

In [3]: `library("tidyverse")`

— **Attaching packages** — tidyverse
1.3.0 —

```
✓ ggplot2 3.3.3    ✓ purrr  0.3.4
✓ tibble  3.0.5    ✓ dplyr  1.0.3
✓ tidyr   1.1.2    ✓ stringr 1.4.0
✓ readr   1.4.0    ✓ forcats 0.5.1
```

— **Conflicts** — tidyverse_conflicts() —
✖ dplyr::filter() masks stats::filter()
✖ dplyr::lag() masks stats::lag()

In [4]: `##instantiate all the variables`

`##create a data frame with the closing prices`
`df <- read_csv("13.5.csv")`

`sigma <- 0.2 #the variance parameter`

`r <- 0.01`

`t <- 252 #there are 252 trading days in a year`

`K <- 52 #strike price`

`print(sigma)`
`print(r)`
`print(t)`

— **Column specification** —

```
cols(
  i = col_double(),
  Zi = col_double(),
  Si = col_double()
)
```

```
[1] 0.2
[1] 0.01
[1] 252
```

In [5]: `mu <- (0.01 - (sigma^2)/2) #drift parameter`

`print(mu)`

```
[1] -0.01
```

In [6]: `df <- df %>% mutate(i = as.integer(i))`

```
In [7]: #write a function that transforms the Zi normal to the price generated
normal_standard <- function(Zi, mu, sigma, t){

  #multiply Zi by the variance and devide by sqrt of 252 trading days
  xi <- Zi*(sigma/sqrt(t))

  #then add mu divided by the variance

  xi <- xi + (mu/252)

}

#test the function

xi <- normal_standard(-0.25,mu,sigma, t)

print(xi)
```

```
[1] -0.003189386
```

```
In [8]: #map the function over the data frame

df<- df%>% mutate(Xi = normal_standard(Zi, mu, sigma, t))

df %>% head(7)
```

A tibble: 7 × 4

i	Zi	Si	Xi
<int>	<dbl>	<dbl>	<dbl>
0	NA	50	NA
1	-0.25	NA	-0.003189386
2	0.30	NA	0.003739962
3	1.50	NA	0.018858541
4	-1.20	NA	-0.015158261
5	-1.65	NA	-0.020827729
6	1.50	NA	0.018858541

```
In [10]: #loop over the Xi vector to calculate closing prices
for (i in 1:nrow(df)){

  lead = i +1
  df$Si[[lead]] <- df$Si[[i]]*exp(1)^df$Xi[[lead]]

}
```

```
[1] 1
[1] 2
[1] 50
[1] -0.003189386
[1] 49.84078
[1] 2
[1] 3
```

```

[1] 49.84078
[1] 0.003739962
[1] 50.02754
[1] 3
[1] 4
[1] 50.02754
[1] 0.01885854
[1] 50.97993
[1] 4
[1] 5
[1] 50.97993
[1] -0.01515826
[1] 50.213
[1] 5
[1] 6
[1] 50.213
[1] -0.02082773
[1] 49.17799
[1] 6
[1] 7
[1] 49.17799
[1] 0.01885854
[1] 50.11421
[1] 7
[1] 8
Error in df$Xi[[lead]]: subscript out of bounds
Traceback:

```

```
1. print(df$Xi[[lead]])
```

In [11]: `df %>% head(7)`

A tibble: 7 × 4

i	Zi	Si	Xi
<int>	<dbl>	<dbl>	<dbl>
0	NA	50.00000	NA
1	-0.25	49.84078	-0.003189386
2	0.30	50.02754	0.003739962
3	1.50	50.97993	0.018858541
4	-1.20	50.21300	-0.015158261
5	-1.65	49.17799	-0.020827729
6	1.50	50.11421	0.018858541

