

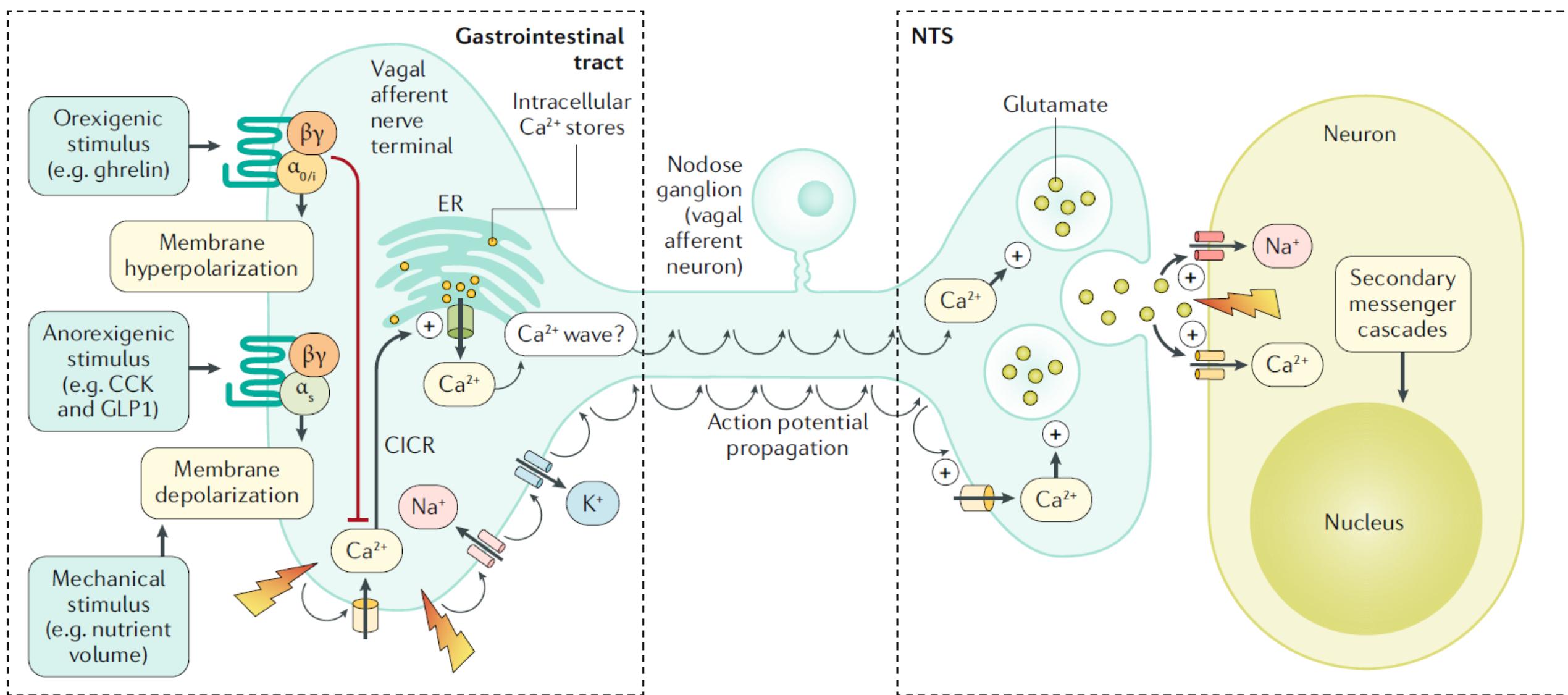
# Microbiota Gut-Brain Axis: Action Potential of Afferent Vagus Nerve Simulation

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LEHIGH  
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# Afferent Vagus Nerve



Metabotropic receptor

$\text{Ca}^{2+}$  channel

ITPR and/or RYR

$\text{Na}^+$  channel

$\text{K}^+$  channel

NMDAR

Non-NMDAR

# Action Potential

In the rat nodose ganglia, there neurons exists to be of the following types:

**Myelinated A-type ~13%**

**Myelinated Ah-type ~12%**

**Unmyelinated C-type afferents ~75%**

Electrophysiological and pharmacological validation of vagal afferent fiber type of neurons enzymatically isolated from rat nodose ganglia

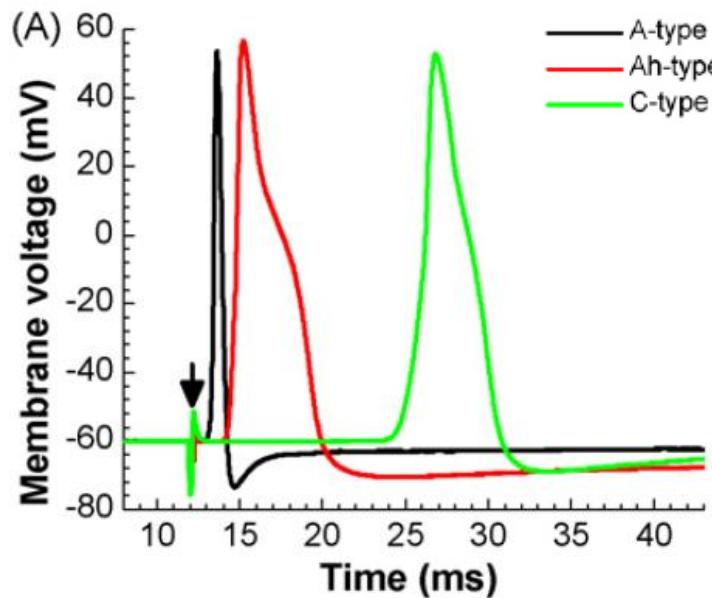
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Received 18 January 2007; received in revised form 26 March 2007; accepted 2 April 2007

