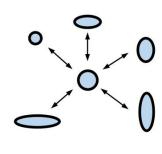
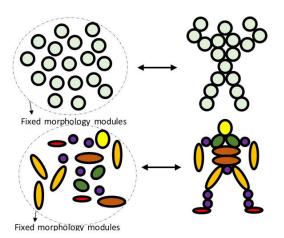
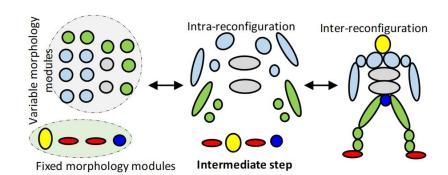
# Self-reconfiguring modular robots





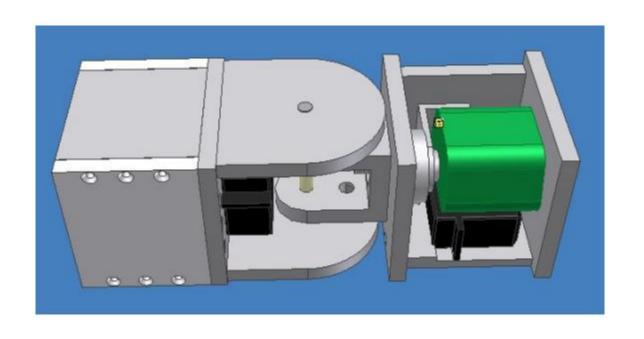
Intra-reconfigurability

Inter-reconfigurability

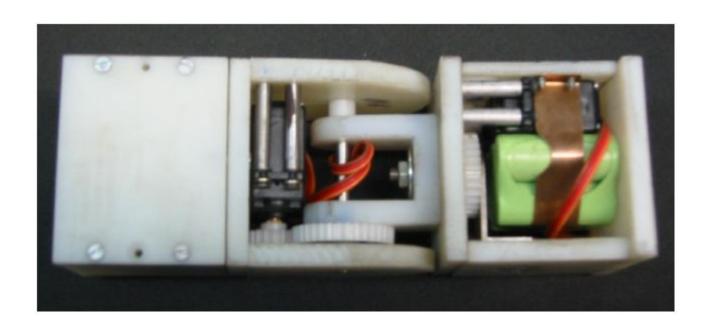


#### Nested-reconfigurability

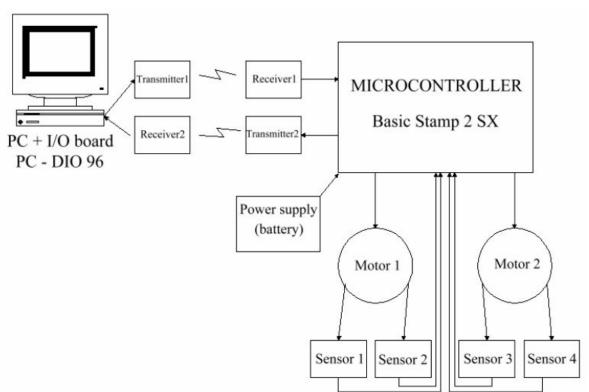
## CAD image of the module



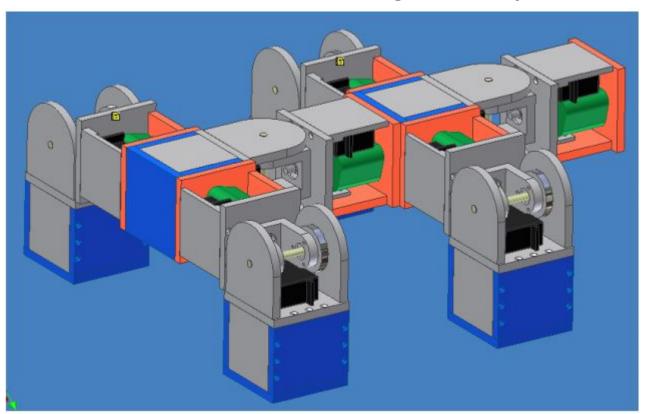
#### Actual module



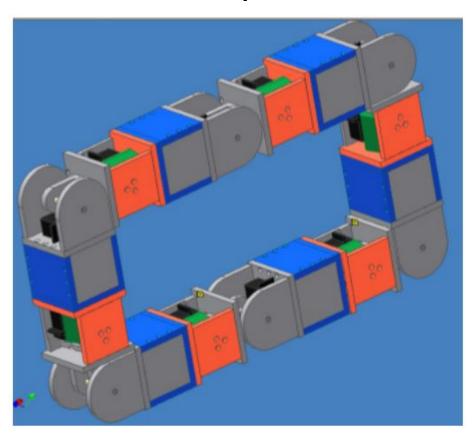
#### Robot control



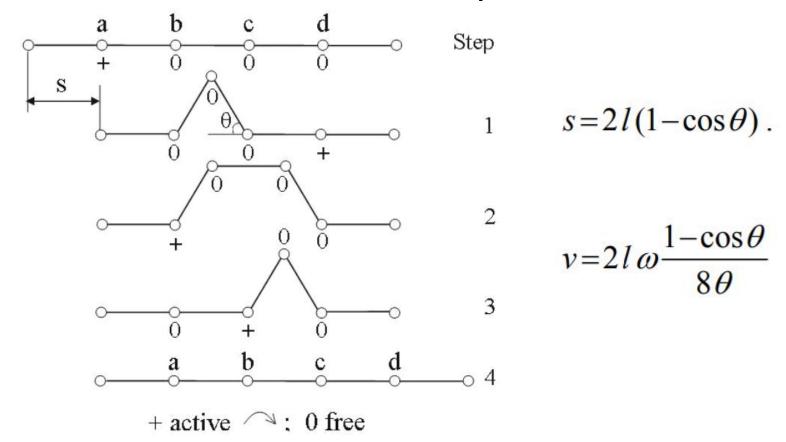
#### Example of the reconfigured system



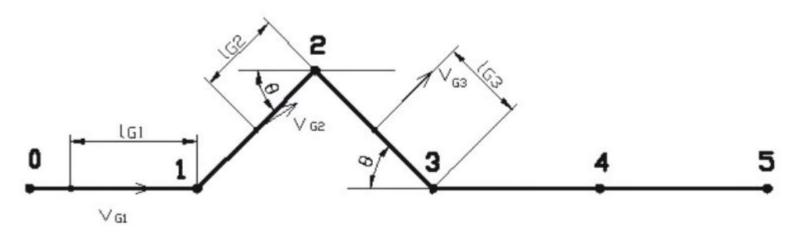
