

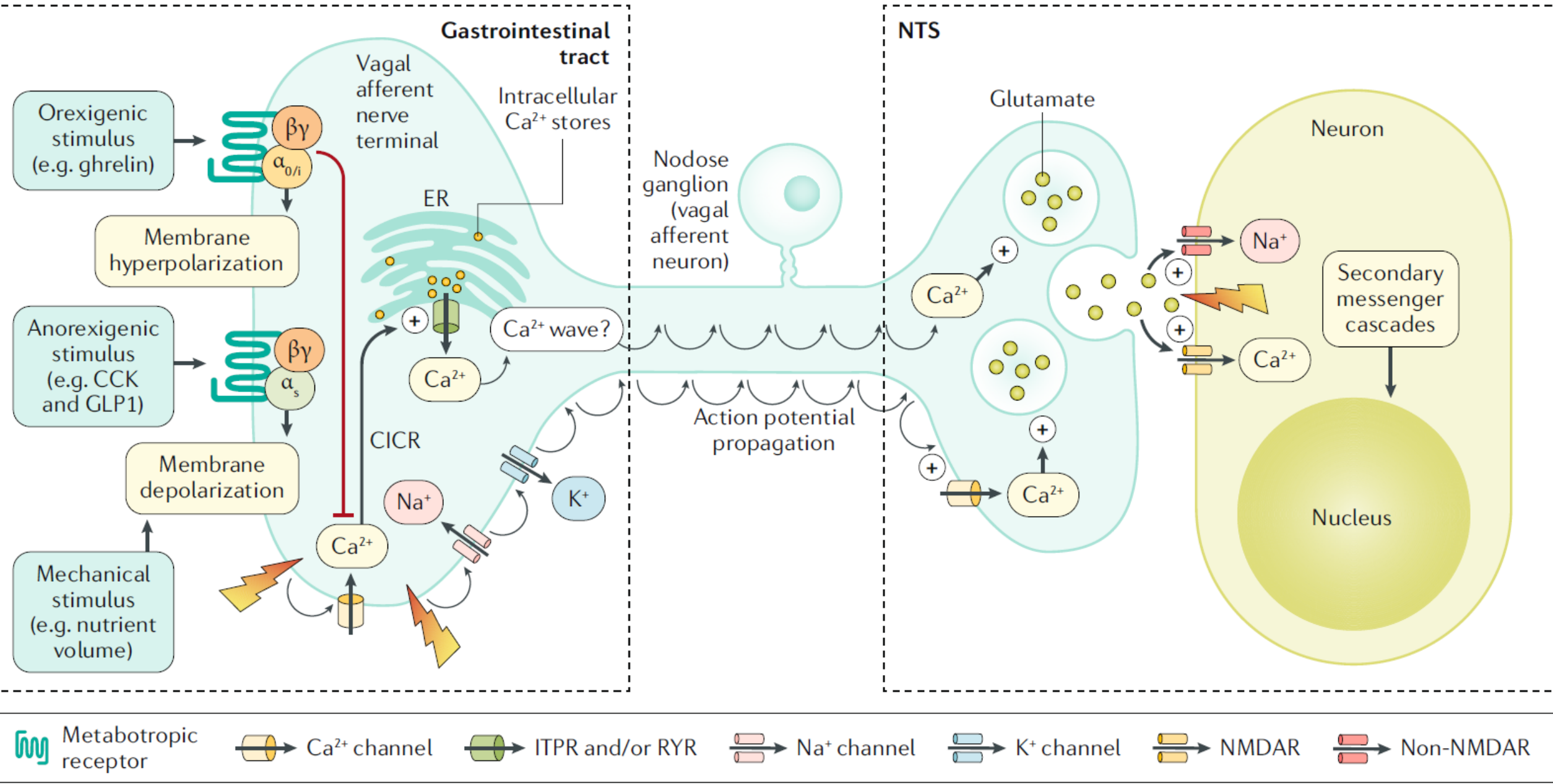
Microbiota Gut-Brain Axis: Action Potential of Afferent Vagus Nerve Simulation

Shannon Q Fernandes



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Afferent Vagus Nerve



Action Potential

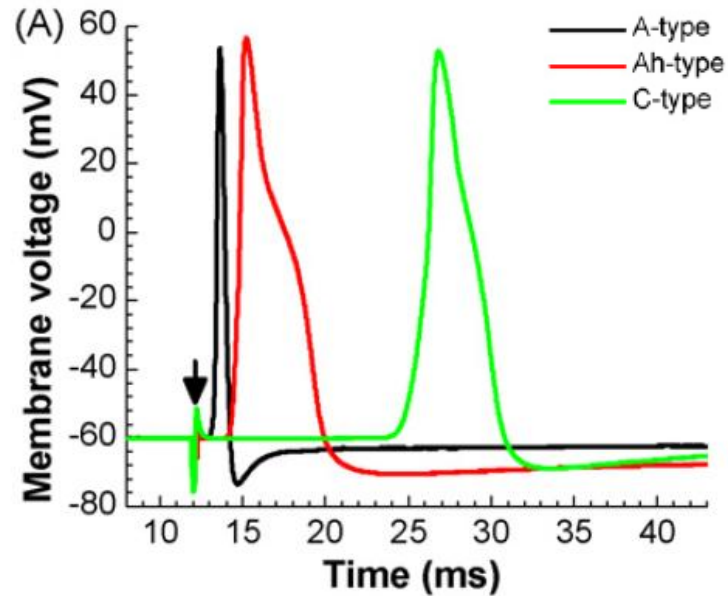
In the rat nodose ganglia, there neurons exists to be of the following types:

Myelinated A-type ~13%

Myelinated Ah-type ~12%

Unmyelinated C-type afferents ~75%

Action potential waveforms



Conduction velocity

A type ~10 m/s

Ah type: ~4 m/s

C type: ~ less than 1 m/s.

