_normality(fit_model)
```

```
## Warning: Non-normality of residuals detected (p < .001).
```

```
check_heteroskedasticity(fit_model)
```

```
## Warning: Heteroscedasticity (non-constant error variance) detected (p <
.001).
```

```
check_outliers(fit_model)
```

```
## OK: No outliers detected.
## - Based on the following method and threshold: cook (0.9).
## - For variable: (Whole model)
```

```
check_autocorrelation(fit_model)
```

```
## OK: Residuals appear to be independent and not autocorrelated (p = 0.314).
```

In order to correct the non constant error of variance, we can use log transformation

Log transformation

```
log_model <- lm(log(tot_claims) ~ age + bmi + children + is_smoker +
working_env, data = insurance_data )
summary(log_model)

##
## Call:
## lm(formula = log(tot_claims) ~ age + bmi + children + is_smoker +
##     working_env, data = insurance_data)
##
## Residuals:
##     Min      1Q  Median      3Q     Max
## -1.1242 -0.2302  0.0434  0.1943  1.4307
##
## Coefficients:
##               Estimate Std. Error t value Pr(>|t|)
## (Intercept)  8.9522671  0.1349223  66.351   <2e-16 ***
## age          0.0291044  0.0007143  40.744   <2e-16 ***
## bmi          0.0003439  0.0016205   0.212    0.832
## children     0.1014024  0.0079623  12.735   <2e-16 ***
## is_smoker    0.5641608  0.0410574  13.741   <2e-16 ***
## working_env -0.7063503  0.0241555 -29.242   <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.3506 on 1332 degrees of freedom
## Multiple R-squared:  0.8551, Adjusted R-squared:  0.8546
## F-statistic:  1573 on 5 and 1332 DF,  p-value: < 2.2e-16
```
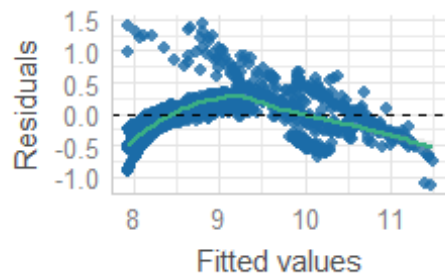
Check the model assumption

```
check_model(log_model, check = c("qq", "linearity", "homogeneity",
"outliers"))
```
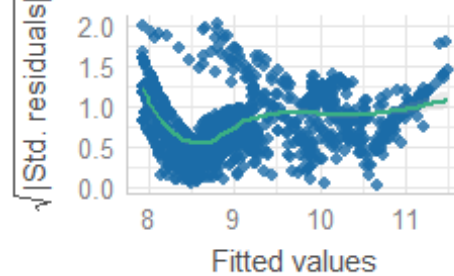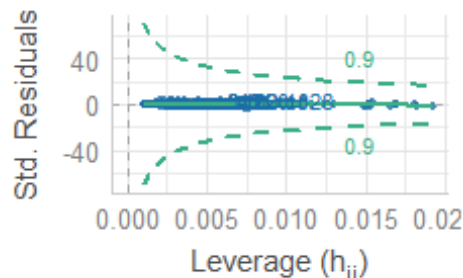
Linearity
Reference line should be flat and horizo

Homogeneity of Variance
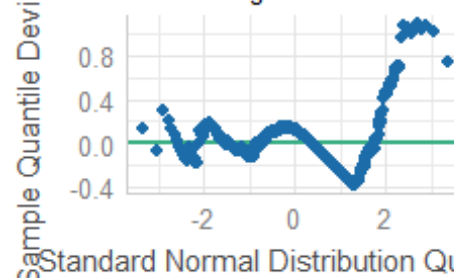Reference line should be flat and horizont

Influential Observations
Points should be inside the contour lin

Normality of Residuals
Dots should fall along the line

```r
check_normality(log_model)
```

```
## Warning: Non-normality of residuals detected (p < .001).
```

```r
check_heteroskedasticity(log_model)
```

```
## OK: Error variance appears to be homoscedastic (p = 0.232).
```

```r
check_outliers(log_model)
```

```
## OK: No outliers detected.
## - Based on the following method and threshold: cook (0.9).
## - For variable: (Whole model)
```

```r
check_autocorrelation(log_model)
```

```
## OK: Residuals appear to be independent and not autocorrelated (p = 0.498).
```

Still normality assumption is violated.

<u>Multicolinearity</u>

