PCFGs: Parsing & Evaluation

LING 571 — Deep Processing Techniques for NLP
October 12, 2022
Shane Steinert-Threlkeld

Announcements

- HW2 due Friday at 11:59pm
 - readme.{txtlpdf}
 - Separate upload to Canvas
 - NOT in hw2.tar.gz
 - Run check_hw2.sh before submitting!
- Start symbol: either "%start S" or first nonterminal
 - NB: needs to be readable by nltk's grammar loading methods
- Condor job: runs conversion, but not parsing before/after; that can be done separately

Roadmap

- CKY + back-pointers
- PCFGs
- PCFG Parsing (PCKY)
- Inducing a PCFG
- Evaluation
- [Earley parsing]
- HW3 + collaboration

CKY Parsing: Backpointers

Backpointers

- Instead of list of possible nonterminals for that node, each cell should have:
 - Nonterminal for the node
 - Pointer to left and right children cells
 - Either direct pointer to cell, or indices

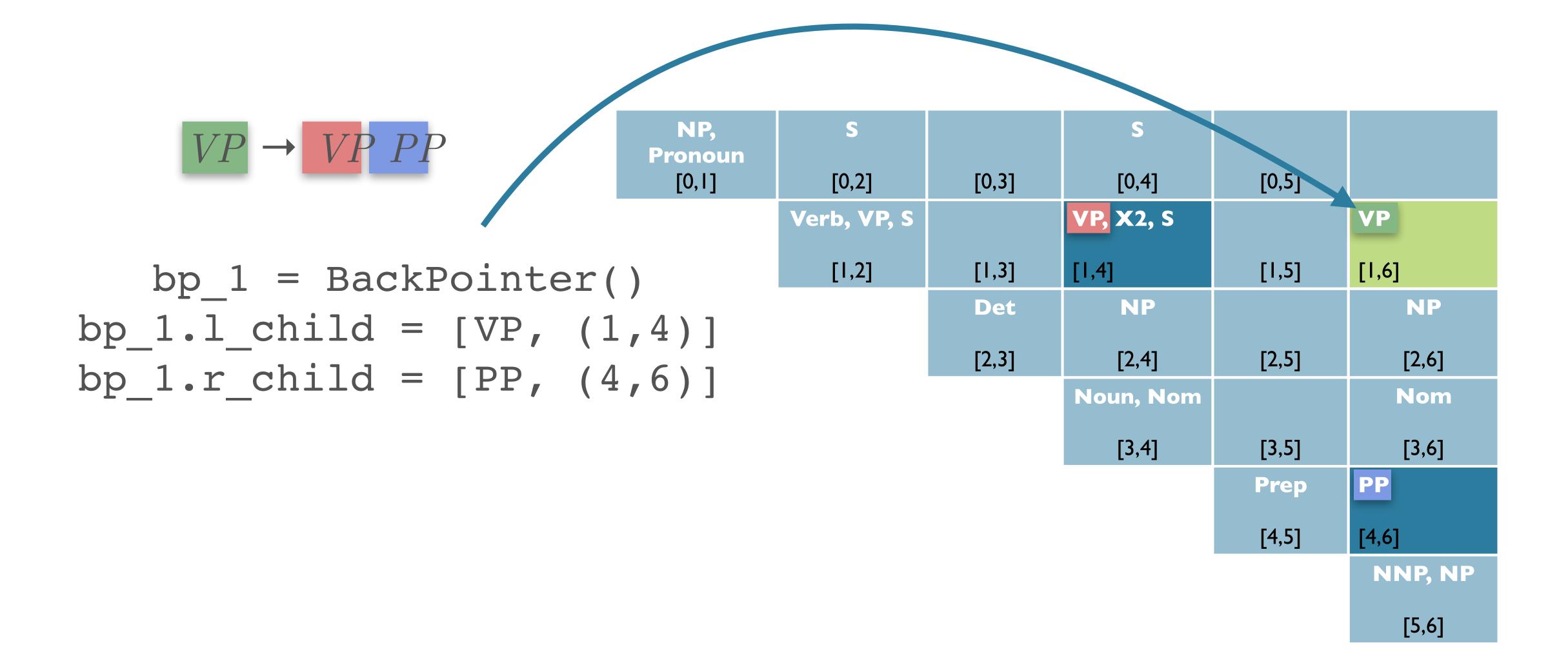
For example:

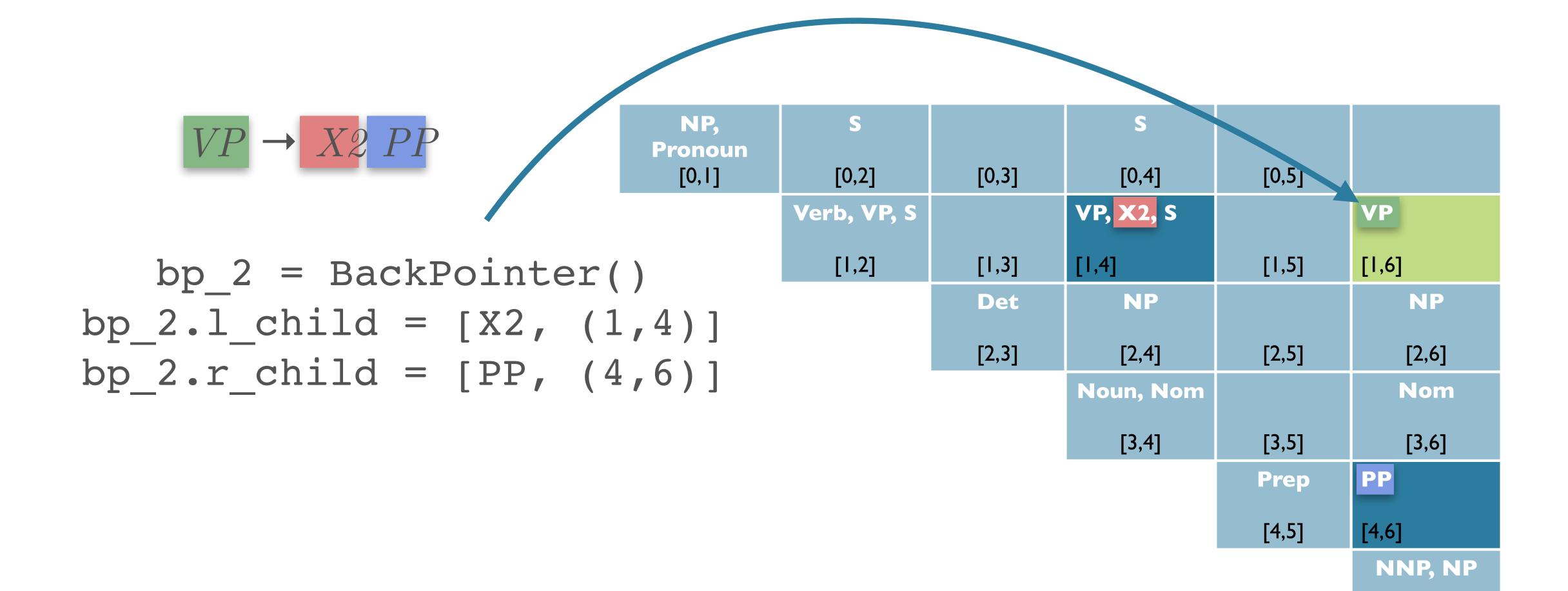
```
bp_2 = BackPointer()
bp_2.l_child = [X2, (1,4)]
bp 2.r child = [PP, (4,6)]
```

CKY Parser

- Pair each nonterminal with back-pointer to cells from which it was derived
- Last step:
 - construct trees from back-pointers in [0, n]

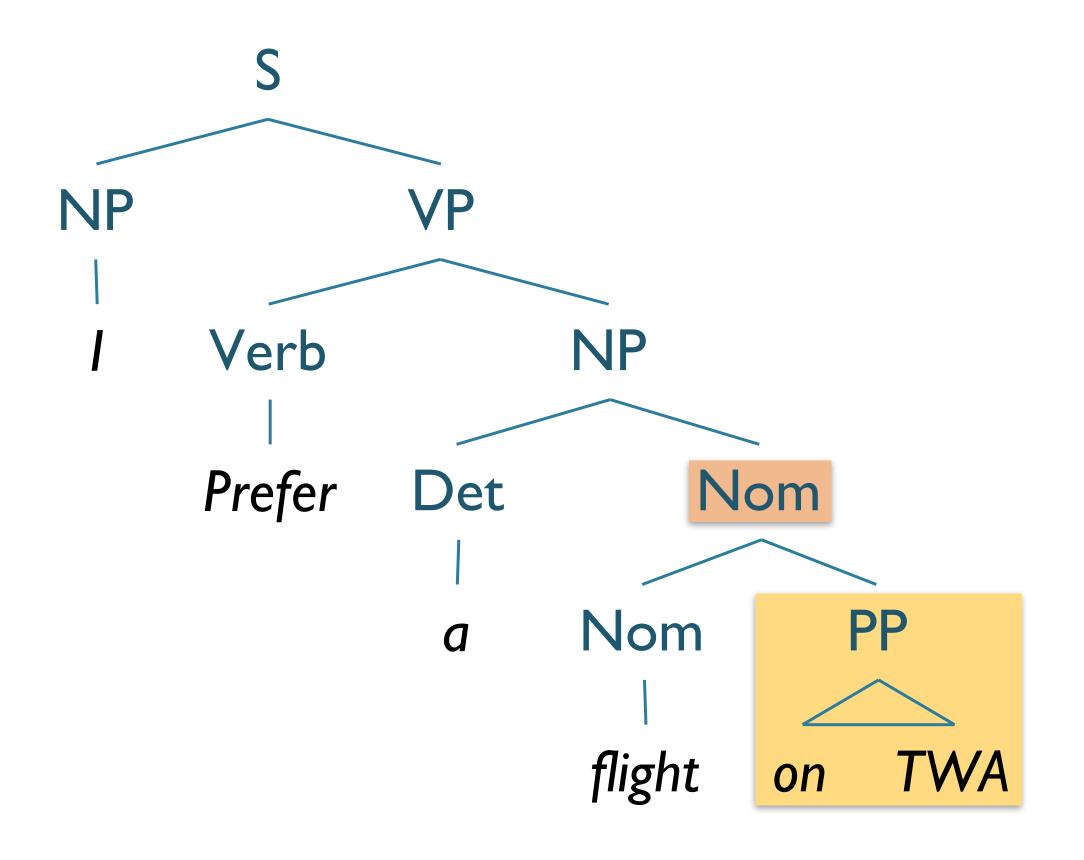
NP, Pronoun	S		S		
[0,1]	[0,2]	[0,3]	[0,4]	[0,5]	
	Verb, VP, S		VP, X2, S		VP
	[1,2]	[1,3]	[1,4]	[1,5]	[1,6]
		Det	NP		NP
		[2,3]	[2,4]	[2,5]	[2,6]
			Noun, Nom		Nom
			[3,4]	[3,5]	[3,6]
				Prep	PP
				[4,5]	[4,6]
					NNP, NP
					[5,6]

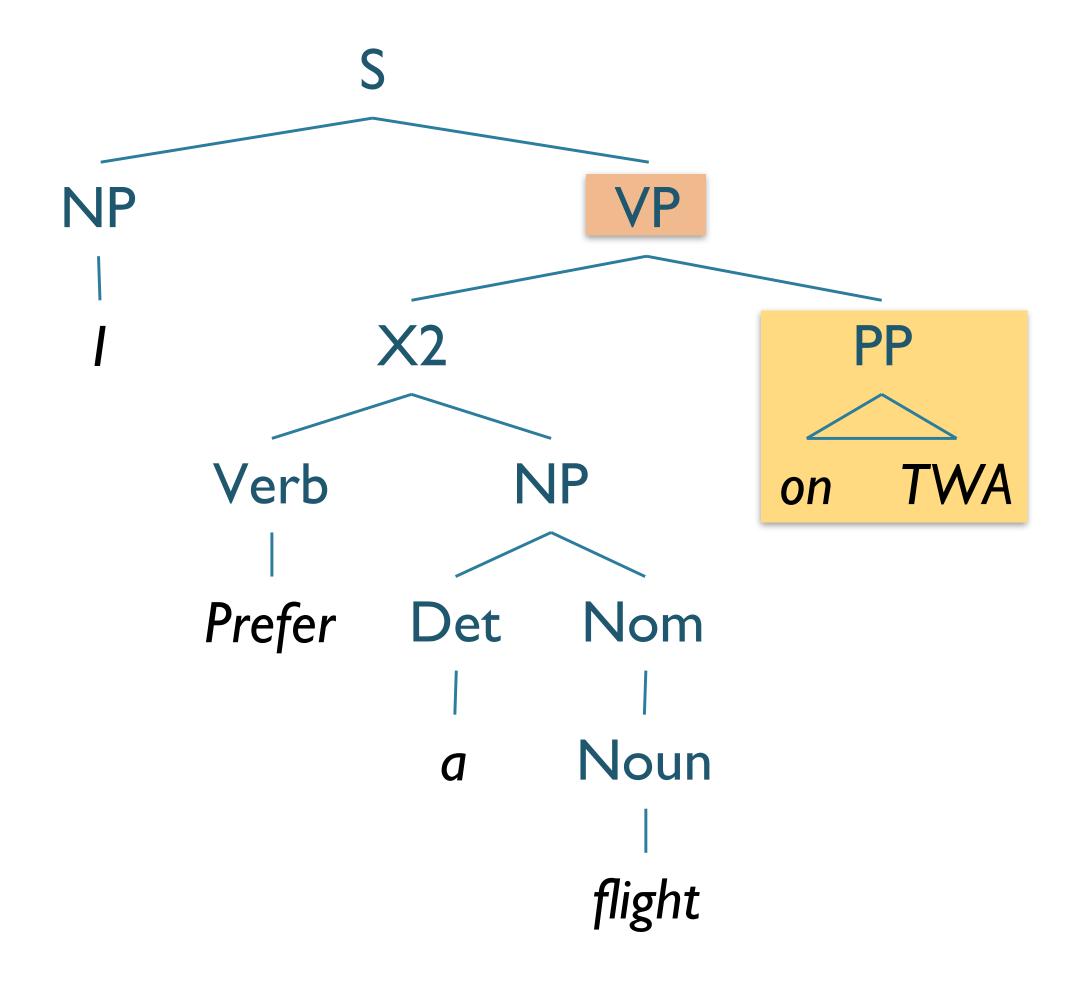




[5,6]

