

IonQ iQuHack2025 Challenge

Before proceeding, register once. Then, comment out the registration function call to avoid re-registering when running the notebook again.

```
In [7]: import requests
        def register():
            team_name = input("Enter your team name: ")
            in_person = input("Enter participation type - in-person or remote: ")
            data = []
            while email := input("Enter email separated by commas (enter to cancel): "):
                firstname = input("Enter your first name: ")
                lastname = input("Enter your last name: ")
                github = input("Enter your github handle: ")
                data.append((firstname, lastname, email, github))
            for firstname, lastname, email, github in data:
                url = f"https://ionquhack2025.azurewebsites.net/api/registration?TeamName={
                req = requests.post(url)
                print("\n\n\n"+req.text)
        # Comment this out after registration:
        # register()
```

Enter the key you've got on the previous step here:

```
In [27]: key = "61f7aaaf50e899e65f777e0e159408b5335faf68fd58ee21d8941de1907d3cfb"
```

Did you comment out the register() function call?

Please share your research process on GitHub: https://github.com/iQuHACK/2025-lonQ/discussions

Maximum Cut problem (max-cut) with variational Quantum Imaginary Time Evolution (varQITE) method

In this challenge, we demonstrate how to leverage IonQ Forte's industry-leading capabilities to solve instances of the NP-hard combinatorial optimization problem known as Maximum Cut (MaxCut) using a novel variational Quantum Imaginary Time Evolution (varQITE) algorithm developed by IonQ in conjunction with researchers at Oak Ridge National Labs (ORNL).

What's the problem?

MaxCut 101

The Maximum Cut Problem (MaxCut) is a classic combinatorial optimization problem commonly used as an algorithm benchmark by scientific computing researchers. It has numerous applications in a variety of fields: for example, it is used in circuit desing as part of Very Large Scale Integration (VLSI) to find the optimal layout of circuit components; it is used in the study of social networks to identify communities; it is used in computer vision for image segmentation, etc.

MaxCut is a graph problem: given a graph G=(V,E) with vertex set V and edge set E, it asks for a partition of V into sets S and T maximizing the number of edges crossing between S and T.

Think of it like this: you're trying to cut the graph into two pieces, and you want to make the cut so that it slices through as many edges as possible.

Prepare the code environment

First, we'll set up the coding environment and install necessary dependencies.

```
In [1]: pip install qiskit qiskit-aer networkx numpy pandas -q
```

Note: you may need to restart the kernel to use updated packages.

To ensure your code runs correctly everywhere, please only use the imported dependencies. Using external libraries may cause your submission to fail due to missing dependencies on our servers.

```
# Hackathon at iQuHack2025 hosted by MIT and only during the Feb 1-2, 2025
# duration of such event.

import matplotlib.pyplot as plt
from IPython import display

import networkx as nx
import numpy as np
import pandas as pd
import time

from typing import List
from qiskit import QuantumCircuit, transpile
from qiskit.circuit import ParameterVector
from qiskit.quantum_info import SparsePauliOp
from qiskit_aer import AerSimulator
```

