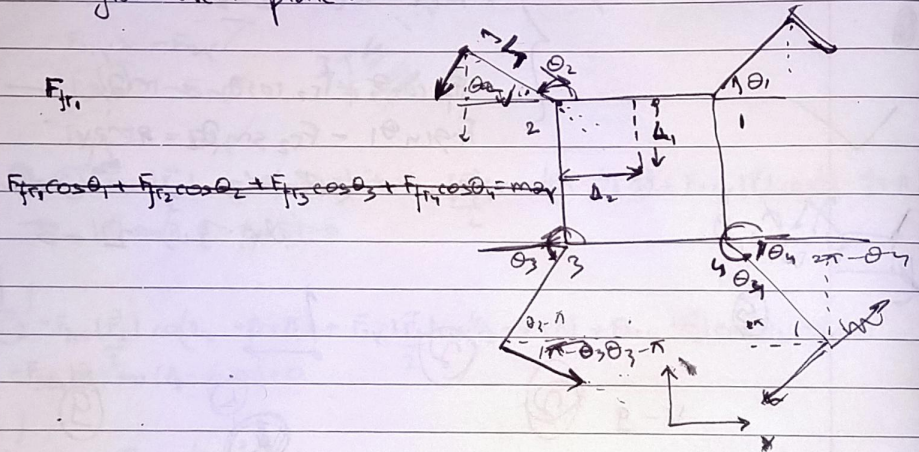




- When making the following assumptions are made
1. Assuming that kinetic friction acting at point of contact ~~is~~ ~~no slipping at the point of contact with the ground~~
 2. The angular acceleration at the joints is 0 at the driving joints is 0
 3. The friction forces is what causes the quadruped to move
 4. All equations together form a system of linear equations.
 5. Movement is along a flat plan even plane. or atleast the point of contacts with the ground form flat even plane.



$$F_{f1} \cos \theta_1 + F_{f2} \cos \theta_2 + F_{f3} \cos \theta_3 + F_{f4} \cos \theta_4 = m a_x$$

$$F_{f1} \cos \theta_1 + F_{f2} \cos \theta_2 + F_{f3} \cos \theta_3 + F_{f4} \cos \theta_4 = m a_x$$

$$F_{f1} \sin \theta_1 + F_{f2} \sin \theta_2 + F_{f3} \sin \theta_3 + F_{f4} \sin \theta_4 = m a_y$$

$$y_1 N_1 + y_2 N_2 + y_3 N_3 + y_4 N_4 = m a_z$$

where $y_i = \begin{cases} 0 & \text{if leg } i \text{ is not in contact with the ground} \\ 1 & \text{if the leg } i \text{ is in contact with the ground} \end{cases}$

Shree

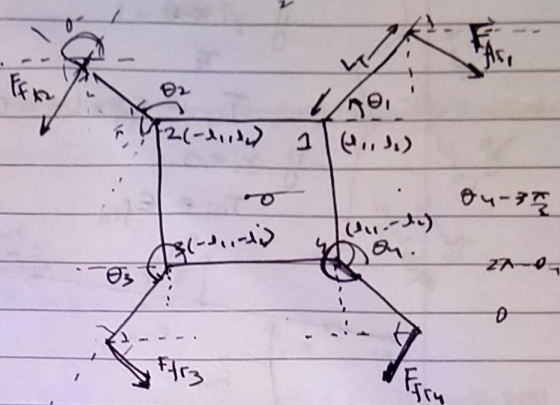
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$\pi - \theta_1$ $\theta_2 - \pi$

net $F_1 \cos \theta_1 + F_2 \cos(\pi - \theta_2) + F_3$



$$F_1 \cos \theta_1 + F_2 \cos(\pi - \theta_2) + F_3 \cos\left(\frac{3\pi}{2} - \theta_3\right) + F_4 \cos\left(\theta_4 - \frac{3\pi}{2}\right) = m a_y = F_y$$

$$F_1 \sin \theta_1 - F_2 \sin(\pi - \theta_2) + F_3 \sin\left(\frac{3\pi}{2} - \theta_3\right) - F_4 \sin\left(\theta_4 - \frac{3\pi}{2}\right) = m a_x = F_x$$