Resulting Parses

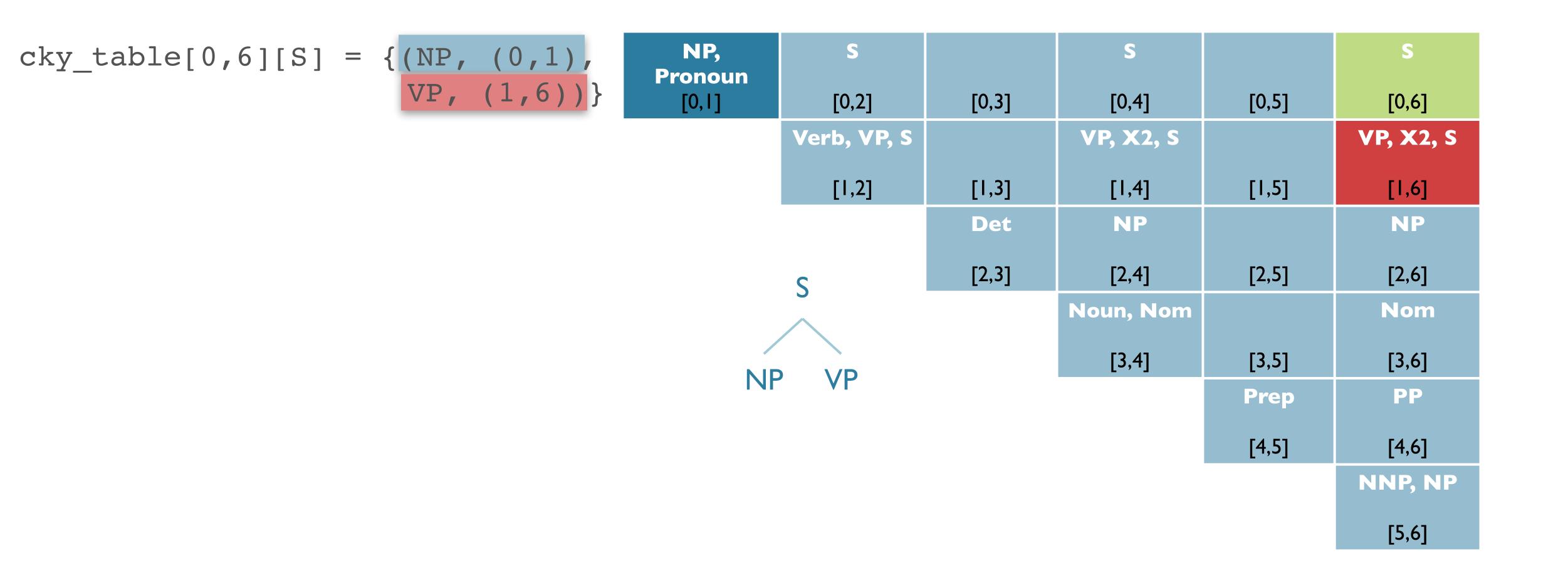


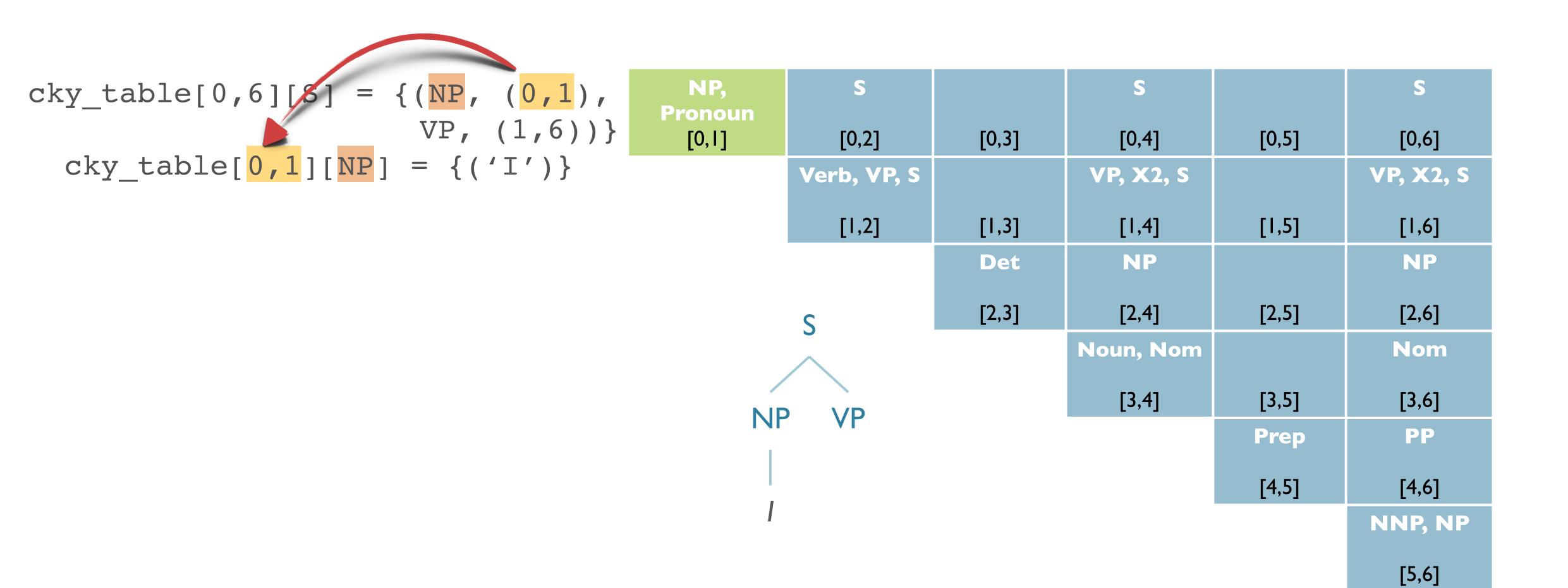


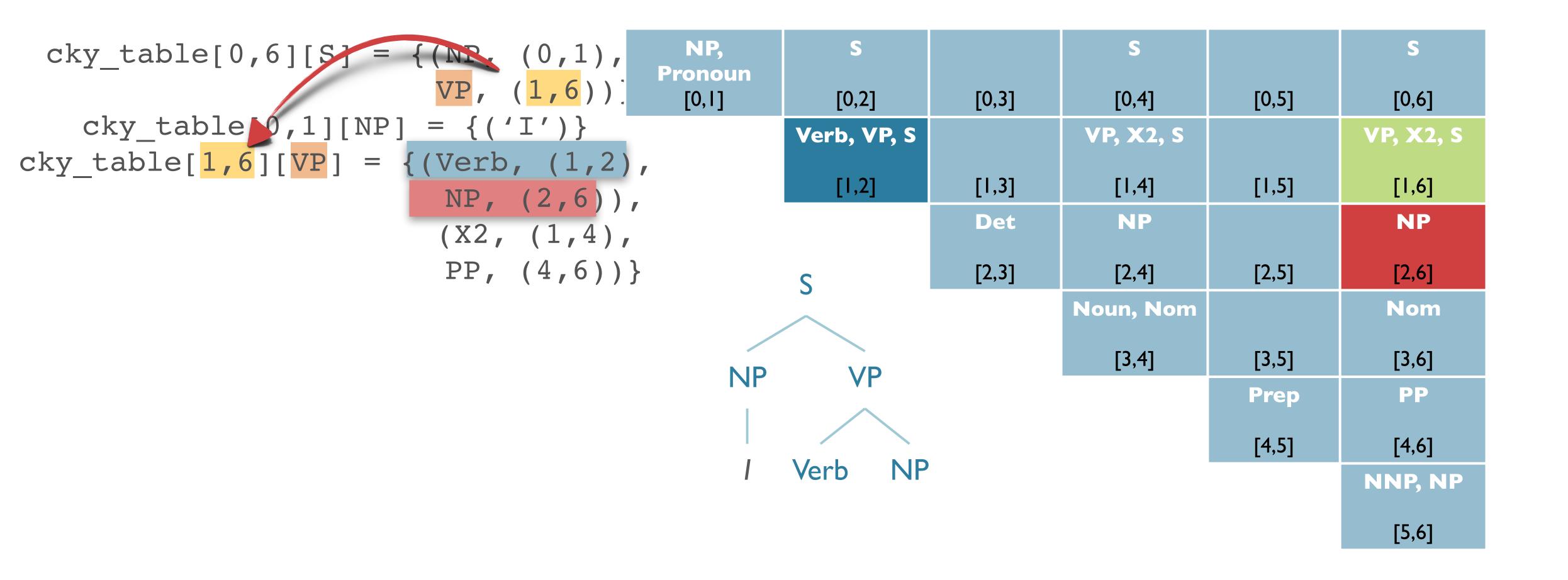
CKY Discussion

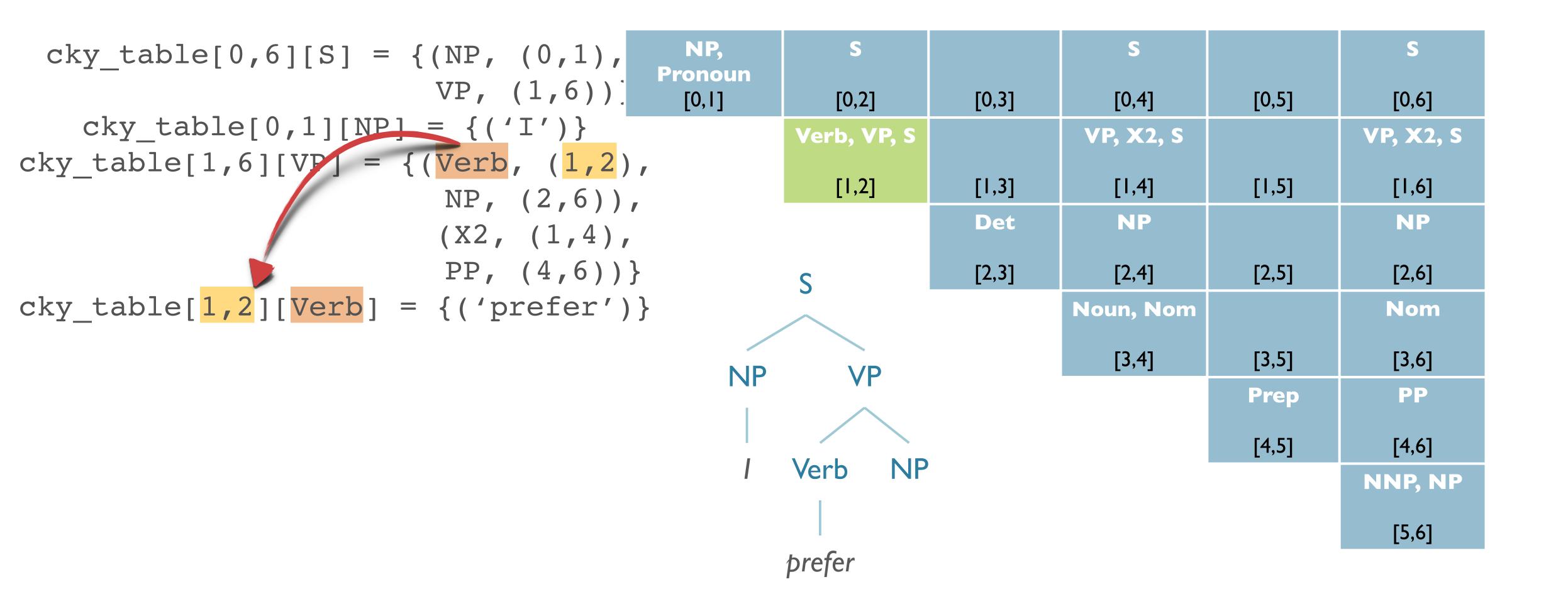
- Running time:
 - ullet $O(n^3)$ where n is the length of the input string
 - Inner loop grows as square of # of non-terminals
- Expressiveness:
 - As implemented, requires CNF
 - Weak equivalence to original grammar
 - Doesn't capture full original structure
 - Back-conversion?
 - Can do binarization, terminal conversion
 - Unit productions requires change in CKY