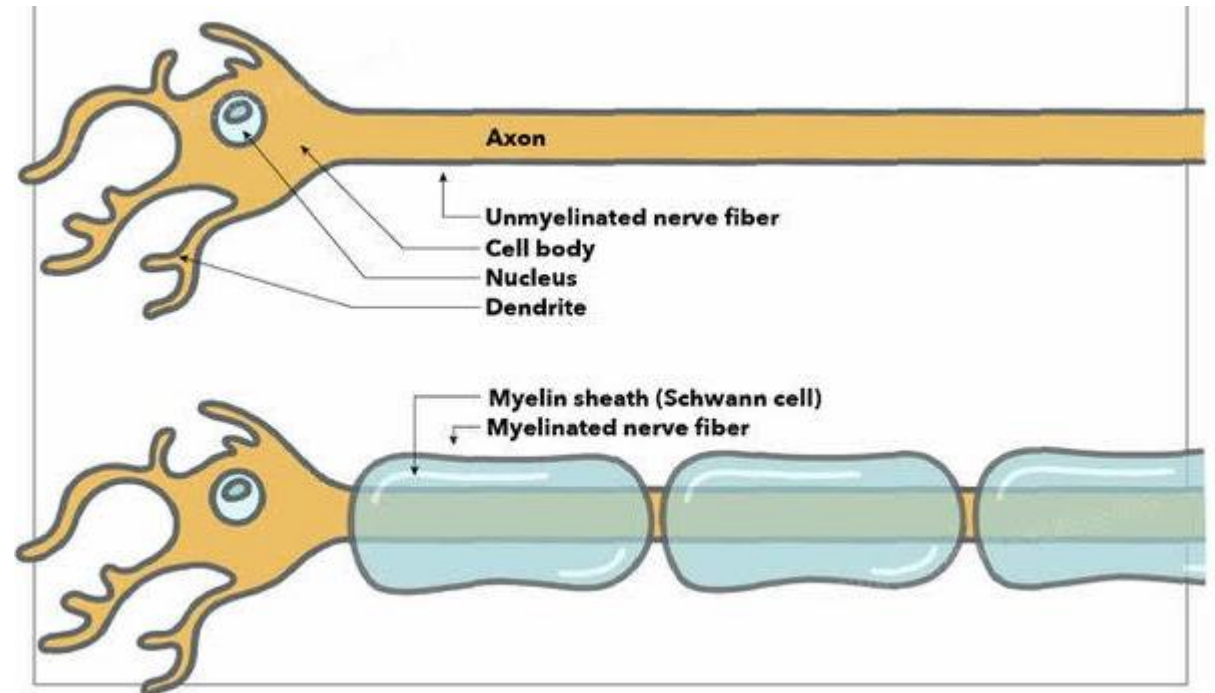
Electrophysiological and pharmacological validation of vagal afferent fiber type of neurons enzymatically isolated from rat nodose ganglia