$$y_1 N_1 + y_2 N_2 + y_3 N_3 + y_4 N_4 = m a_z = m a_z = F_z$$

where $y_i = \begin{cases} 0 & \text{if foot } i \text{ is in contact with the } z\text{-channel} \\ 1 & \text{if foot } i \text{ is in contact with the ground.} \end{cases}$

$$F_{f1} \leq \mu N_1$$

$$F_{f2} \leq \mu N_2$$

$$F_{f3} \leq \mu N_3$$

$$F_{f4} \leq \mu N_4$$

$$F_{f1} = \mu N_1$$

$$F_{f2} = \mu N_2$$

$$F_{f3} = \mu N_3$$

$$F_{f4} = \mu N_4$$

$$\vec{P}_{N_1} = (l_1 + r \cos \theta_1) \hat{i} + (l_2 + r \sin \theta_1) \hat{j} + 0 \hat{k}$$

$$\vec{P}_{N_2} = (-l_1 + r \cos \theta_2) \hat{i} + (l_2 + r \sin \theta_2) \hat{j} + 0 \hat{k}$$

$$\vec{P}_{N_3} = (-l_1 + r \cos \theta_3) \hat{i} + (-l_2 + r \sin \theta_3) \hat{j} + 0 \hat{k}$$

$$\vec{P}_{N_4} = (l_1 + r \cos \theta_4) \hat{i} + (-l_2 + r \sin \theta_4) \hat{j} + 0 \hat{k}$$

$$\vec{F}_{f1} = F_{f1} (\cos \theta_1 \hat{i} + \sin \theta_1 \hat{j} + 0 \hat{k})$$

$$\vec{F}_{f2} = F_{f2} (\cos$$

$$\vec{F}_{f1} = F_{f1} (\cos(\theta_1 - \frac{\pi}{2}) \hat{i} + \sin(\theta_1 - \frac{\pi}{2}) \hat{j})$$

$$\vec{F}_{f2} = F_{f2} (\cos(\theta_2 + \frac{\pi}{2}) \hat{i} + \sin(\theta_2 + \frac{\pi}{2}) \hat{j})$$

$$\vec{F}_{f3} = F_{f3} (\cos(\theta_3 + \frac{\pi}{2}) \hat{i} + \sin(\theta_3 + \frac{\pi}{2}) \hat{j})$$

$$\vec{F}_{f4} = F_{f4} (\cos(\theta_4 - \frac{\pi}{2}) \hat{i} + \sin(\theta_4 - \frac{\pi}{2}) \hat{j})$$

$$\vec{F}_{f1} \times \vec{P}_{N_1} + \vec{F}_{f2} \times \vec{P}_{N_2} + \vec{F}_{f3} \times \vec{P}_{N_3} + \vec{F}_{f4} \times \vec{P}_{N_4} = N_z \hat{k}$$

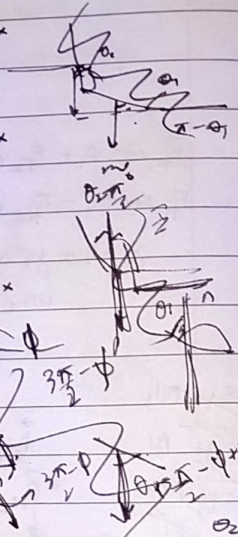
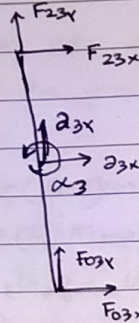
$$\sum |\vec{F}_{f_i} \times \vec{P}_{N_i}| y_i = N_z$$

$$y_4 N_4 (l_1 + r \cos \theta_4) + y_1 N_1 (l_1 + r \cos \theta_1) + y_2 N_2 (-l_2 + r \cos \theta_2) + y_3 N_3 (-l_1 + r \cos \theta_3) = N_z$$

$$y_1 N_1 (l_2 + r \sin \theta_1) + y_2 N_2 (l_2 + r \sin \theta_2) + y_3 N_3 (-l_2 + r \sin \theta_3) + y_4 N_4 (-l_2 + r \sin \theta_4) = N_x$$