Graph definition

A simple graph, defined using the Python NetworkX library, will serve to illustrate the problem and you can explore further complexities.

```
In [3]: # other graphs candidates to check
        import networkx as nx
        import matplotlib.pyplot as plt
        import random
        #-> Cycle Graph C8
        def cycle_graph_c8():
            G = nx.cycle_graph(8)
            plt.figure(figsize=(6, 6))
            pos = nx.circular_layout(G)
            nx.draw(G, pos, with labels=True, node color='lightblue', edge color='gray', no
            plt.title("Cycle Graph C8")
            plt.show()
            return G
        # Path Graph P16
        def path_graph_p16():
            G = nx.path graph(16)
            plt.figure(figsize=(12, 2))
            pos = nx.spring_layout(G, seed=42)
            nx.draw(G, pos, with_labels=True, node_color='lightgreen', edge_color='gray', n
            plt.title("Path Graph P16")
            plt.show()
            return G
        #-> Complete Bipartite Graph K8,8
        def complete_bipartite_graph_k88():
            G = nx.complete_bipartite_graph(8, 8)
            plt.figure(figsize=(8, 6))
            pos = nx.bipartite_layout(G, nodes=range(8))
```

```
nx.draw(G, pos, with_labels=True, node_color=['lightcoral'] * 8 + ['lightblue']
            edge_color='gray', node_size=300)
   plt.title("Complete Bipartite Graph K8,8")
   plt.show()
   return G
#-> Complete Bipartite Graph K8,8
def complete_bipartite_graph_k_nn(n):
   G = nx.complete bipartite graph(n, n)
   plt.figure(figsize=(8, 6))
   pos = nx.bipartite_layout(G, nodes=range(n))
   nx.draw(G, pos, with_labels=True, node_color=['lightcoral'] * n + ['lightblue']
            edge_color='gray', node_size=300)
   plt.title("Complete Bipartite Graph K{},{}".format(n,n))
   plt.show()
   return G
# Star Graph S16
def star_graph_s16():
   G = nx.star_graph(16)
   plt.figure(figsize=(8, 8))
   pos = nx.spring_layout(G, seed=42)
   nx.draw(G, pos, with_labels=True, node_color='gold', edge_color='gray', node_si
   plt.title("Star Graph S16")
   plt.show()
   return G
# Grid Graph 8x4
def grid_graph_8x4():
   G = nx.grid_graph(dim=[8, 4])
   plt.figure(figsize=(12, 6))
   pos = {node: node for node in G.nodes()}
   nx.draw(G, pos, with_labels=True, node_color='lightblue', edge_color='gray', no
   plt.title("Grid Graph 8x4")
   plt.show()
   return G
# Grid Graph 8x4
def grid_graph_nxm(n,m):
   G = nx.grid_graph(dim=[n, m])
   plt.figure(figsize=(12, 6))
   pos = {node: node for node in G.nodes()}
   nx.draw(G, pos, with_labels=True, node_color='lightblue', edge_color='gray', no
   plt.title("Grid Graph {}x{}".format(n,m))
   plt.show()
   return G
#-> 4-Regular Graph with 8 Vertices
def regular graph 4 8():
   G = nx.random_regular_graph(d=4, n=8, seed=42)
   plt.figure(figsize=(6, 6))
   pos = nx.circular_layout(G)
   nx.draw(G, pos, with_labels=True, node_color='lightgreen', edge_color='gray', n
   plt.title("4-Regular Graph with 8 Vertices")
   plt.show()
```

```
return G
#-> Cubic (3-Regular) Graph with 16 Vertices
def cubic_graph_3_16():
   G = nx.random_regular_graph(d=3, n=16, seed=42)
   plt.figure(figsize=(8, 6))
   pos = nx.spring_layout(G, seed=42)
   nx.draw(G, pos, with_labels=True, node_color='lightcoral', edge_color='gray', n
   plt.title("Cubic (3-Regular) Graph with 16 Vertices")
   plt.show()
   return G
# Disjoint Union of Four C4 Cycles
def disjoint_union_c4():
   cycles = [nx.cycle_graph(4) for _ in range(4)]
   G = nx.disjoint_union_all(cycles)
   plt.figure(figsize=(12, 6))
   pos = \{\}
   shift x = 0
   for component in nx.connected_components(G):
        subgraph = G.subgraph(component)
        pos_sub = nx.circular_layout(subgraph, scale=1, center=(shift_x, 0))
        pos.update(pos_sub)
        shift_x += 3
   nx.draw(G, pos, with_labels=True, node_color='lightblue', edge_color='gray', no
   plt.title("Disjoint Union of Four C4 Cycles")
   plt.show()
   return G
# Complete Bipartite Graph K16,16
def complete bipartite graph k1616():
   G = nx.complete bipartite graph(16, 16)
   plt.figure(figsize=(12, 6))
   pos = nx.bipartite layout(G, nodes=range(16))
   nx.draw(G, pos, with_labels=False, node_color=['lightcoral'] * 16 + ['lightblue']
            edge_color='gray', node_size=100)
   plt.title("Complete Bipartite Graph K16,16")
   plt.show()
   return G
# 5-Dimensional Hypercube Graph Q5
def hypercube_graph_q5():
   G = nx.hypercube_graph(5)
   plt.figure(figsize=(10, 8))
   pos = nx.spring_layout(G, seed=42)
   nx.draw(G, pos, with_labels=False, node_color='lightgreen', edge_color='gray',
   plt.title("5-Dimensional Hypercube Graph Q5")
   plt.show()
   return G
# Tree Graph with 8 Vertices
def tree_graph_8():
   G = nx.balanced_tree(r=2, h=2)
   G.add edge(6, 7)
   plt.figure(figsize=(8, 6))
   pos = nx.spring layout(G, seed=42)
```

```
nx.draw(G, pos, with_labels=True, node_color='lightblue', edge_color='gray', no
    plt.title("Tree Graph with 8 Vertices")
    plt.show()
    return G
# Wheel Graph W16
def wheel graph w16():
    G = nx.wheel_graph(16)
    plt.figure(figsize=(8, 8))
    pos = nx.circular_layout(G)
    nx.draw(G, pos, with_labels=True, node_color='lightcoral', edge_color='gray', n
    plt.title("Wheel Graph W16")
    plt.show()
    return G
#-> Random Connected Graph with 16 Vertices
def random_connected_graph_16(p=0.15):
    \#n, p = 16, 0.25
   n=16
    while True:
        G = nx.erdos_renyi_graph(n, p, seed=random.randint(1, 10000))
        if nx.is_connected(G):
            break
    plt.figure(figsize=(10, 8))
    pos = nx.spring_layout(G, seed=42)
    nx.draw(G, pos, with_labels=False, node_color='lightgreen', edge_color='gray',
    plt.title("Random Connected Graph with 16 Vertices")
    plt.show()
    return G
# Expander Graph with 32 Vertices
def expander graph 32():
    G = nx.random_regular_graph(4, 32, seed=42)
    plt.figure(figsize=(10, 8))
    pos = nx.spring_layout(G, seed=42)
    nx.draw(G, pos, with_labels=False, node_color='lightblue', edge_color='gray', n
    plt.title("Expander Graph with 32 Vertices")
    plt.show()
    return G
#-> Expander Graph with n Vertices
def expander_graph_n(n):
    G = nx.random_regular_graph(4, n, seed=42)
    plt.figure(figsize=(10, 8))
    pos = nx.spring_layout(G, seed=42)
    nx.draw(G, pos, with_labels=False, node_color='lightblue', edge_color='gray', n
    plt.title("Expander Graph with {} Vertices".format(n))
    plt.show()
    return G
# Planar Connected Graph with 16 Vertices
def planar_connected_graph_16():
    G = nx.grid_graph(dim=[8, 2])
    G = nx.convert_node_labels_to_integers(G)
    additional_edges = [(0, 9), (1, 10), (2, 11), (3, 12), (4, 13), (5, 14), (6, 15
                        (7, 15), (8, 7)]#, (6, 15), (14, 1), (1, 13), (10, 9), (0, 15)
```

```
G.add_edges_from([e for e in additional_edges if e[0] < 16 and e[1] < 16])
assert nx.check_planarity(G)[0], "Graph is not planar."
pos = {node: (node // 2, node % 2) for node in G.nodes()}
plt.figure(figsize=(16, 8))
nx.draw(G, pos, with_labels=False, node_color='lightcoral', edge_color='gray',
plt.title("Planar Connected Graph with 16 Vertices")
plt.axis('equal')
plt.show()
return G</pre>
```

