Final Project

Air Quality Dataset

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BUS2-193

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Part 1 & 2 Introduction of Dataset

Within an Italian city, there was a dataset collection of hourly average air quality responses. The data was collected from a field within a populated area at road level over a one year time span, from the date March 2004 to February 2005. By using an Air Quality Chemical Multisensor Device, the data was separated into what different metal oxide chemical observations were found, CO, Non Metanic Hydrocarbons, Benzene, Total Nitrogen Oxides (NOx) and Nitrogen Dioxide (NO2). The dataset of 9358 recordings includes the date, time, and hourly averages of each chemical looked for in each individual data point collected.

Our chosen dataset includes 14 variables when input into R. Below are included each variable type that will be found.

Variable	Description			
Date	Tells us when the data was recorded			
Time	The exact time the data was collected			
CO(GT)	Averaged concentration of Carbon Monoxide in mg per cubic meter - CO is colorless, odorless gas that is harmful when inhaled,			
PT08.S1(CO)	Hourly average sensor response of Tin Oxide			
NMHC(GT)	Hourly Average measurement of Non methane Hydrocarbons concentration in micrograms / cubic meters. - Important reactive gasses that play a key role in production and destruction of the ozone troposphere.			
С6Н6	Hourly Average measurement of Benzene concentration in micrograms / cubic meters			
PT08.S2 (NMHC) (Titania)	Hourly average sensor response			
NOx(GT)	True Hourly average NOx concentration in parts per billion - When in the presence of NMHC's, the reaction helps the formation of tropospheric ozone and stratospheric H2			
PT08.S3(NOx)	Hourly average measurement of Tungsten oxide (NOx targeted) - Contribute to the formation of tropospheric ozone and stratosphere			

NO2	Hourly Average of Nitrous DiOxide in micrograms / cubic meters			
PT08.S4	Hourly Average sensor response (NO2 Targeted)			
PT08.S5(O3)	Hourly average sensor response of Tungsten oxide (O3 Targeted)			
Т	Temperature in celsius			
RH	Relative Humidity			
АН	Absolute Humidity			

Figure 0. Attribute Information

Using this dataset, we want to observe how different the air quality was throughout the year. By inputting the data in R, we can make charts to observe if we can find any correlation between variables, any outliers, and maybe see if different times or dates affect the responses. With the data, we want to be able to achieve a linear regression to show if there are any trends throughout the year. Our group decided on using temperature as our independent variable to report our findings being affected by temperature.

The data that was chosen comes from a main road in an urban area within an Italian city. The reason for the collection by the original collectors was to observe the pollutant levels in the area with a concentration of Co, No_x , NO_2 , and benzene.

Part 3 Preliminary Analysis

```
> str(atrquality)
tibble [9,357 x 15] ($3: tbl_df/tbl/data.frame)
$ Date : POSIXct[1:9357], format: "2004-03-10" "2004-03-10" ...
$ Time : POSIXct[1:9357], format: "1899-12-31 18:00:00" "1899-12-31 19:00:00" ...
$ CO(GT) : num [1:9357] 2.6 2 2 .2 2 .2 1.6 1.2 1 0.9 0.6 ...
$ PT08.51(CO) : num [1:9357] 1360 1292 1402 1376 1272 ...
$ NMHC(GT) : num [1:9357] 150 112 88 80 51 38 31 31 24 19 ...
$ C6H6(GT) : num [1:9357] 11.88 9.4 9 9.23 6.52 ...
$ PT08.52(NMHC): num [1:9357] 1046 955 939 948 836 ...
$ NOX(GT) : num [1:9357] 1046 955 939 948 836 ...
$ NOX(GT) : num [1:9357] 1056 1174 1140 1092 1205 ...
$ NOZ(GT) : num [1:9357] 139 2 114 122 116 96 77 76 60 -200 ...
$ PT08.53(NOX) : num [1:9357] 139 2 114 122 116 96 77 76 60 -200 ...
$ PT08.54(NO2) : num [1:9357] 1692 1559 1554 1584 1490 ...
$ PT08.55(03) : num [1:9357] 13 31 1.9 11 11 11.2 ...
$ RH : num [1:9357] 48.9 47.7 54 60 59.6 ...
$ AH : num [1:9357] 0.758 0.755 0.787 0.789 ...
```

>Str(airquality)

Figure 1. Structure analysis of the data set

In figure 1, all of our variables are numerical data besides Date and Time which is using a date time format.