```r
library(caTools)
library(car)
```

```
## Loading required package: carData
```

```
##
## Attaching package: 'car'
```

```
## The following object is masked from 'package:dplyr':
##
##     recode

## The following object is masked from 'package:purrr':
##
##     some
```

```r
library(quantmod)
```

```
## Loading required package: xts

## Loading required package: zoo

##
## Attaching package: 'zoo'

## The following objects are masked from 'package:base':
##
##     as.Date, as.Date.numeric

##
## ######################### Warning from 'xts' package
###########################
## #
#
## # The dplyr lag() function breaks how base R's lag() function is supposed
to  #
## # work, which breaks lag(my_xts). Calls to lag(my_xts) that you type or
#
## # source() into this session won't work correctly.
#
## #
#
## # Use stats::lag() to make sure you're not using dplyr::lag(), or you can
add #
## # conflictRules('dplyr', exclude = 'lag') to your .Rprofile to stop
#
## # dplyr from breaking base R's lag() function.
#
## #
#
## # Code in packages is not affected. It's protected by R's namespace
mechanism #
## # Set `options(xts.warn_dplyr_breaks_lag = FALSE)` to suppress this
warning.   #
## #
#
##
############################################################################
##
```
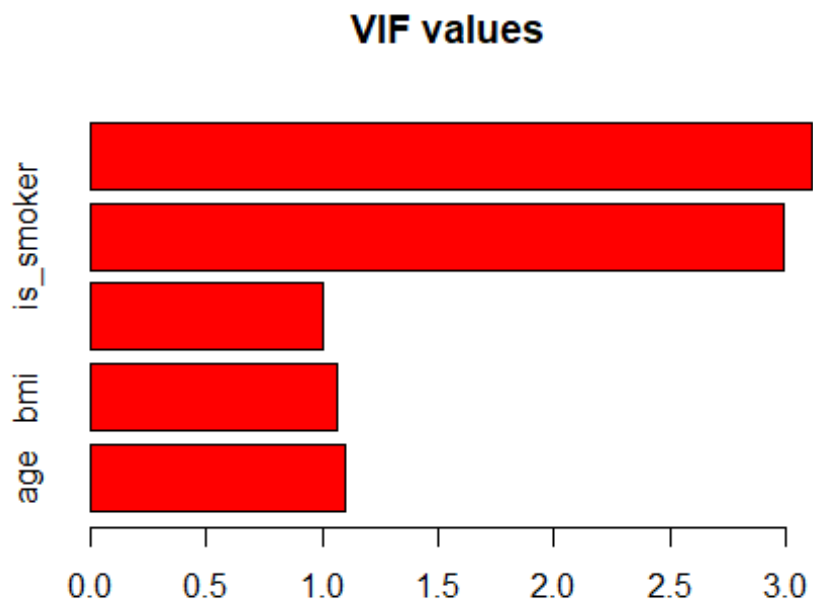
```
## 
## Attaching package: 'xts'

## The following objects are masked from 'package:dplyr':
## 
##     first, last

## Loading required package: TTR

## Registered S3 method overwritten by 'quantmod':
##   method            from
##   as.zoo.data.frame zoo

library(xts)
library(zoo)

vif_values <- vif(reduced_model)
barplot(vif_values, main = "VIF values", horiz = TRUE, col = "red")
abline(v = 4, lwd = 3, lty = 2)
```
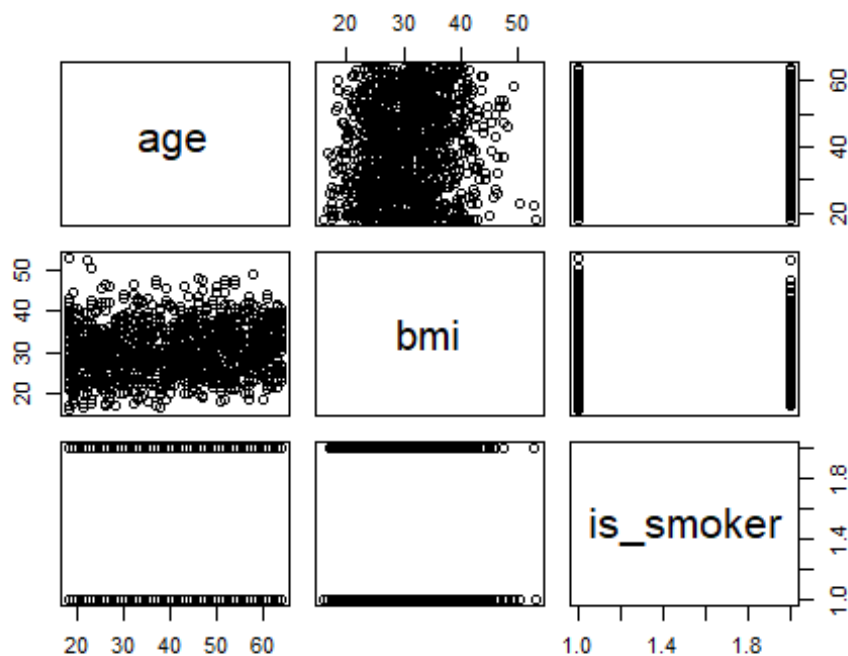
VIF values