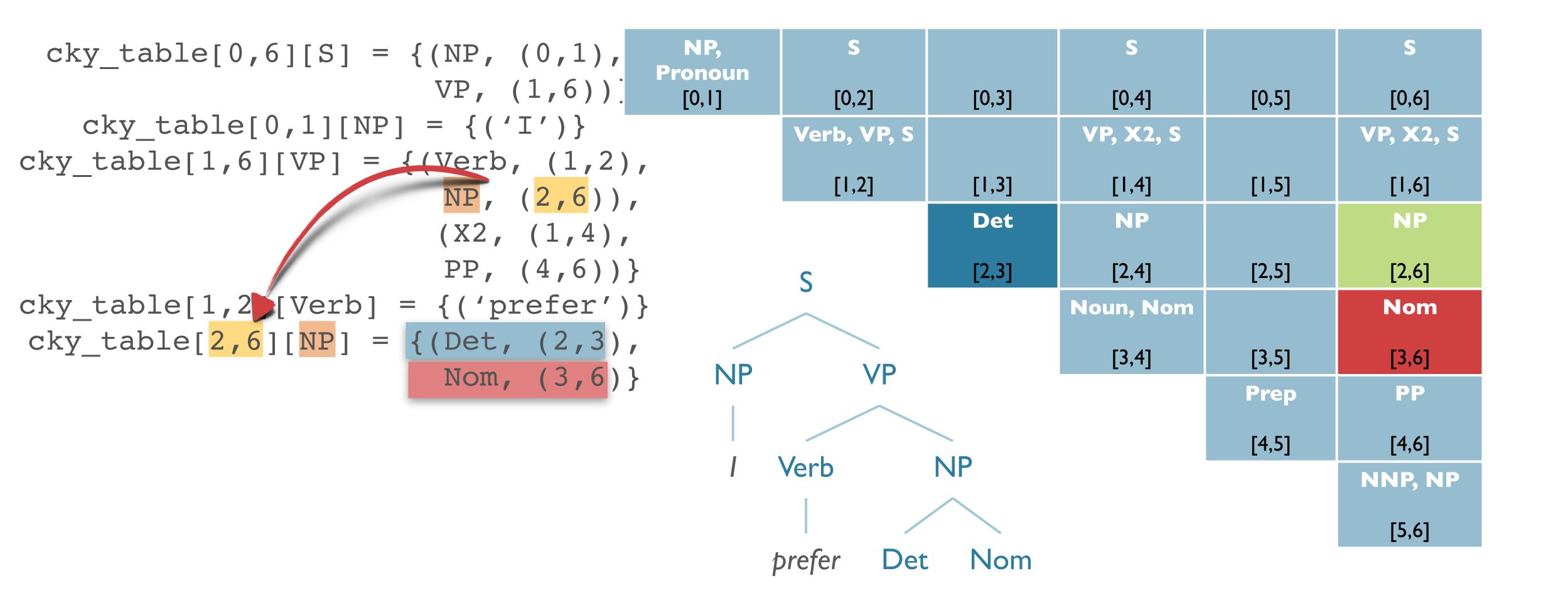
CKY + Back-pointers Example

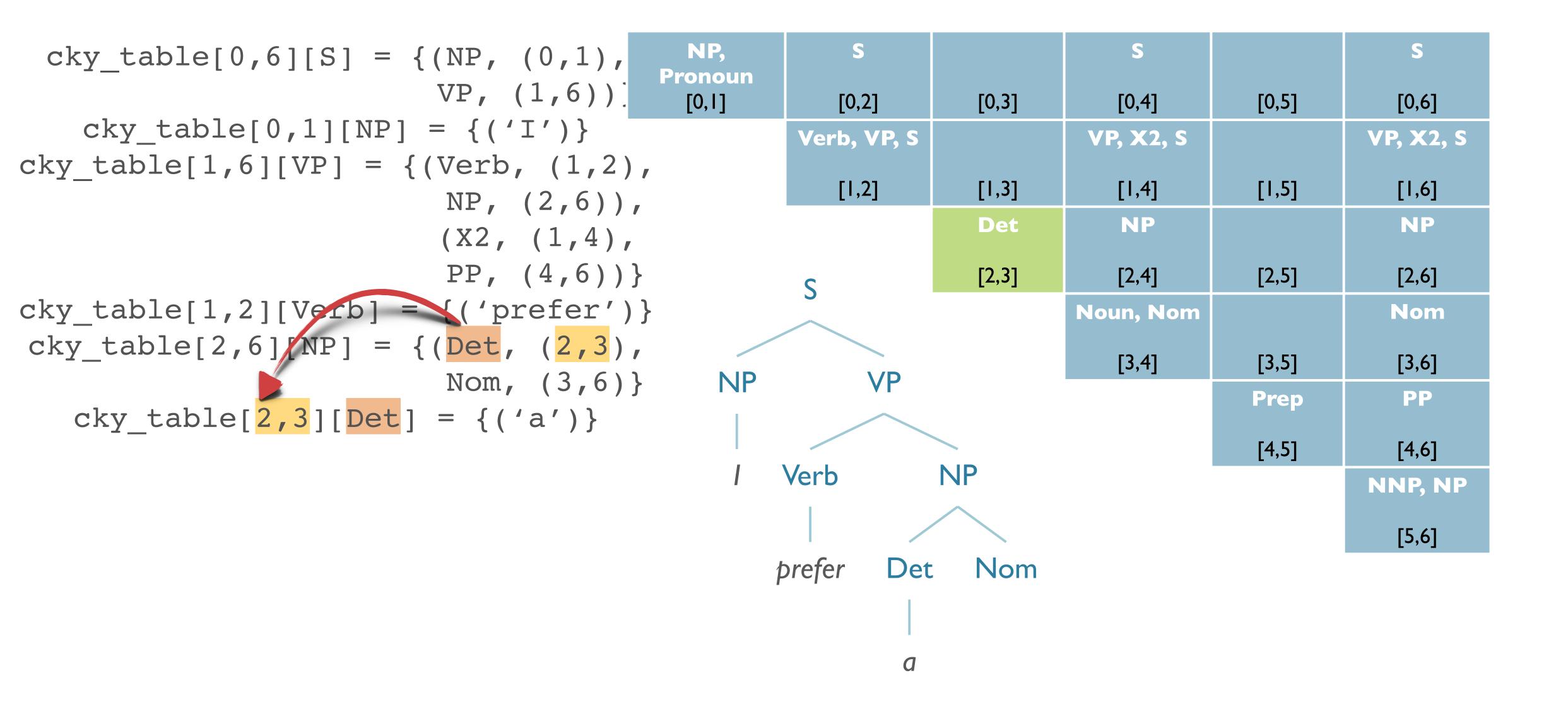




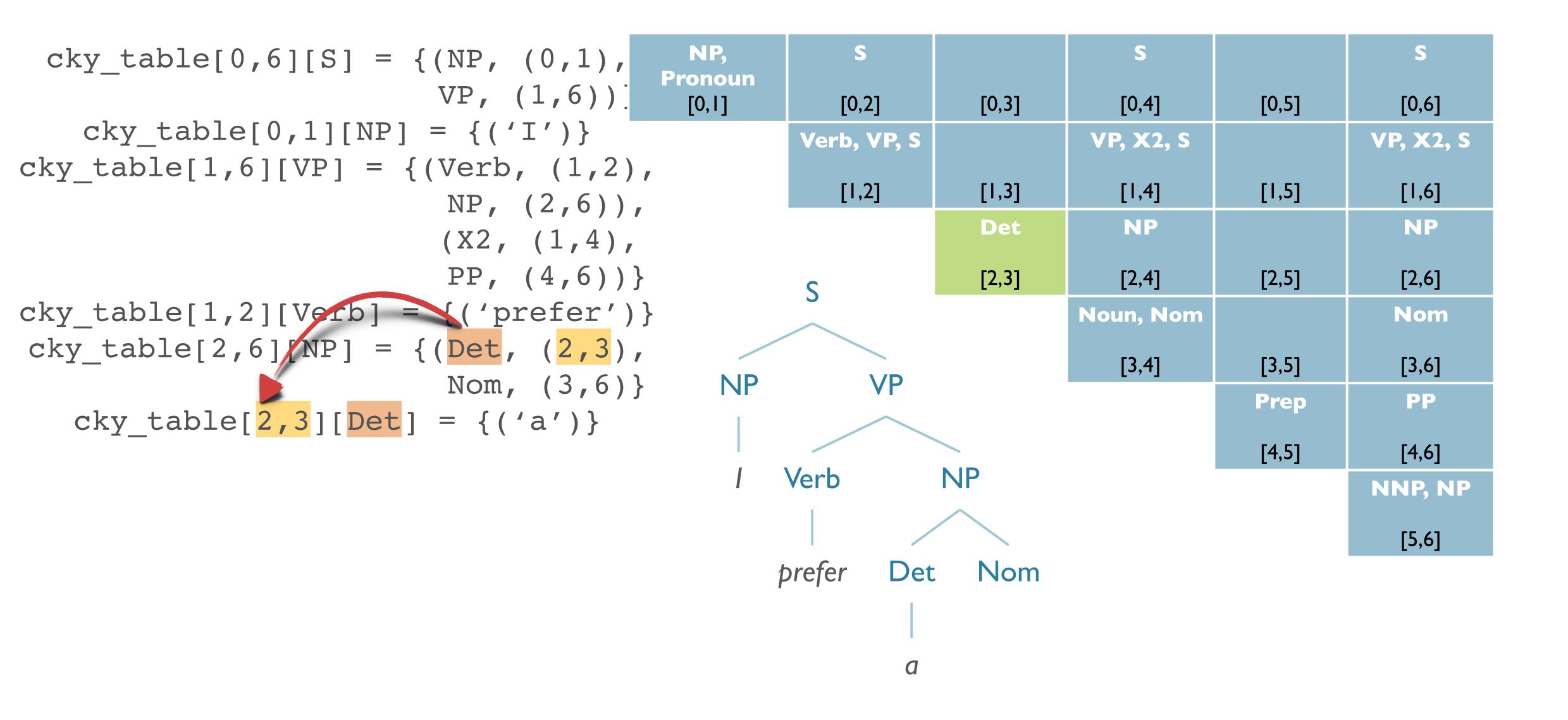


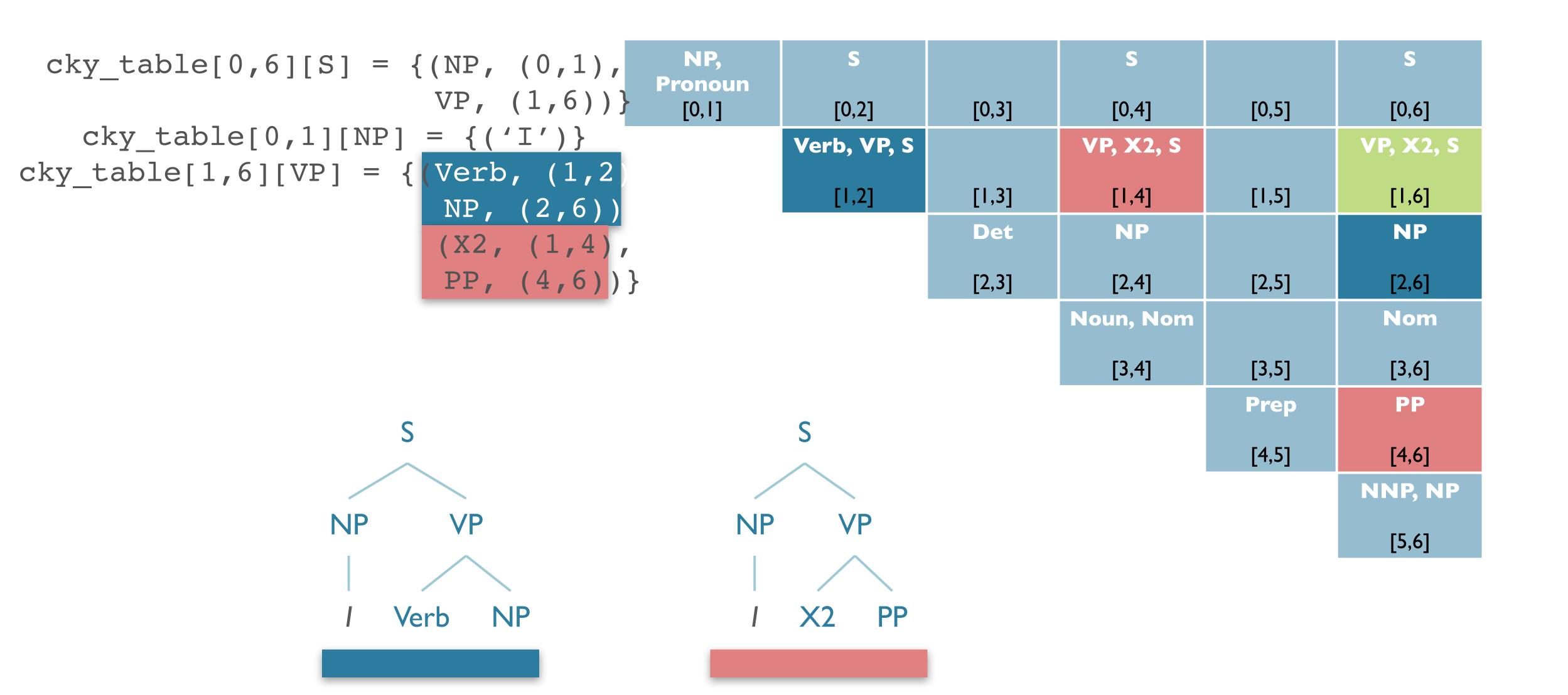






TWA





Probabilistic Context-Free Grammars

Probabilistic Context-free Grammars: Roadmap

Motivation: Ambiguity

Approach:

Definition

Disambiguation

Parsing

Evaluation

Enhancements

Motivation

What about ambiguity?

Current algorithm can *represent* it

...can't resolve it.

Probabilistic Parsing

- Provides strategy for solving disambiguation problem
 - Compute the probability of all analyses
 - Select the most probable

- Employed in language modeling for speech recognition
 - N-gram grammars predict words, constrain search
 - Also, constrain generation, translation

N

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R	a set of rules of productions, each of the form $A o eta[p]$, where A is a non-terminal where A is a non-terminal, eta is a string of symbols from the infinite set of strings $(\Sigma\cup N)_*$ and p		
	is a number between 0 and 1 expressing $P(oldsymbol{eta} oldsymbol{A})$		

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\overline{S}	a designated start symbol

PCFGs

- Augment each production with probability that LHS will be expanded as RHS
 - $\bullet P(A \rightarrow \beta)$
 - $\bullet P(A \rightarrow \beta | A)$
 - $\bullet P(\beta|A)$
 - \bullet $P(RHS \mid LHS)$
- NB: the first is often used; but the latter are what's really meant.

PCFGs

Sum over all possible expansions is 1

$$\sum_{\beta} P(A \to \beta) = 1$$

- A PCFG is consistent if sum of probabilities of all sentences in language is 1
 - Recursive rules often yield inconsistent grammars (Booth & Thompson, 1973)

Example PCFG: Augmented \mathcal{L}_1

Grammar		Lexicon
$S \rightarrow NP \ VP$	[.80]	$Det \rightarrow that [.10] \mid a [.30] \mid the [.60]$
$S \rightarrow Aux NP VP$	[.15]	$Noun \rightarrow book [.10] \mid flight [.30] \mid meal [.15] \mid money [0.5]$
$S \rightarrow VP$	[.05]	$ \mathit{flights}\ [0.40]\ \ \mathit{dinner}\ [.10]$
$NP \rightarrow Pronoun$	[.35]	$Verb \rightarrow book [.30] \mid include [.30] \mid prefer [.40]$
$NP \rightarrow Proper-Noun$	[.30]	$Pronoun \rightarrow I[.40] \mid she[.05] \mid me[.15] \mid you[.40]$
$NP \rightarrow Det\ Nominal$	[.20]	$Proper-Noun \rightarrow Houston [.60] \mid NWA [.40]$
$NP \rightarrow Nominal$	[.15]	$Aux \rightarrow does [.60] \mid can [.40]$
$Nominal \rightarrow Noun$	[.75]	$Preposition \rightarrow from [.30] \mid to [.30] \mid on [.20] \mid near [.15]$
$Nominal \rightarrow Nominal \ Noun$	[.20]	$\mid through \; [.05]$
$Nominal \rightarrow Nominal PP$	[.05]	
$VP \rightarrow Verb$	[.35]	
$VP \rightarrow Verb NP$	[.20]	
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$PP \rightarrow Preposition NP$	[1.0]	

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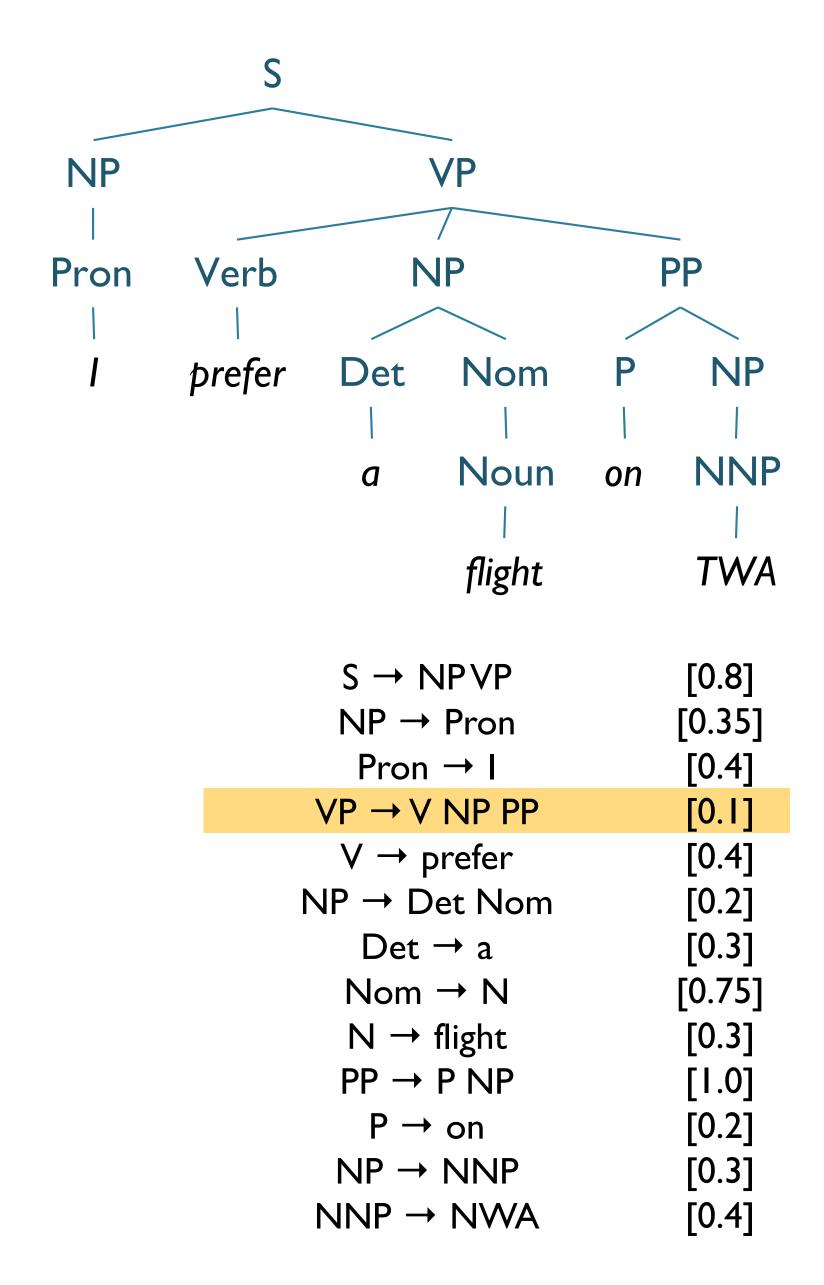
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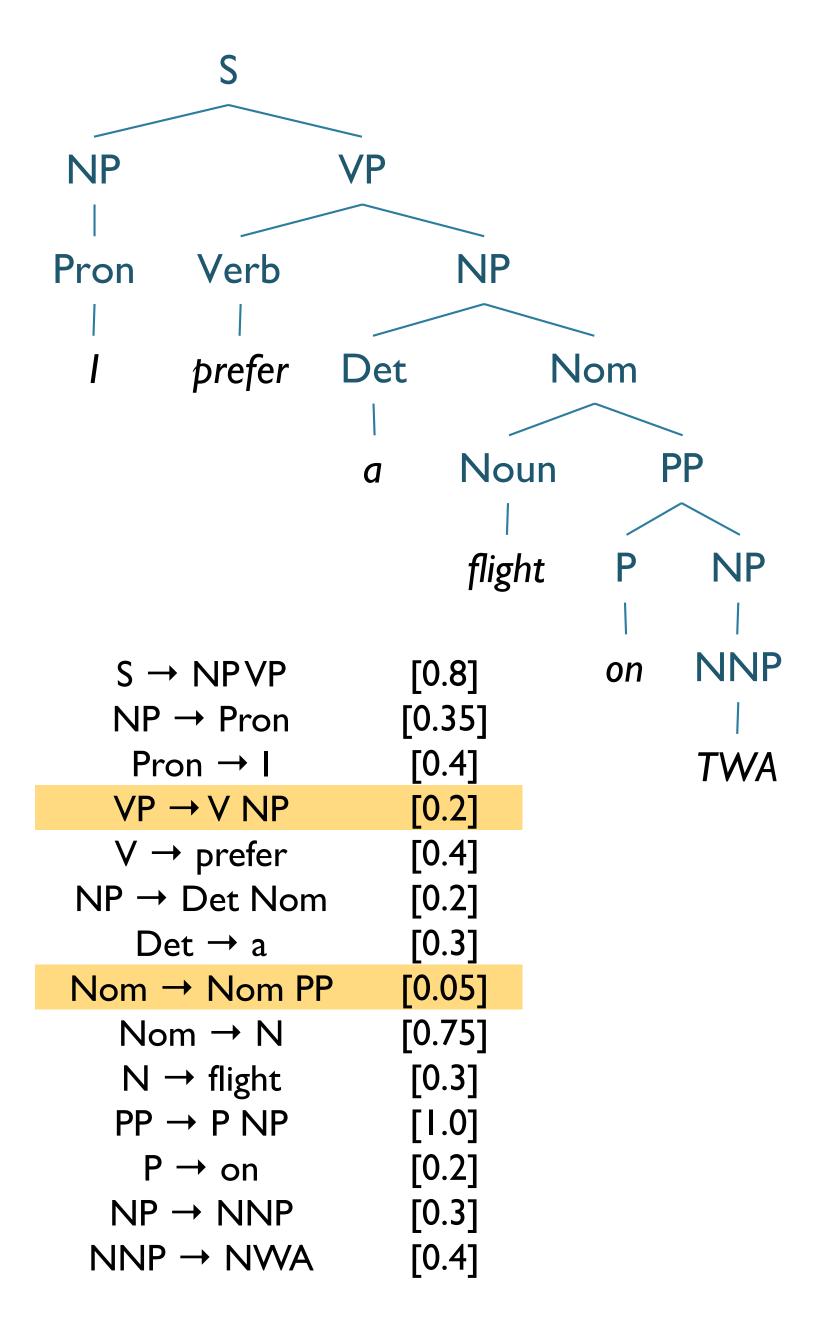
Disambiguation

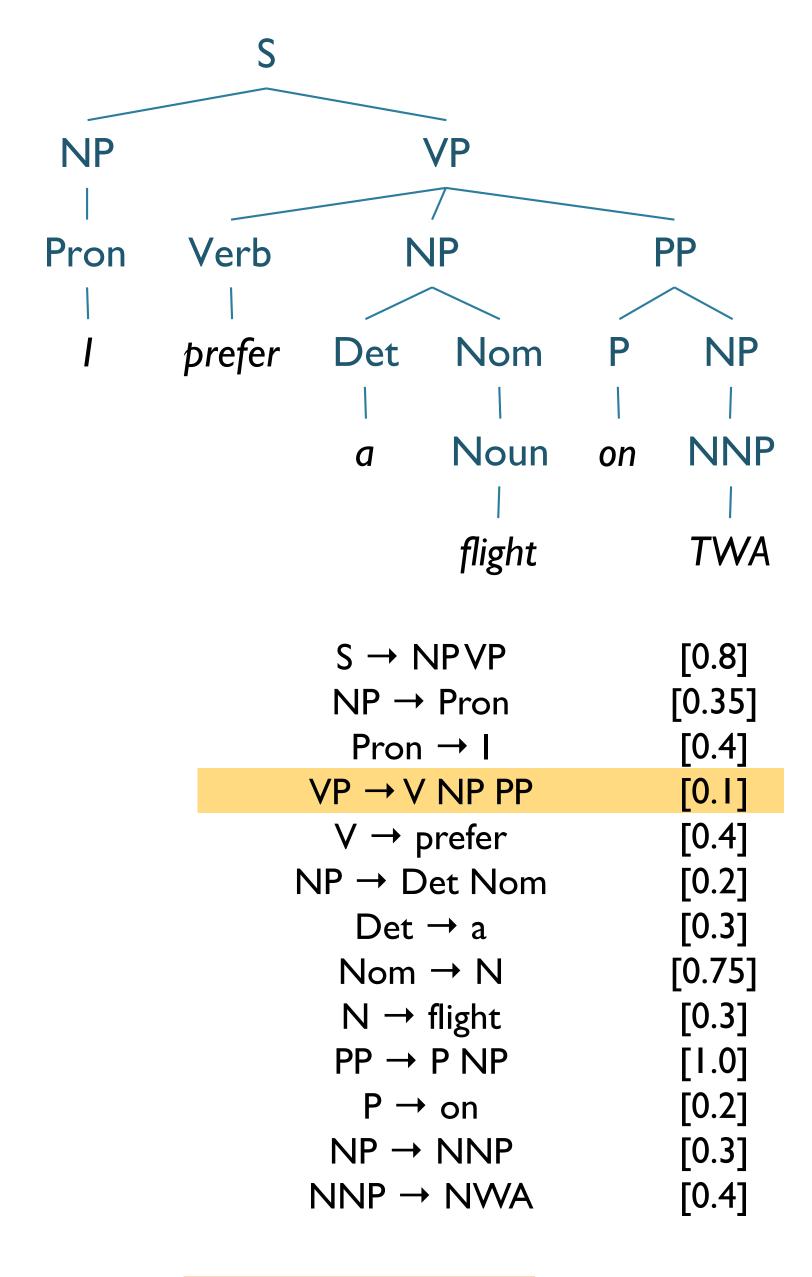
- ullet A PCFG assigns probability to each parse tree T for input S
- ullet Probability of T: product of all rules used to derive T

$$P(T,S) = \prod_{i=1}^{n} P(RHS_i | LHS_i)$$

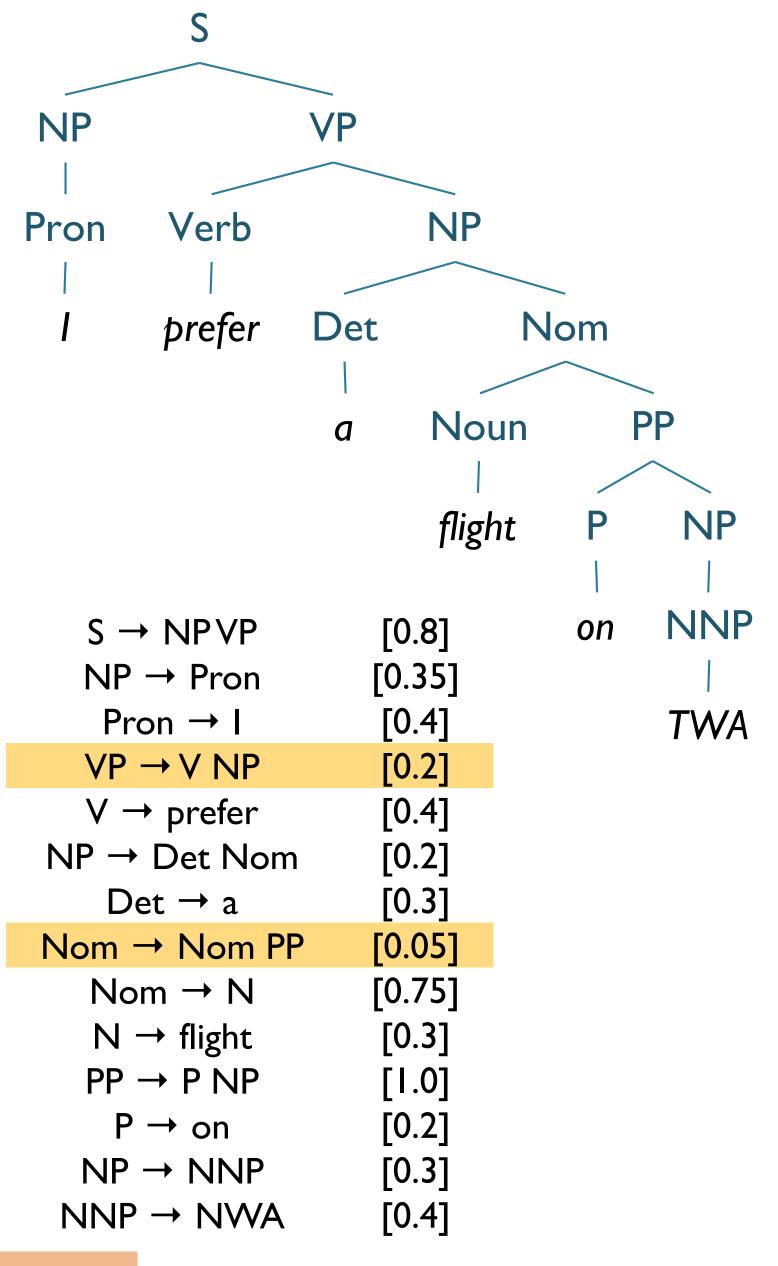
$$P(T, S) = P(T)P(S | T) = P(T)$$







$$\sim 1.452 \times 10^{-6}$$



 $\sim 1.452 \times 10^{-7}$

Parsing Problem for PCFGs

• Select T such that (s.t.)