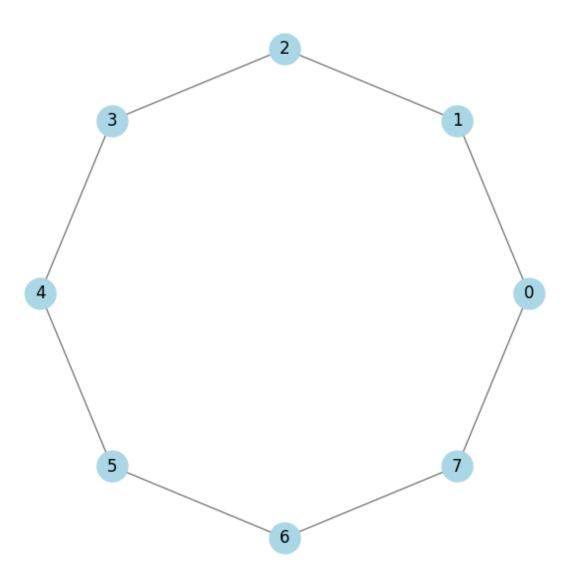
We've suggested a few graph ideas above.

The list below highlights those achievable with minimal computational resources, whether on a local laptop or a cloud instance. Some are simply too large.

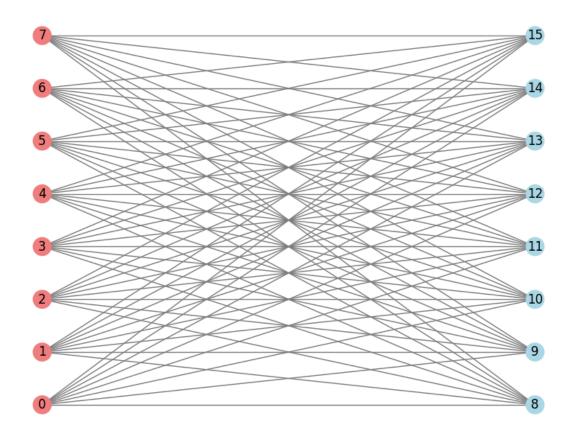
```
In [4]: # Choose your favorite graph and build your winning ansatz!

graph1 = cycle_graph_c8()
graph2 = complete_bipartite_graph_k88()
graph3 = complete_bipartite_graph_k_nn(5)
graph4 = regular_graph_4_8()
graph5 = cubic_graph_3_16()
graph6 = random_connected_graph_16(p=0.18)
graph7 = expander_graph_n(16)
#graph8 = -> make your own cool graph
```