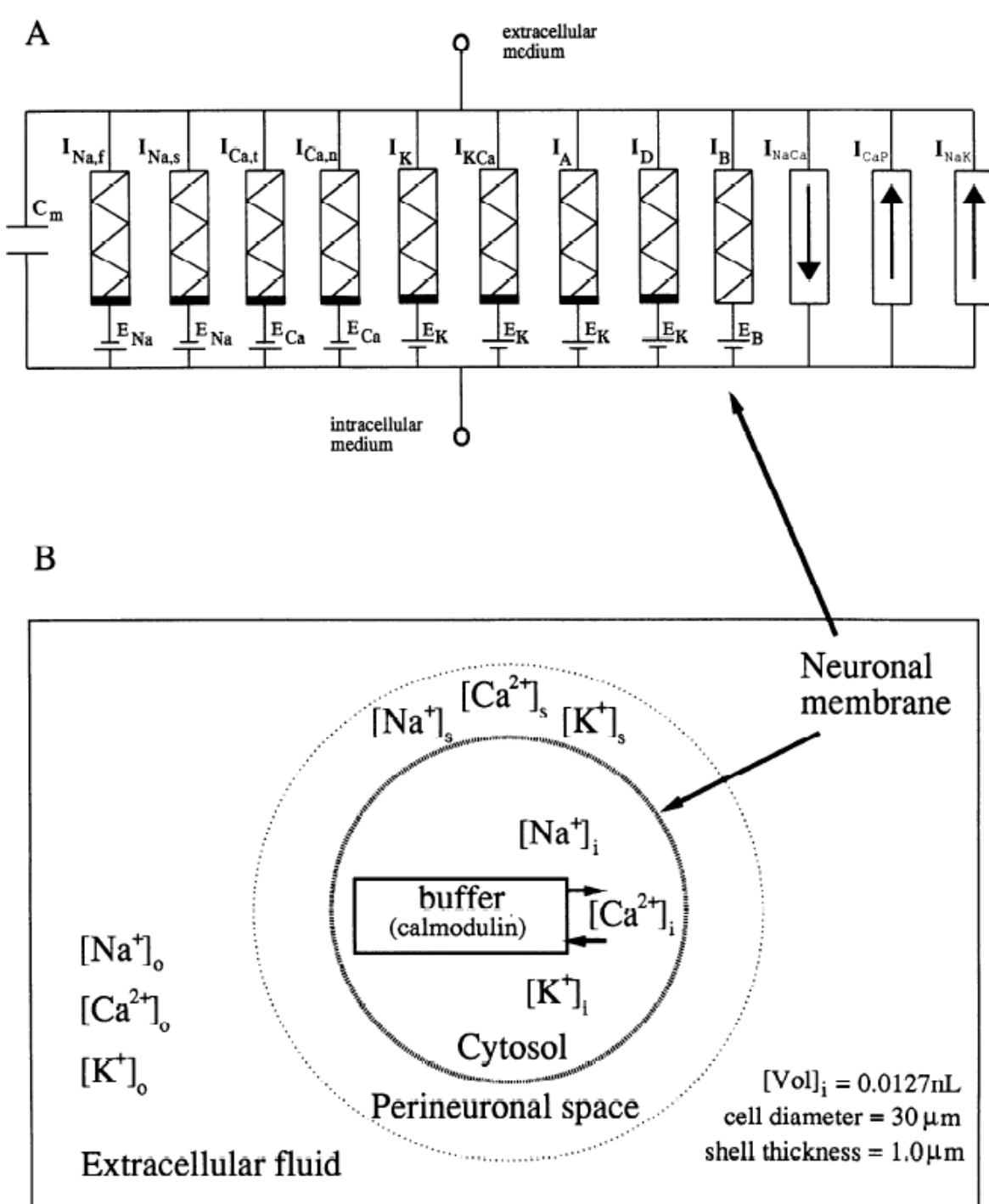
Bai-Yan Li^{a,b}, John H. Schild^{a,*}

^a Department of Biomedical Engineering, Indiana University Purdue University Indianapolis, 723 W. Michigan St., Suite SL174, Indianapolis, IN 46202, United States

^b Department of Pharmacology, Harbin Medical University, Harbin 150081, China

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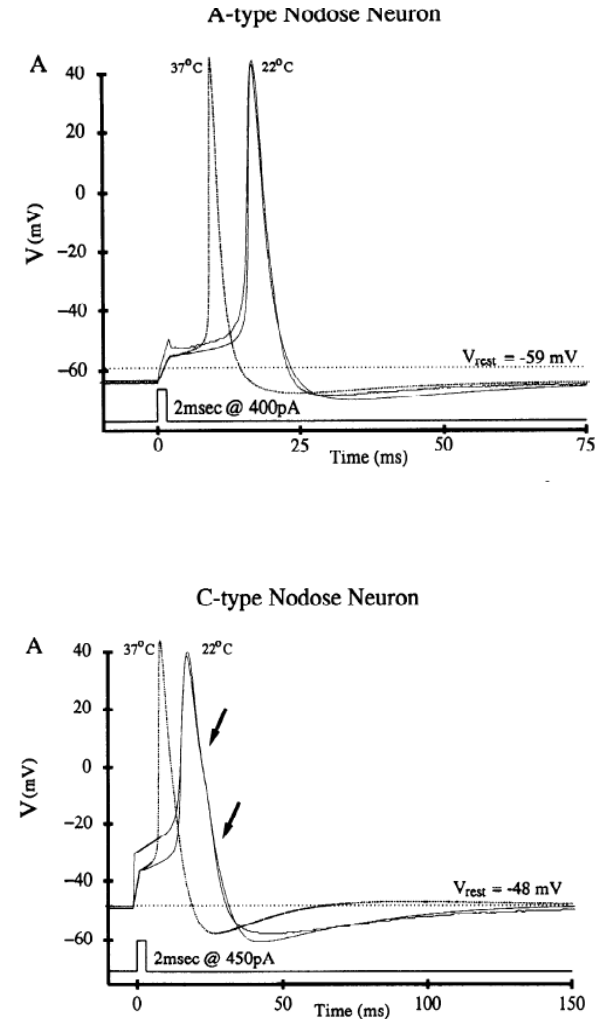


A- and C-Type Rat Nodose Sensory Neurons: Model Interpretations of Dynamic Discharge Characteristics

J. H. SCHILD, J. W. CLARK, M. HAY, D. MENDELOWITZ, M. C. ANDRESEN, AND D. L. KUNZE
Department of Electrical and Computer Engineering, Rice University, Houston 77251-1892; Department of Molecular Physiology and Biophysics, Baylor College of Medicine, Houston, 77030; and Department of Physiology and Biophysics, University of Texas Medical Branch, Galveston, Texas 77555

FIG. 2. Parallel conductance membrane model of a rat nodose neuron. **A:** equivalent circuit of the neuron where membrane capacitance C_m is shunted by time- and voltage-dependent sodium, calcium, and potassium channel-mediated currents ($I_{Na,f}$, $I_{Na,s}$, $I_{Ca,t}$, $I_{Ca,n}$, I_K), a Ca^{2+} activated potassium current (I_{KCa}), a transient outward current (I_A), a delay current (I_D), a linear leakage current (I_B), and electrogenic transporter-mediated currents (Na^+-Ca^{2+} exchanger, Na^+-K^+ pump, Ca^{2+} pump). E_{Na} , E_K , E_{Ca} , and E_B are the equilibrium potentials for the sodium, potassium, calcium, and background ion-mediated channels, respectively. **B:** lumped fluid compartmental model. This model consists of 3 separate well-stirred fluid compartments containing Na^+ , K^+ , and Ca^{2+} in different concentrations. The 3 compartments are 1) an intracellular fluid space describing lumped ion concentrations ($[Ca^{2+}]_i$, $[Na^+]_i$, $[K^+]_i$) and protein binding sites for Ca^{2+} on a calmodulin type buffer, 2) a $1.0 \mu\text{m}$ annular fluid space describing local ion concentrations ($[Ca^{2+}]_s$, $[Na^+]_s$, $[K^+]_s$) around the external surface of the neuron (not drawn to scale), and 3) a large extracellular volume where all ionic concentrations ($[Ca^{2+}]_o$, $[Na^+]_o$, $[K^+]_o$) are assumed to be constant.