## Rolled-up snake



#### Crawl sequence

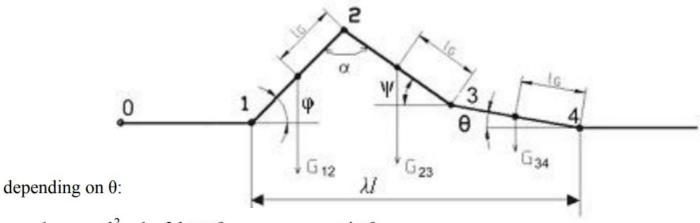


#### Dynamic model - step 1



$$J_r = 2J_G + ml_G^2 + 2m(l^2 + l_G^2) - 4ml_G \cos^2 \theta + 4ml^2 \sin^2 \theta$$

#### Step 2 and equations



 $\varphi = \frac{1}{2} \arccos \frac{\lambda^2 - 1 - 2\lambda \cos \theta}{2} + \arcsin \frac{\sin \theta}{\sqrt{2} + 2\lambda \cos \theta}$ 

where: 
$$\lambda = 1 + \sin(\alpha/2)$$

$$\psi = \frac{1}{2}\arccos\frac{\lambda^2 - 1 - 2\lambda\cos\theta}{2} - \arcsin\frac{\sin\theta}{\sqrt{\lambda^2 + 1 - 2\lambda\cos\theta}}$$

The equivalent moment of inertia about the 4-th axis is:

The equivalent moment of inertia about the 4-th axis is:
$$J_r = \left(J_G + ml_G^2 + ml^2\right) \frac{\dot{\varphi}^2}{\dot{\theta}^2} + \left[J_G + ml_G^2 + m(l - l_G)^2\right] \frac{\dot{\psi}^2}{\dot{\theta}^2} - \frac{1}{2} \left[J_G + ml_G^2 + m(l - l_G)^2\right] \frac{\dot{\psi}^2}{\dot{\theta}^2} - \frac{1}{2} \left[J_G + ml_G^2 + m(l - l_G)^2\right] \frac{\dot{\psi}^2}{\dot{\theta}^2} - \frac{1}{2} \left[J_G + ml_G^2 + m(l - l_G)^2\right] \frac{\dot{\psi}^2}{\dot{\theta}^2} - \frac{1}{2} \left[J_G + ml_G^2 + m(l - l_G)^2\right] \frac{\dot{\psi}^2}{\dot{\theta}^2} - \frac{1}{2} \left[J_G + ml_G^2 + m(l - l_G)^2\right] \frac{\dot{\psi}^2}{\dot{\theta}^2} - \frac{1}{2} \left[J_G + ml_G^2 + m(l - l_G)^2\right] \frac{\dot{\psi}^2}{\dot{\theta}^2} - \frac{1}{2} \left[J_G + ml_G^2 + m(l - l_G)^2\right] \frac{\dot{\psi}^2}{\dot{\theta}^2} - \frac{1}{2} \left[J_G + ml_G^2 + m(l - l_G)^2\right] \frac{\dot{\psi}^2}{\dot{\theta}^2} - \frac{1}{2} \left[J_G + ml_G^2 + m(l - l_G)^2\right] \frac{\dot{\psi}^2}{\dot{\theta}^2} - \frac{1}{2} \left[J_G + ml_G^2 + m(l - l_G)^2\right] \frac{\dot{\psi}^2}{\dot{\theta}^2} - \frac{1}{2} \left[J_G + ml_G^2 + m(l - l_G)^2\right] \frac{\dot{\psi}^2}{\dot{\theta}^2} - \frac{1}{2} \left[J_G + ml_G^2 + m(l - l_G)^2\right] \frac{\dot{\psi}^2}{\dot{\theta}^2} - \frac{1}{2} \left[J_G + ml_G^2 + m(l - l_G)^2\right] \frac{\dot{\psi}^2}{\dot{\theta}^2} - \frac{1}{2} \left[J_G + ml_G^2 + m(l - l_G)^2\right] \frac{\dot{\psi}^2}{\dot{\theta}^2} - \frac{1}{2} \left[J_G + ml_G^2 + m(l - l_G)^2\right] \frac{\dot{\psi}^2}{\dot{\theta}^2} - \frac{1}{2} \left[J_G + ml_G^2 + m(l - l_G)^2\right] \frac{\dot{\psi}^2}{\dot{\theta}^2} - \frac{1}{2} \left[J_G + ml_G^2 + m(l - l_G)^2\right] \frac{\dot{\psi}^2}{\dot{\theta}^2} - \frac{1}{2} \left[J_G + ml_G^2 + m(l - l_G)^2\right] \frac{\dot{\psi}^2}{\dot{\theta}^2} - \frac{1}{2} \left[J_G + ml_G^2 + m(l - l_G)^2\right] \frac{\dot{\psi}^2}{\dot{\phi}^2} - \frac{1}{2} \left[J_G + ml_G^2 + m(l - l_G)^2\right] \frac{\dot{\psi}^2}{\dot{\phi}^2} - \frac{1}{2} \left[J_G + ml_G^2 + m(l - l_G)^2\right] \frac{\dot{\psi}^2}{\dot{\phi}^2} - \frac{1}{2} \left[J_G + ml_G^2 + m(l - l_G)^2\right] \frac{\dot{\psi}^2}{\dot{\phi}^2} - \frac{1}{2} \left[J_G + ml_G^2 + m(l - l_G)^2\right] \frac{\dot{\psi}^2}{\dot{\phi}^2} - \frac{1}{2} \left[J_G + ml_G^2 + m(l - l_G)^2\right] \frac{\dot{\psi}^2}{\dot{\phi}^2} + \frac{1}{2} \left[J_G + ml_G^2 + m(l - l_G)^2\right] \frac{\dot{\psi}^2}{\dot{\phi}^2} - \frac{1}{2} \left[J_G + ml_G^2 + m(l - l_G)^2\right] \frac{\dot{\psi}^2}{\dot{\phi}^2} + \frac{1}{2} \left[J_G + ml_G^2 + m(l - l_G)^2\right] \frac{\dot{\psi}^2}{\dot{\phi}^2} + \frac{1}{2} \left[J_G + ml_G^2 + m(l - l_G)^2\right] \frac{\dot{\psi}^2}{\dot{\phi}^2} + \frac{1}{2} \left[J_G + ml_G^2 + m(l - l_G)^2\right] \frac{\dot{\psi}^2}{\dot{\phi}^2} + \frac{1}{2} \left[J_G + ml_G^2 + m(l - l_G)^2\right] \frac{\dot{\psi}^2}{\dot{\phi}^2} + \frac{1}{2} \left[J_G + ml_G^2 + m(l - l_G)^2\right] \frac{\dot{\psi}^2}{\dot{\phi}^2} + \frac{1}{2} \left[J_G + ml_G^2\right]$$

$$-ml(l-l_G)(\lambda^2-1-2\lambda\cos\theta)\frac{\dot{\psi}\dot{\phi}}{\dot{\theta}^2}+J_G+ml_G^2$$
 where:  $\theta$  - angular speed of the segment 34;  $\dot{\phi}$  - angular speed of the segment 12;  $\dot{\psi}$  - angular speed of the segment 23;  $J_G$  -

moment of inertia for modules 12, 23 and 34; m - module mass;  $l_G$  – the distance between the gravity center of a module and its rotation axis.

#### Motion equation

$$u = L\frac{di}{dt} + Ri + \gamma k_e \dot{\theta}$$

$$\gamma k_t i = J_r(\theta) \ddot{\theta} + c \dot{\theta} + M_r(\theta)$$

where: L, R – motor winding inductance and resistance; u, i – control voltage and current;  $k_e$ ,  $k_t$  – electromechanical coupling coefficients; c – damping coefficient;  $\theta$ ,  $\dot{\theta}$  - position and angular speed respectively, of the active joint;  $\gamma$  – additional gear ratio.

Thank you for watching!

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