Part 2

Generate 6 more simulated daily closing prices

```
In [87]: #generate 6 random points from a normal distribution

cent <- mu/t
dev <- (sigma^2)/t

print(cent)
print(dev)

#random normal generated values for Xi
rand_Xi <- rnorm(6, mean = cent, sd = dev)

print(rand_Xi)
```

```
[1] -3.968254e-05
[1] 0.0001587302
[1] -2.628115e-04  4.731965e-05  3.698051e-05 -1.415038e-05 -1.262229e-04
[6] -9.184504e-05
```

```
In [88]: #create an empty vector for Xi
Xi <- c()
#
Xi <- append(0,rand_vars)

print(Xi)
```

```
[1] 0.000000e+00 -1.381145e-05 -2.681216e-04  1.764453e-04  4.329975e-05
[6] 1.345644e-04 -1.725527e-04
[1] 0.000000e+00 -1.381145e-05 -2.681216e-04  1.764453e-04  4.329975e-05
[6] 1.345644e-04 -1.725527e-04
```

```
In [89]: #create a dataframe with the new vectors
df2 <-tibble(i = rep(0:6),
             Xi = Xi,
             Si = rep(NA,7) ) #add the closing prices

#adding day 1 price
df2$Si[1] <- 50

df2 %>%head()
```

A tibble: 6 × 3

	i	Xi	Si
	<int>	<dbl>	<dbl>
0	0	0.000000e+00	50
1	1	-1.381145e-05	NA
2	2	-2.681216e-04	NA
3	3	1.764453e-04	NA
4	4	4.329975e-05	NA

```
In [93]: df2 %>% head(7)
```

A tibble: 7 × 3

i	Xi	Si
<int>	<dbl>	<dbl>
0	0.000000e+00	50
1	-1.381145e-05	NA
2	-2.681216e-04	NA
3	1.764453e-04	NA
4	4.329975e-05	NA
5	1.345644e-04	NA
6	-1.725527e-04	NA

```
In [99]: for (n in 1:nrow(df2)){
  lead = n +1
  df2$Si[[lead]] <- df2$Si[[i]]*exp(1)^df2$Xi[[lead]]
}
```

```
[1] 0
[1] 50
[1] 1
[1] 49.99931
[1] 2
[1] 49.98591
[1] 3
[1] 49.99473
[1] 4
[1] 49.99689
[1] 5
[1] 50.00362
[1] 6
[1] 49.99499
```

```
In [100... df2
```

A tibble: 7 × 3

i	Xi	Si
<int>	<dbl>	<dbl>
0	0.000000e+00	50.00000
1	-1.381145e-05	49.99931
2	-2.681216e-04	49.98591
3	1.764453e-04	49.99473
4	4.329975e-05	49.99689

i xi Si

Problem 3

If the strike price of a European call is $K = 52$, and the expiration of this call is at the end of 6 days, what is the payoff on the call?, that is what is the value of $(S_6 - K)^+$?

The answer is zero because S_6 is less than the strike price

Problem 4

Could you use the present value of $(S_6 - K)^+$ in 3) as an approximation of the cost on the call.

In short yes, but a better method is to run the simulation for multiple times and take the average of the day 6 pay offs to get a better approximation of the risk neutral payoff.

In [127...

```
#calculate the PV of the strike price
```

```
PvK <- K*exp(1)^(r * (-6/252))
```

```
print(PvK)
```

```
[1] 51.98762
```

```

In [128... #instantiate an empty array
payout <- c()

#run the simulation 100 times
for (i in rep(1:10)){

  #print(i)

  #generate 6 closing prices from the distribution
  Xi <- rnorm(6, mean = cent, sd = dev)

  #instantiate an empty array of closing prices
  Si <- rep(NA,6)

  #adding day 1 price
  Si[1] <- 50

  #loop through the entire closing prices and convert Sd from the ran
  for(n in rep(1:length(Si))){

    lead = n+1
    Si[lead] = Si[n]*exp(1)^Xi[lead]

  }

  #calculate the payout
  if (Si[6] < PvK){
    pay <- 0
  }else{
    pay <- (Si[6] - PvK)
  }

  payout<- append(payout, pay)

}

#average the payout over the number of times the simulation was ran
valuation <- sum(payout) / length(payout)

#print the valuation
print(valuation)

```

```
[1] 0
```

```
In [119...
```

```
6
```

```
In [ ]:
```