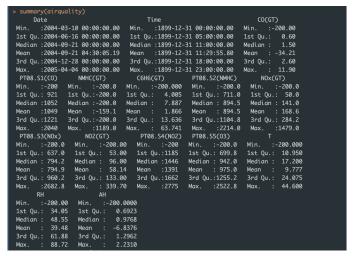
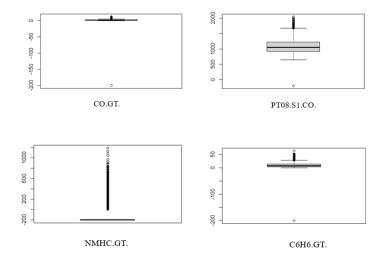


Figure 2. Summary Statistics of Air Quality dataset

In Figure 2. We can see most of our variables have a minimum quantity of -200. Some things to note, each of our variables are in different measurement values. CO(GT) is mg/gm³, NMHC(GT) and NO2(GT) are in microg/m³, T (temperature) in °C, RH and possibly AH in percentage, and the rest are measured in hourly average sensor responses.



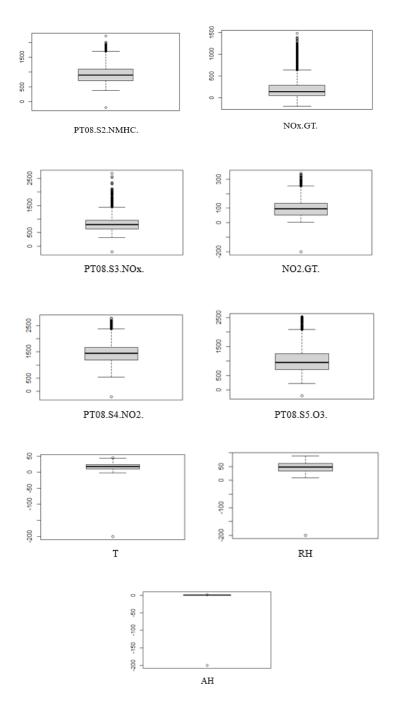


Fig. 3 Boxplots of each variable

With the boxplot() function, we use it to observe how the data is spread out with date and time not included. This way, we can identify outliers within our dataset by a visual representation. It seems as if every variable has at least one outlier. While looking through each, we can see that NCHC.GT, NOx.GT, and PT08.S3.NOx have the most outliers when compared to the rest. By

