

Applied Financial Econometrics, Spring Semester, 2023  
Problem Set 1, March 22, 2023

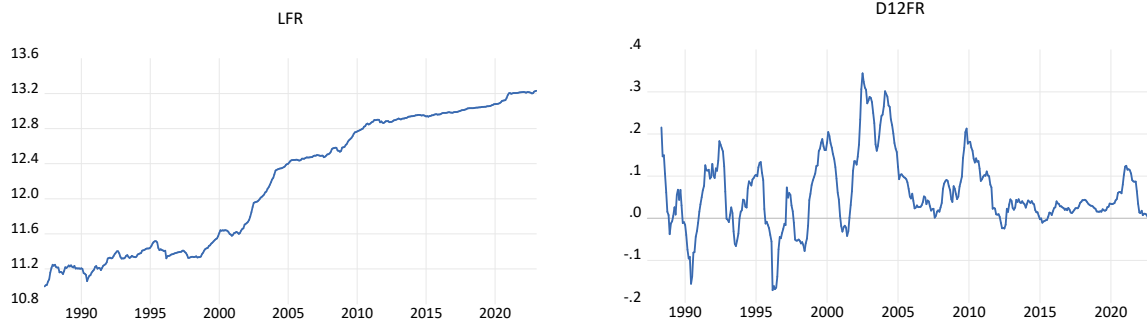
1. [Ex. 1.4]

**Ans.** By definition,  $Y_{t1} \stackrel{d}{=} Y_{t2}, \forall t1, t2$ .

□

2. [Ex. 2.2]

**Ans.**



$$\overline{DUM}_t = 0.812950$$

□

3. [Ex. 3.1]

**Ans.**

(a)

$$\gamma(j) = \begin{cases} (1 + \theta^2)\sigma^2 & \text{if } j = 0 \\ \theta\sigma^2 & \text{if } j = 1 \\ 0 & \text{if } j > 1 \end{cases}$$

(b) Yes.

$$\begin{aligned} E(Y_t) &= 0 \\ Var(Y_t) &= (1 + \theta^2)\sigma^2 < \infty \\ \gamma(j) \end{aligned}$$

□

4. [Ex. 3.2]

**Ans.**

(a)

$$\begin{aligned} (1 - 1.2L + 0.2L^2)Y_t &= \epsilon_t \\ (1 - 1.2L + 0.4L^2)Y_t &= \epsilon_t \\ (1 - 1.2L - 1.2L^2)Y_t &= \epsilon_t \\ (1 + 1.2L)Y_t &= \epsilon_t \\ (1 - 0.7L - 0.25L^2 + 0.175L^3)Y_t &= \epsilon_t \end{aligned}$$

□

(b)