## Action potential waveforms

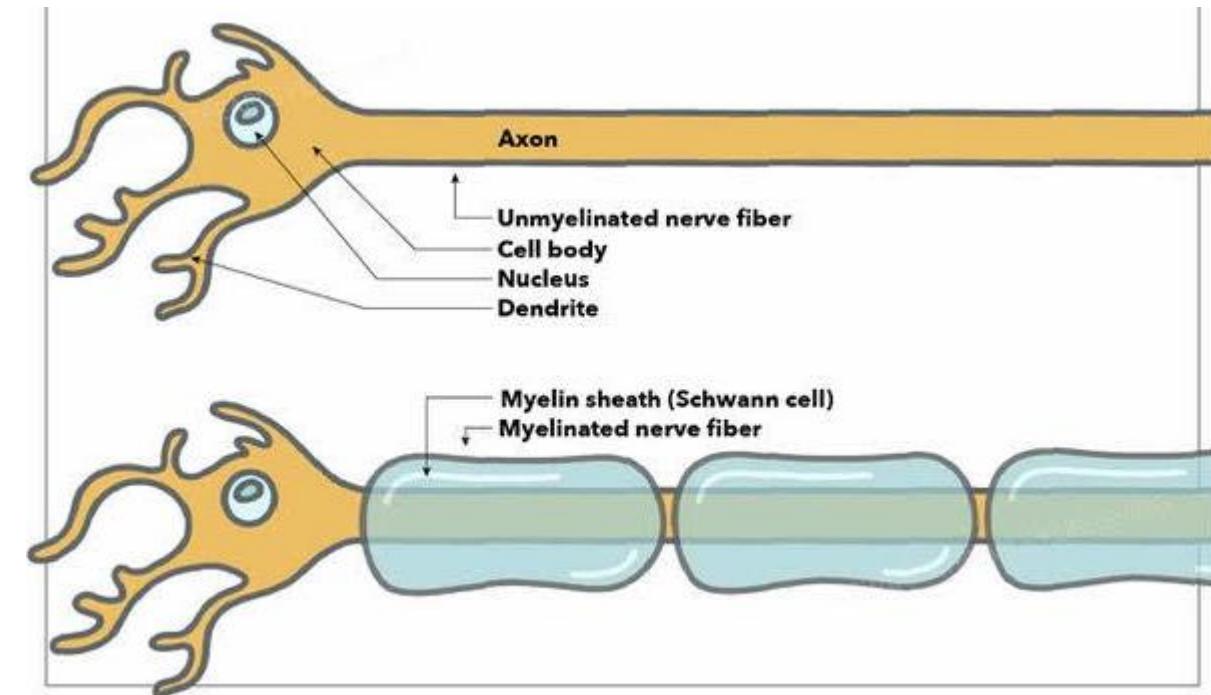


## Conduction velocity

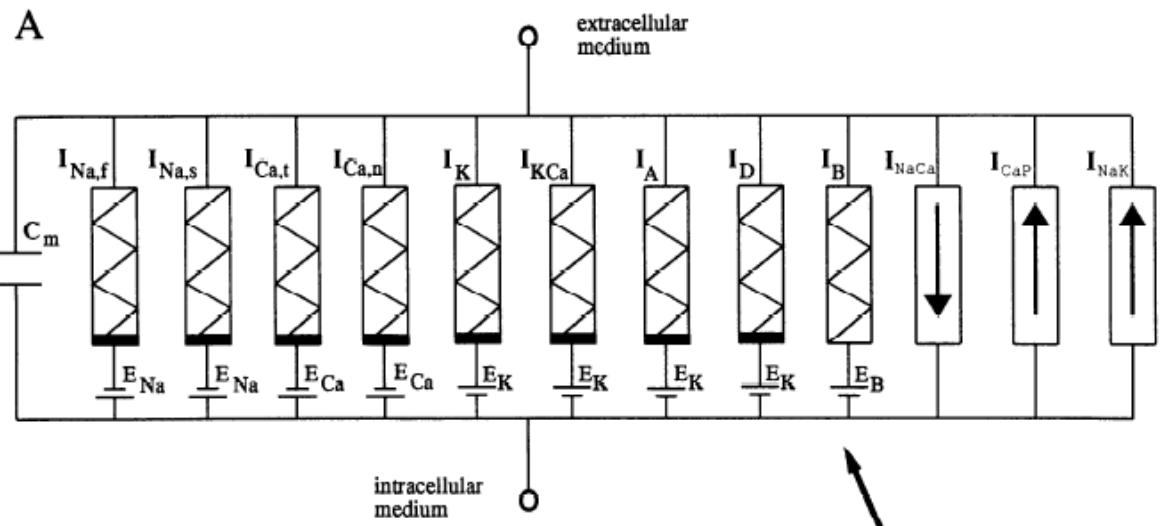
A type ~10 m/s

Ah type: ~4 m/s

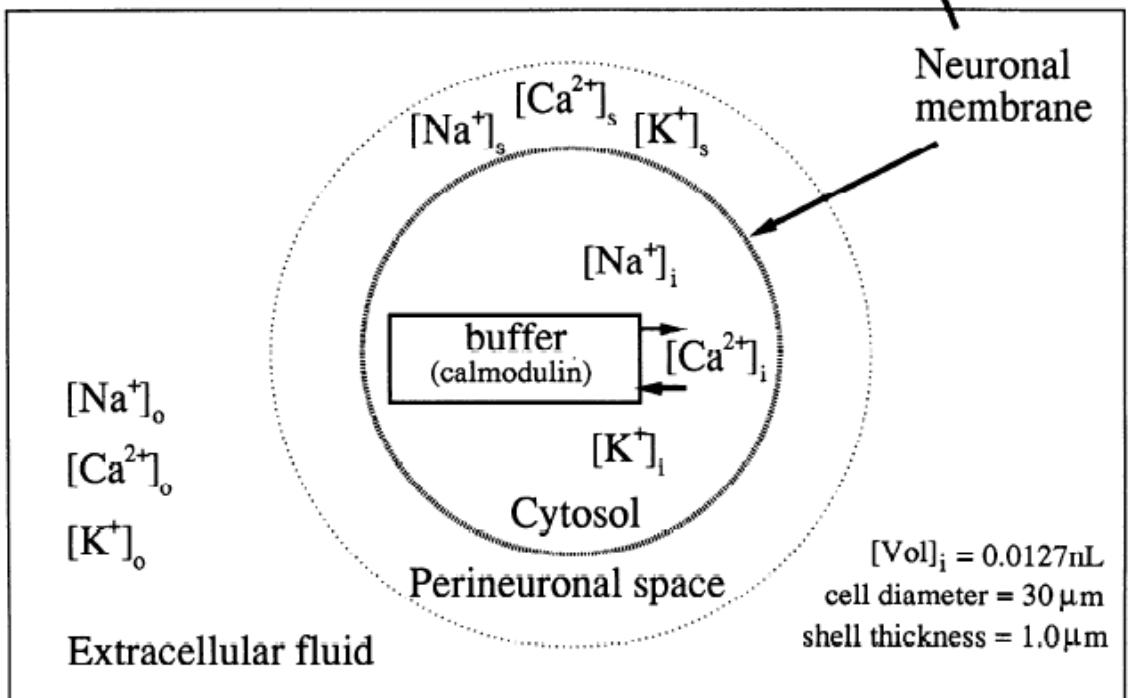
C type: ~ less than 1 m/s.



A



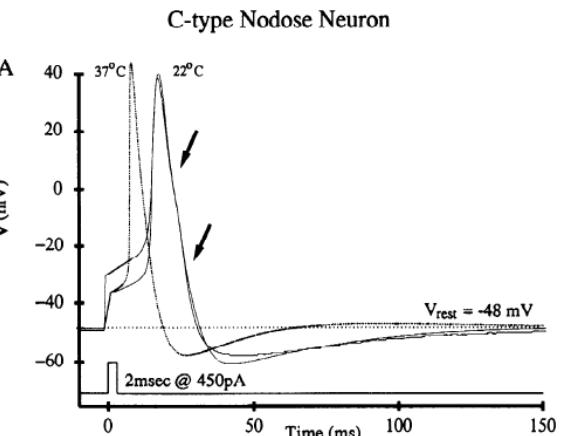
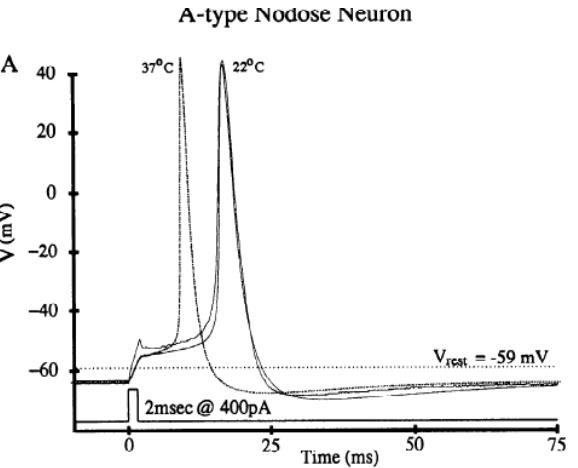
B



# A- and C-Type Rat Nodose Sensory Neurons: Model Interpretations of Dynamic Discharge Characteristics

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**FIG. 2.** Parallel conductance membrane model of a rat nodose neuron. *A*: equivalent circuit of the neuron where membrane capacitance  $C_m$  is shunted by time- and voltage-dependent sodium, calcium, and potassium channel-mediated currents ( $I_{Na,f}$ ,  $I_{Na,s}$ ,  $I_{Ca,t}$ ,  $I_{Ca,n}$ ,  $I_K$ ), a  $Ca^{2+}$  activated potassium current ( $I_{K,Ca}$ ), a transient outward current ( $I_A$ ), a delay current ( $I_D$ ), a linear leakage current ( $I_B$ ), and electrogenic transporter-mediated currents ( $Na^+$ - $Ca^{2+}$  exchanger,  $Na^+$ - $K^+$  pump,  $Ca^{2+}$  pump).  $E_{Na}$ ,  $E_K$ ,  $E_{Ca}$ , and  $E_B$  are the equilibrium potentials for the sodium, potassium, calcium, and background ion-mediated channels, respectively. *B*: lumped fluid compartmental model. This model consists of 3 separate well-stirred fluid compartments containing  $Na^+$ ,  $K^+$ , and  $Ca^{2+}$  in different concentrations. The 3 compartments are 1) an intracellular fluid space describing lumped ion concentrations ( $[Ca^{2+}]_i$ ,  $[Na^+]_i$ ,  $[K^+]_i$ ) and protein binding sites for  $Ca^{2+}$  on a calmodulin type buffer, 2) a 1.0  $\mu\text{m}$  annular fluid space describing local ion concentrations ( $[Ca^{2+}]_s$ ,  $[Na^+]_s$ ,  $[K^+]_s$ ) around the external surface of the neuron (not drawn to scale), and 3) a large extracellular volume where all ionic concentrations ( $[Ca^{2+}]_o$ ,  $[Na^+]_o$ ,  $[K^+]_o$ ) are assumed to be constant.