Mathematical model



Action potential

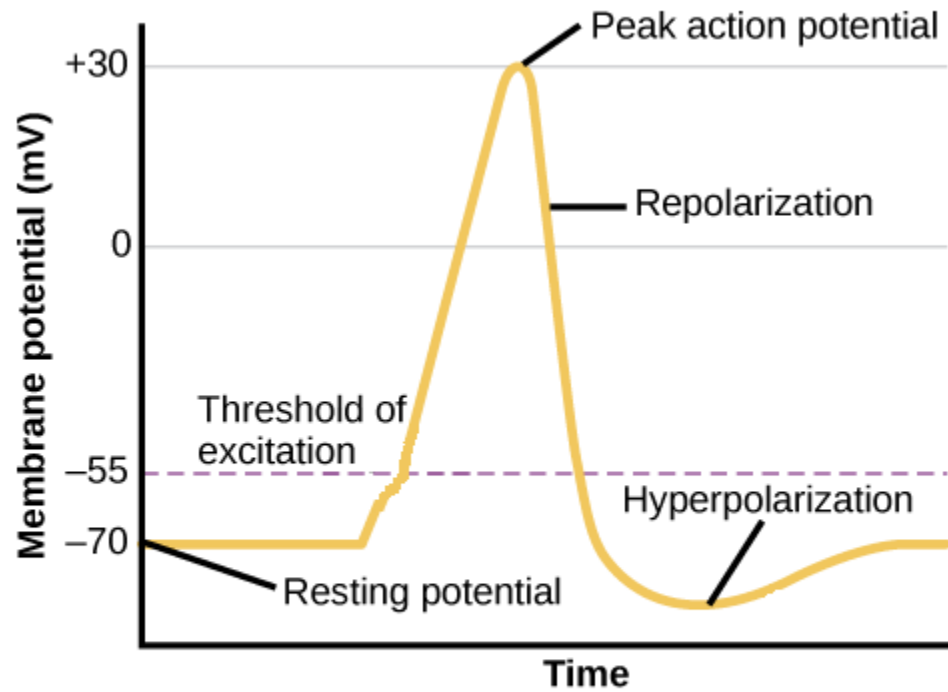
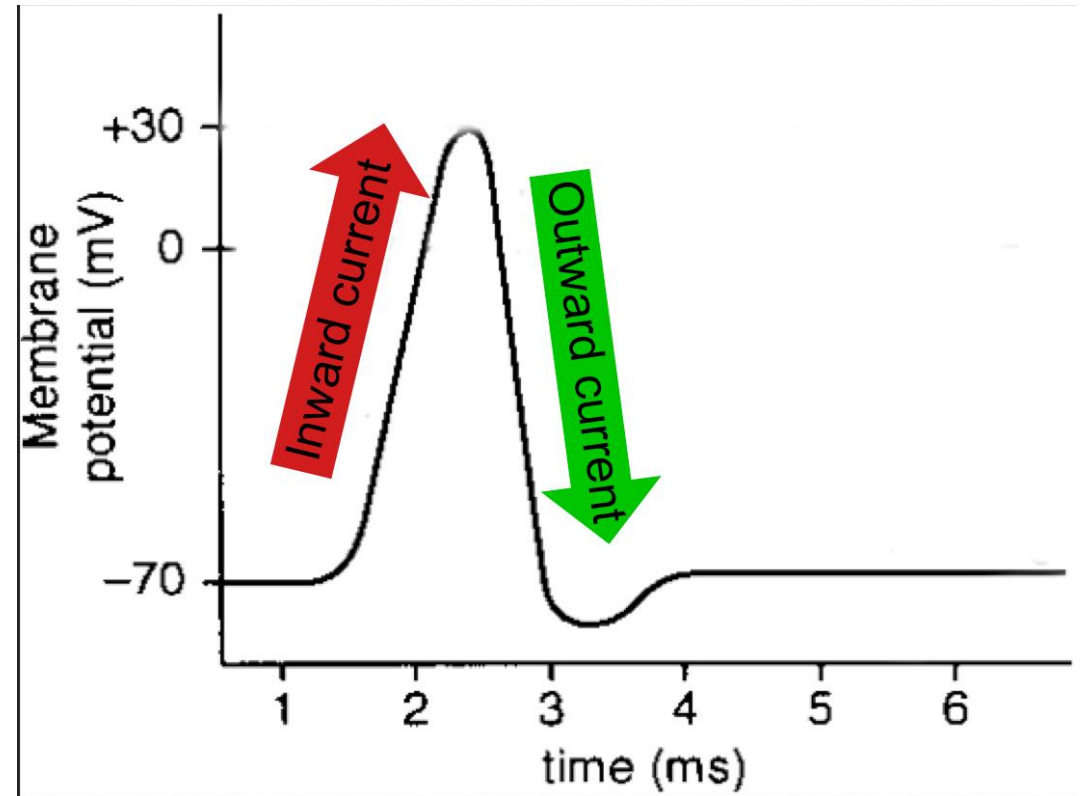


Image modified from "[How neurons communicate: Figure 3](#)," by OpenStax College, Biology ([CC BY 3.0](#)).



