

Historical approach to estimating the volatility parameter

```
In [9]: library("tidyverse")
library("lubridate")
```

Attaching package: 'lubridate'

The following objects are masked from 'package:base':

date, intersect, setdiff, union

```
In [54]: MSFT_orig <- read_csv("StockPrice.csv")

MSFT <- MSFT_orig

MSFT <- MSFT %>% mutate(Date = dmy(Date))
```

— Column specification —

```
cols(
  Date = col_character(),
  Close = col_double()
)
```

```
In [48]: MSFT %>% glimpse()
```

```
Rows: 61
Columns: 2
$ Date <date> 2001-11-12, 2001-11-09, 2001-11-08, 2001-11-07, 2001-11-
06, 20...
$ Close <dbl> 65.79, 65.21, 64.42, 64.25, 64.78, 63.27, 61.40, 61.84, 5
8.15, ...
```

```
In [56]: MSFT <- MSFT %>% mutate(LagClose = lag(Close), #get the lag 1 Close da
RatioPriceChange = Close / LagClose,
logPriceRat = log(RatioPriceChange, base = exp(1)),
Xi = logPriceRat) # calculate the price ratio

MSFT
```

A spec_tbl_df: 61 × 6

| Date | Close | LagClose | RatioPriceChange | logPriceRat | Xi |
|------------|-------|----------|------------------|--------------|--------------|
| <date> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> |
| 2001-11-12 | 65.79 | NA | NA | NA | NA |
| 2001-11-09 | 65.21 | 65.79 | 0.9911841 | -0.008855020 | -0.008855020 |

| Date | Close | LagClose | RatioPriceChange | logPriceRat | Xi |
|------------|-------|----------|------------------|--------------|--------------|
| <date> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> |
| 2001-11-08 | 64.42 | 65.21 | 0.9878853 | -0.012188688 | -0.012188688 |
| 2001-11-07 | 64.25 | 64.42 | 0.9973611 | -0.002642420 | -0.002642420 |
| 2001-11-06 | 64.78 | 64.25 | 1.0082490 | 0.008215190 | 0.008215190 |
| 2001-11-05 | 63.27 | 64.78 | 0.9766903 | -0.023585631 | -0.023585631 |
| 2001-11-02 | 61.40 | 63.27 | 0.9704441 | -0.030001448 | -0.030001448 |
| 2001-11-01 | 61.84 | 61.40 | 1.0071661 | 0.007140569 | 0.007140569 |
| 2001-10-31 | 58.15 | 61.84 | 0.9403299 | -0.061524525 | -0.061524525 |
| 2001-10-30 | 58.88 | 58.15 | 1.0125537 | 0.012475595 | 0.012475595 |
| 2001-10-29 | 59.64 | 58.88 | 1.0129076 | 0.012825015 | 0.012825015 |
| 2001-10-26 | 62.20 | 59.64 | 1.0429242 | 0.042028510 | 0.042028510 |
| 2001-10-25 | 62.56 | 62.20 | 1.0057878 | 0.005771096 | 0.005771096 |
| 2001-10-24 | 61.32 | 62.56 | 0.9801790 | -0.020020042 | -0.020020042 |
| 2001-10-23 | 60.43 | 61.32 | 0.9854860 | -0.014620384 | -0.014620384 |
| 2001-10-22 | 60.16 | 60.43 | 0.9955320 | -0.004477991 | -0.004477991 |
| 2001-10-19 | 57.90 | 60.16 | 0.9624335 | -0.038290295 | -0.038290295 |
| 2001-10-18 | 56.76 | 57.90 | 0.9803109 | -0.019885532 | -0.019885532 |
| 2001-10-17 | 56.03 | 56.76 | 0.9871388 | -0.012944591 | -0.012944591 |
| 2001-10-16 | 58.45 | 56.03 | 1.0431911 | 0.042284426 | 0.042284426 |
| 2001-10-15 | 58.06 | 58.45 | 0.9933276 | -0.006694729 | -0.006694729 |
| 2001-10-12 | 56.38 | 58.06 | 0.9710644 | -0.029362473 | -0.029362473 |
| 2001-10-11 | 56.32 | 56.38 | 0.9989358 | -0.001064774 | -0.001064774 |
| 2001-10-10 | 55.51 | 56.32 | 0.9856179 | -0.014486527 | -0.014486527 |
| 2001-10-09 | 54.56 | 55.51 | 0.9828860 | -0.017262171 | -0.017262171 |
| 2001-10-08 | 58.04 | 54.56 | 1.0637830 | 0.061831414 | 0.061831414 |
| 2001-10-05 | 57.72 | 58.04 | 0.9944866 | -0.005528694 | -0.005528694 |
| 2001-10-04 | 56.64 | 57.72 | 0.9812890 | -0.018888285 | -0.018888285 |
| 2001-10-03 | 56.23 | 56.64 | 0.9927613 | -0.007265027 | -0.007265027 |
| 2001-10-02 | 53.05 | 56.23 | 0.9434466 | -0.058215557 | -0.058215557 |
| : | : | : | : | : | : |
| 2001-09-28 | 51.17 | 51.79 | 0.9880286 | -0.012043658 | -0.012043658 |
| 2001-09-27 | 49.96 | 51.17 | 0.9763533 | -0.023930738 | -0.023930738 |
| 2001-09-26 | 50.27 | 49.96 | 1.0062050 | 0.006185792 | 0.006185792 |