## Mathematical model

# Action potential

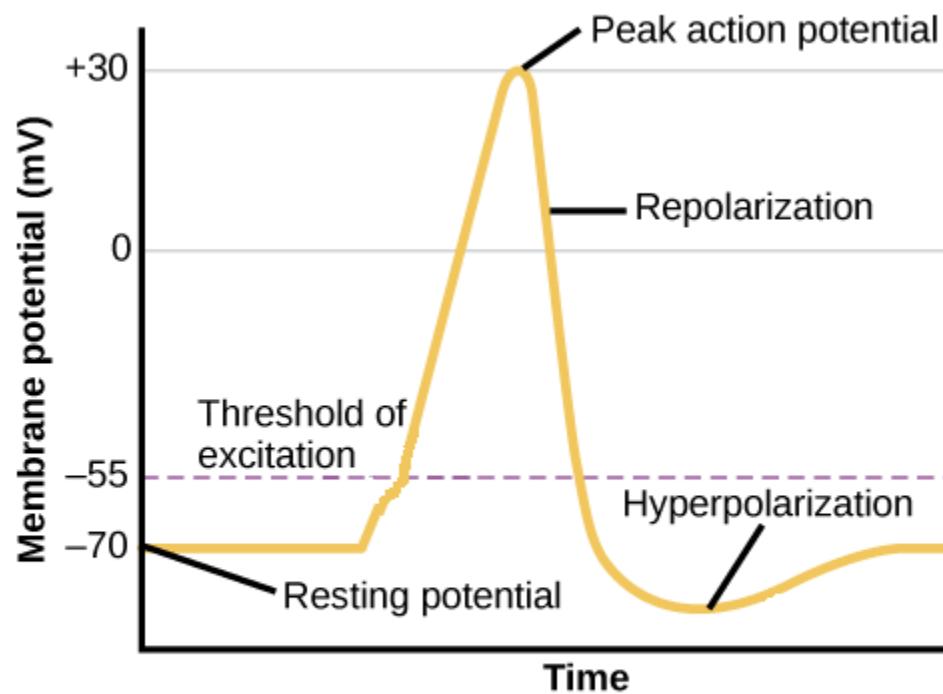
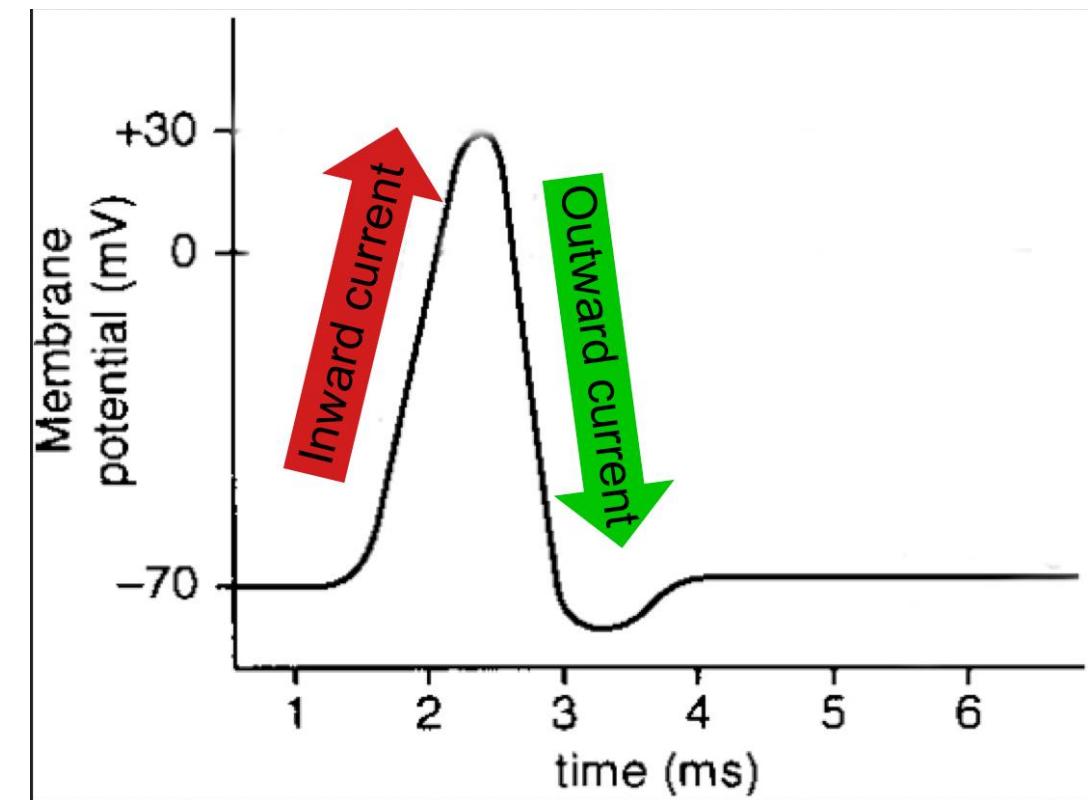


Image modified from "[How neurons communicate: Figure 3](#)," by OpenStax College, Biology ([CC BY 3.0](#)).



# Inward Ca<sup>2+</sup> channels

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$I_{Ca,t}$ : Low Threshold, Transient Calcium Current

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$$I_{Ca,t} = \bar{g}_{Ca,t} d_t f_t (V - E_{Ca})$$

$$\dot{d}_t = \frac{d_{t\infty} - d_t}{\tau_{dt}}$$

$$\dot{f}_t = \frac{f_{t\infty} - f_t}{\tau_{ft}}$$

$$E_{Ca} = \frac{RT}{Z_{Ca}F} \ln \frac{[Ca^{2+}]_s}{[Ca^{2+}]_i} - 78.7$$

$$\tau_{dt} = 22.0 \exp(-(0.052)^2(V + 68.0)^2) + 2.5$$

$$\tau_{ft} = 103.0 \exp(-(0.050)^2(V + 58.0)^2) + 12.5$$

$$d_{t\infty} = \frac{1.0}{1.0 + \exp((V + 54.00)/-5.75)}$$

$$f_{t\infty} = \frac{1.0}{1.0 + \exp((V + 68.00)/6.0)}$$

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$I_{Ca,n}$ : High Threshold, Long-Lasting Calcium Current