$$\hat{T}(S) = \underset{T \text{ s.t. } S = yield(T)}{\operatorname{argmax}} P(T)$$

- String of words S is yield of parse tree
- Select the tree \hat{T} that maximizes the probability of the parse

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- PCFGs are able to give probability of entire string without as bad sparsity
- Model probability of syntactically valid sentences
 - Not just probability of sequence of words

PCFGs: Parsing

Probabilistic CKY (PCKY)

- Like regular CKY
 - Assumes grammar in Chomsky Normal Form (CNF)
 - \bullet $A \rightarrow B C$
 - \bullet $A \rightarrow w$
 - Represent input with indices b/t words:
 - Book 1 that 2 flight 3 through 4 Houston 5

Probabilistic CKY (PCKY)

- For input string length n and non-terminals V
 - Cell [i, j, A] in (n+1) × (n+1) × V matrix
 - Contains probability that A spans [i, j]

```
function Probabilistic-CKY-PARSE(words, grammar) returns most probable parse and its probability
for j ← from 1 to LENGTH(words) do
for all \{A \mid A \rightarrow words[j] \in grammar\}
      table[j-1, j, A] \leftarrow P(A \rightarrow words[j])
 for i \leftarrow \text{from } j-2 \text{ downto } 0 \text{ do}
  for k \leftarrow i + 1 to i-1 do
  for all \{A \mid A \rightarrow B \ C \in grammar,
         and table[i, k, B] > 0 and table[k, j, C] > 0
  if (table[i, j, A] < P(A \rightarrow BC) \times table[i, k, B] \times table[k, j, C]) then
      table[i, j, A] \leftarrow P(A \rightarrow BC) \times table[i, k, B] \times table[k, j, C]
      back[i, j, A] \leftarrow \{k, B, C\}
  return Build_Tree(back[1, Length(words), S]), table[1, Length(words), S]
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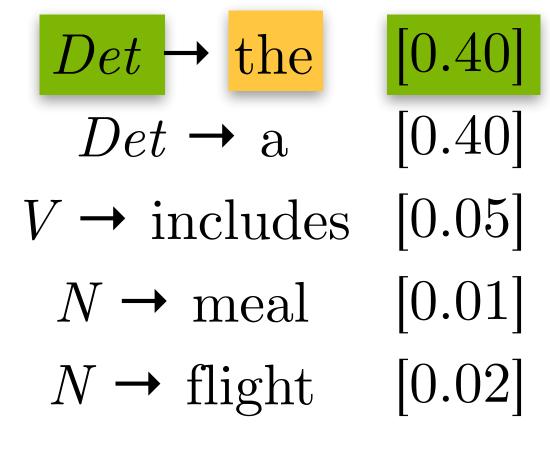
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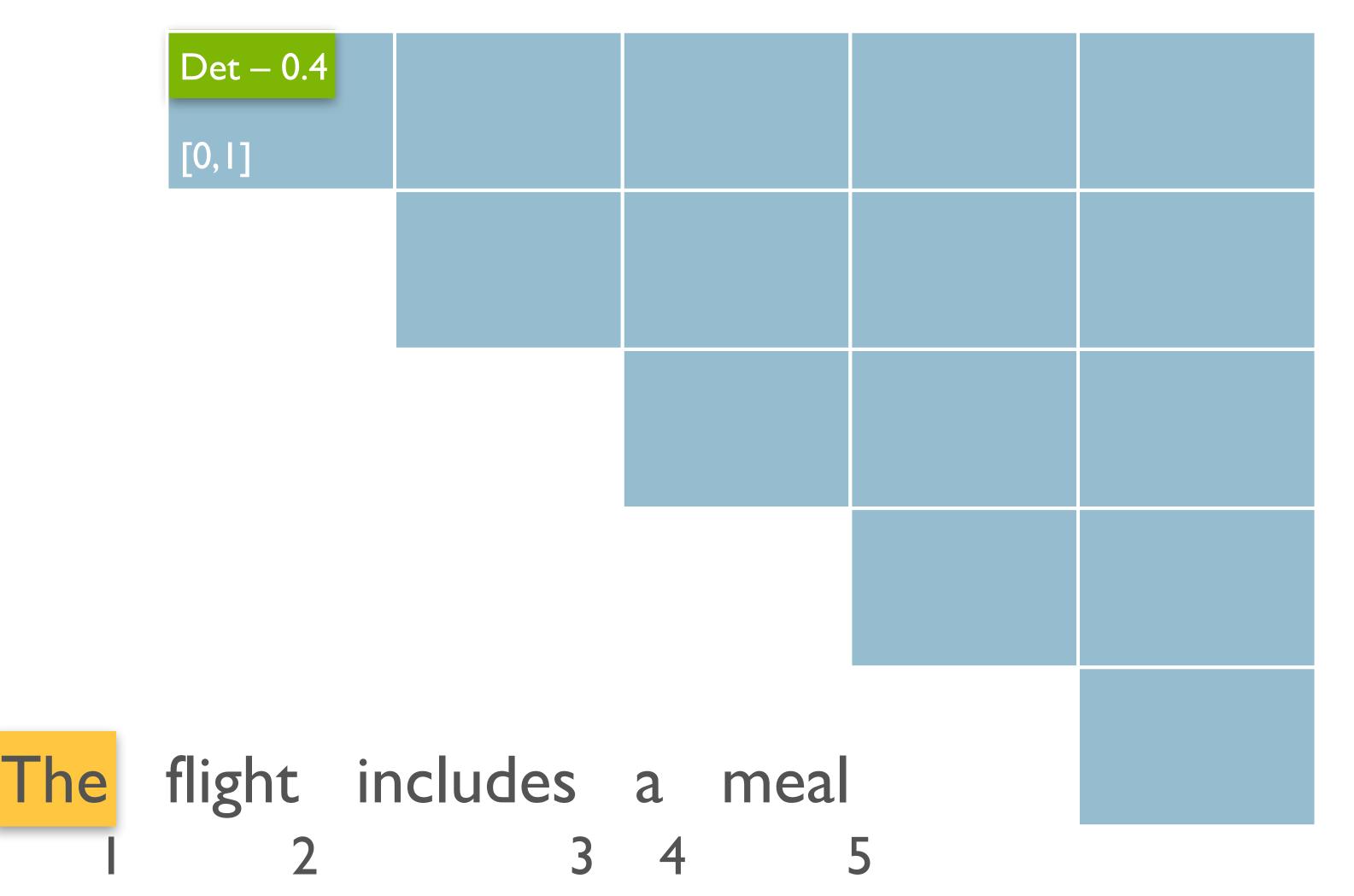
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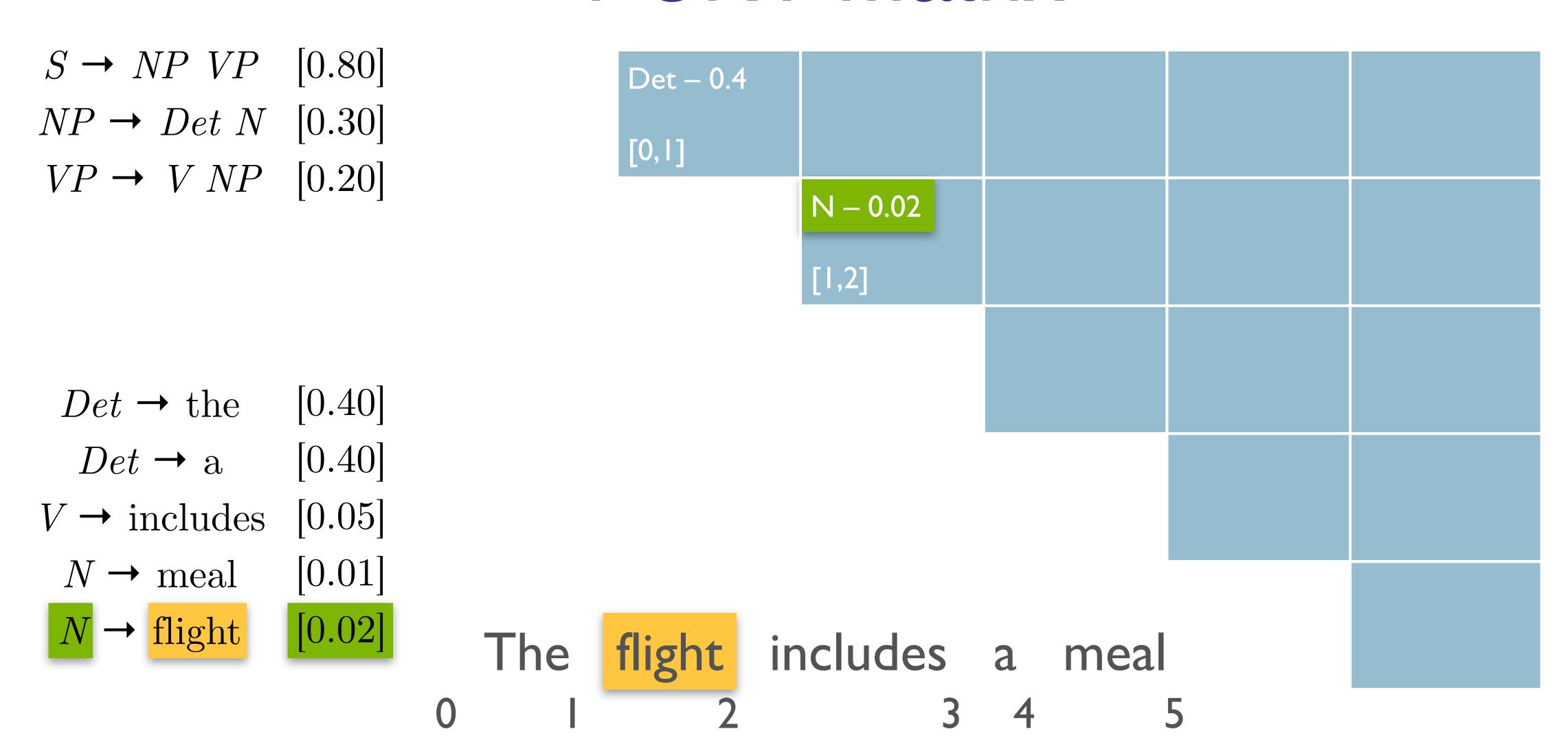
PCKY Grammar Segment

```
S \rightarrow NP \ VP \quad [0.80] Det \rightarrow the \quad [0.40] NP \rightarrow Det \ N \quad [0.30] Det \rightarrow a \quad [0.40] VP \rightarrow V \ NP \quad [0.20] V \rightarrow includes \quad [0.05] N \rightarrow meal \quad [0.01] N \rightarrow flight \quad [0.02]
```

$$S \rightarrow NP \ VP \quad [0.80]$$
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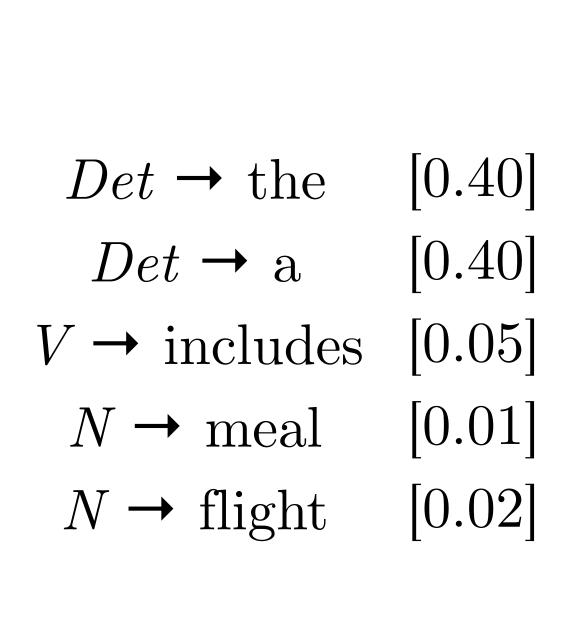


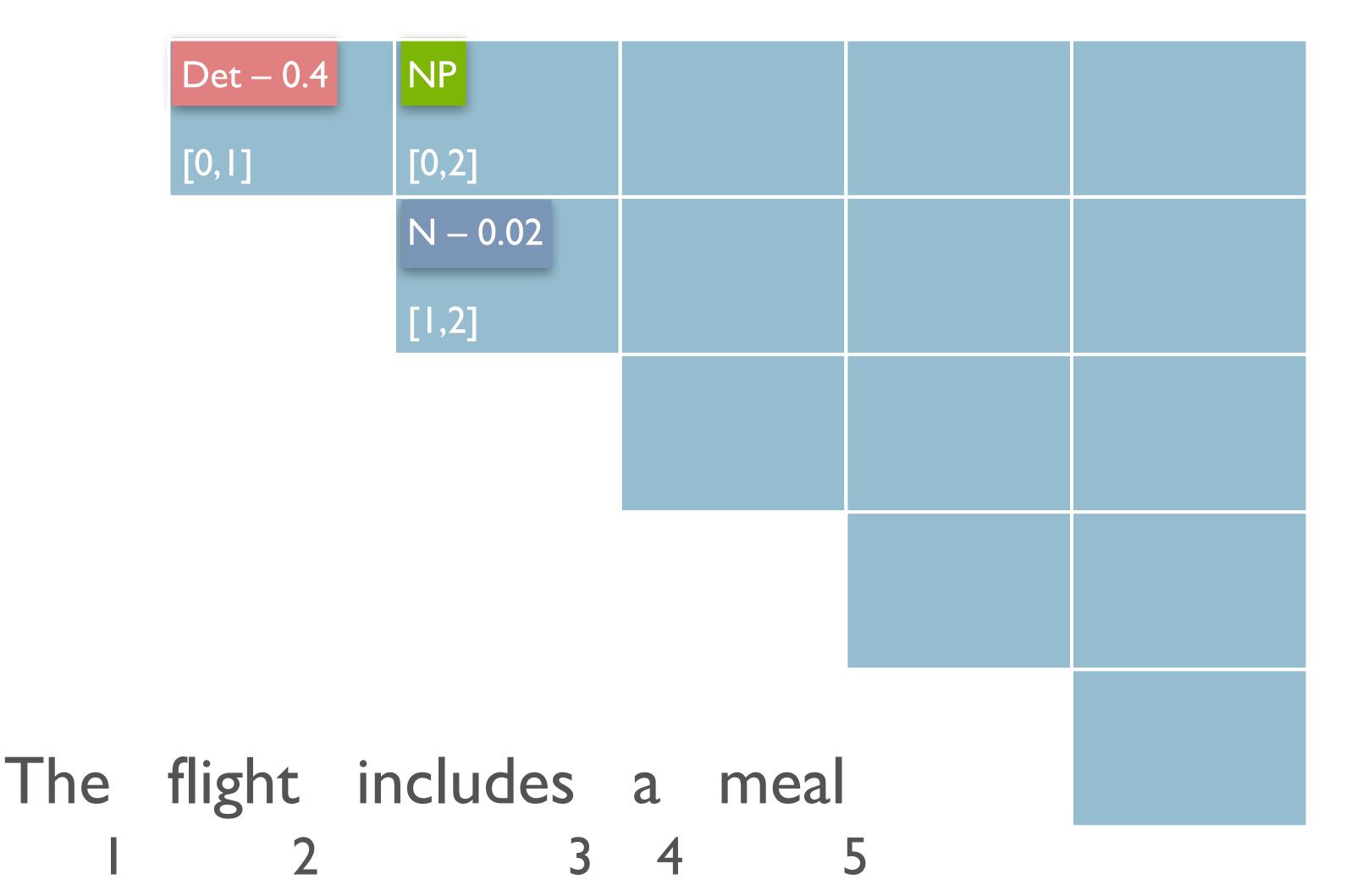


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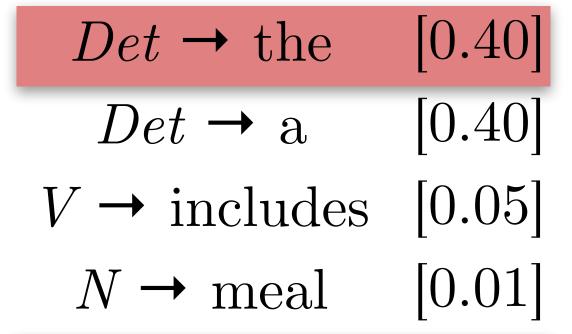
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N \rightarrow meal \quad [0.01]
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```