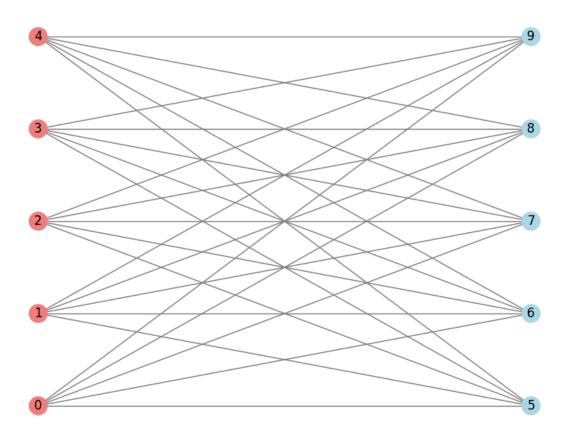
Cycle Graph C8



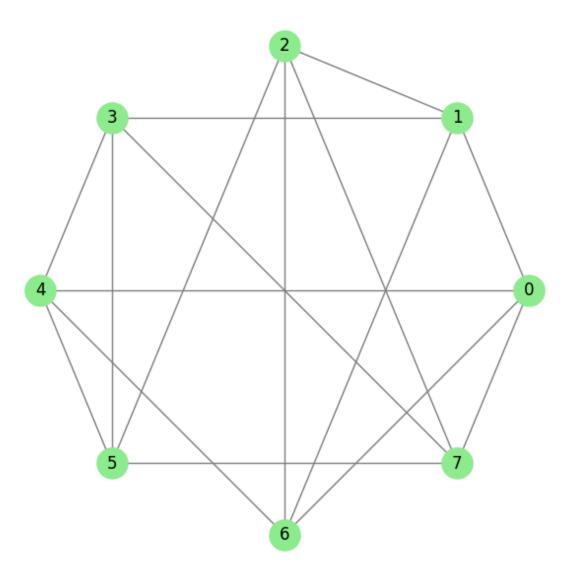
Complete Bipartite Graph K8,8



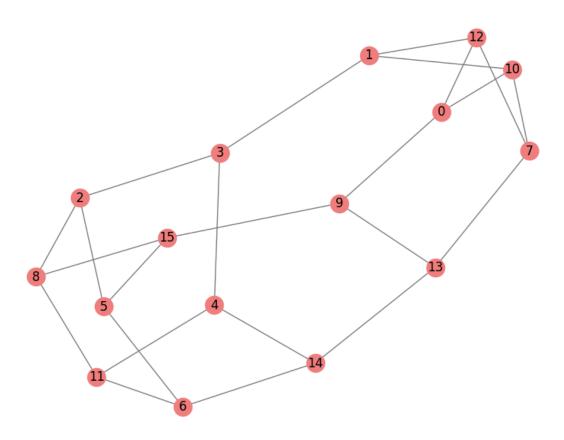
Complete Bipartite Graph K5,5



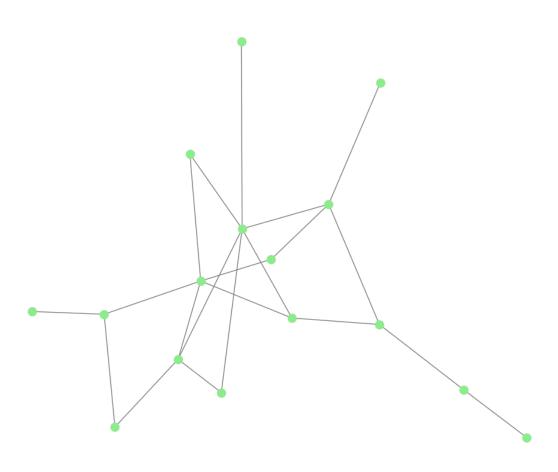
4-Regular Graph with 8 Vertices



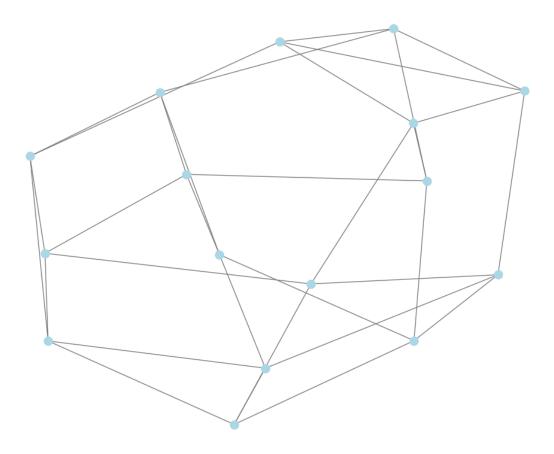
Cubic (3-Regular) Graph with 16 Vertices



Random Connected Graph with 16 Vertices



Expander Graph with 16 Vertices



Input graph

In [128... graph = graph1 graph

Out[128... <networkx.classes.graph.Graph at 0x20809168b90>

Play around with all of them

Quantum Circuit Generator

We start by generating parameterized circuit based on a given graph.

Note: Future experiments will focus on optimizing this circuit generator (this function below). Maximizing your score requires minimizing the number of gates in the generated parameterized circuit.

Set of Rules:

Rules: Do not rename the function, import external libraries (except Qiskit), or use classical solvers. Implement any needed algorithms (e.g., sorting) within the function. Minimize gate count. Run locally for all the graphs before submitting the results.

Let's iterate again.

This challenge requires you to work within the provided function's name and scope. You may only use Qiskit libraries. Do not import additional libraries or call external functions. If your solution requires operations like sorting, implement them directly within the function. Critically, do *not* use a classical algorithm to solve the problem and simply input the result. Optimize your code to minimize the number of quantum gates, while aiming for the correct solutions distribution. Thoroughly get your solution results to report at the end.

Important note: To confirm your results, please save this notebook including all cell outputs and upload it in the form here: https://forms.gle/tAjnUd7b5t3oX3b2A . To avoid exceeding the notebook's 10MB file size limit, please be mindful of the number of print statements you use. Feel free to modify the notebook as needed. However, please ensure your code is readable. Please thoroughly comment your code; we will evaluate your problem-solving approach based on the educational clarity of your explanations.

Good luck, and have fun!

```
In [129... # Visualization will be performed in the cells below;

def build_ansatz(graph: nx.Graph) -> QuantumCircuit:
    ansatz = QuantumCircuit(graph.number_of_nodes())
    ansatz.h(range(graph.number_of_nodes()))

theta = ParameterVector(r"$\theta$", graph.number_of_edges())
    for t, (u, v) in zip(theta, graph.edges):
        ansatz.cx(u, v)
        ansatz.ry(t, v)
        ansatz.cx(u, v)

return ansatz
```

```
# alternate method to make the ansatz

# function to generate a maximum spanning tree of the graph
def generate_max_spanning_tree(G):
    # for u, v in G.edges:
    # G[u][v]['weight'] *= -1
    return nx.minimum_spanning_tree(G, algorithm='kruskal')

# function to return the graph with the spanning tree edges removed
def remove_spanning_tree_edges(G, T):
    H = G.copy()
    for edge in T.edges:
```

```
H.remove_edge(*edge)
return H
```

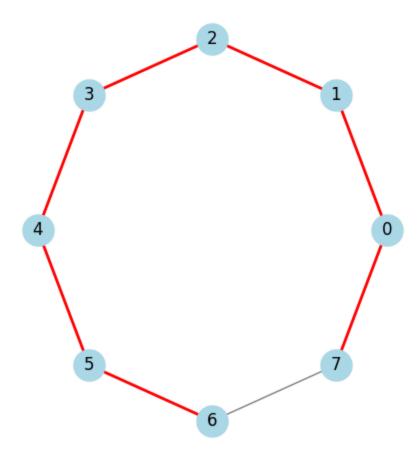
```
# get the maximum spanning tree of the graph by negating all the edge weights and c
T = generate_max_spanning_tree(graph)

# remove the edges of the spanning tree from the graph
H = remove_spanning_tree_edges(graph, T)

# visualize the tree and the graph with the tree edges removed
plt.figure(figsize=(12, 6))
plt.subplot(121)
pos = nx.circular_layout(graph)
nx.draw(graph, pos, with_labels=True, node_color='lightblue', edge_color='gray', no
nx.draw_networkx_edges(T, pos, edge_color='red', width=2)
plt.title("Graph with Maximum Spanning Tree")
```

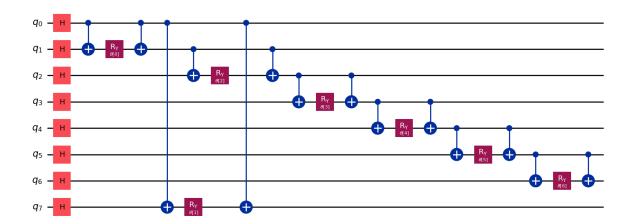
Out[131... Text(0.5, 1.0, 'Graph with Maximum Spanning Tree')

Graph with Maximum Spanning Tree



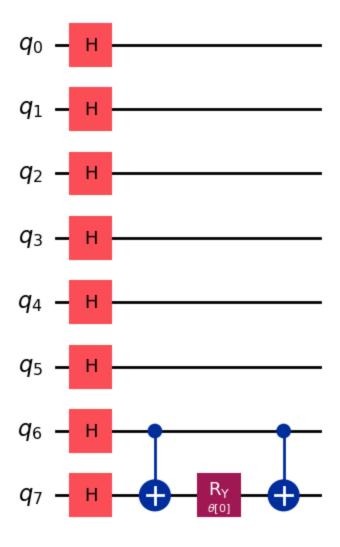
```
In [132... # build the ansatz circuit for both T and H
ansatz_T = build_ansatz(T)
ansatz_H = build_ansatz(H)
In [133... # visualize the ansatz circuit for the tree
ansatz_T.draw("mpl", fold=-1)
```

Out[133...