having this many outliers, our results can be affected by this and possibly give us inaccurate results.

```
Call:
Im(formula = T ~ ., data = airquality)

Residuals:
Min 1Q Median 3Q Max
-11.026 -1.879 -0.121 1.744 32.425

Coefficients:
Estimate Std. Error t value Pr(>1t1)
(Intercept) 4.642e-03 3.199e-03 1.451 0.14675
Date 2.564e-07 7.172e-09 35.746 <2e-16 ***
Time 2.232e-06 1.448e-06 1.541 0.12327
(**O(GT)** 1.387e-03 5.326e-04 2.604 0.09023 ***
'PT08.51(C0)* -3.742e-03 4.317e-04 -7.969 1.79e-15 ***
NMH(CGT)* -3.742e-03 2.858e-04 -13.093 2.e-16 ***
'CGHG(GT)* -1.400e-00 2.835e-02 -40.216 <2e-16 ***
'PT08.52(NMHC)* 1.230e-02 9.788e-04 12.563 <2e-16 ***
'NOX(GT)* 5.033e-03 3.111e-04 16.177 <2e-16 ***
'PT08.52(NMHC)* 1.330e-03 3.111e-04 16.177 <2e-16 ***
'PT08.52(NMHC)* 3.088e-04 3.243e-04 0.932 0.32614
'NOZ(GT)* -1.083e-03 2.787e-04 -14.050 <2e-16 ***
'PT08.55(03)* -3.200e-03 2.787e-04 -10.870 <2e-16 ***
'PT08.55(03)* -3.200e-03 2.787e-04 -10.050 **, 0.1 ** 1
'PT08.55(03)* -3.200e-03 2.787e-04 **, 0.000 **, 0.000 ** 1 ** 1
'PT08.55(03)* -3.200e-03 2.787e-04 **, 0.000 **, 0.000 ** 1 ** 1
'PT08.55(03)* -3.200e-03 2.787e-04 **, 0.000 **, 0.000 ** 1 ** 1
'PT08.55(03)* -3.200e-03 2.787e-04 **, 0.000 **, 0.000 ** 1 ** 1
'PT08.55(03)* -3.200e-03 2.787e-04 **, 0.000 **, 0.000 **, 0.000 ** 1 ** 1
'PT08.55(03)* -3.200e-03 2.787e-04 **, 0.000 **, 0.000 **, 0.000 ** 1
'PT08.55(03
```

Fig 4. Regression Model

We ran a linear regression model and here we can see Date, CO, PT08.S1, NHMC,C6H6, PT08.S2, NOx, NO2, PT08.S4, PT08.S5, RH, AH are significant.

```
> model_summary$r.squared
[1] 0.9955002
> model_summary$adj.r.squared
[1] 0.9954934
> AIC(model1)
[1] 46497.87
> BIC(model1)
[1] 46612.17
>
```

Fig 5. Checking goodness of fit

When checking our model fit, we had an r-squared of 0.9955002, and adjusted r-squared of 0.9954934, AIC of 46497.87 and BIC of 46612.17. Our r-squared and adjusted r-squared values are both good but our AIC and BIC is telling us we have a lot of information lost. This could be from our variable "PT08.S3(NOx)" being insignificant.

Part 4 Proposed Work

From this data, our next step will be to separate our dataset into a training and testing set. By reviewing the outputs, we will see if the outliers are similar to the raw data in both the training and testing datasets. We will continue our project with using the training dataset to fit a new linear regression model. The model will show us if any variables are significant for our data. Using the training model, we will use the goodness of fit to then find the MSE, adjusted R², AIC and BIC. With this we can conclude if our results are reasonable. We also plan to do an out-of-sample prediction with the testing dataset and compare to our training set to conclude which is the best fitted model.

Our group still needs to overview which new data mining set we will use for our project but will be deciding soon. As of now, we are reviewing our dataset to be sure we can find suitable results for our end goal of identifying possible trends within our datasets. With the results we will prepare a presentation explaining our findings. This will show what results were achieved by using new data mining techniques and give us what we hoped to achieve from this project.

Part 5 Corrections

After reviewing our results from our proposed section, we decided to delete some of the variables from the model. The variables removed are "Date", "Time", and "NMHC(GT)" for our final model building. The reason for removing date and time is that both variables do not give any significant measurements to help predict a linear regression for our project. We also decided to remove "NMHC(GT)" since much of the data was not measured, giving us a lot of blank data points that can affect our end results. Another issue we ran across was that many data points were set at -200 which were used as no data recorded for those points. Each -200 were converted

to NA and then replaced to an average measurement in their original column to help fill in the blank spots for our data.

