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2-bosqich talabasi

Toshqobilov Shamshodbek ning  
Kriptografiyaning matematik asosi  
fanidan bajargan  
5,6-Amaliy ishlari

713-23 guruh  
MFC002-2



Fan o'qituvchisi: Qozoqova To'xtajon  
Qaxramon qizi

## Eyler funksiyasi, berilgan modul bo'yicha birlamchi ildizni hisoblashni SageMath instrumenti orqali amalga oshirish:

20-variant:

5-amaliy ish:

Eyler funksiyasi va uning ahamiyati, berilgan modul bo'yicha birlamchi ildizni hisoblash bo'yicha amaliy ko'nikmalarga ega bo'lish.

1) Berilgan qiymat bo'yicha Eyler funksiyasi qiymati hisoblansin

$n = 66$ ; 66 – Murakkab son va uni ishlasa bo'ladi:

$$66 = 2 * 3 * 11$$

$$\phi(66) = 66 * (1 - 1/2) * (1 - 1/3) * (1 - 1/11) = 66 * (1/2) * (2/3) * (10/11) = 20;$$

Demak, berilgan qiymat bo'yicha Eyler funksiyasi qiymati 20 ga teng ekan.

2) Berilgan modul bo'yicha birlamchi ildizlar soni va ularning qiymatlari topilsin

$n = 28$ ; 28- Murakkab son(Primitive root):

$$28 = 2^2 * 7$$

$$\phi(\phi(28)) = \phi(28 * (1 - 1/2) * (1 - 1/7)) = \phi(12)$$

$$12 = 2^2 * 3$$

$$\phi(12) = 12 * (1 - 1/2) * (1 - 1/3) = 4;$$

4 – Birlamchi ildizlar soni;

Endi bu misol uchun tub guvohlikni topamiz:

$$(2)^{28/2} * \text{mod}(28) = 4;$$

$$(3)^{28/2} * \text{mod}(28) = 9;$$

$$(5)^{28/2} * \text{mod}(28) = 25;$$

$$(7)^{28/2} * \text{mod}(28) = 21;$$

$$(11)^{28/2} * \text{mod}(28) = 9;$$

$$(13)^{28/2} * \text{mod}(28) = 1;$$

## 6-amaliy ish:

### 20-variant

#### Eyler va Gamilton graflari va ularni SageMath instrumentida amalga oshirish

Talabalarda SageMath dasturiy muhitidan foydalanib Gamilton va Eyler graflarini yaratish, vizuallashtirish hamda tekshirish bo'yicha amaliy ko'nikmalarni shakllantirishdan iborat.

- 1) Berilgan graf Eyler grafiga aylanishi uchun unga eng kam nechta qirra qo'shish kerak?

$V = \{A, B, C, D, E, F\}$

$E = \{AB, AC, BD, CE, CF, DE, DF, FA\}$

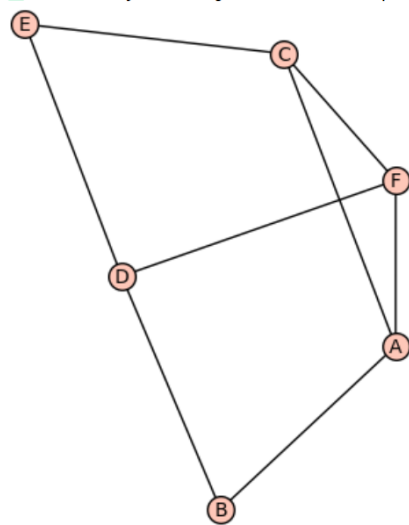


Type some Sage code below and press Evaluate.

```
1 # SageMath-da Gamilton siklni tekshirish
2 G = Graph()
3 # Tugunlar
4 V = ["A", "B", "C", "D", "E", "F"]
5 G.add_vertices(V)
6 # Qirralar
7 E = [("A", "B"), ("A", "C"), ("B", "D"), ("C", "E"), ("C", "F"),
8      ("D", "E"), ("D", "F"), ("F", "A")]
9 G.add_edges(E)
10 # Gamilton siklni tekshirish (xatolikni oldini olish)
11 try:
12     hamiltonian_cycle = G.hamiltonian_cycle()
```

Evaluate

✓ Gamilton sikl mavjud: TSP from  
✓ Gamilton yo'li mavjud: Hamiltonian path from



2) Berilgan grafda Gamilton sikli va Gamilton yo‘li mavjudmi? Agar bo‘lmasa uni hosil qilish uchun eng kam nechta qirra qo‘shish kerakligi aniqlansin.

$V = \{A, B, C, D, E, F, G, H, I, J, K, L, M, N\}$

$E = \{AB, BC, CD, DE, EF, FG, GH, HI, IJ, JK, KL, LM, MN, NA, BE\}$



Type some Sage code below and press Evaluate.

```
1 import sage.all as sg
2 import matplotlib.pyplot as plt
3 # Grafikni yaratamiz
4 V = ["A", "B", "C", "D", "E", "F", "G", "H", "I", "J", "K", "L", "M", "N"]
5 E = [("A", "B"), ("B", "C"), ("C", "D"), ("D", "E"), ("E", "F"), ("F", "G"), ("G", "H"), ("H", "I"),
6      ("I", "J"), ("J", "K"), ("K", "L"), ("L", "M"), ("M", "N"), ("N", "A"), ("B", "E")]
7 graph = sg.Graph()
8 graph.add_vertices(V)
9 graph.add_edges(E)
10 # Grafikni chizamiz
11 def draw_graph(G, title="Grafik"):
12     G.plot(vertex_labels=True, edge_labels=False, layout="spring")
13     show(title=title)
```

Evaluate