~~4-20-2010~~

where E_{fm} is a constant



$$F_{01y} + F_{21y} = m_1 a_{1y}$$

$$T^* - m_2 p^*$$

$$F_{\text{max}} \frac{r_1}{2} (\cos(\theta_1 - \phi + \pi) + \cos(\theta_1 - \phi + \pi)) + F_{2, y} \frac{r_2}{2} \cos(\theta_2 - \phi + \pi) - F_{2, x} \frac{r_2}{2}$$

V 14 14 14 14 11
E 13 13 13 13 10

13

13

13

✓

$$\frac{\pi}{2} \rightarrow \theta, -\pi$$
$$\theta_{1-\frac{\alpha}{2}}$$
 $\Theta_1 - \pi$



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6 + 1

(1)

F

$$F_{01x} + F_{11x} = m_1 a_{1x}$$

$$F_{01y} + F_{11y} = m_1 a_{1y}$$

$$T - m_1 g \frac{|\vec{r}_1|}{2} \cos(\theta_1 - \phi + \pi) + m_1 a_{1x} \frac{|\vec{r}_1|}{2} \sin(\theta_1 - \phi + \pi) + F_{11x} |\vec{r}_1| \cos(\theta_1 - \phi + \pi) - F_{11y} |\vec{r}_1| \sin(\theta_1 - \phi + \pi) = I_1 \alpha_1$$

$$F_{12x} + F_{21x} + N \cos(\theta_2 - \phi + \pi) = m_2 a_{2x}$$

$$T + F_{01x} \frac{|\vec{r}_1|}{2} \sin(\theta_1 - \phi + \pi) - F_{01y} \frac{|\vec{r}_1|}{2} \sin(\theta_1 - \phi + \pi) - F_{11x} \frac{|\vec{r}_1|}{2} \cos(\theta_1 - \phi + \pi) + F_{11y} \frac{|\vec{r}_1|}{2} \cos(\theta_1 - \phi + \pi) = I_1 \alpha_1$$

$$F_{01x} + F_{21x} = m_1 a_{1x}$$

$$F_{01x} + F_{21x} - m_1 g \cos(\phi - \frac{3\pi}{2}) = m_1 a_{1x}$$

$$F_{01y} + F_{21y} - m_1 g \sin(\phi - \frac{3\pi}{2}) = m_1 a_{1y}$$

$$F_{01x} + F_{21x} - m_1 g \cos(\phi - \frac{3\pi}{2}) = m_1 a_{1x}$$

$$F_{01y} + F_{21y} - m_1 g \sin(\phi - \frac{3\pi}{2}) = m_1 a_{1y}$$

$$F_{12x} \sin(\theta_2 - \phi + \pi) \frac{|\vec{r}_2|}{2} - F_{22x} \frac{|\vec{r}_2|}{2} \sin(\theta_2 - \phi + \pi) - F_{12y} \frac{|\vec{r}_2|}{2} \cos(\theta_2 - \phi + \pi) + F_{21y} \frac{|\vec{r}_2|}{2} \cos(\theta_2 - \phi + \pi) = I_2 \alpha_2$$

$$F_{12x} + F_{32x} + N \cos(\theta_2 - \phi + \pi) - m_2 g \cos(\phi - \frac{3\pi}{2}) = m_2 a_{2x}$$

$$F_{12y} + F_{32y} + N \sin(\theta_2 - \phi + \pi) - m_2 g \sin(\phi - \frac{3\pi}{2}) = m_2 a_{2y}$$

$$F_{03x} \sin(\theta_3 - \phi + \pi) \frac{|\vec{r}_3|}{2} - F_{23x} \frac{|\vec{r}_3|}{2} \sin(\theta_3 - \phi + \pi) - F_{03y} \frac{|\vec{r}_3|}{2} \cos(\theta_3 - \phi + \pi) + F_{23y} \frac{|\vec{r}_3|}{2} \cos(\theta_3 - \phi + \pi) = I_3 \alpha_3$$

$$F_{03x} + F_{23x} - m_3 g \cos(\phi - \frac{3\pi}{2}) = m_3 a_{3x}$$

$$F_{03y} + F_{23y} - m_3 g \sin(\phi - \frac{3\pi}{2}) = m_3 a_{3y}$$

$$F_{12x} = -F_{21x} \quad F_{12y} = -F_{21y}$$

$$F_{23x} = -F_{32x} \quad F_{23y} = -F_{32y}$$