Part 6 Model Building

To begin our model building, we split our data into 80% for a training data set and 20% for testing data set. We fit the training data set to a linear regression model with the response variable being temperature (T). Below is the summary output of our training model.

```
lm(formula = T \sim ., data = air.train)
Residuals:
 Min 1Q Median 3Q Max
-9.3190 -1.3473 -0.1487 1.0938 13.3906
Coefficients:
                                         t value Pr(>|t|)
                 Estimate Std. Error
                8.902e+00 6.703e-01
                                          13.281 < 2e-16 ***
(Intercept)
                                          -4.518 6.34e-06 ***
CO.GT.
                -1.983e-01 4.389e-02
PT08.S1.CO.
               -2.012e-05
                             3.528e-04
                                                    0.9545
                                          -0.057
C6H6.GT. -3.870e-01
PT08.S2.NMHC. 1.057e-02
                                                   < 2e-16 ***
                -3.870e-01
                            2.295e-02
                                         -16.864
                             7.938e-04
                                          13.310
                                                   < 2e-16 ***
NOX.GT.
                                                   < 2e-16 ***
                 2.650e-03
                             3.173e-04
                                           8.353
PT08.53.NOx.
                 3.367e-04
                             2.442e-04
                                           1.378
                                                    0.1681
                -2.337e-03
NO2.GT.
                             1.152e-03
                                           -2.029
                                                    0.0425 *
PT08.54.NO2.
                 5.722e-03
                             2.779e-04
                                          20.590
                                                   < 2e-16 ***
                                                   < 2e-16 ***
PT08.55.03.
                -2.691e-03
                             1.932e-04
                                         -13.925
                                                     2e-16 ***
                 -3.388e-01
                             2.059e-03
                                        -164.548
                                                   < 2e-16 ***
                 1.392e+01 1.418e-01
                                          98.142
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '
Residual standard error: 2.257 on 7564 degrees of freedom
Multiple R-squared: 0.9311, Adjusted R-squared: 0.931
F-statistic: 9296 on 11 and 7564 DF, p-value: < 2.2e-16
                                   Adjusted R-squared: 0.931
```

Fig. 6 Logistic Regression of Air Quality Training Set

Here we can see each variable besides PT08.S1.CO, PT08.S3.N0X, and NO2.GT are highly significant to our response variable temperature (T).

Next we want to do the in-sample model evaluation using the training data and then compare with the out-of-sample model that uses the testing data set.

```
> #Evaluating Model Fitness
> #In-sample with training data
> #MSE
> air_summary <- (summary(air1))
> (air_summary$sigma)^2
[1] 5.094892
> #R^2 of model
> air_summary$r.squared
[1] 0.9311228
> #Adjusted R^2
> air_summary$adj.r.squared
[1] 0.9310226
> AIC(air1)
[1] 33849.28
> BIC(air1)
[1] 33939.41
```

Fig. 7 Model Evaluations

Here are the MSE, R², adjusted R², AIC, and BIC of our in-sample model. For the out-of-sample, we use the testing data set and predict the performance on future data. With the predict() function, we can get the MSE and MAE of the model.

```
> #MSE
> mean((pi - air.test$T)^2)
[1] 309.4123
> #MAE
> mean(abs(pi - air.test$T))
[1] 15.35963
```

Fig. 8 MSE and MAE

We also want to look at variable selection by using regression trees with our model. By using the rpart() function, we get a similar output model just as the lm() function would give us.

```
> alr_rpart
n= 7576

node), split, n, deviance, yval
   * denotes terminal node

1) root 7576 559513.700 18.282470
2) AH< 0.8333 2406 108048.100 11.043020
4) RH>=31.85 1901 37359.740 8.813624
8) AH< 0.5814 840 8629.403 6.322024 *
9) AH>=0.5814 1061 19386.980 10.786240
18) RH>=52.15 640 4139.600 8.037500 *
19) RH< 52.15 421 3060.840 14.964850 *
5) RH< 31.85 505 25673.090 19.433250
10) AH< 0.49305 212 5213.570 13.428300 *
11) AH>=0.49305 293 7274.920 23.781570 *
3) AH>=0.8333 5170 266684.800 21.651550
6) RH>=39.95 3812 87017.060 18.550710
12) AH< 1.2964 2402 30136.160 16.137810
24) RH>=57.65 1061 5821.148 13.113100 *
25) RH< 57.65 1341 6927.956 18.530960 *
13) AH>=1.2964 1410 19072.610 22.661210
26) RH>=60.65 613 4195.823 19.654000 *
27) RH< 60.65 797 5069.508 24.974150 *
7) RH< 39.95 1358 40126.730 30.355820
14) RH>=7.85 772 13437.250 27.250520
28) AH< 1.257 449 2818.552 24.486860 *
29) AH>=1.257 449 2818.552 24.486860 *
29) AH>=1.257 449 2818.552 24.486860 *
29) AH>=1.257 323 2422.171 31.092260 *
15) RH< 27.85 586 9437.999 34.446760 *
```