Inward Ca²⁺ channels

$I_{Ca,t}$: Low Threshold, Transient Calcium Current

$$I_{Ca,t} = \bar{g}_{Ca,t} d_t f_t (V - E_{Ca})$$

$$\dot{d}_t = \frac{d_{t\infty} - d_t}{\tau_{dt}}$$

$$\dot{f}_t = \frac{f_{t\infty} - f_t}{\tau_{ft}}$$

$$E_{Ca} = \frac{RT}{Z_{Ca}F} \ln \frac{[Ca^{2+}]_s}{[Ca^{2+}]_i} - 78.7$$

$$\tau_{dt} = 22.0 \exp(-(0.052)^2(V + 68.0)^2) + 2.5$$

$$\tau_{ft} = 103.0 \exp(-(0.050)^2(V + 58.0)^2) + 12.5$$

$$d_{t\infty} = \frac{1.0}{1.0 + \exp((V + 54.00)/-5.75)}$$

$$f_{t\infty} = \frac{1.0}{1.0 + \exp((V + 68.00)/6.0)}$$

$I_{Ca,n}$: High Threshold, Long-Lasting Calcium Current

$$I_{Ca,n} = \bar{g}_{Ca,n} d_n (0.55 f_{n_1} + 0.45 f_{n_2}) (V - E_{Ca})$$

$$\dot{d}_n = \frac{d_{n\infty} - d_n}{\tau_{dn}}$$

$$\dot{f}_{n_1} = \frac{f_{n_1\infty} - f_{n_1}}{\tau_{fn_1}}$$

$$\dot{f}_{n_2} = \frac{f_{n_2\infty} - f_{n_2}}{\tau_{fn_2}}$$

$$\tau_{dn} = 3.25 \exp(-(0.042)^2(V + 31.0)^2) + 0.395$$

$$\tau_{fn_1} = 33.5 \exp(-(0.0395)^2(V + 30.0)^2) + 5.0$$

$$\tau_{fn_2} = 225.0 \exp(-(0.0275)^2(V + 40.0)^2) + 75.00$$

$$d_{n\infty} = \frac{1.0}{1.0 + \exp((V + 20.0)/-4.5)}$$

$$f_{n_1\infty} = \frac{1.0}{1.0 + \exp((V + 20.0)/25.0)}$$

$$f_{n_2\infty} = r_n + \frac{1.0}{1.0 + \exp((V + 40.0)/10.0)}$$

$$r_n = \frac{0.2}{1.0 + \exp(\frac{V + 5.0}{-10.0})}$$