In [134... # visualize the ansatz circuit for the graph with the tree edges removed
ansatz_H.draw("mpl", fold=-1)

Out[134...



On Parametrized Quantum Circuits

Parametrized quantum circuits (PQC) recently have gained significant attention as a prominent way to reach quantum advantage in many different fields. They are characterized by their use of varying parameters within quantum gates and can be optimized to solve specific problems, such as machine learning, quantum optimization, or quantum chemistry.

PQCs usually consist of three main parts:

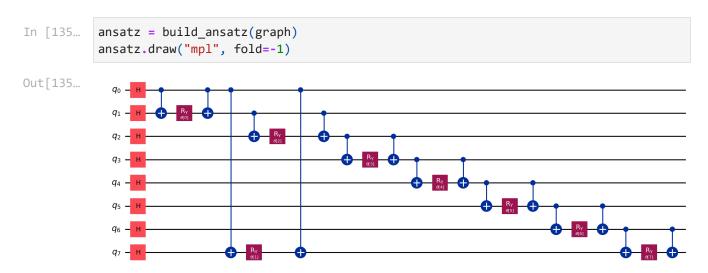
- 1. Initialization: The qubits are set to a known starting state (usually $|0\rangle$) and then set into superposition with Hadamard gates.
- 2. Parameterized gates, such as rotation gates (Rx, Ry, Rz), and entanglement gates are adjustable. Their parameters can be optimized to reflect the relationships between the encoded problem data.
- 3. Measurement: After applying the parameterized gates, the qubits are measured to get results.

These circuits are important elements in Variational Quantum Algorithms (VQA), hybrid quantum-classical systems where classical optimization helps to improve quantum operations. Two most notable examples of VQAs are Variational Quantum Eigensolver (VQE), an algorithm that finds a ground state energy of a given Hamiltonian, and Quantum Approximate Optimization Algorithm (QAOA), which is designed for solving combinatorial optimization problems. Near-term quantum computers are noisy and limited in size, and PQCs provide a practical way for us to use them more effectively.

More on that topic: https://arxiv.org/abs/2207.06850

Back to the problem in hand

This function produces parametrized quantum circuits (PQCs), a visualization of which is provided below.



Building the MaxCut Hamiltonian

In [136...

Formally, we write MaxCut as a Quadratic Program (QP) with binary decision variables as follows. For each node $v \in V$, we let x_v denote a binary variable indicating whether v belongs to S or T. The objective is to maximize the number of cut edges:

$$ext{maximize}_x \quad \sum_{(v,w) \in E} (x_v + x_w - 2x_v x_w)$$

Let's break this down. Notice that for each edge e=(v,w) in the graph, the quantity $(x_v+x_w-2x_vx_w)$ indicates whether e is cut by the partition represented by x; that is, the quantity $(x_v+x_w-2x_vx_w)$ is zero or one, and it equals one only if v and w lie on different sides of the partition specified by x.

The code cell below obtains a symbolic representation of the maximization objective corresponding to the graph above.

def build_maxcut_hamiltonian(graph: nx.Graph) -> SparsePauliOp:

```
Build the MaxCut Hamiltonian for the given graph H = (|E|/2)*I - (1/2)*\Sigma_{\{(i,j)\}}
              num qubits = len(graph.nodes)
              edges = list(graph.edges())
              num_edges = len(edges)
              pauli_terms = ["I"*num_qubits] # start with identity
              coeffs = [-num_edges / 2]
              for (u, v) in edges: # for each edge, add -(1/2)*Z_i Z_j
                   z_{term} = ["I"] * num_qubits
                   z_{term[u]} = "Z"
                   z_{term[v]} = "Z"
                   pauli_terms.append("".join(z_term))
                   coeffs.append(0.5)
              return SparsePauliOp.from_list(list(zip(pauli_terms, coeffs)))
          # get the maxcut hamiltonian for the tree
In [137...
          H_maxcut_T = build_maxcut_hamiltonian(T)
          # get the maxcut hamiltonian for the graph with the tree edges removed
          H_maxcut_H = build_maxcut_hamiltonian(H)
In [138... print(H_maxcut_T)
          print(H_maxcut_H)
         SparsePauliOp(['IIIIIIII', 'ZZIIIIII', 'ZIIIIIIZ', 'IZZIIIII', 'IIZZIIII', 'IIIZZII
         I', 'IIIIZZII', 'IIIIIZZI'],
                       coeffs=[-3.5+0.j, 0.5+0.j, 0.5+0.j, 0.5+0.j, 0.5+0.j, 0.5+0.j,
         0.5+0.j
           0.5+0.j
         SparsePauliOp(['IIIIIIII', 'IIIIIIZZ'],
                       coeffs=[-0.5+0.j, 0.5+0.j])
```

Let's keep this function contained within its own cell, as you might need to adapt it for various max-cut problem types later.

As a Hamiltonian energy minimization problem

Quantum MaxCut

Quantum computers are good at finding the ground state of particle systems evolving under the action of a given Hamiltonian. In this section, we'll construct a Hamiltonian whose energies are exactly the values of the MaxCut objective function. This correspondence will effectively translate our classical combinatorial optimization problem into a quantum problem, which we'll approach using our novel heuristic.