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$$I_{Ca,n} = \bar{g}_{Ca,n} d_n (0.55 f_{n1} + 0.45 f_{n2}) (V - E_{Ca})$$

$$\dot{d}_n = \frac{d_{n\infty} - d_n}{\tau_{dn}}$$

$$\dot{f}_{n1} = \frac{f_{n1\infty} - f_{n1}}{\tau_{fn1}}$$

$$\dot{f}_{n2} = \frac{f_{n2\infty} - f_{n2}}{\tau_{fn2}}$$

$$\tau_{dn} = 3.25 \exp(-(0.042)^2(V + 31.0)^2) + 0.395$$

$$\tau_{fn1} = 33.5 \exp(-(0.0395)^2(V + 30.0)^2) + 5.0$$

$$\tau_{fn2} = 225.0 \exp(-(0.0275)^2(V + 40.0)^2) + 75.00$$

$$d_{n\infty} = \frac{1.0}{1.0 + \exp((V + 20.0)/-4.5)}$$

$$f_{n1\infty} = \frac{1.0}{1.0 + \exp((V + 20.0)/25.0)}$$

$$f_{n2\infty} = r_n + \frac{1.0}{1.0 + \exp((V + 40.0)/10.0)}$$

$$r_n = \frac{0.2}{1.0 + \exp(\frac{V + 5.0}{-10.0})}$$

# Inward Na<sup>+</sup> channels

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$I_{Na_f}$ : Fast, TTX Sensitive Sodium Current

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$$I_{Na_f} = \bar{g}_{Na_f} m_f^3 h_f j(V - E_{Na})$$

Nav1.3, Nav1.7

$$\dot{m}_f = \frac{m_{f\infty} - m_f}{\tau_{m_f}}$$

$$\dot{h}_f = \frac{h_{f\infty} - h_f}{\tau_{h_f}}$$

$$\dot{j} = \frac{j_\infty - j}{\tau_j}$$

$$\tau_{m_f} = 0.75 \exp(-(0.0635)^2(V + 40.35)^2) + 0.12$$

$$\tau_{h_f} = 6.5 \exp(-(0.0295)^2(V + 75.00)^2) + 0.55$$

$$m_{f\infty} = \frac{1.0}{1.0 + \exp((V + 41.35) / -4.75)}$$

$$h_{f\infty} = \frac{1.0}{1.0 + \exp((V + 62.00) / 4.50)}$$

$$j_\infty = \frac{1.0}{1.0 + \exp((V + 40.00) / 1.50)}$$

$$\tau_j = \frac{25.0}{1.0 + \exp((V - 20.00) / 4.50)} + 0.01$$

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$I_{Na_s}$ : Slower, TTX Insensitive Sodium Current

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$$I_{Na_s} = \bar{g}_{Na_s} m_s^3 h_s (V - E_{Na})$$

Nav1.8, Nav1.9

$$\dot{m}_s = \frac{m_{s\infty} - m_s}{\tau_{m_s}}$$

$$\dot{h}_s = \frac{h_{s\infty} - h_s}{\tau_{h_s}}$$

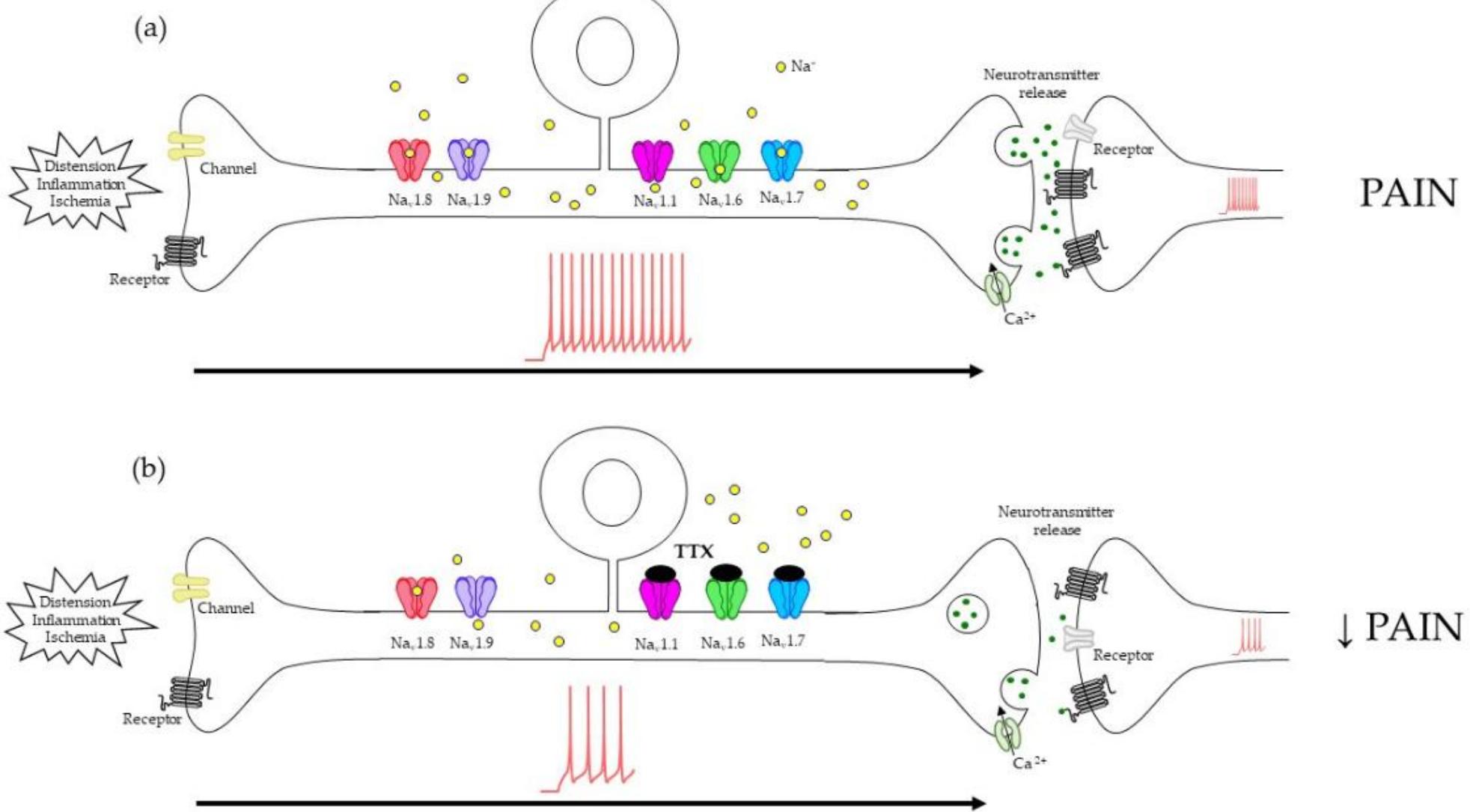
$$\tau_{m_s} = 1.50 \exp(-(0.0595)^2(V + 20.35)^2) + 0.15$$