Inward Na⁺ channels

Tetrodotoxin (TTX) is a sodium channel blocker.

I_{Na_f} : Fast, TTX Sensitive Sodium Current

$$I_{Na_f} = \bar{g}_{Na_f} m_f^3 h_f j (V - E_{Na})$$

Nav1.3, Nav1.7

$$\dot{m}_f = \frac{m_{f\infty} - m_f}{\tau_{m_f}}$$

$$\dot{h}_f = \frac{h_{f\infty} - h_f}{\tau_{h_f}}$$

$$\dot{j} = \frac{j_{\infty} - j}{\tau_j}$$

$$\tau_{m_f} = 0.75 \exp(-(0.0635)^2 (V + 40.35)^2) + 0.12$$

$$\tau_{h_f} = 6.5 \exp(-(0.0295)^2 (V + 75.00)^2) + 0.55$$

$$m_{f\infty} = \frac{1.0}{1.0 + \exp((V + 41.35)/-4.75)}$$

$$h_{f\infty} = \frac{1.0}{1.0 + \exp((V + 62.00)/4.50)}$$

$$j_{\infty} = \frac{1.0}{1.0 + \exp((V + 40.00)/1.50)}$$

$$\tau_j = \frac{25.0}{1.0 + \exp((V - 20.00)/4.50)} + 0.01$$

I_{Na_s} : Slower, TTX Insensitive Sodium Current

$$I_{Na_s} = \bar{g}_{Na_s} m_s^3 h_s (V - E_{Na})$$

Nav1.8, Nav1.9

$$\dot{m}_s = \frac{m_{s\infty} - m_s}{\tau_{m_s}}$$

$$\dot{h}_s = \frac{h_{s\infty} - h_s}{\tau_{h_s}}$$

$$\tau_{m_s} = 1.50 \exp(-(0.0595)^2 (V + 20.35)^2) + 0.15$$

$$\tau_{h_s} = 4.95 \exp(-(0.0335)^2 (V + 20.00)^2) + 0.75$$

$$m_{s\infty} = \frac{1.0}{1.0 + \exp((V + 20.35)/-4.45)}$$

$$h_{s\infty} = \frac{1.0}{1.0 + \exp((V + 18.00)/4.50)}$$

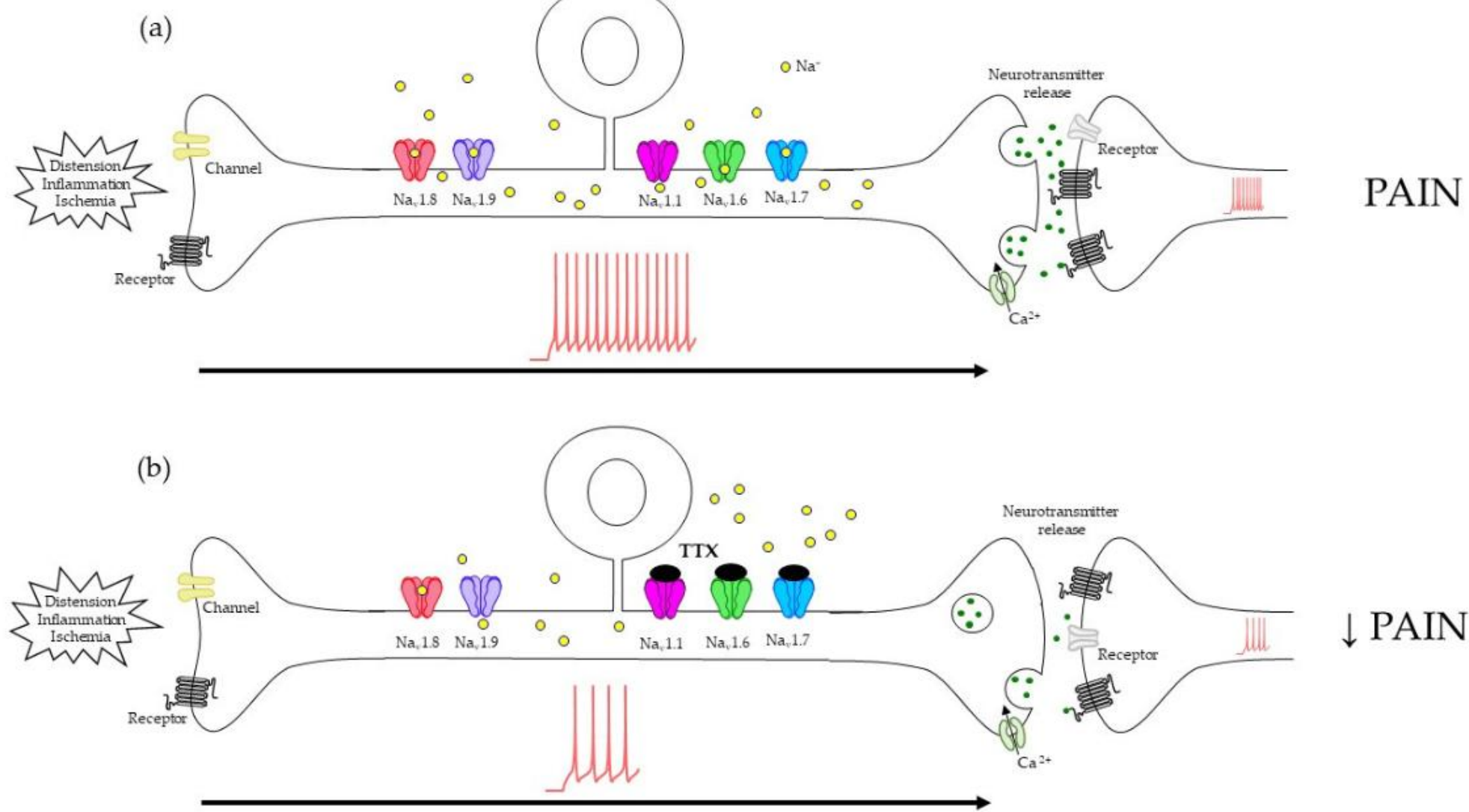
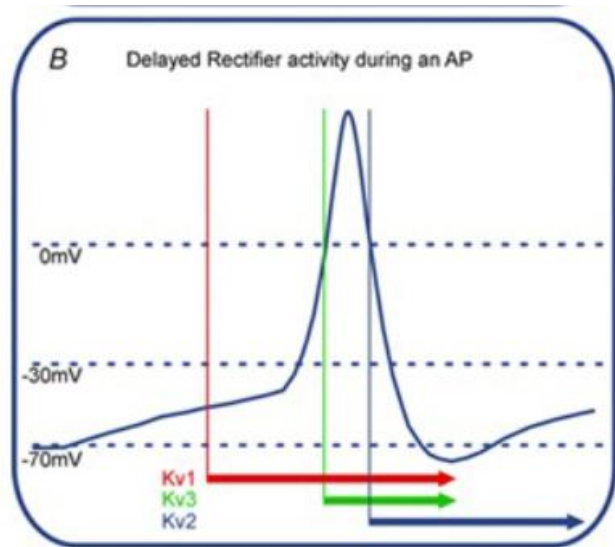


