Q3. No.

Counter Example

Consider the function $f(x) = x$ $\forall\ x \in \mathbb{R}$

clearly the function is not bounded below and

thus does not have global minimum.