$$\tau_{h_s} = 4.95 \exp(-(0.0335)^2(V + 20.00)^2) + 0.75$$

$$m_{s\infty} = \frac{1.0}{1.0 + \exp((V + 20.35) / -4.45)}$$

$$h_{s\infty} = \frac{1.0}{1.0 + \exp((V + 18.00) / 4.50)}$$

Tetrodotoxin (TTX) is a sodium channel blocker.



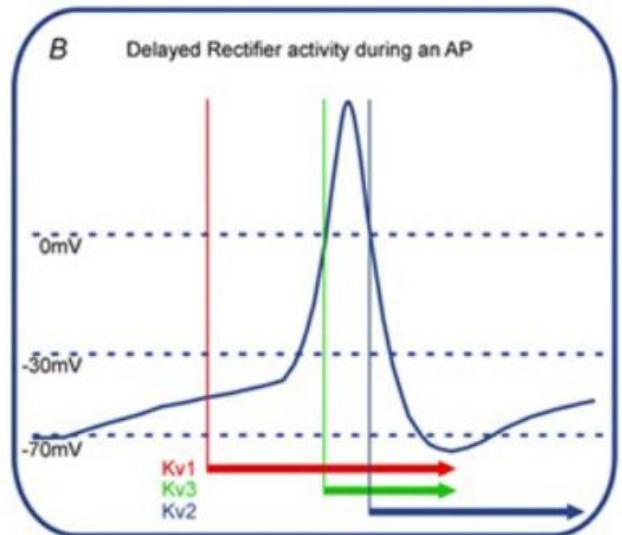
**Figure 2.** Mechanism proposed for the blockade of tetrodotoxin (TTX) sensitive voltage-gated sodium channels (VGSCs) to diminish pain transduction in primary sensory neurons. (a) After a noxious stimulus reaches the depolarization threshold, TTX-sensitive and -resistant VGSCs are activated, generating action potentials (APs) along the axon to the presynaptic terminal. Here, neurotransmitter release activates the postsynaptic neuron, and the stimulus is transmitted to the central nervous system, evoking pain sensations. (b) By blocking TTX-sensitive VGSCs with TTX, AP transmission is dampened and consequently, painful sensations decrease.

# Outward K<sup>+</sup> channels

## I<sub>K</sub>: Delayed Rectifier

$$I_K = \bar{g}_K n(V - E_K)$$

$$\dot{n} = \frac{n_\infty - n}{\tau_n}$$



$$\tau_n = \frac{1.0}{(\alpha_n + \beta_n)} + 1.0$$

$$n_\infty = \frac{1.0}{1.0 + \exp((V + 14.62)/-18.38)}$$

$$\alpha_n = \frac{0.001265(V + 14.273)}{1.0 - \exp((V + 14.273)/-10.0)}$$

$$\beta_n = 0.125 \exp\left(\frac{V + 55.0}{-2.5}\right)$$

## I<sub>A</sub>: Early Transient Outward Current

$$I_A = \bar{g}_A p^3 q(V - E_K)$$

$$\dot{p} = \frac{p_\infty - p}{\tau_p}$$

$$\dot{q} = \frac{q_\infty - q}{\tau_q}$$

$$\tau_p = 5.0 \exp(-(0.022)^2(V + 65.0)^2) + 2.5$$

$$\tau_q = 100.0 \exp(-(0.035)^2(V + 30.0)^2) + 10.5$$

$$p_\infty = \frac{1.0}{1.0 + \exp((V + 28.0)/-28.0)}$$

$$q_\infty = \frac{1.0}{1.0 + \exp((V + 58.0)/7.0)}$$

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## $I_{CaP}$ : Calcium Pump Current

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$$I_{CaP} = \bar{I}_{CaP} \left( \frac{[Ca^{2+}]_i}{[Ca^{2+}]_i + K_{M,CaP}} \right)$$