Figure 2. Mechanism proposed for the blockade of tetrodotoxin (TTX) sensitive voltage-gated sodium channels (VGSCs) to diminish pain transduction in primary sensory neurons. **(a)** After a noxious stimulus reaches the depolarization threshold, TTX-sensitive and -resistant VGSCs are activated, generating action potentials (APs) along the axon to the presynaptic terminal. Here, neurotransmitter release activates the postsynaptic neuron, and the stimulus is transmitted to the central nervous system, evoking pain sensations. **(b)** By blocking TTX-sensitive VGSCs with TTX, AP transmission is dampened and consequently, painful sensations decrease.

Outward K⁺ channels



I_K : Delayed Rectifier

$$I_K = \bar{g}_K n (V - E_K)$$

$$\dot{n} = \frac{n_{\infty} - n}{\tau_n}$$

$$\tau_n = \frac{1.0}{(\alpha_n + \beta_n)} + 1.0$$

$$n_{\infty} = \frac{1.0}{1.0 + \exp((V + 14.62)/-18.38)}$$

$$\alpha_n = \frac{0.001265(V + 14.273)}{1.0 - \exp((V + 14.273)/-10.0)}$$

$$\beta_n = 0.125 \exp\left(\frac{V + 55.0}{-2.5}\right)$$

I_A : Early Transient Outward Current

$$I_A = \bar{g}_A p^3 q (V - E_K)$$

$$\dot{p} = \frac{p_{\infty} - p}{\tau_p}$$

$$\dot{q} = \frac{q_{\infty} - q}{\tau_q}$$

$$\tau_p = 5.0 \exp(-(0.022)^2 (V + 65.0)^2) + 2.5$$

$$\tau_q = 100.0 \exp(-(0.035)^2 (V + 30.0)^2) + 10.5$$

$$p_{\infty} = \frac{1.0}{1.0 + \exp((V + 28.0)/-28.0)}$$

$$q_{\infty} = \frac{1.0}{1.0 + \exp((V + 58.0)/7.0)}$$

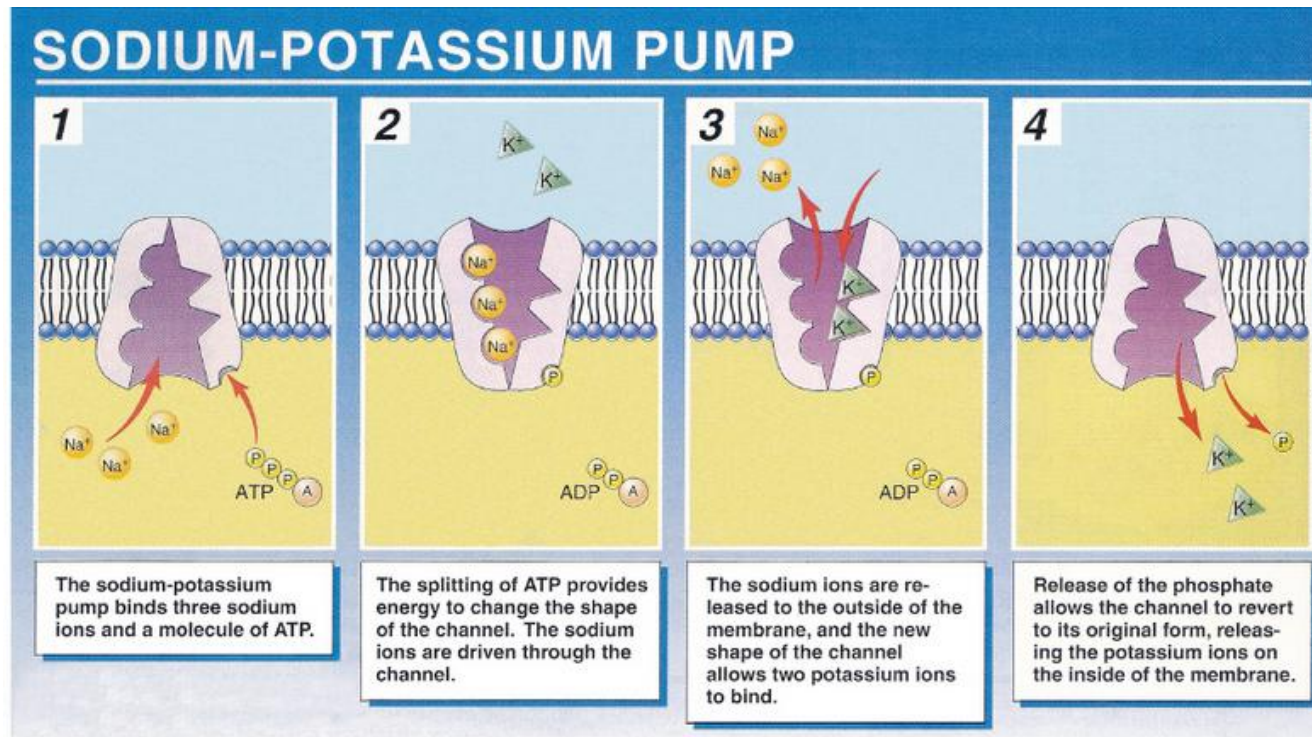
I_{CaP} : Calcium Pump Current

$$I_{CaP} = \bar{I}_{CaP} \left(\frac{[Ca^{2+}]_i}{[Ca^{2+}]_i + K_{M,CaP}} \right)$$

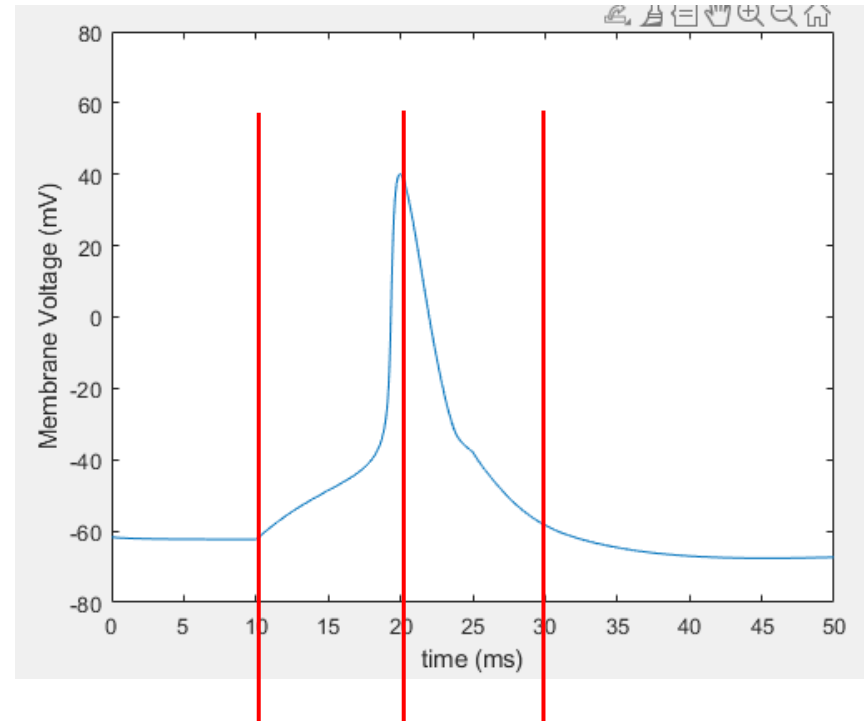
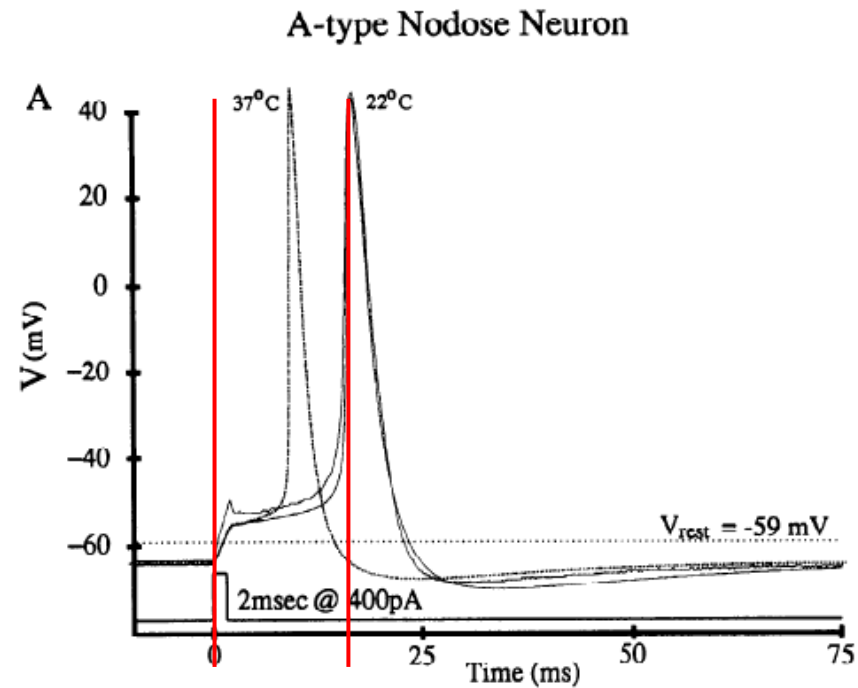
I_{NaK} : Sodium-Potassium Pump Current