```
Det – 0.4
                 NP
       [0,1]
                 [0,2]
                 N - 0.02
                 [1,2]
The flight includes a meal
```

$$S \rightarrow NP \ VP \quad [0.80]$$

$$NP \rightarrow Det \ N \quad [0.30]$$

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[0.02]

 $N \rightarrow \text{flight}$

```
Det – 0.4
                 NP
       [0,1]
                 [0,2]
                 N - 0.02
                 [1,2]
               = 0.00024
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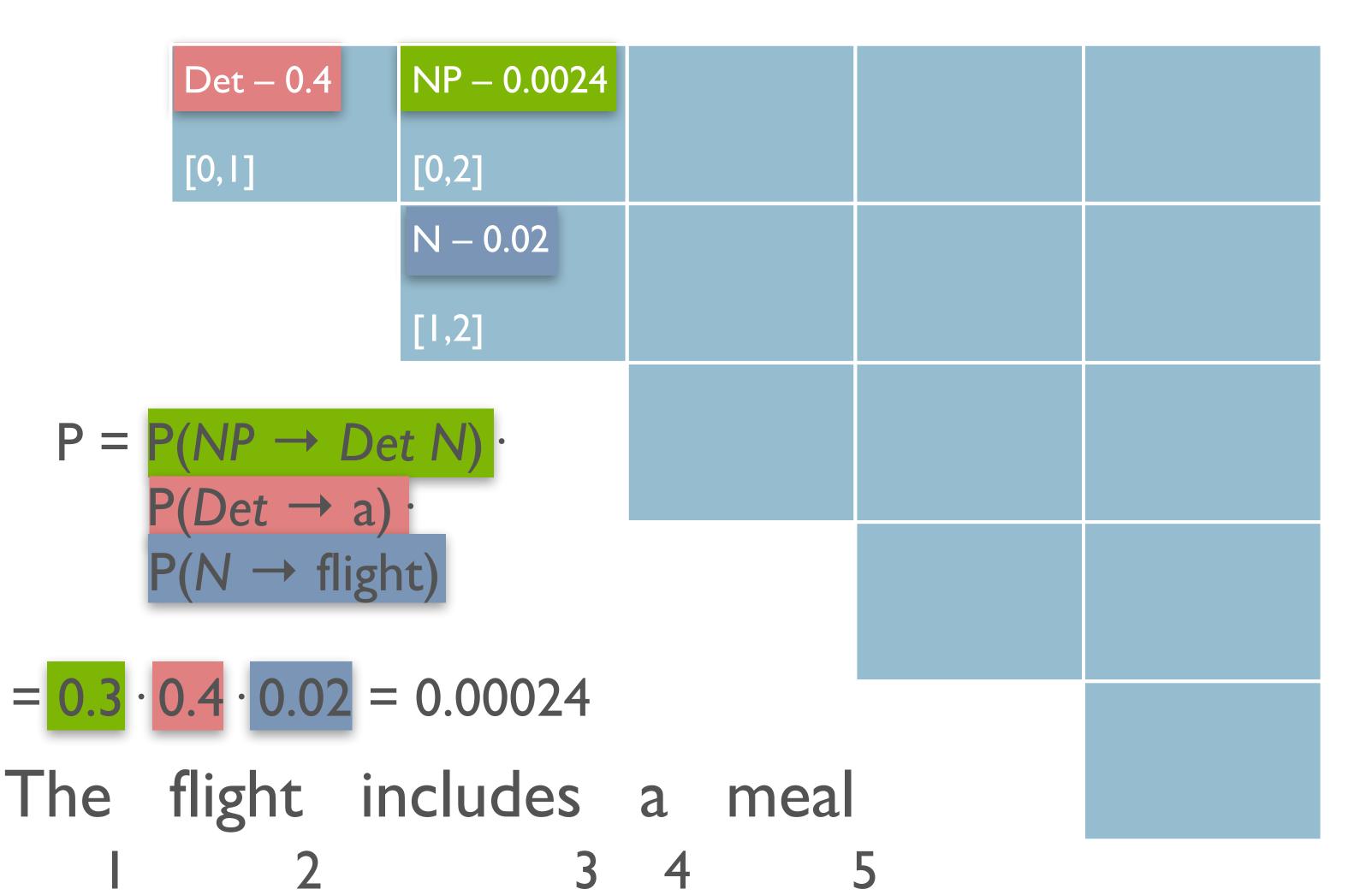
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 [0.01]

$$N \rightarrow \text{flight} \quad [0.02]$$



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The

Det - 0.4	NP - 0.0024			S - 2.304×10-8
[0,1]	[0,2]	[0,3]	[0,4]	[0,5]
	N - 0.02			
	[1,2]	[1,3]	[1,4]	[1,5]
		V — 0.05		VP - 1.2×10-5
		[2,3]	[2,4]	[2,5]
			Det – 0.4	NP - 0.0012
			[3,4]	[3,5]
			N - 0.01	
flight includes a meal			[4,5]	

Inducing a PCFG

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$$P(\alpha \to \beta \mid \alpha) = \frac{Count(\alpha \to \beta)}{\sum_{\gamma} Count(\alpha \to \gamma)} = \frac{Count(\alpha \to \beta)}{Count(\alpha)}$$

$$\Sigma_{\gamma} Count(\alpha \rightarrow \gamma)$$

$$Count(\alpha \rightarrow \beta)$$

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- Alternative: Learn probabilities by re-estimating
 - (Later)

Probabilistic Parser Development Paradigm

	Train	Dev	Test
	Large	Small	Small/Med
Size	(eg.WSJ 2-21, 39,830 sentences)	(e.g.WSJ 22)	(e.g. WSJ, 23, 2,416 sentences)
Usage	Estimate rule probabilities	Tuning/Verification, Check for Overfit	Held Out, Final Evaluation

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 - Partial credit:

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- How can we tell how good the parser is?
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 - Maximally strict: identical to 'gold standard'
 - Partial credit:
 - Constituents in output match those in reference

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- How can we tell how good the parser is?
- How can we tell how good a parse is?
 - Maximally strict: identical to 'gold standard'
 - Partial credit:
 - Constituents in output match those in reference
 - Same start point, end point, non-terminal symbol

Parseval

- How can we compute parse score from constituents?
- Multiple Measures:

```
Labeled Recall (LR) = 
# of correct constituents in hypothetical parse
# of total constituents in reference parse

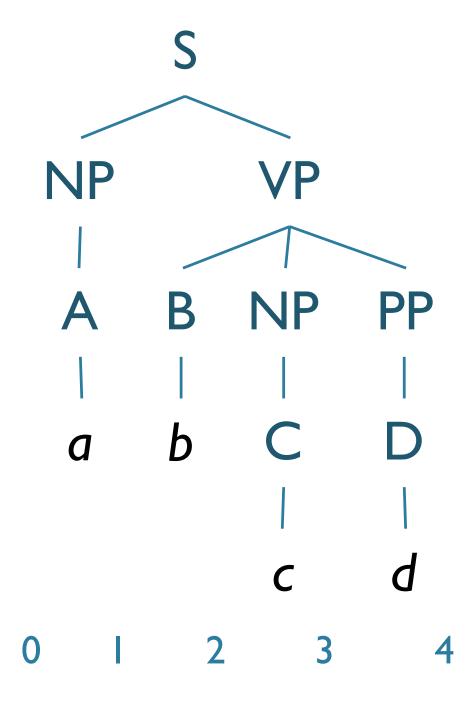
Labeled Precision (LP) = 
# of correct constituents in hypothetical parse
# of total consituents in hypothetical parse
```

Parseval

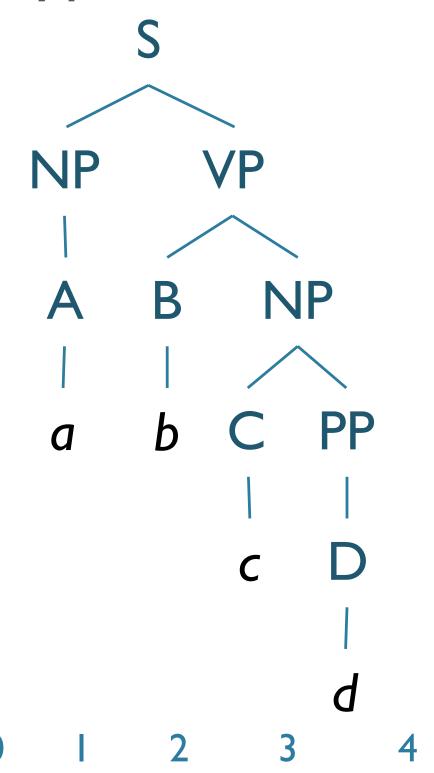
• F-measure:

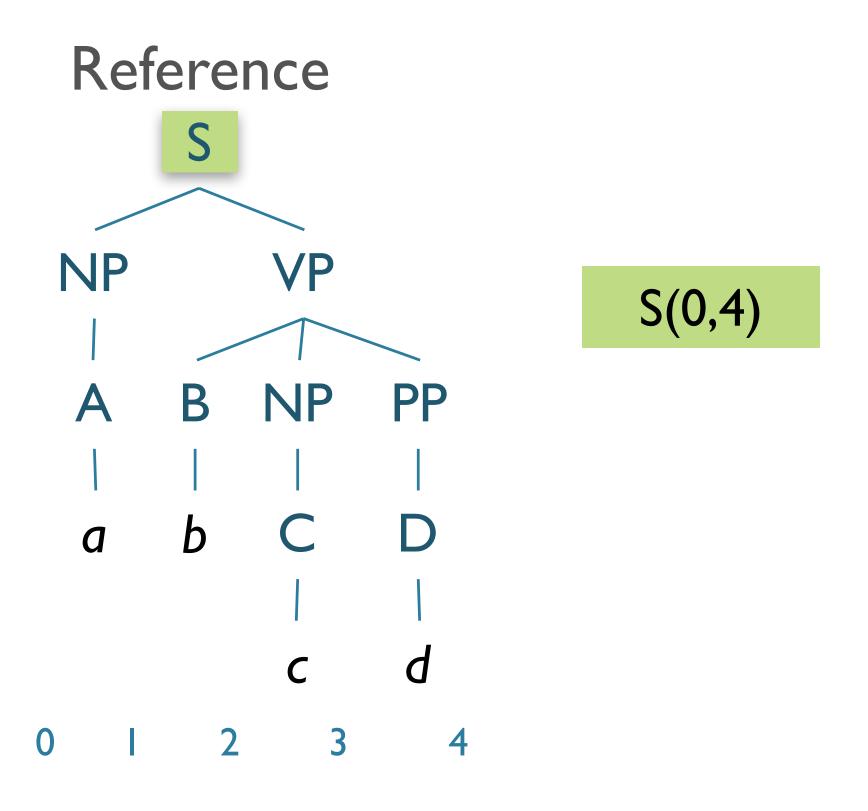
- Combines precision and recall
- Let $\beta \in \mathbb{R}$, $\beta > 0$ that adjusts P vs. R s.t. $\beta \propto \frac{R}{P}$
- F_{β} -measure is then: $F_{\beta} = (1 + \beta^2) \cdot \frac{P \cdot R}{\beta^2 \cdot P + R}$
- With F1-measure as $F_1 = \frac{2PR}{P+R}$