Fig. 9 rpart Model

Here we use our training data set to build into our new rpart model. By having this output, the next step is to build the tree using the prp() to draw the tree for use. What we noticed is our outcome only gives the variables relative and absolute humidity. Looking at our tree build, it reads by comparing the values we want to test through the trees but only with absolute and relative humidity.

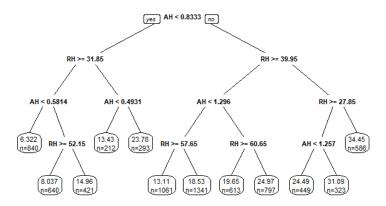


Fig. 10 Regression Tree

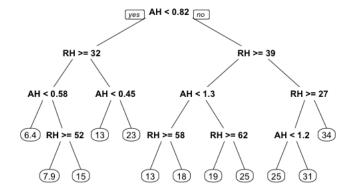


Fig. 10-1 Pruned Tree

Next, we want to compare the in and out-of-sample performance of the regression tree. For the in-sample, we used the predict() function to help report the MSE of the model. The in-sample prediction uses the training data set of the rpart model.

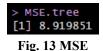
	, , , , , , , , , , , , , , , , , , , ,									
> train_pred_tree			34.446758 1				8.037500		23.781570	
8230 2257 2418 2	2846 5879 8656	2778 2765	6599	2168	2666	9329	2767	946	767	426
6.322024 34.446758 31.092260 24.486	5860 8.037500 6.322024 34.4	446758 24.486860	13.428302 2							
3822 4253 2479 4	1890 8029 9341	2452 4669	2038	4952	4439	4362	2169	5141	5336	8132
31.092260 31.092260 18.530957 18.530	0957 6.322024 18.530957 18.5	530957 19.653997	34.446758 1			18.530957			13.113101	
3725 1554 7835 9	9236 2323 9018	2565 6568	7805	9464	2478	1896	4117	4012	687	7580
24.974153 23.781570 6.322024 24.486	5860 34.446758 18.530957 34.4	446758 18.530957	6.322024 1	8.530957	18.530957	18.530957	19.653997	24.974153	8.037500	13.428302
8498 3793 2194	3896 1374 7760	6936 205	7435	5593	4908	2142	8677	836	3875	9151
6.322024 34.446758 24.974153 24.974	153 13.113101 6.322024 8.0	037500 13.113101	8.037500 1	9.653997	19.653997	18.530957	6.322024	23.781570	24.974153	13.113101
4072 3461 6290 7	7392 4614 9	6854 2118	1484	4494	9251	6534	5465	6909	3771	5172
18.530957 24.974153 13.113101 18.530	0957 18.530957 8.037500 6.3	322024 18.530957	24.486860 2	4.974153	13.113101	13.113101	19.653997	6.322024	24.974153	13.113101
2304 3025 4513	3435 9271 4973	9048 2387	4550	3841	8622	1766	7204	6101	6047	7110
24.486860 23.781570 24.974153 31.092	2260 14.964846 24.974153 23.7	781570 24.974153	19.653997 3	4.446758	8.037500	18.530957	18.530957	13.428302	14.964846	6.322024
5987 5815 5633 7	7809 8438 4944	8614 3656	71	8394	6144	268	4861	5554	7107	413
6, 322024 13, 113101 19, 653997 6, 322	2024 8.037500 24.974153 14.9	964846 24, 974153	14.964846	8.037500	13.428302	18.530957	13.113101	19.653997	6.322024	14.964846
4688 7662 4876	3960 1923 1862	5550 8952	478	998	4363	7933	460	6183	8846	5340
19.653997 8.037500 18.530957 23.781	1570 14.964846 18.530957 19.6		23.781570 1	3.113101	18.530957	6.322024	6.322024	13.113101	8.037500	13.113101
8325 5520 7657 1	1463 7265 6316	4260 8009	18	120	6963	9296	2704	164	8639	3796
8.037500 24.974153 8.037500 24.486	5860 8.037500 13.113101 24.9	974153 6.322024	8.037500 2	4.486860	13.113101	6.322024	24.974153	23.781570	13,428302	24.486860
3403 4453 325 7	7057 5028 1176	2700 3691	906	8179	4452	6072	6355	8149	1303	1437
			13.113101	6.322024	24.974153	18,530957	13.113101	13.113101	19.653997	13.113101
1375 9426 2221 4	1686 4572 6335	2007 9342	6665	1562	2295	6747	2599	4392	7420	803
	1153 24.974153 18.530957 19.6	653997 18,530957	8.037500 2	3.781570	18.530957	18.530957	24.974153	34.446758	13.113101	8.037500
	7779 8335 7756	9288 2735	8897	1905	6532	2756	2493	5391	9014	5081
34.446758 18.530957 31.092260 18.530			14.964846 1				34.446758	19.653997		24.974153
	9329 2767 946	767 426	4106	2146	1236	1400	9202	9099	2638	6059
13.428302 24.974153 31.092260 23.781			31.092260 1			13.113101			34.446758	8.037500
2038 4952 4439 4	1362 2169 5141	5336 8132	8572	2436	9365	4664	2934	8598	1317	8874