Given an objective function C(x), with domain $x \in \{0,1\}^n$, we'll produce a Hamiltonian H_C on n qubits such that

$$H_C \setminus \ker x = C(x) \setminus \ker x.$$

In the last equation, $\backslash \ker x$ denotes the n-qubit computational basis state indexed by the bit-string $x \in \{0,1\}$. Thus the last equation says each of the 2^n computational basis states is an eigenvector of H_C , and the eigenvalue corresponding to $\backslash \ker x$ is C(x); that is, H_C is diagonal with respect to the computational basis, and its energies are the values of the objective function C.

We'll obtain the Hamiltonian H_C by replacing each x_j in the expression of C(x) by the operator

$$\hat{X}_j \setminus \operatorname{coloneqq} \frac{1}{2} (I - Z_j),$$

where I denotes the identity operator on n qubits and Z_j denotes the Pauli-Z operator acting on the jth qubit. Notice that \hat{X}_j is diagonal with respect to the computational basis, and its eigenvalues are zero and one; in particular,

$$\hat{X}_i \backslash \text{ket} x = x_i \backslash \text{ket} x.$$

MaxCut Hamiltonian

When we apply the Ising map construction to the MaxCut objective

$$M(x) = \sum_{(v,w) \in E} (x_v + x_w - 2x_v x_w)$$

we obtain the Hamiltonian

$$H_M = \sum_{(v,w) \in E} (X_v + X_w - 2X_v X_w) = rac{1}{2} \sum_{(v,w) \in E} ig(2I - Z_v - Z_w - (I - Z_v)(I - Z_w) ig) = rac{1}{2} ig|$$

In the last equation, |E| denotes the number of edges in the graph.

Energy minimization via QITE

Enter varQITE

With the MaxCut Hamiltonian in hand, we can turn to minimizing its energy using our novel quantum-classical varQITE heuristic. Much like any Variataional Quantum Algorithm (VQA), our novel varQITE method provides a recipe for iteratively updating the parameters in a variational quantum circuit to minimize the expectation value of the MaxCut Hamiltonian, measured with respect to the parametrized state.

A key novelty is that our varQITE algorithm does *not* rely on a classical optimizer to update the circuit parameters; instead, it specifies an explicit update rule based on the solution of a system linear Ordinary Differential Equations (ODEs). The ODEs relate the gradient of the variational circuit parameters to the expected value of certain operators related to the MaxCut Hamiltonian, and they are derived from an Ehrenfest Theorem that applies to imaginary time evolution. For details, see Equation (5) in our varQITE paper.

In any case, setting up the ODE system at each step of the algorithm requires executing a batch of quantum circuits and running some post-processing to evaluate the results.

The code cell below illustrates how to set up the variational ansatz $\backslash \ker \Psi(\theta)$ introduced by our varQITE paper in Equation (2). We'll set up the required circuits and the ODEs further down.

Below is simplified version of Quantum Imaginary Time Evolution (QITE). It uses a finite differences approach to estimate gradients, then performs gradient descent updates.

```
In [140...
class QITEvolver:
    """
    A class to evolve a parametrized quantum state under the action of an Ising
    Hamiltonian according to the variational Quantum Imaginary Time Evolution
    (QITE) principle described in IonQ's latest joint paper with ORNL.
    """
    def __init__(self, hamiltonian: SparsePauliOp, ansatz: QuantumCircuit):
        self.hamiltonian = hamiltonian
        self.ansatz = ansatz
```

```
# Define some constants
    self.backend = AerSimulator()
    self.num shots = 10000
    self.energies, self.param_vals, self.runtime = list(), list(), list()
def evolve(self, num_steps: int, lr: float = 0.4, verbose: bool = True):
    Evolve the variational quantum state encoded by ``self.ansatz`` under
    the action of ``self.hamiltonian`` according to varQITE.
    curr_params = np.zeros(self.ansatz.num_parameters)
    for k in range(num steps):
        # Get circuits and measure on backend
        iter qc = self.get iteration circuits(curr params)
        job = self.backend.run(iter_qc, shots=self.num_shots)
        q0 = time.time()
        measurements = job.result().get_counts()
        quantum_exec_time = time.time() - q0
        # Update parameters-- set up defining ODE and step forward
        Gmat, dvec, curr_energy = self.get_defining_ode(measurements)
        dcurr_params = np.linalg.lstsq(Gmat, dvec, rcond=1e-2)[0]
        curr_params += lr * dcurr_params
        # Progress checkpoint!
        if verbose:
            self.print status(measurements)
        self.energies.append(curr_energy)
        self.param_vals.append(curr_params.copy())
        self.runtime.append(quantum exec time)
def get_defining_ode(self, measurements: List[dict[str, int]]):
    Construct the dynamics matrix and load vector defining the varQITE
    iteration.
    # Load sampled bitstrings and corresponding frequencies into NumPy arrays
    dtype = np.dtype([("states", int, (self.ansatz.num_qubits,)), ("counts", "f
    measurements = [np.fromiter(map(lambda kv: (list(kv[0]), kv[1]), res.items(
    # Set up the dynamics matrix by computing the gradient of each Pauli word
    # with respect to each parameter in the ansatz using the parameter-shift ru
    pauli_terms = [SparsePauliOp(op) for op, _ in self.hamiltonian.label_iter()
    Gmat = np.zeros((len(pauli_terms), self.ansatz.num_parameters))
    for i, pauli_word in enumerate(pauli_terms):
        for j, jth_pair in enumerate(zip(measurements[1::2], measurements[2::2]
            for pm, pm_shift in enumerate(jth_pair):
                Gmat[i, j] += (-1)**pm * expected_energy(pauli_word, pm_shift)
    # Set up the Load vector
    curr_energy = expected_energy(self.hamiltonian, measurements[0])
    dvec = np.zeros(len(pauli_terms))
    for i, pauli_word in enumerate(pauli_terms):
        rhs_op_energies = get_ising_energies(pauli_word, measurements[0]["state
        rhs_op_energies *= get_ising_energies(self.hamiltonian, measurements[0]
```

```
dvec[i] = -np.dot(rhs_op_energies, measurements[0]["counts"]) / self.nu
    return Gmat, dvec, curr_energy
def get_iteration_circuits(self, curr_params: np.array):
    Get the bound circuits that need to be evaluated to step forward
    according to QITE.
    # Use this circuit to estimate your Hamiltonian's expected value
    circuits = [self.ansatz.assign_parameters(curr_params)]
    # Use these circuits to compute gradients
    for k in np.arange(curr_params.shape[0]):
        for j in range(2):
            pm shift = curr params.copy()
            pm_shift[k] += (-1)**j * np.pi/2
            circuits += [self.ansatz.assign_parameters(pm_shift)]
    # Add measurement gates and return
    [qc.measure_all() for qc in circuits]
    return circuits
def plot_convergence(self):
    Plot the convergence of the expected value of ``self.hamiltonian`` with
    respect to the (imaginary) time steps.
    plt.plot(self.energies)
    plt.xlabel("(Imaginary) Time step")
    plt.ylabel("Hamiltonian energy")
    plt.title("Convergence of the expected energy")
def print_status(self, measurements):
    Print summary statistics describing a QITE run.
    stats = pd.DataFrame({
        "curr energy": self.energies,
        "num_circuits": [len(measurements)] * len(self.energies),
        "quantum_exec_time": self.runtime
    })
    stats.index.name = "step"
    display.clear_output(wait=True)
    display.display(stats)
```