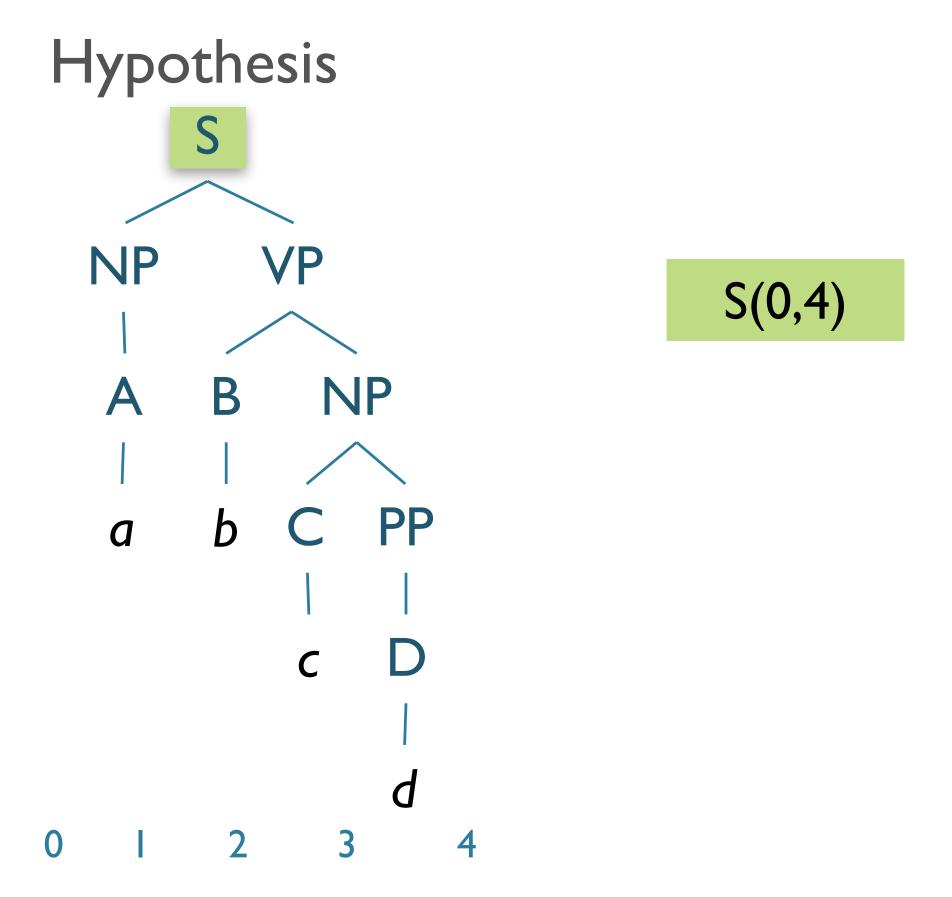
Reference

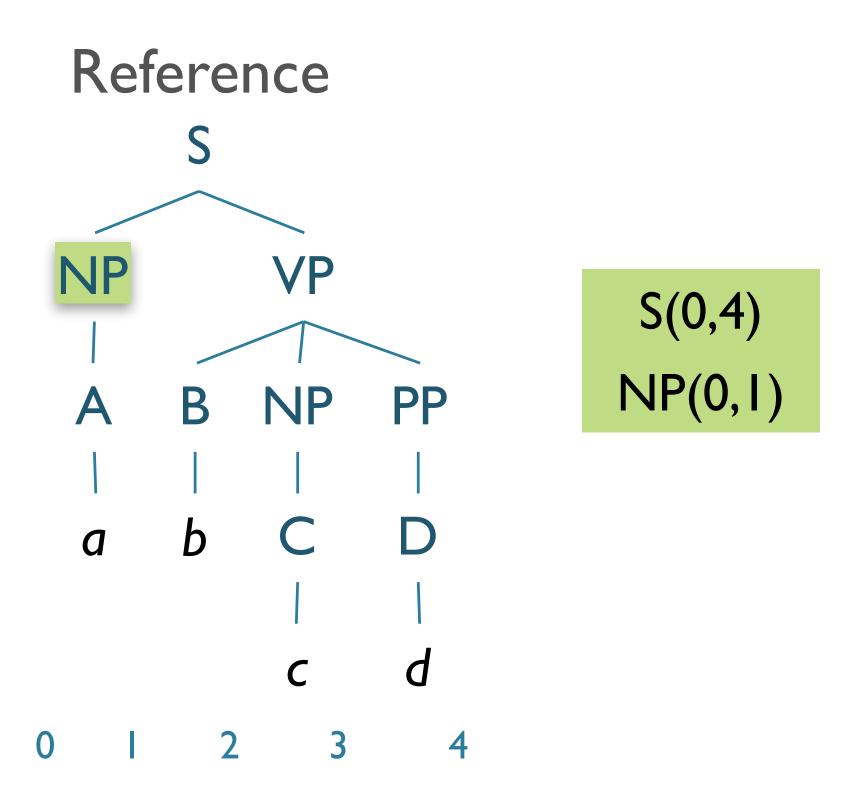


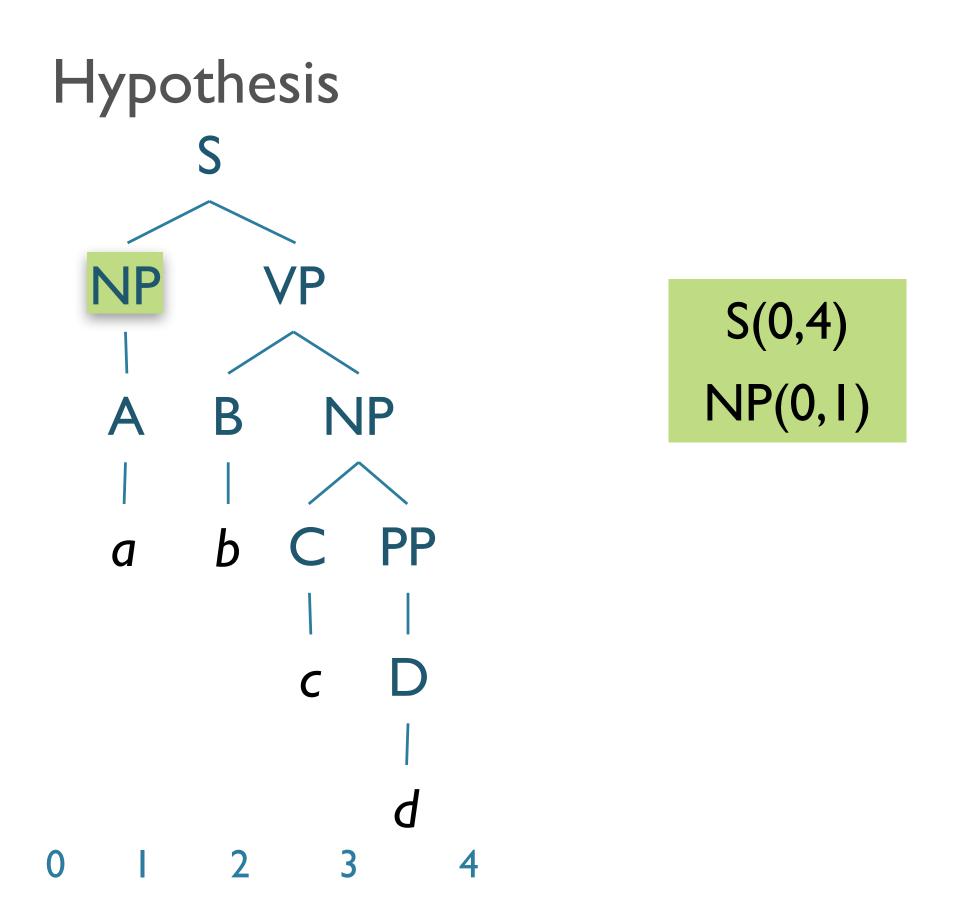
Hypothesis

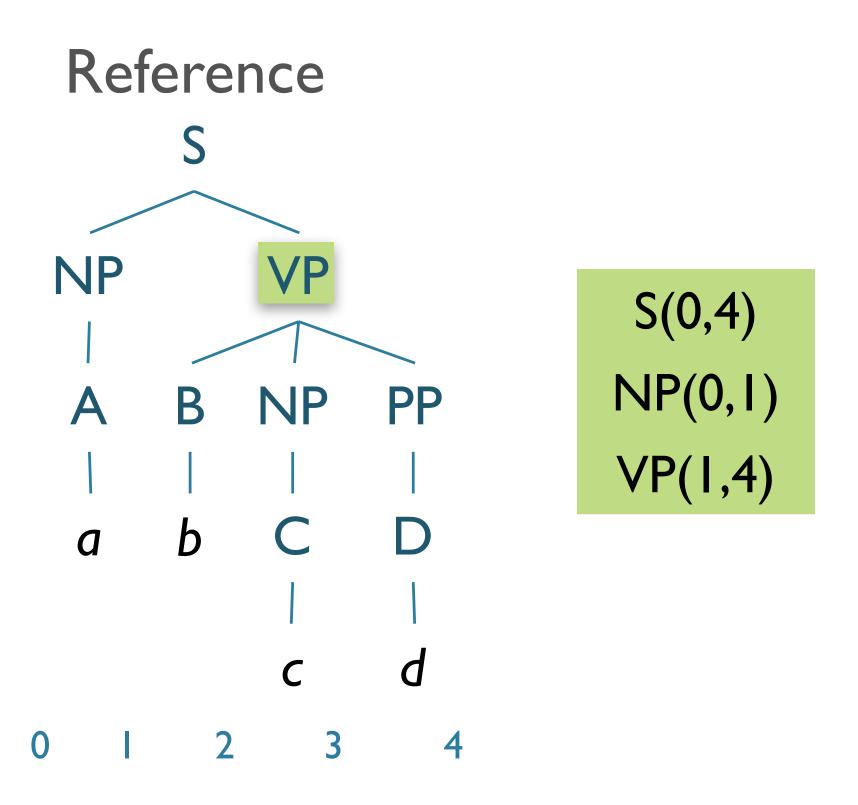


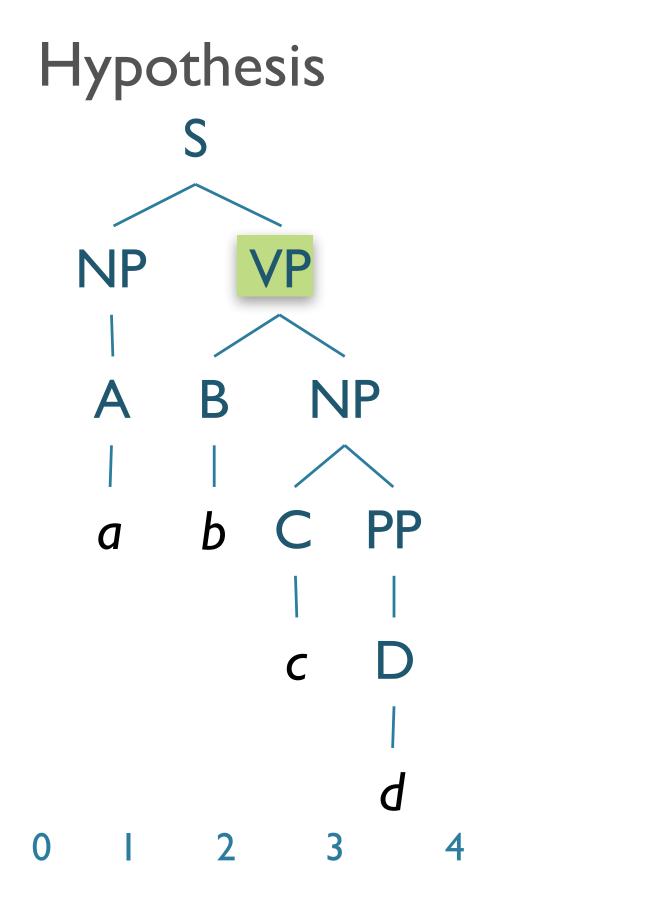


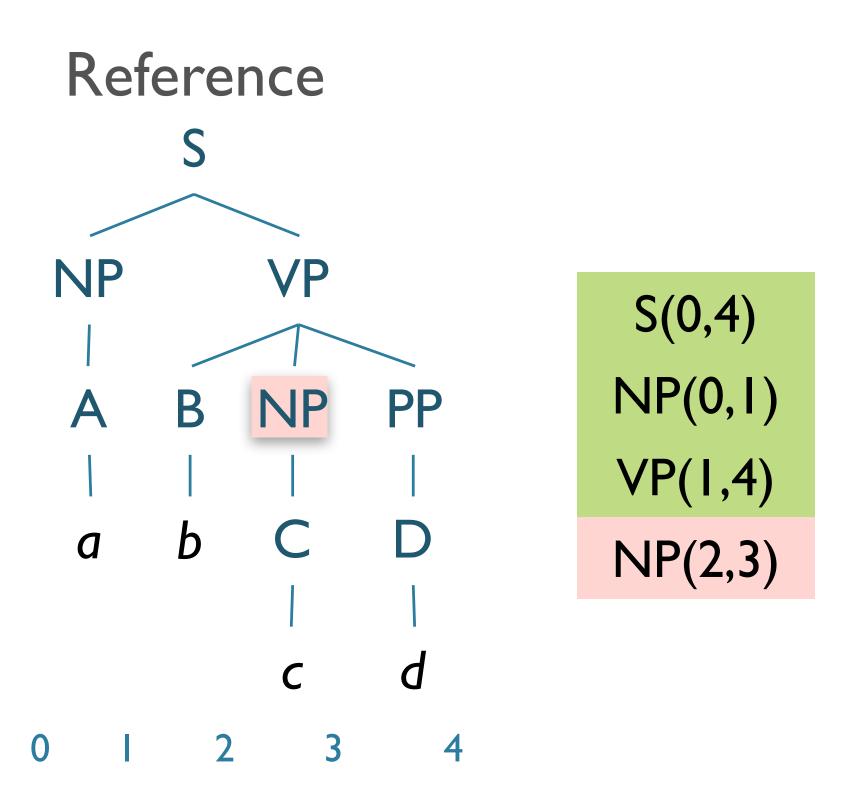


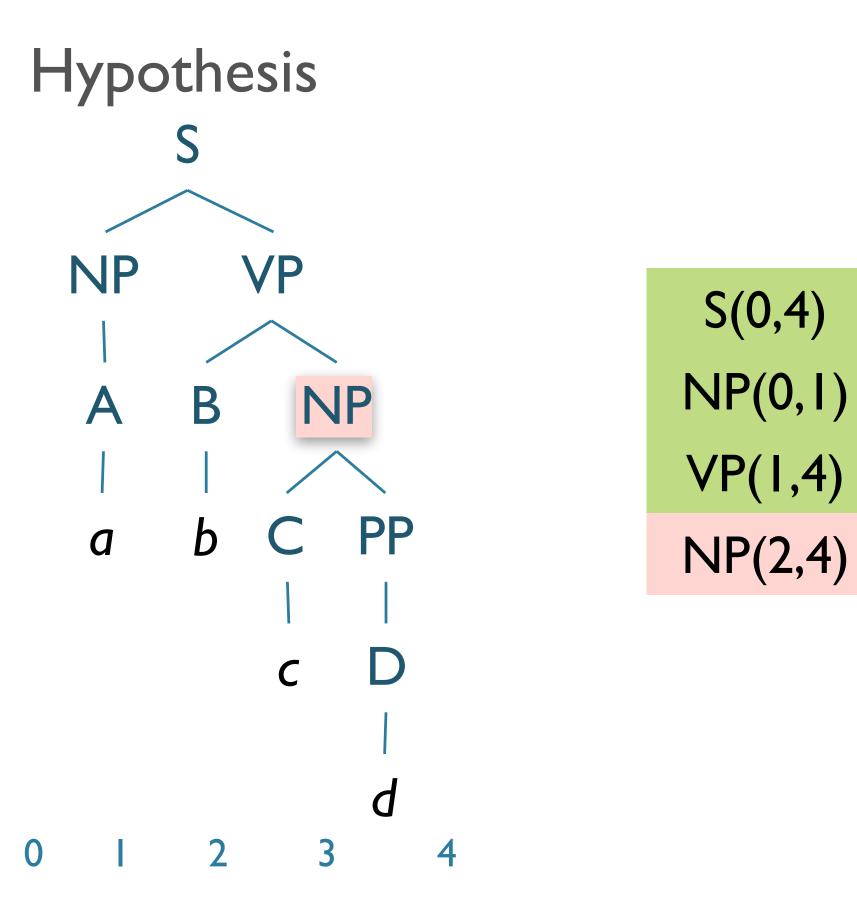


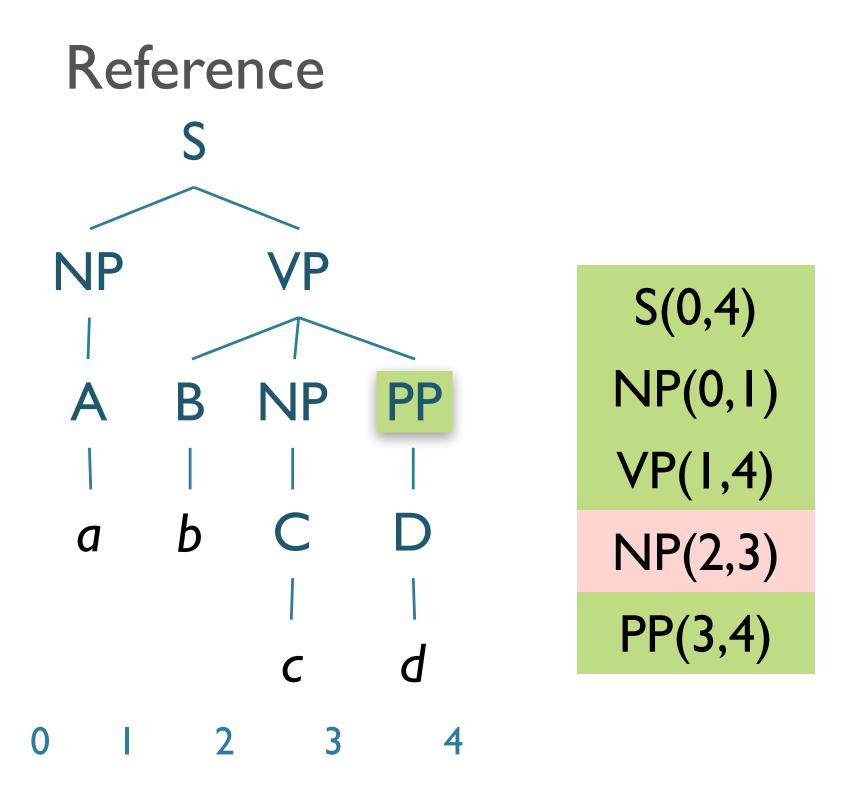


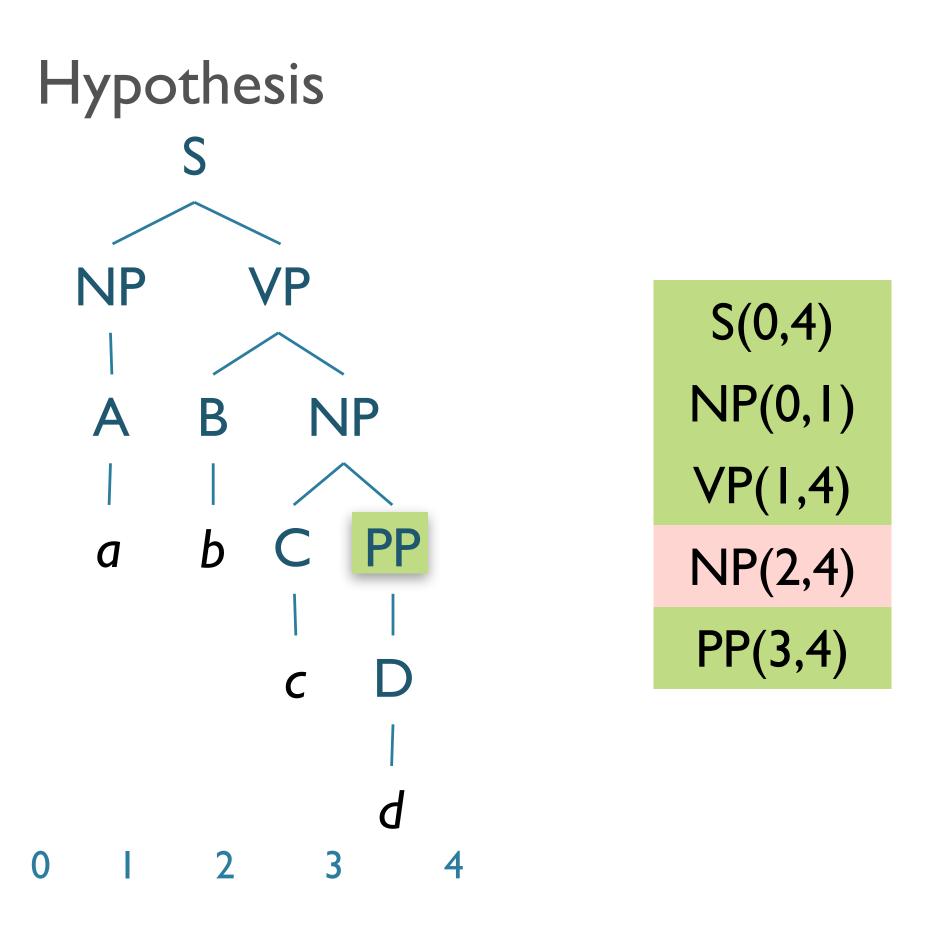




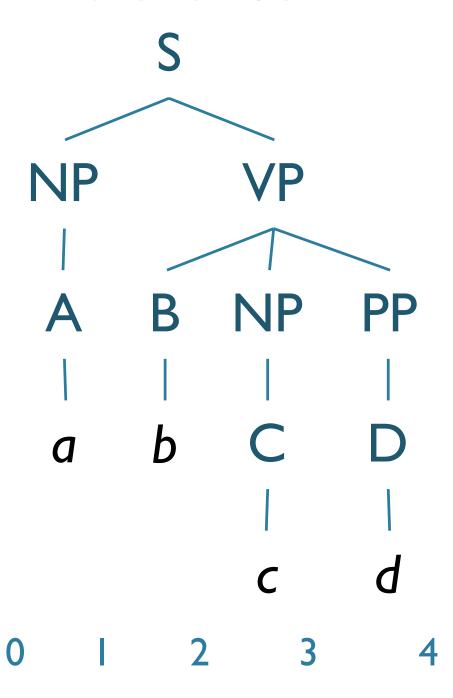








Reference



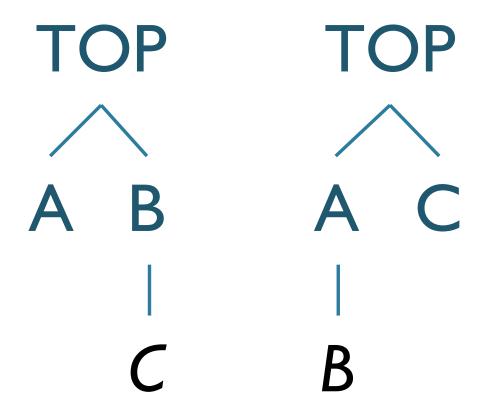
S(0,4) NP(0,1) VP(1,4) NP(2,3) PP(3,4)

> LP: 4/5 LR: 4/5

Hypothesis **VP** NP NP a

S(0,4) NP(0,1) VP(1,4) NP(2,4) PP(3,4)

- Crossing Brackets:
 - # of constituents where produced parse has bracketings that overlap for the siblings:
 - ((A B) C) { (0,2), (2,3) }
 and hyp. has
 (A (B C)) { (0,1), (1, 3) }



```
/* crossing is counted based on the brackets */
/* in test rather than gold file (by Mike) */
for(j=0;j<bn2;j++){
  for(i=0;i<bn1;i++){
    if(bracket1[i].result != 5 &&
        bracket2[j].result != 5 &&
        ((bracket1[i].start < bracket2[j].start &&
        bracket1[i].end > bracket2[j].start &&
        bracket1[i].end < bracket2[j].end) ||
        (bracket1[i].start > bracket2[j].start &&
        bracket1[i].start < bracket2[j].end &&
        bracket1[i].end > bracket2[j].end))){
```

from evalb.c

State-of-the-Art Parsing

- Parsers trained/tested on Wall Street Journal PTB
 - LR: 90%+;
 - LP: 90%+;
 - Crossing brackets: 1%

- Standard implementation of Parseval:
 - evalb

Evaluation Issues

- Only evaluating constituency
- There are other grammar formalisms:
 - LFG (Constraint-based)
 - Dependency Structure
- Extrinsic evaluation
 - How well does getting the correct parse match the semantics, etc?