Fig. 11 Training Data Prediction Model

The out-of-sample prediction snippet is below. We did not show everything since there are many data points that it does cut off at a certain point. This prediction uses the rpart model with an additional argument of the testing data set. To compare, we use the out-of-sample performance and the linear regression model to get the MSE.

> #out-of-sample prediciton	
<pre>> test_pred_tree = predict(air_rpart, air.test)</pre>	7,707586 7,291423 6,296809 6,881382 8,758792 11,861021 20,731689 11,332529
> test_pred_reg	
1 5 11 13 17 19 27 2	
15.588955 11.685862 9.654368 10.796903 12.004958 9.883587 10.439393 10.11298	7.380253 8.327640 17.877828 20.220387 15.751325 19.630166 11.926812 14.216424
31 32 33 40 41 46 51 5	449 453 454 466 488 494 499 523
10.098976 9.503177 8.477322 12.432223 16.310376 18.736669 14.565121 10.58654	16.749287 19.567362 19.605644 13.339257 16.008559 15.234188 11.974708 21.851594
60 64 74 77 80 83 88 10	528 539 543 551 552 554 568 572
8.029994 11.324730 17.475336 15.598918 14.842670 11.737409 12.783525 16.29944	
121 125 132 136 138 141 143 14	573 576 578 583 584 599 601 605
23.153376 16.075456 11.715463 15.532544 21.793318 24.183296 25.007202 20.90214	
149 152 154 155 162 165 166 16	615 617 622 627 628 631 633 636
18.135678 15.517123 12.856921 11.715210 21.245725 24.469831 24.013033 22.72069	16.644100 16.383390 22.695088 19.159272 18.439281 17.005684 14.546717 15.023497
174 178 181 182 183 184 190 20	645 652 654 657 666 669 671 678
16.231063 14.097464 10.365552 11.226402 12.998491 15.273550 24.304516 12.21935	
213 214 217 218 219 222 223 22	
18.362015 18.431680 17.446688 16.971413 16.850463 14.771689 14.248182 14.50476	7.433441 5.493845 17.645733 18.997048 16.803526 18.055175 18.231765 17.962122
229 235 238 240 242 246 249 25	723 732 735 736 738 739 746 751
13.643421 17.335741 20.682169 20.696265 18.746405 16.963458 16.212619 14.03345	
256 257 276 279 291 306 310 33	755 757 766 772 774 776 788 789
15.146494 16.801242 16.151628 18.060786 17.292615 14.609533 16.270324 17.54234	6.546785 6.434872 20.764010 17.086142 16.001172 15.380167 10.337239 9.791843
337 344 346 350 352 359 362 36	791 793 798 802 807 813 816 838
11.477754 11.496560 8.842568 6.426441 9.040587 19.782244 15.703026 9.56242	8.921624 11.714415 10.939954 10.562765 13.767615 19.181077 18.425633 22.402674
370 371 372 373 374 375 379 39	840 847 856 859 862 865 870 874