A few utility functions:

```
In [141...

def compute_cut_size(graph, bitstring):
    """

    Get the cut size of the partition of ``graph`` described by the given
    ``bitstring``.
    """

    cut_sz = 0
    for (u, v) in graph.edges:
        if bitstring[u] != bitstring[v]:
```

```
cut sz += 1
              return cut_sz
In [142...
          def get_ising_energies(
                  operator: SparsePauliOp,
                  states: np.array
              ):
              0.00
              Get the energies of the given Ising ``operator`` that correspond to the
              given ``states``.
              # Unroll Hamiltonian data into NumPy arrays
              paulis = np.array([list(ops) for ops, _ in operator.label_iter()]) != "I"
              coeffs = operator.coeffs.real
              # Vectorized energies computation
              energies = (-1) ** (states @ paulis.T) @ coeffs
              return energies
In [143...
          def expected_energy(
                  hamiltonian: SparsePauliOp,
                  measurements: np.array
          ):
              Compute the expected energy of the given ``hamiltonian`` with respect to
              the observed ``measurement``
              The latter is assumed to by a NumPy records array with fields ``states``
              --describing the observed bit-strings as an integer array-- and ``counts``,
              describing the corresponding observed frequency of each state.
              energies = get_ising_energies(hamiltonian, measurements["states"])
              return np.dot(energies, measurements["counts"]) / measurements["counts"].sum()
In [144...
          def interpret_solution(graph, bitstring):
              Visualize the given ``bitstring`` as a partition of the given ``graph``.
              pos = nx.spring_layout(graph, seed=42)
              set 0 = [i for i, b in enumerate(bitstring) if b == '0']
              set_1 = [i for i, b in enumerate(bitstring) if b == '1']
              plt.figure(figsize=(4, 4))
              nx.draw_networkx_nodes(graph, pos=pos, nodelist=set_0, node_color='blue', node_
              nx.draw_networkx_nodes(graph, pos=pos, nodelist=set_1, node_color='red', node_s
              cut_edges = []
              non_cut_edges = []
              for (u, v) in graph.edges:
                  if bitstring[u] != bitstring[v]:
                      cut_edges.append((u, v))
                  else:
                      non_cut_edges.append((u, v))
              nx.draw_networkx_edges(graph, pos=pos, edgelist=non_cut_edges, edge_color='gray
```

```
nx.draw_networkx_edges(graph, pos=pos, edgelist=cut_edges, edge_color='green',
nx.draw_networkx_labels(graph, pos=pos, font_color='white', font_weight='bold')
plt.axis('off')
plt.show()
```

```
In [145...
# Set up your QITEvolver and evolve!
    qit_evolver = QITEvolver(ham, ansatz)
    qit_evolver.evolve(num_steps=40, lr=0.1, verbose=True) # lr was 0.5
# Visualize your results!
    qit_evolver.plot_convergence()
```

curr_energy num_circuits quantum_exec_time

step			
0	-3.9856	17	1.116726
1	-4.1240	17	1.258594
2	-4.2118	17	1.207713
3	-4.3196	17	1.167748
4	-4.3958	17	1.176317
5	-4.4806	17	1.239019
6	-4.6232	17	1.167920
7	-4.6894	17	1.181148
8	-4.8070	17	1.204362
9	-4.8894	17	1.219521
10	-5.0138	17	1.215552
11	-5.0716	17	1.208433
12	-5.1700	17	1.217103
13	-5.2424	17	1.226270
14	-5.3426	17	1.172891
15	-5.4230	17	1.221435
16	-5.5158	17	1.164816
17	-5.6064	17	1.176880
18	-5.6582	17	1.196762
19	-5.7700	17	1.239296
20	-5.8368	17	1.172674
21	-5.9102	17	1.245610
22	-5.9766	17	1.212670
23	-6.0430	17	1.230855
24	-6.1190	17	1.150891
25	-6.1988	17	1.189471
26	-6.2524	17	1.180200
27	-6.2696	17	1.233273
28	-6.3506	17	1.177387