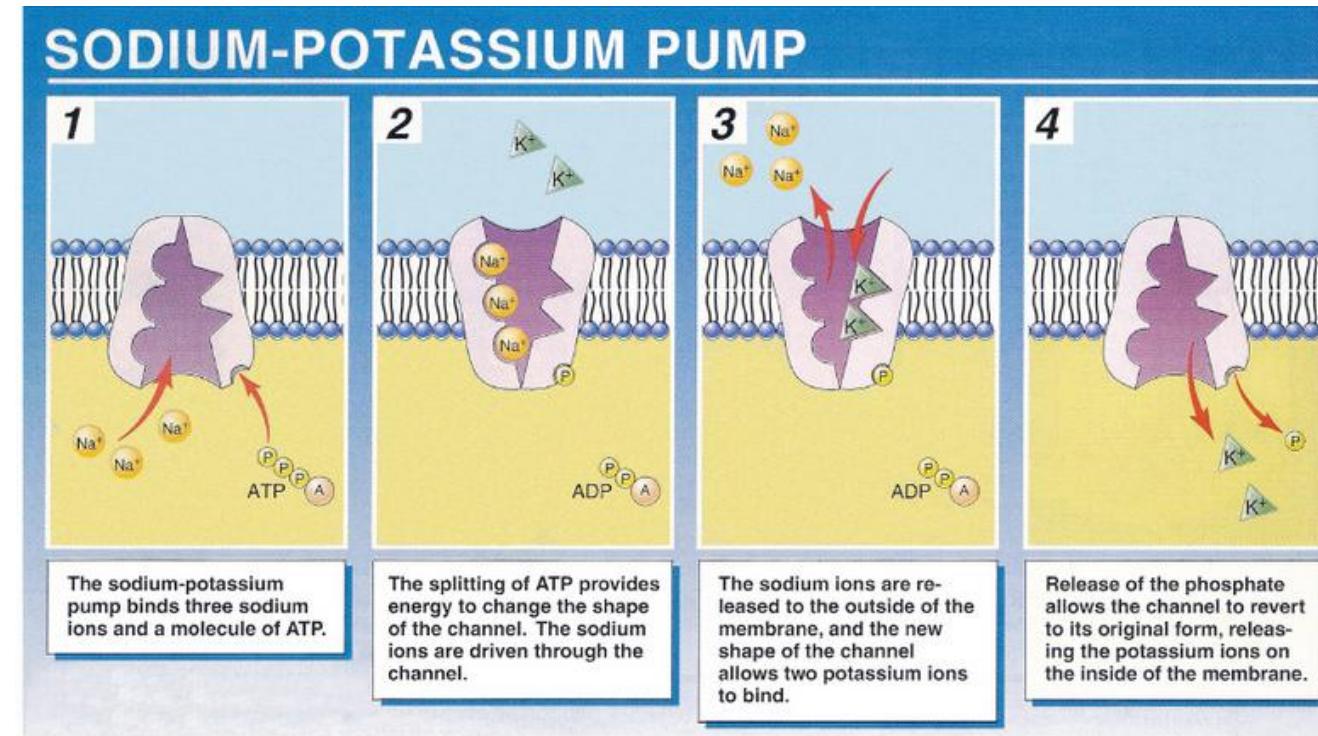
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## $I_{NaK}$ : Sodium-Potassium Pump Current

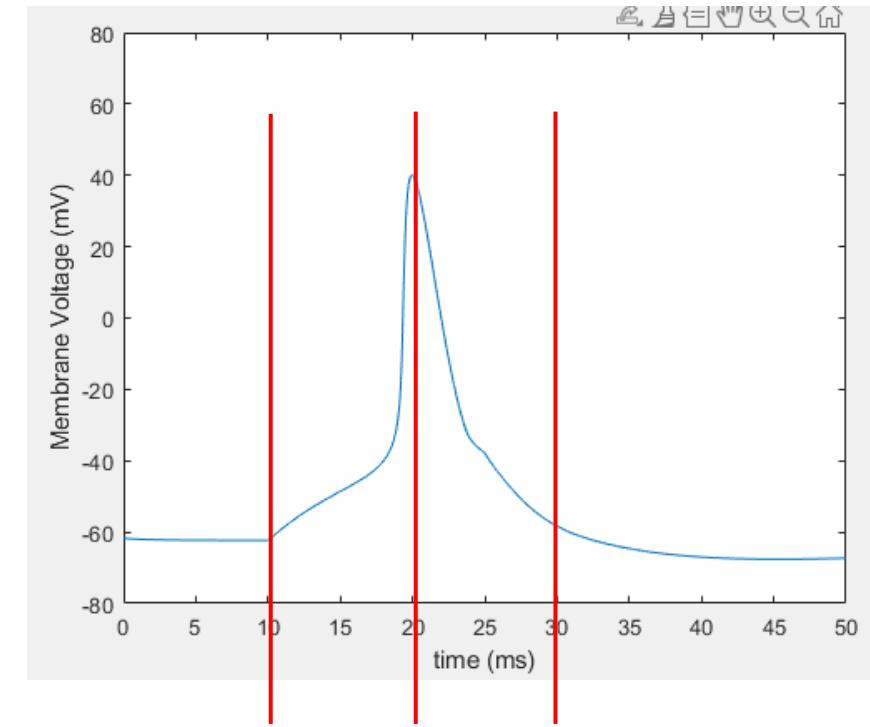
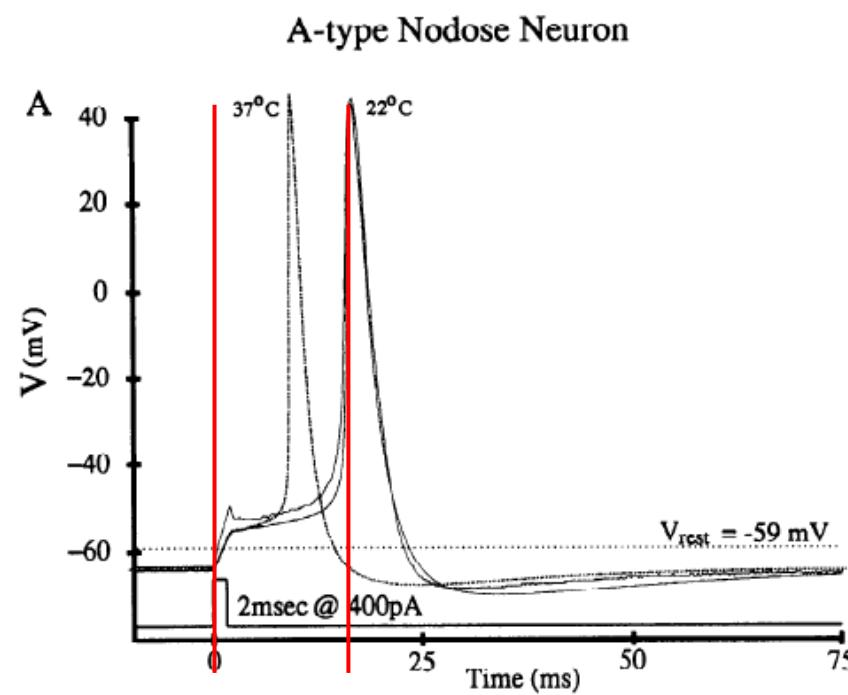
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# Pumps