Earley Parsing

Earley vs. CKY

- CKY doesn't capture full original structure
 - Can back-convert binarization, terminal conversion
 - Unit non-terminals require change in CKY

Earley vs. CKY

- CKY doesn't capture full original structure
 - Can back-convert binarization, terminal conversion
 - Unit non-terminals require change in CKY
- Earley algorithm
 - Supports parsing efficiently with arbitrary grammars
 - Top-down search
 - Dynamic programming
 - Tabulated partial solutions
 - Some bottom-up constraints

Earley Algorithm

- Another dynamic programming solution
 - Partial parses stored in "chart"
 - Compactly encodes ambiguity
 - O(N³)
- Chart entries contain:
 - Subtree for a single grammar rule
 - Progress in completing subtree
 - Position of subtree w.r.t. input

Earley Algorithm

- First, left-to-right pass fills out a chart with *N+1* states
 - Chart entries sit between words in the input string
 - Keep track of states of the parse at those positions
 - For each word position, chart contains set of states representing all partial parse trees generated so far
 - e.g. chart[0] contains all partial parse trees generated at the beginning of sentence

Chart Entries

- Three types of constituents:
 - Predicted constituents
 - In-progress constituents
 - Completed constituents

Parse Progress

- Represented by Dotted Rules
 - Position of indicates type of constituent
- 0 Book 1 that 2 flight 3
 - $S \rightarrow VP$ [0,0] (predicted)
 - $NP \rightarrow Det \cdot Nom$ [1,2] (in progress)
 - $VP \rightarrow VNP$ [0,3] (completed)
- [x,y] tells us what portion of the input is spanned so far by rule
- Each state *s_i*: <*dotted rule*>, [<*back pointer*>, <*current position*>]

o Book 1 that 2 flight 3

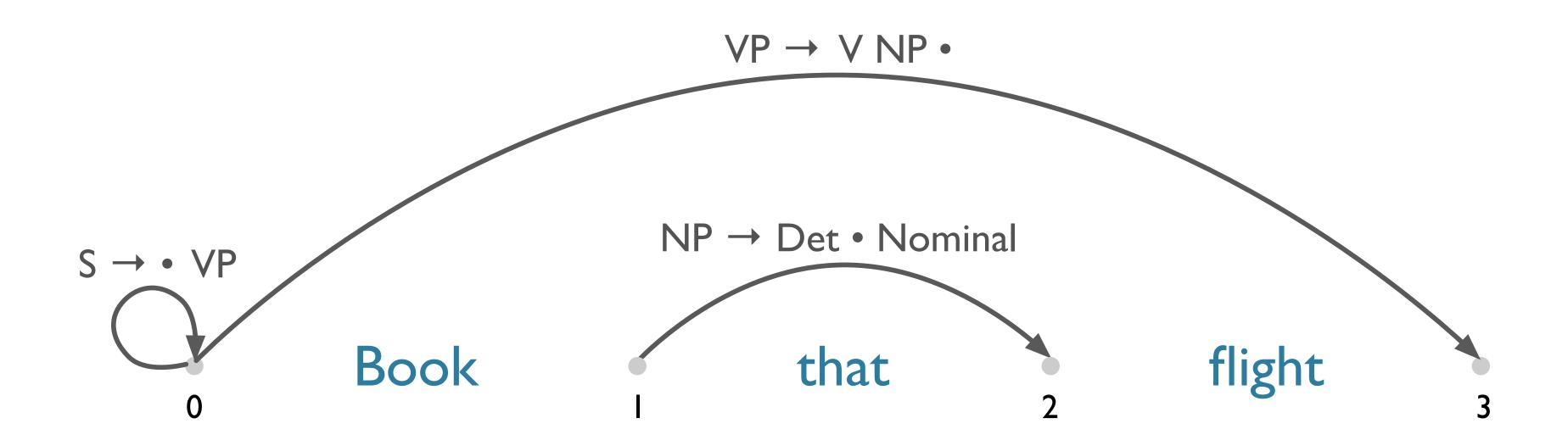
- $S \to VP, [0,0]$
 - First 0 means S constituent begins at the start of input
 - Second 0 means the dot is here too
 - So, this is a top-down prediction

o Book 1 that 2 flight 3

- $S \rightarrow VP$, [0,0]
 - First 0 means S constituent begins at the start of input
 - Second 0 means the dot is here too
 - So, this is a top-down prediction
- *NP* → *Det Nom*, [1,2]
 - the NP begins at position 1
 - the dot is at position 2
 - so, Det has been successfully parsed
 - Nom predicted next

o Book 1 that 2 flight 3 (continued)

- $V \rightarrow V NP \cdot [0,3]$
 - Successful VP parse of entire input



Successful Parse

- Final answer found by looking at last entry in chart
- If entry resembles $S \rightarrow \alpha \cdot [0,N]$ then input parsed successfully
- Chart will also contain record of all possible parses of input string, given the grammar

Parsing Procedure for the Earley Algorithm

- Move through each set of states in order, applying one of three operations:
 - predictor: add predictions to the chart
 - scanner: read input and add corresponding state to chart
 - completer: move dot to right when new constituent found
- Results (new states) added to current or next set of states in chart
- No backtracking and no states removed: keep complete history of parse

Earley Algorithm

```
function Earley-Parse(words, grammar) returns chart
 ENQUEUE((\gamma \rightarrow \bullet S, [0,0]), chart[\theta])
 for i \leftarrow \text{from } 0 \text{ to LENGTH}(words) \text{ do}
   for each state in chart[i] do
      if INCOMPLETE?(state) and
          Next-Cat(state) is not a part of speech then
        \mathbf{PREDICTOR}(state)
      elseif Incomplete: (state) and
          NEXT-CAT(state) is a part of speech then
        SCANNER(state)
      else
        Complete Energy (state)
      end
    end
 return(chart)
```

Earley Algorithm

```
procedure PREDICTOR((A \rightarrow \alpha \bullet B \beta, (i,j)))
  for each (B \rightarrow \gamma) in Grammar-Rules-For(B,grammar) do
    ENQUEUE((B \rightarrow \bullet \gamma, [j,j]), chart[j])
  end
procedure SCANNER((A \rightarrow a \bullet B \beta, [i,j]))
  if B c Parts-of-Speech(word/j/) then
    ENQUEUE((B \rightarrow word[j] \bullet, [j,j+1]), chart[j+1])
procedure Completer (B \rightarrow \gamma \bullet, [j,k])
 for each (A \rightarrow \alpha \bullet B \beta, [i,j]) in chart[j] do
    ENQUEUE((A \rightarrow a B \bullet \beta, [i,k]), chart[k])
  end
```

3 Main Subroutines of Earley

- Predictor
 - Adds predictions into the chart
- Scanner
 - Reads the input words and enters states representing those words into the chart
- Completer
 - Moves the dot to the right when new constituents are found

Predictor

- Intuition:
 - Create new state for top-down prediction of new phrase
- Applied when non part-of-speech non-terminals are to the right of a dot:
 - $S \rightarrow VP[0,0]$
- Adds new states to current chart
 - One new state for each expansion of the non-terminal in the grammar

$$VP \rightarrow \cdot V$$
 [0,0]
 $VP \rightarrow \cdot V NP$ [0,0]

Chart[0]

S0	$\gamma \rightarrow \cdot S$	[0,0]	Dummy start state
S1	$S \rightarrow \cdot NP VP$	[0.0]	Predictor
S2	$S \rightarrow \cdot Aux NP VP$	[0,0]	Predictor
S3	$S \rightarrow \cdot VP$	[0,0]	Predictor
S4	NP → • Pronoun NP → • Proper-Noun NP → • Det Nominal	[0,0]	Predictor
S5		[0,0]	Predictor
S6		[0,0]	Predictor
S7 S8 S9 S10 S11	$VP \rightarrow \cdot Verb$ $VP \rightarrow \cdot Verb NP$ $VP \rightarrow \cdot Verb NP PP$ $VP \rightarrow \cdot Verb PP$ $VP \rightarrow \cdot VP PP$	[0,0] [0,0] [0,0] [0,0]	Predictor Predictor Predictor Predictor Predictor

Chart[1]

S12	Verb → book •	[0,1]	Scanner
S13 S14 S15 S16	$VP \rightarrow Verb \cdot NP$ $VP \rightarrow Verb \cdot NP$ $VP \rightarrow Verb \cdot NP PP$ $VP \rightarrow Verb \cdot PP$	[0,1] [0,1] [0,1]	Completer Completer Completer Completer
S17	$S \rightarrow VP$.	[0,1]	Completer
S18	$VP \rightarrow VP \cdot PP$	[0,1]	Completer
S19 S20 S21 S22	$NP \rightarrow \cdot Pronoun$ $NP \rightarrow \cdot Proper-Noun$ $NP \rightarrow \cdot Det Nominal$ $PP \rightarrow \cdot Prep NP$	[1,1] [1,1] [1,1]	Predictor Predictor Predictor Predictor

Book that flight

S0: $\gamma \to S[0,0]$



Book that flight

S0:
$$\gamma \rightarrow \cdot S[0,0]$$

S3:
$$S \rightarrow VP[0,0]$$

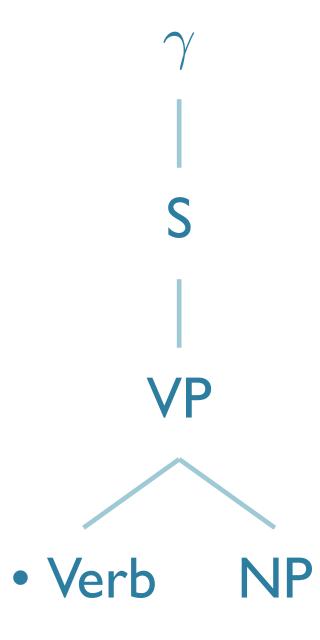


Book that flight

S0: $\gamma \to S[0,0]$

S3: $S \rightarrow VP[0,0]$

S8: *VP* → • *Verb NP* [0,0]

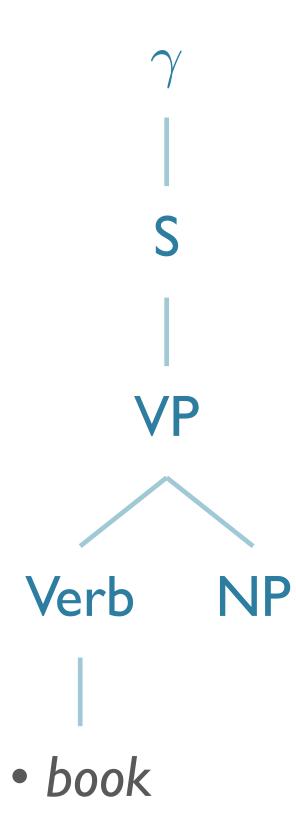


```
S0: \gamma \to S[0,0]
```

S3: $S \rightarrow VP[0,0]$

S8: *VP* → • *Verb NP* [0,0]

S12: *Verb* → • *book* [0,0]

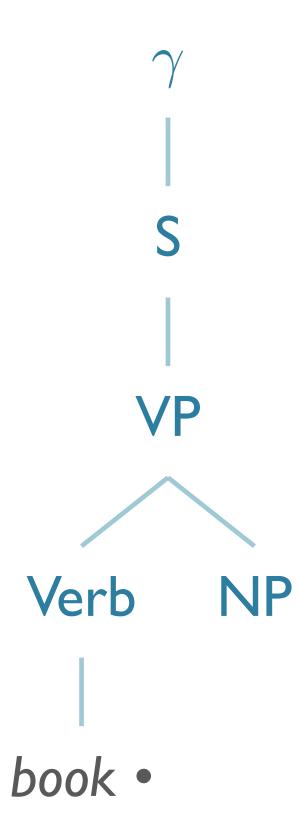


```
S0: \gamma \to S[0,0]
```

S3: $S \rightarrow VP[0,0]$

S8: *VP* → • *Verb NP* [0,0]

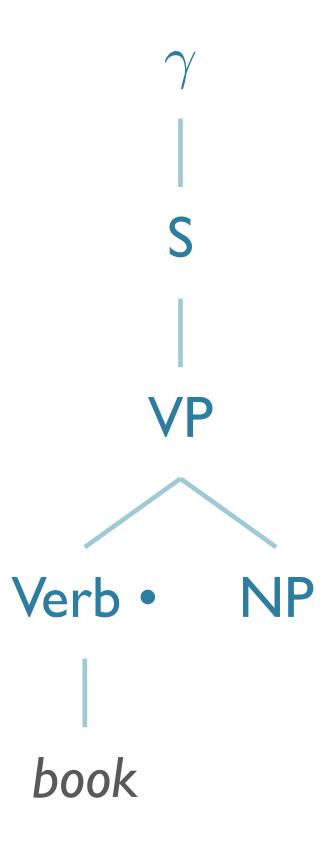
S12: *Verb* → *book* • [0,1]



```
S0: \gamma \to S[0,0]
```

S3: $S \rightarrow VP[0,0]$

S8: *VP* → *Verb* • *NP* [0,1]



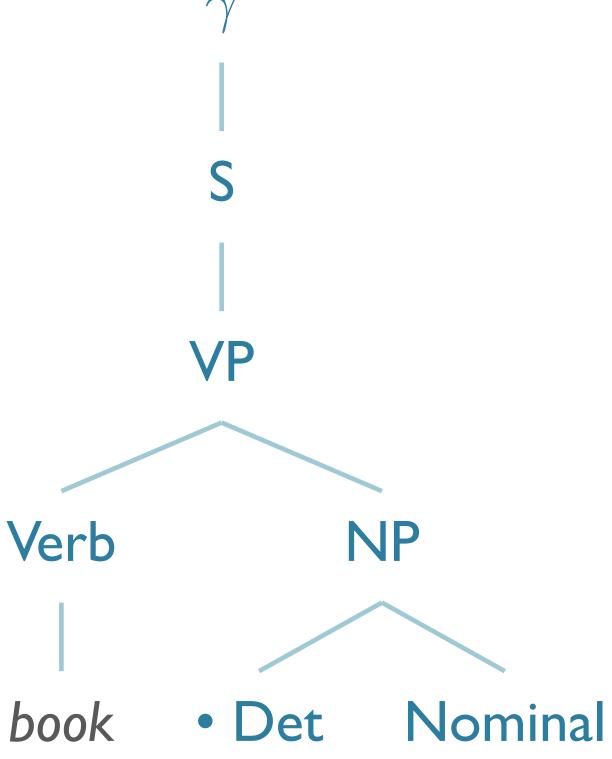
```
S0: \gamma \to S[0,0]
```

S3: $S \rightarrow VP \cdot [0,1]$

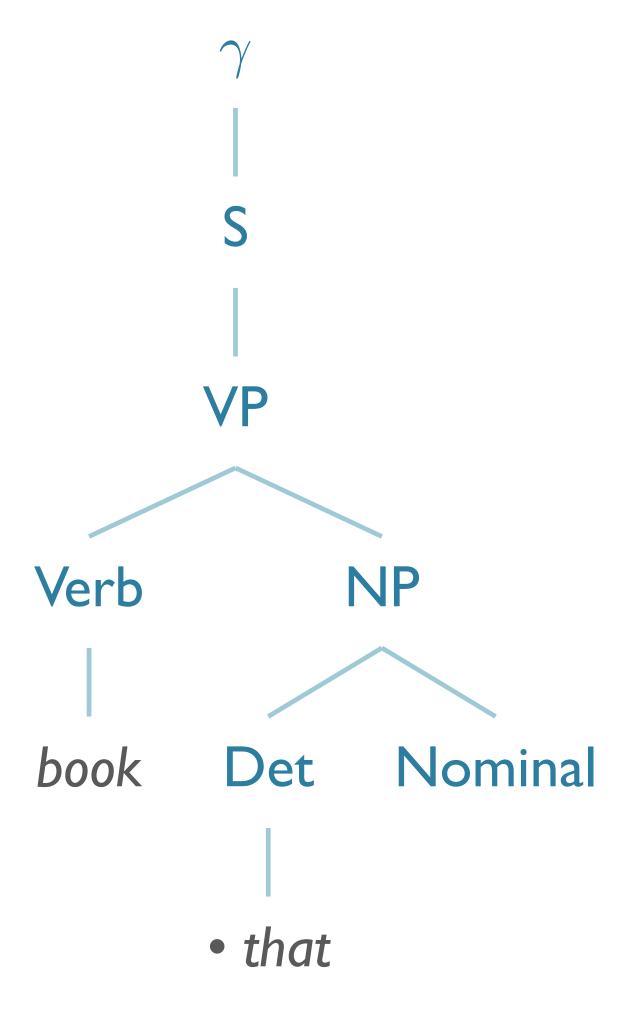
S8: *VP* → *Verb* • *NP* [0,1]



```
S0: \gamma \rightarrow \cdot S[0,0]
S3: S \rightarrow VP \cdot [0,1]
S8: VP \rightarrow Verb \cdot NP[0,1]
S21: NP \rightarrow \cdot Det Nominal[1,1]
```

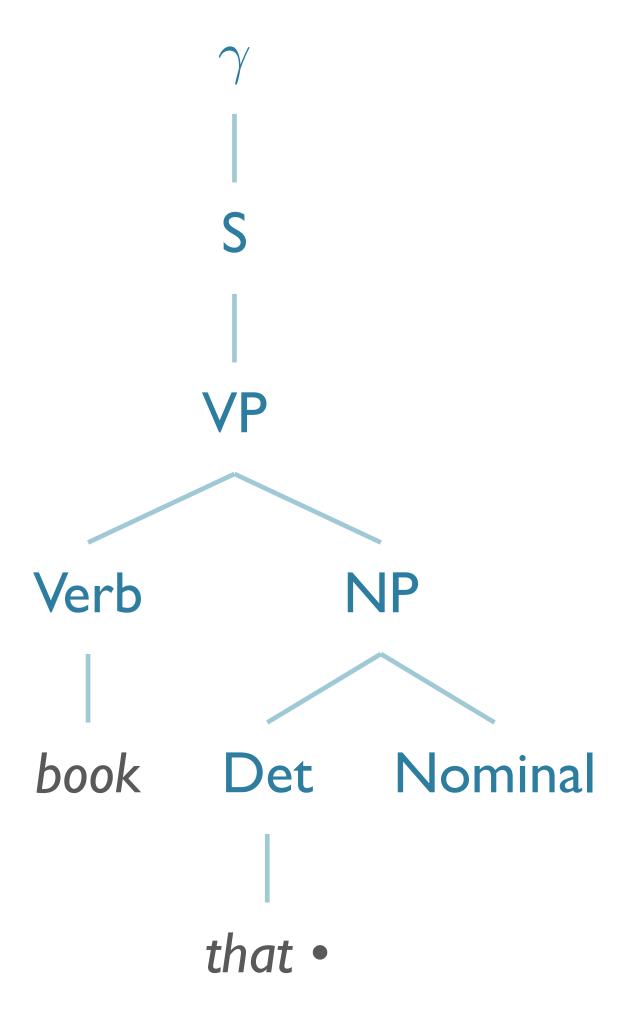


```
S0: \gamma \to \cdot S[0,0]
S3: S \to VP \cdot [0,1]
S8: VP \to Verb \cdot NP[0,1]
S21: NP \to \cdot Det Nominal[1,1]
S23: Det \to \cdot \text{"that"}[1,1]
```



```
S0: \gamma \rightarrow \cdot S[0,0]
S3: S \rightarrow VP \cdot [0,1]
S8: VP \rightarrow Verb \cdot NP[0,1]
S21: NP \rightarrow \cdot Det Nominal[1,1]
```

