## **Cue combination lecture notes**

## the maximum likelihood cue combination model

- two depth cues; r.v.'s D1, D2 with known standard deviations sigma1, sigma2
- assume cues are unbiased, with means mu1, mu2 (= mu)
- one sample from each cue, d1, d2
  - capitals for r.v.'s, lower case for samples
- what is the true depth? try an ML estimate
  - give formulas
  - -d = w1\*d1 + w2\*d2, with w1 = ..., w2 = ...
  - so our ML depth estimates are a new r.v., D = w1\*D1 + w2\*D2; w1 + w2 = 1
- what are the properties of this ML estimate?
- if mu1=mu2=mu, then E[D] = mu; also unbiased
- if  $mu1 \neq mu2$ , then E[D] = w1\*mu1 + w2\*mu2
  - so the results of a cue conflict experiment can be predicted from sigma1, sigma2
- $var[D] = sigma12^2$ , where  $1/sigma12^2 = 1/sigma1^2 + 1/sigma2^2$ 
  - smaller variance than either cue
  - note that this doesn't depend on mu1, mu2, or mu1-mu2

## testing the ML cue combination model

- how can we test the ML model? we need to measure sigma1, sigma2, mu12, sigma12
- we will use a model of the psychometric function in a 2afc task
  - task: shown two stimuli in random order; say which has a greater depth
  - difference rule: choose stimulus that has a greater decision variable

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R = A \text{ if } DA \ge DB, B if DB \ge DA
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- $-P(R=B) = P(DB>DA) = P(DA-DB<0) = pnorm(0, muA-muB, sqrt(sigmaA^2+sigmaB^2))$ 
  - if sigmaA=sigmaB=sigma, then
  - = pnorm(0, muA-muB, sqrt(2)\*sigma)
  - = pnorm( muB, muA, sqrt(2)\*sigma )
  - so if we hold muA fixed and vary muB, P(R=B) is a normal cdf
    - P(R=B)=0.5 where muA=muB; this is the PSE
      - useful, because we may not be controlling muA and muB directly
      - we may be controlling stimulus properties xA and xB, giving muA(xA), muB(xB), e.g., depth from disparity and depth from motion
      - it may be interesting to know the x for which muA(xA) = muB(xB)
    - standard deviation of normcdf is sqrt(2)\*sigma
      - so sigmaA=sigmaB=sigma can be estimated as sigma\_fit/sqrt(2)

- test 1: see whether sigma12 is as predicted
  - prediction:  $1/\text{sigma}12^2 = 1/\text{sigma}1^2 + 1/\text{sigma}2^2$
  - measure sigma1
    - let A be a fixed depth stimulus with cue 1; muA1
    - let B be a varying depth stimulus with cue 1; muB1
    - note that sigmaA=sigmaB (=sigma1)
    - measure psychometric function; then sigma1=sigma\_fit/sqrt(2)
  - measure sigma2 (same method as for sigma1)
    - let A be a fixed depth stimulus with cue 2; muA2
    - let B be a varying depth stimulus with cue 2; muB2
    - note that sigmaA=sigmaB (=sigma2)
    - measure psychometric function; then sigma2=sigma\_fit/sqrt(2)
  - measure sigma12 (same method as for sigma1)
    - let A be a fixed depth stimulus with cues 1 and 2; muA1, muA2
      - note that it doesn't matter here whether muA1=muA2; sigmaA is the same
    - let B be a varying depth stimulus with cues 1 and 2; muB1, muB2
      - let this be a consistent stimulus, muB1=muB2
    - note that sigmaA=sigmaB (=sigma12)
    - measure psychometric function; then sigma12=sigma\_fit/sqrt(2)
- test 2: see whether w1 and w2 are as predicted
  - prediction: w1 = ..., w2 = ...
  - use measurements of sigma1, sigma2 from test 1 to calculate w1, w2
  - measure a PSE between consistent and inconsistent stimuli
    - let A be a cue conflict stimulus of fixed depth; muA1≠muA2
    - let B be a consistent stimulus of varying depth; muB1=muB2=muB
    - measure a psychometric function and PSE
      - PSE should be at muB = w1\*muA1 + w2\*muA2