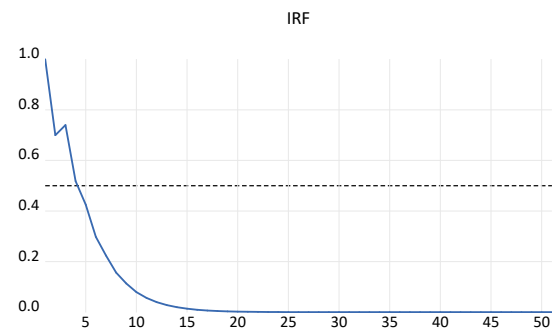
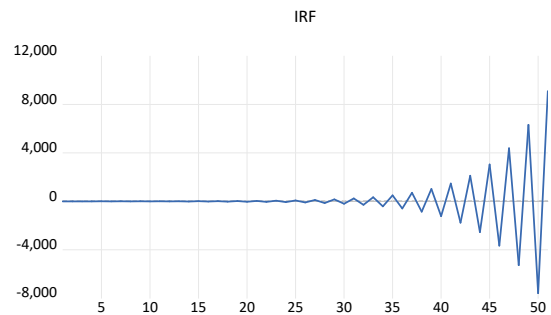
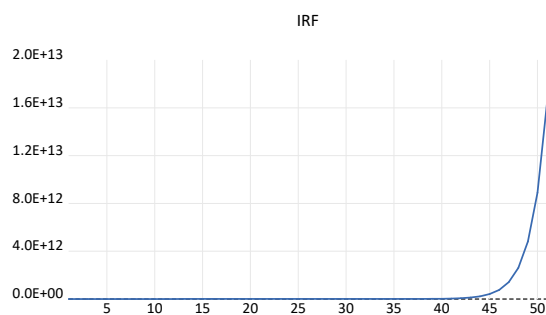
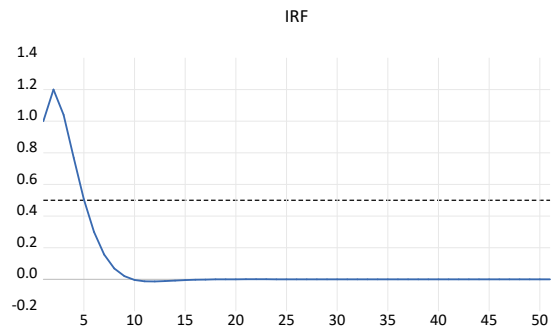
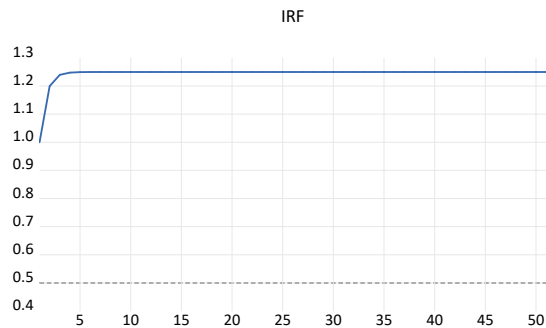
$$\beta(z) = 1 - 1.2z + 0.2z^2 = 0, \quad z = 1, 5 \Rightarrow \text{nonstationary}$$

$$\beta(z) = 1 - 1.2z + 0.4z^2 = 0, \quad z = 1.5 + 0.5i, 1.5 - 0.5i \Rightarrow \text{stationary}$$

$$\beta(z) = 1 - 1.2z - 1.2z^2 = 0, \quad z = 0.540833, -1.540833 \Rightarrow \text{nonstationary}$$

$$\beta(z) = 1 + 1.2z = 0, \quad z = -0.8333333 \Rightarrow \text{nonstationary}$$

$$\beta(z) = 1 - 0.7z - 0.25z^2 + 0.175z^3 = 0, \quad z = 1.428571, -2.000000, 2.000000 \Rightarrow \text{stationary}$$



□

5. [Ex. 3.3]

**Ans.**

$$Cov(Y_1, Y_0) = 0 \neq \phi_1 \sigma^2 = Cov(Y_2, Y_1)$$

□

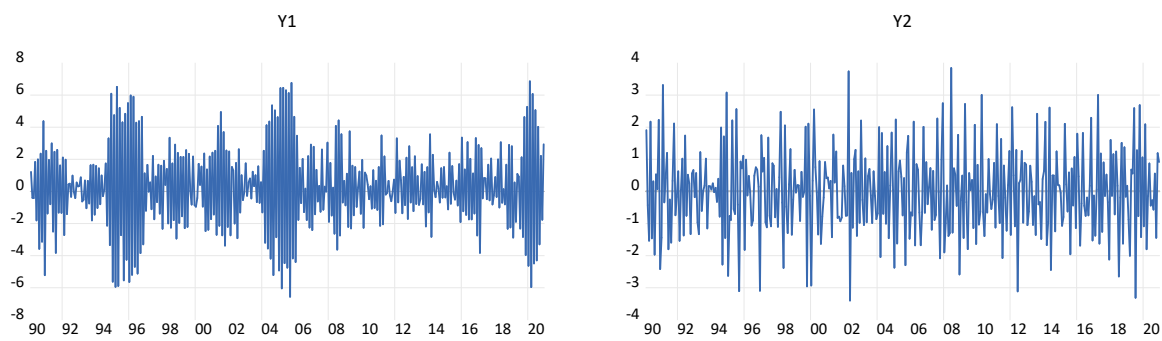
6. [Ex. 3.4]

**Ans.**

$$|\phi_1| < 1 \text{ (given)}, \quad E(Y_0) = \frac{\phi_0}{1 - \phi_1}, \quad Var(Y_0) = \frac{\sigma^2}{1 - \phi_1^2}$$

□

7. [Ex. 3.19]  
**Ans.**



□