S23: *Det* → "that" • [1,2]



```
S0: \gamma \to S[0,0]
S3: S \rightarrow VP \cdot [0,1]
S8: VP → Verb • NP [0,1]
S21: NP → Det • Nominal [1,2]
                                              VP
                                      Verb
                                                    NP
                                                      Nominal
                                       book
                                              Det •
                                               that
```

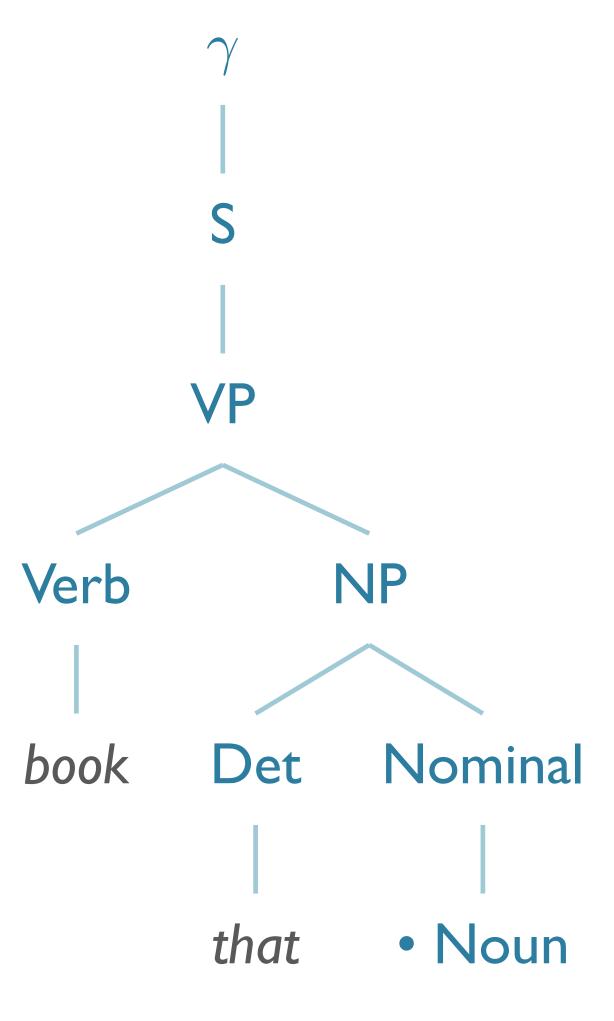
```
S0: \gamma \to S[0,0]
```

S3: $S \rightarrow VP \cdot [0,1]$

S8: *VP* → *Verb* • *NP* [0,1]

S21: *NP* → *Det* • *Nominal* [1,2]

S25: *Nominal* → • *Noun* [2,2]



```
S0: \gamma \to S[0,0]
```

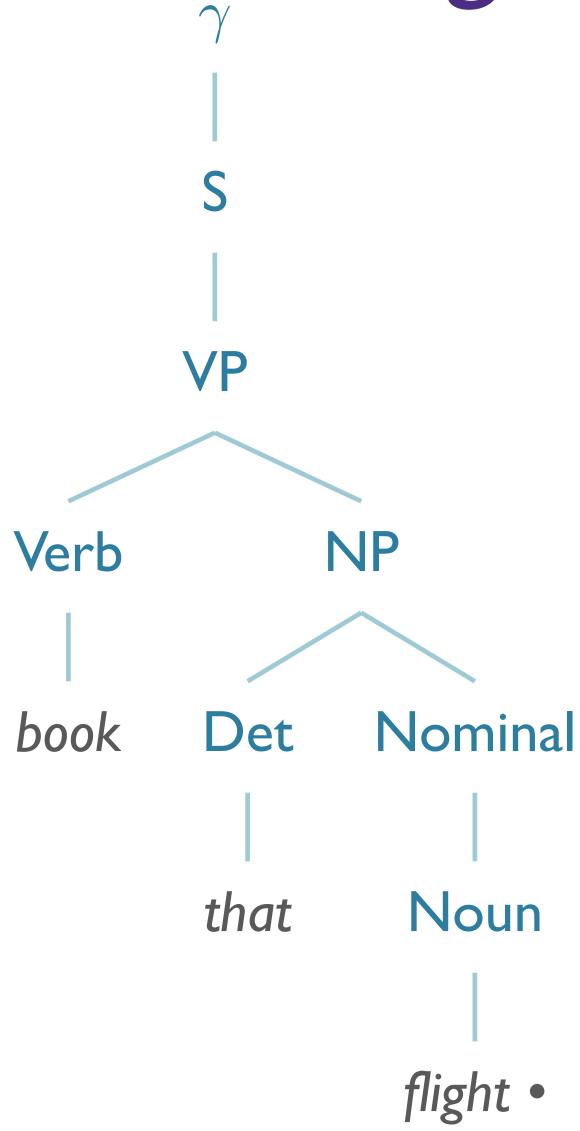
S3:
$$S \rightarrow VP \cdot [0,1]$$

S8: *VP* → *Verb* • *NP* [0,1]

S21: *NP* → *Det* • *Nominal* [1,2]

S25: *Nominal* → • *Noun* [2,2]

S28: *Noun* → "*flight*" • [2,3]



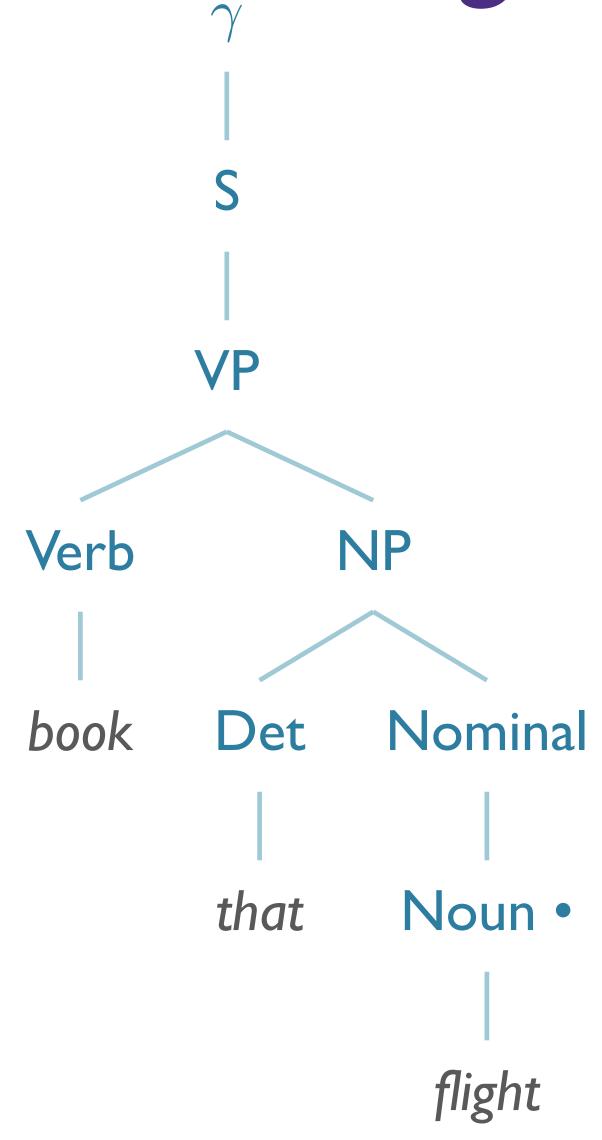
```
S0: \gamma \rightarrow \cdot S[0,0]
```

S3: $S \rightarrow VP \cdot [0,1]$

S8: *VP* → *Verb* • *NP* [0,1]

S21: *NP* → *Det* • *Nominal* [1,2]

S25: *Nominal* → *Noun* • [2,3]

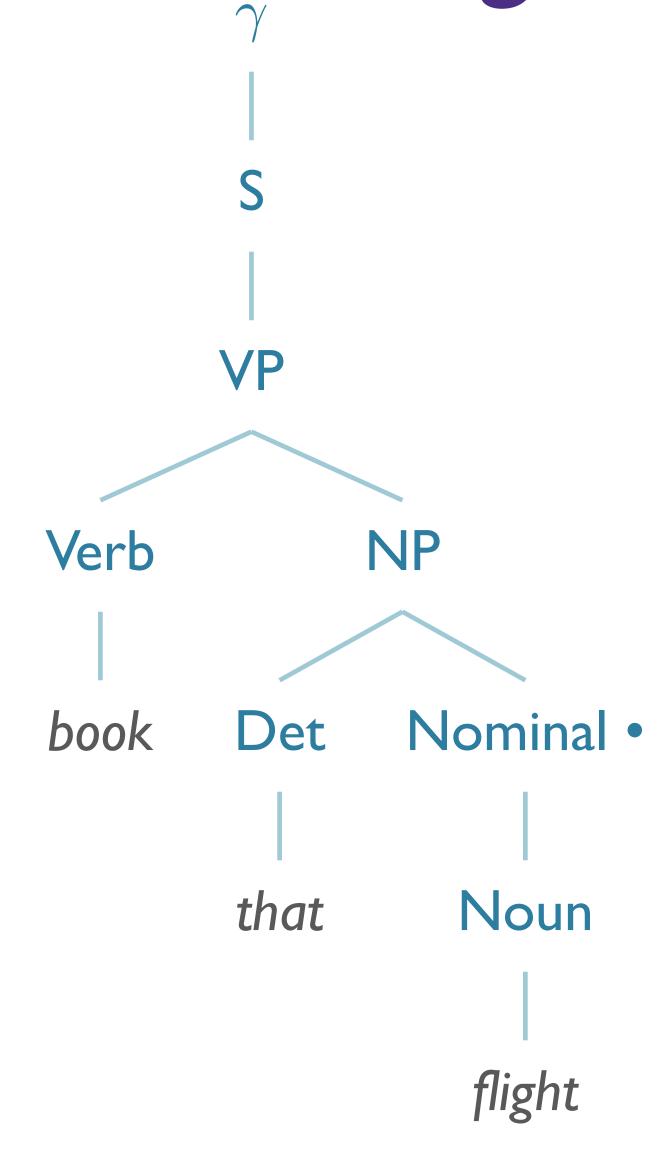


S0: $\gamma \rightarrow \cdot S[0,0]$

S3: $S \rightarrow VP \cdot [0,1]$

S8: *VP* → *Verb* • *NP* [0,1]

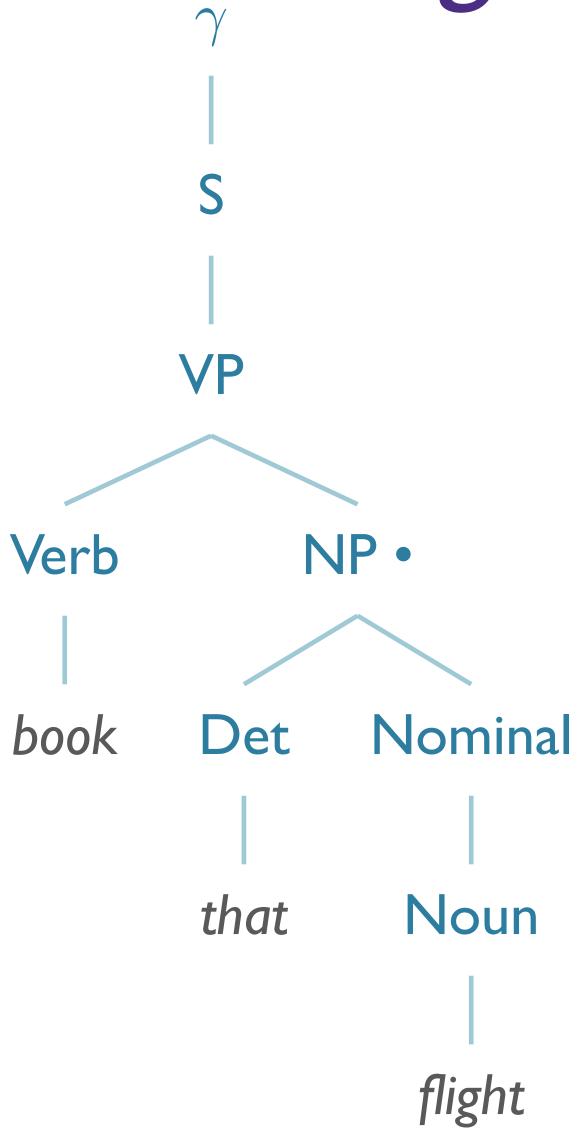
S21: *NP* → *Det Nominal* • [1,3]



S0: $\gamma \to S[0,0]$

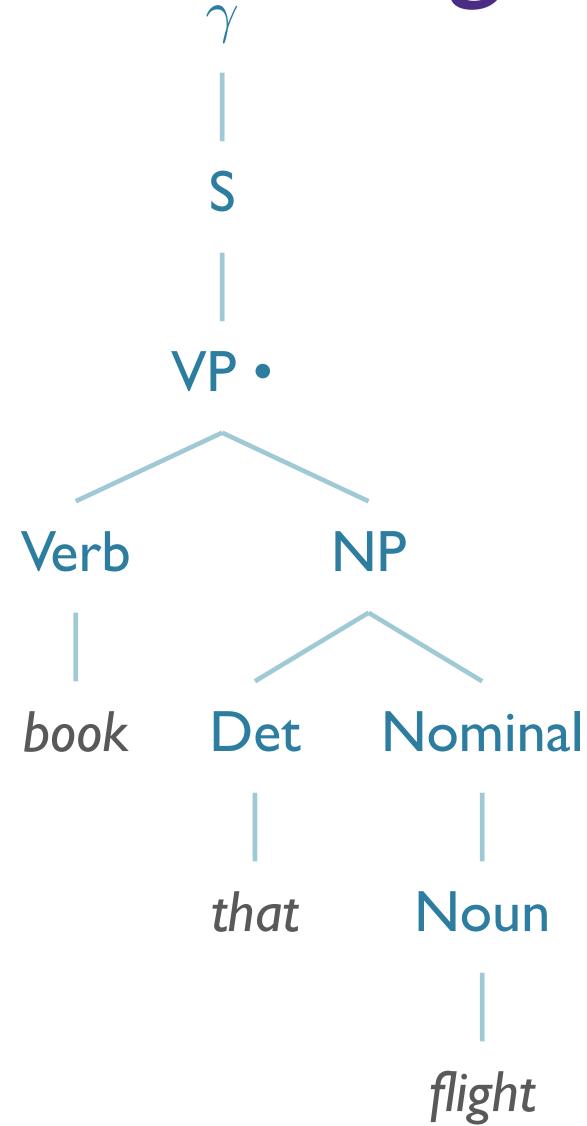
S3: $S \rightarrow VP \cdot [0,1]$

S8: *VP* → *Verb NP* • [0,3]



S0: $\gamma \to S[0,0]$

S3: $S \rightarrow VP \cdot [0,3]$



What About Dead Ends?

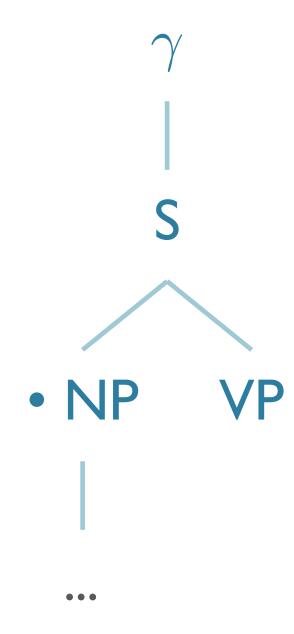
S0: $\gamma \to S[0,0]$

S1: $S \rightarrow \cdot NP VP$ [0,0]

NP → • Pronoun

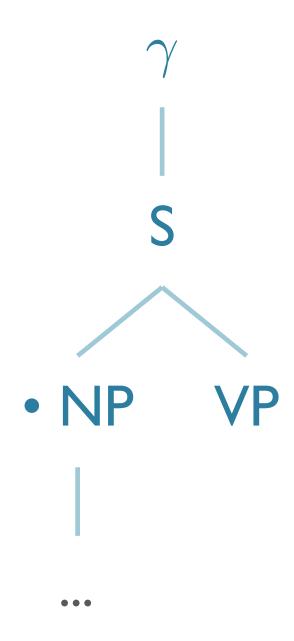
NP → • Proper-Noun

NP → • Det Nominal



book

```
S0: \gamma \to S[0,0]
S1: S \to NP VP[0,0]
```



book

 We now have a top-down parser in hand. Does it enter infinite loops on rules like S -> S 'and' S?

- We now have a top-down parser in hand. Does it enter infinite loops on rules like S -> S 'and' S?
- No!

```
procedure ENQUEUE(state, chart-entry)
  if state is not already in chart-entry then
    Push(state, chart-entry)
  end
```

- We now have a top-down parser in hand. Does it enter infinite loops on rules like S -> S 'and' S?
- No!

```
procedure ENQUEUE(state, chart-entry)
if state is not already in chart-entry then
    Push(state, chart-entry)
end
```

Exercise: parse 'table and chair' using the very simple grammar Nom -> Nom 'and' Nom | 'table' | 'chair'