Pumps

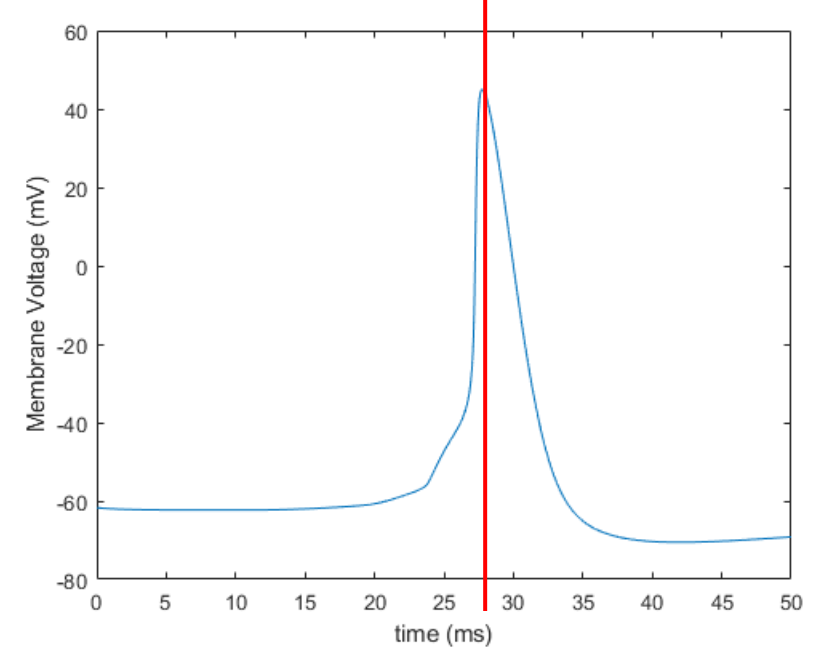
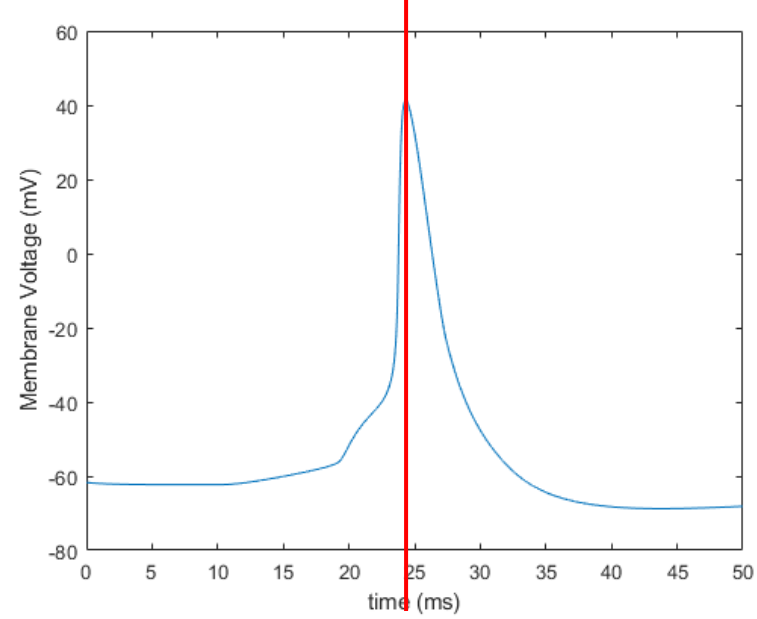
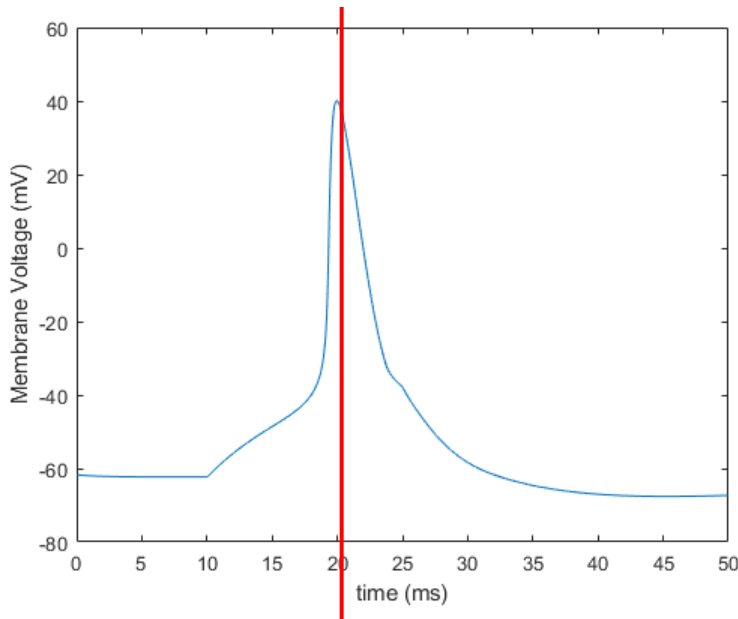
$$I_{NaK} = \bar{I}_{NaK} \left(\frac{[Na^+]_i}{[Na^+]_i + K_{M,Na}} \right)^3 \left(\frac{[K^+]_o}{[K^+]_o + K_{M,K}} \right)^2 \left(\frac{V+150}{V+200} \right)$$



Action potential: A- type Nodose Neuron (37°C)



Action potential Propagation: Cable theory



Stimulation current in 1st
compartment

Axon: 3 compartments

$$a/(2r_L) = 0.7 \text{ cm}^2/\text{s}$$

→ Cable equation:

$$c_m \frac{\partial V}{\partial t} = \frac{1}{2ar_L} \frac{\partial}{\partial x} \left(a^2 \frac{\partial V}{\partial x} \right) - i_m + i_e$$

Thank you & Questions

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