```
insurance_data %>% dplyr::select(age, bmi, is_smoker) %>% pairs()
```

According to the above plot, we can conclude that the variables are uncorrelated. Therefore, the multicolinearity does not effect when predict the annual claims.

Discussion

In the best fitted model, each and every exploratory variables should be uncorrelated. If we detect the multicolinearity of the fitted model, It would be directly effected when predict the response variable. So, in this multiple linear regression analysis, we didn't detect the multicolinearity. When checking the assumption, normality assumption was violated even use the log and boxcox transfor mation.

```
dim(insurance_data)
```
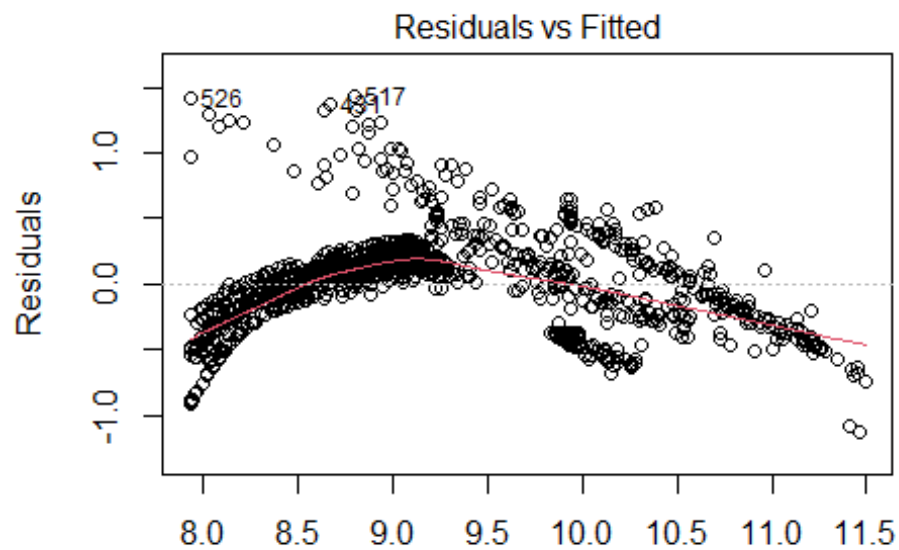
```
## [1] 1338    7
```

This data set contains 1338 observations. By Central Limit Therom for sufficiently large sample we can conclude that the residual will approximately normal.

## Conclusion