Fig. 12 Testing Data Prediction Model



Neural Network

The new data mining tool our group decided to use was Neural Network. This tool can be used to improve the accuracy of the data over time using our training data. Something to note, the outputs are suspicious that our data returned a very small MSE although we changed our code to the parameters required to mirror our code. We are not really sure what happened to give us small MSEs, but these were the results given for the Neural Network code.

Since we already have our data split, we use our air train set to build our model. For this section, we included what code was used. The column was changed to -12 since we have 12 variables and the highest temperature is 44.6 which our data was divided and multiplied by as well.

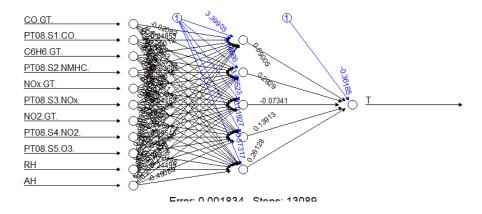


Fig. 14 Neural Network Model 1 Hidden Layer

Now we want to do a prediction on the testing sample set to get the MSE to compare our testing data set with the predicted set. We get a MSE of 0.0011 which we can confidently say that our data points from both sets are close to each other.

```
> air.pred1<- compute(air.ann1, air.test)
> air.pred1<- air.pred1$net.result*44.6
> mean((air.test$T-air.pred1)^2)
[1] 0.001137391
```

Fig. 15 MSE of Prediction and Testing Data

Let's try with another hidden layer in our network.

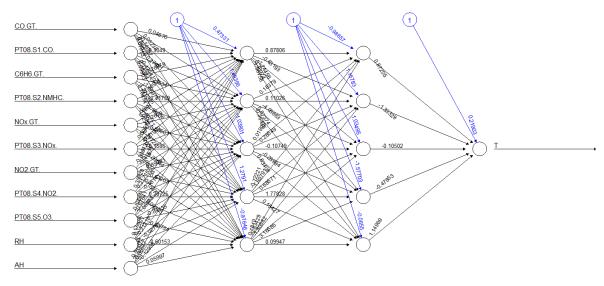


Fig. 16 Neural Network Model 2 Hidden Layers

Our MSE for the second comparison with a second hidden layer gives us a number of 0.0046 which is very small. This could mean that our second comparison is even closer to being a similar data point when compared to the first.

```
> air.pred2<- compute(air.ann2, air.test)
> air.pred2<- air.pred2$net.result*44.6
> mean((air.test$T-air.pred2)^2)
[1] 0.004584932
```

Fig. 17 MSE of Prediction2 and Testing Data

For both plots, the leftmost nodes are our raw data variables. Each arrow has a weight that seems to contribute to the next node it leads to. The blue arrows from the hidden nodes are bias weights that can shift a value closer to the output we would want. Last part we did was compare our air quality regression prediction with the air.test data to get the MSE. This model comparison is not the better model. The second one we compared using the air prediction and air test was the best model with the lowest MSE.

```
> mean((air.test$T-air.reg.pred)^2)
[1] 0.06887571
```

Fig. 18 MSE of Prediction Linear Regression and Testing

After comparing all 3 models, We can conclude the linear regression model is the best. Even though the neural network model has the lowest MSE, it is suspiciously too low. We cannot feel comfortable with choosing that model.

List of references

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