| Date | Close | LagClose | RatioPriceChange | logPriceRat | Xi |
|------------|-------|----------|------------------|--------------|--------------|
| <date> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> |
| 2001-09-25 | 51.30 | 50.27 | 1.0204894 | 0.020282274 | 0.020282274 |
| 2001-09-24 | 52.01 | 51.30 | 1.0138402 | 0.013745256 | 0.013745256 |
| 2001-09-21 | 49.71 | 52.01 | 0.9557777 | -0.045229888 | -0.045229888 |
| 2001-09-20 | 50.76 | 49.71 | 1.0211225 | 0.020902523 | 0.020902523 |
| 2001-09-19 | 53.87 | 50.76 | 1.0612687 | 0.059465094 | 0.059465094 |
| 2001-09-18 | 54.32 | 53.87 | 1.0083534 | 0.008318747 | 0.008318747 |
| 2001-09-17 | 52.91 | 54.32 | 0.9740427 | -0.026300126 | -0.026300126 |
| 2001-09-10 | 57.58 | 52.91 | 1.0882631 | 0.084582928 | 0.084582928 |
| 2001-09-07 | 55.40 | 57.58 | 0.9621396 | -0.038595691 | -0.038595691 |
| 2001-09-06 | 56.02 | 55.40 | 1.0111913 | 0.011129176 | 0.011129176 |
| 2001-09-05 | 57.74 | 56.02 | 1.0307033 | 0.030241404 | 0.030241404 |
| 2001-09-04 | 56.10 | 57.74 | 0.9715968 | -0.028814362 | -0.028814362 |
| 2001-08-31 | 57.05 | 56.10 | 1.0169340 | 0.016792264 | 0.016792264 |
| 2001-08-30 | 56.94 | 57.05 | 0.9980719 | -0.001929994 | -0.001929994 |
| 2001-08-29 | 60.25 | 56.94 | 1.0581314 | 0.056504491 | 0.056504491 |
| 2001-08-28 | 60.74 | 60.25 | 1.0081328 | 0.008099887 | 0.008099887 |
| 2001-08-27 | 62.31 | 60.74 | 1.0258479 | 0.025519467 | 0.025519467 |
| 2001-08-24 | 62.05 | 62.31 | 0.9958273 | -0.004181415 | -0.004181415 |
| 2001-08-23 | 59.12 | 62.05 | 0.9527800 | -0.048371235 | -0.048371235 |
| 2001-08-22 | 60.66 | 59.12 | 1.0260487 | 0.025715226 | 0.025715226 |
| 2001-08-21 | 60.78 | 60.66 | 1.0019782 | 0.001976285 | 0.001976285 |
| 2001-08-20 | 62.70 | 60.78 | 1.0315893 | 0.031100660 | 0.031100660 |
| 2001-08-17 | 61.00 | 62.70 | 0.9569362 | -0.044101100 | -0.044101100 |

```
In [70]: Xi <- MSFT$logPriceRat #Create an Array of all independent variables
Xi
X_bar <- mean(Xi, na.rm = TRUE) #this is the average
X_bar #this is the average
MSFT <- MSFT %>% mutate(DevFromMean = Xi - X_bar)
```

```
<NA> · -0.00885501969279577 · -0.012188687502058 ·
-0.00264242012772366 · 0.00821518996785407 · -0.0235856305843902 ·
-0.0300014480056963 · 0.00714056912606979 · -0.0615245253144932 ·
0.0124755954559475 · 0.0128250154759168 · 0.0420285098485961 ·
```

```

0.00577109649192187 · -0.0200200422334423 · -0.0146203836301462 ·
-0.00447799073188281 · -0.0382902950626349 · -0.0198855322871077 ·
-0.0129445907146487 · 0.0422844263408844 · -0.00669472932159364 ·
-0.0293624729105174 · -0.00106477383617953 · -0.0144865271477171 ·
-0.0172621711668632 · 0.0618314144807804 · -0.00552869411031694 ·
-0.0188882845202057 · -0.00726502708135401 · -0.0582155572441182 ·
-0.024037784624192 · -0.0120436576187996 · -0.0239307375596236 ·
0.00618579244710699 · 0.0202822744722398 · 0.0137452556082572 ·
-0.0452298876783998 · 0.0209025227396055 · 0.0594650938462554 ·
0.00831874655799834 · -0.0263001263344004 · 0.0845829282679896 ·
-0.0385956914307917 · 0.0111291760787245 · 0.0302414044028266 ·
-0.0288143617061385 · 0.0167922637794339 · -0.00192999445819315 ·
0.0565044905208729 · 0.00809988724683835 · 0.0255194669385279 ·
-0.00418141490551447 · -0.0483712350106699 · 0.0257152256204888 ·
0.00197628522821196 · 0.031100660150228 · -0.0131644219340096 ·
0.0433269346914869 · -0.0222196592435405 · 0.0233023289030823 ·
0.0174690314238913
1.01301730313107e-05

```

In [85]:

```

n = length(Xi) -1

Ssquared = sum(MSFT$DevFromMean, na.rm = TRUE) / n

S = sqrt(Ssquared)

n # number of observations
Ssquared
S # volatility parameter

```

```

60
1.04806210006932e-19
3.23737872370429e-10

```

In []:

#