```
coef_log_model <- coef(log_model)
coef_log_model
```

```
##   (Intercept)           age           bmi      children     is_smoker
##   8.9522670887  0.0291043745  0.0003438572  0.1014024291  0.5641607659
##    working_env
## -0.7063503004
```
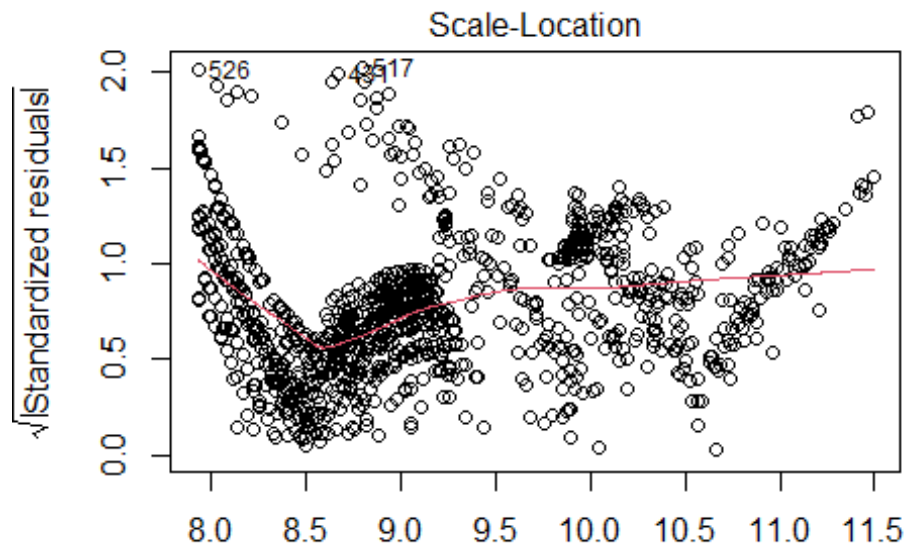
```r
plot(log_model) + geom_abline(intercept = coef_log_model[1], slope =
coef_log_model[2], color = "red")
```
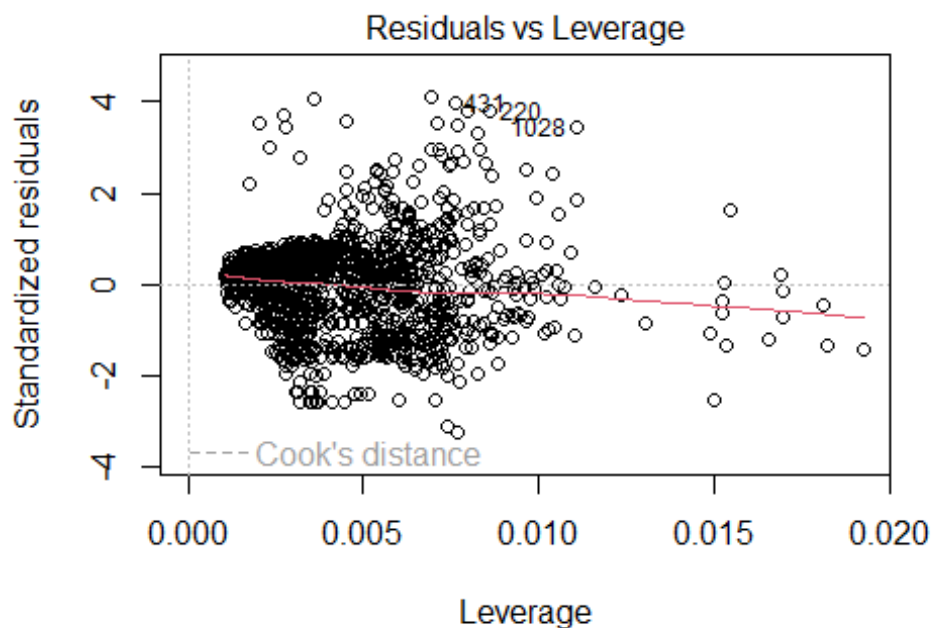
Residuals vs Fitted

Fitted values
lm(log(tot_claims) ~ age + bmi + children + is_smoker + working_e

Q-Q Residuals
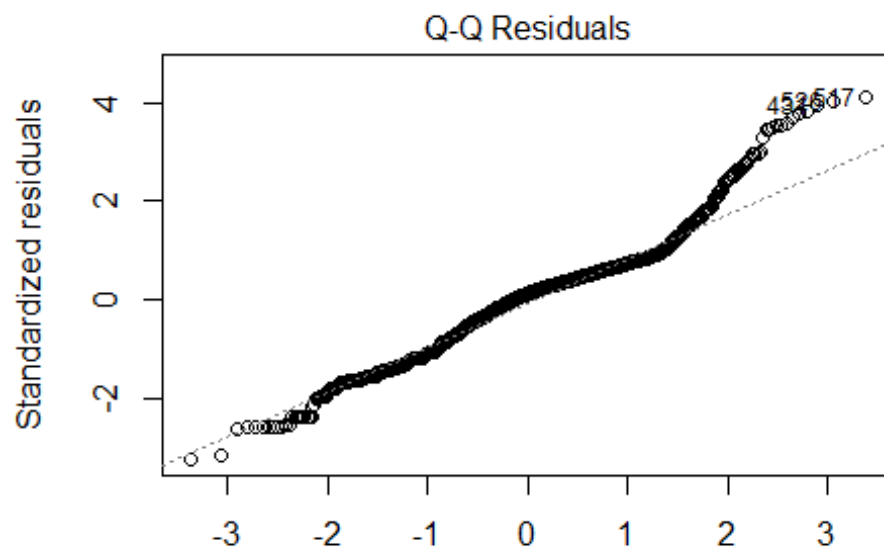
Theoretical Quantiles
lm(log(tot_claims) ~ age + bmi + children + is_smoker + working_e

Scale-Location

√|Standardized residuals|

Fitted values
lm(log(tot_claims) ~ age + bmi + children + is_smoker + working_e

Residuals vs Leverage

Standardized residuals

Cook's distance

Leverage
lm(log(tot_claims) ~ age + bmi + children + is_smoker + working_e

```
## NULL
```

Best fitted model log(tot_claims) = 8.95226 + (0.0291)age + (0.00034)bmi + (0.1014)children + (0.56416)is_smoker

<u>Interpretation :</u>

The estimates in the multiple linear regression model tell us that for every one percent increase in age of the policyholder there is an associated 0.0291 percent increase in log(tot_claims) and that for every one percent increase in bmi of the policyholder there is an associated 0.00034 percent increase in log(tot_claims) and that for every one percent increase in number of dependents covered by health insurance there is an associated 0.1014 percent increase in log(tot_claims) and that for every one percent increase in smoking status of the policyholder there is an associated 0.56416 percent increase in log(tot_claims)