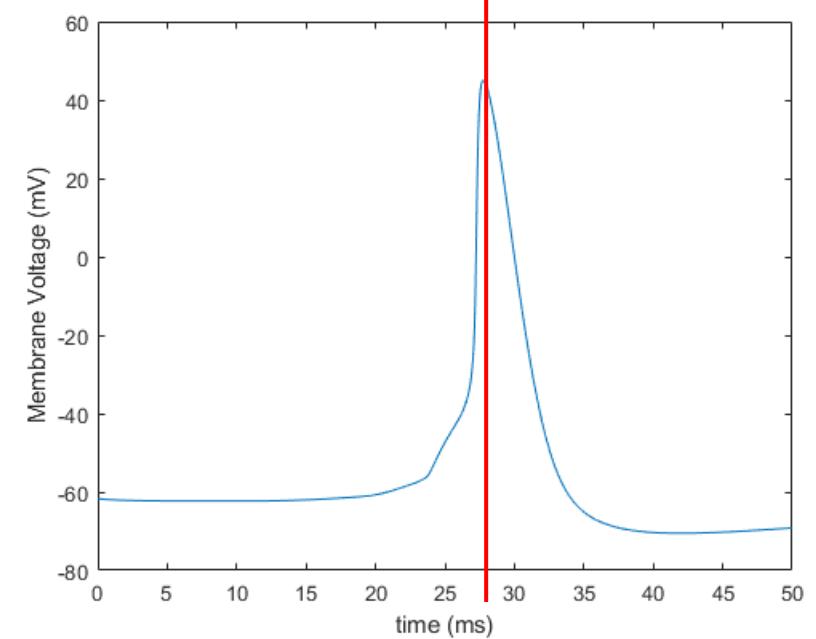
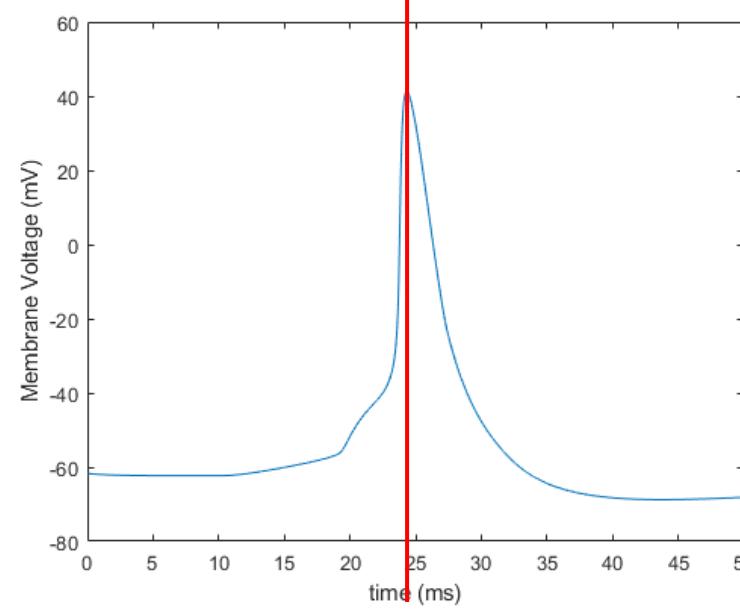
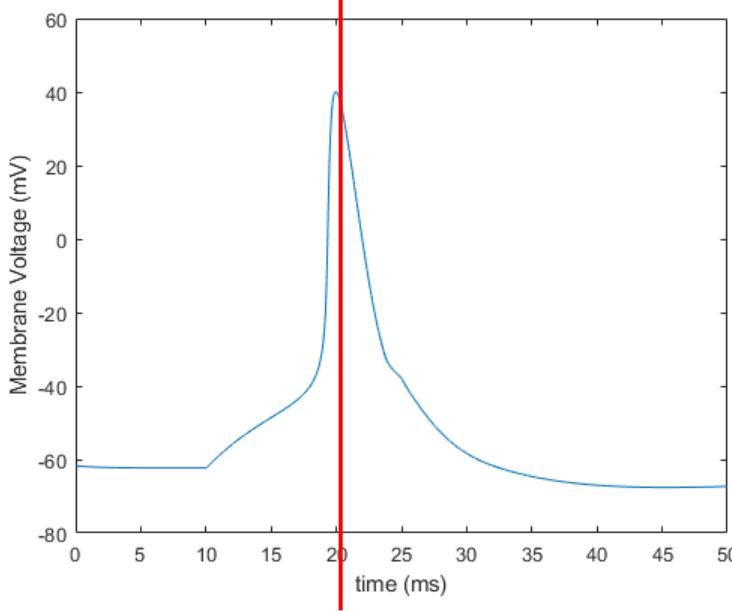
$$I_{NaK} = \bar{I}_{NaK} \left( \frac{[Na^+]_i}{[Na^+]_i + K_{M,Na}} \right)^3 \left( \frac{[K^+]_o}{[K^+]_o + K_{M,K}} \right)^2 \left( \frac{V+150}{V+200} \right)$$



# Action potential: A- type Nodose Neuron (37°C)



# Action potential Propagation: Cable theory



Stimulation current in 1<sup>st</sup> compartment

$$a/(2r_L) = 0.7 \text{ cm}^2/\text{s}$$



Axon: 3 compartments

→ Cable equation:

$$c_m \frac{\partial V}{\partial t} = \frac{1}{2ar_L} \frac{\partial}{\partial x} \left( a^2 \frac{\partial V}{\partial x} \right) - i_m + i_e$$

Thank you & Questions

# References

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