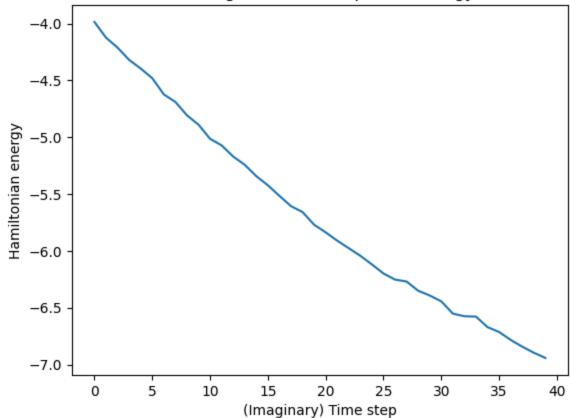
curr_energy num_circuits quantum_exec_time

step			
29	-6.3924	17	1.230455
30	-6.4440	17	1.223171
31	-6.5518	17	1.213212
32	-6.5750	17	1.195563
33	-6.5780	17	1.178016
34	-6.6708	17	1.188533
35	-6.7134	17	1.151463
36	-6.7830	17	1.148260
37	-6.8424	17	1.173934
38	-6.8958	17	1.185962

CPU times: total: 11min 16s

Wall time: 50 s

Convergence of the expected energy



```
qit_evolver_T.evolve(num_steps=40, lr=0.1, verbose=True)
# Visualize your results!
qit_evolver_T.plot_convergence()
```

curr_energy num_circuits quantum_exec_time

step			
0	-3.4999	15	0.917646
1	-3.5706	15	1.081908
2	-3.6825	15	1.024604
3	-3.7432	15	1.061090
4	-3.8414	15	1.047837
5	-3.8812	15	1.089578
6	-3.9509	15	1.055255
7	-4.0519	15	1.023758
8	-4.1255	15	1.007456
9	-4.1687	15	1.059985
10	-4.2612	15	1.065635
11	-4.3209	15	1.068485
12	-4.4074	15	1.022863
13	-4.4622	15	1.049885
14	-4.5411	15	1.068680
15	-4.6098	15	1.042266
16	-4.6783	15	1.053987
17	-4.7326	15	1.035232
18	-4.7859	15	1.052152
19	-4.8475	15	1.057591
20	-4.9042	15	1.072317
21	-4.9457	15	1.065712
22	-5.0186	15	1.067645
23	-5.0783	15	1.043957
24	-5.1425	15	1.064821
25	-5.2055	15	1.028622
26	-5.2677	15	1.075222
27	-5.2639	15	1.029957
28	-5.3265	15	1.068135

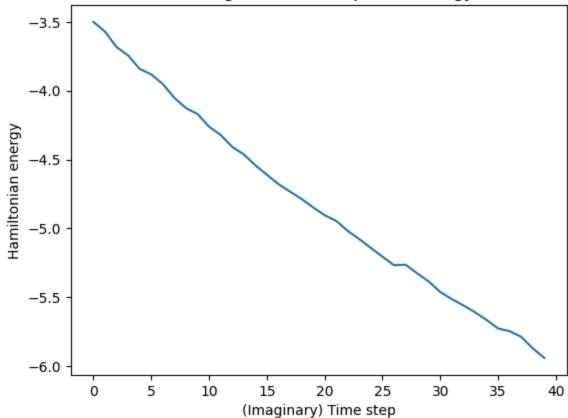
curr_energy num_circuits quantum_exec_time

step			
29	-5.3856	15	1.021477
30	-5.4627	15	1.047461
31	-5.5140	15	1.041347
32	-5.5596	15	1.023687
33	-5.6091	15	1.046060
34	-5.6652	15	1.055617
35	-5.7268	15	1.030224
36	-5.7468	15	1.086784
37	-5.7879	15	1.059183
38	-5.8718	15	1.058912

CPU times: total: 10min 3s

Wall time: 43.9 s

Convergence of the expected energy



```
qit_evolver_H.evolve(num_steps=40, lr=0.1, verbose=True)
# Visualize your results!
qit_evolver_H.plot_convergence()
```

curr_energy num_circuits quantum_exec_time

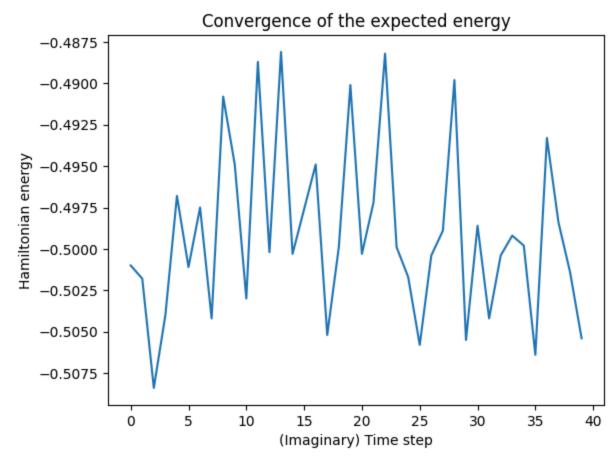
		_	
step			
0	-0.5010	3	0.131467
1	-0.5018	3	0.179009
2	-0.5084	3	0.214893
3	-0.5040	3	0.225893
4	-0.4968	3	0.216763
5	-0.5011	3	0.200153
6	-0.4975	3	0.216691
7	-0.5042	3	0.226025
8	-0.4908	3	0.215778
9	-0.4949	3	0.228082
10	-0.5030	3	0.238853
11	-0.4887	3	0.214051
12	-0.5002	3	0.224296
13	-0.4881	3	0.221195
14	-0.5003	3	0.202111
15	-0.4976	3	0.209109
16	-0.4949	3	0.192441
17	-0.5052	3	0.212367
18	-0.4999	3	0.197809
19	-0.4901	3	0.217182
20	-0.5003	3	0.216813
21	-0.4972	3	0.201377
22	-0.4882	3	0.201429
23	-0.4999	3	0.229549
24	-0.5017	3	0.216919
25	-0.5058	3	0.214272
26	-0.5004	3	0.215825
27	-0.4989	3	0.217781
28	-0.4898	3	0.225631

curr_energy num_circuits quantum_exec_time

step			
29	-0.5055	3	0.211634
30	-0.4986	3	0.223167
31	-0.5042	3	0.230766
32	-0.5004	3	0.214459
33	-0.4992	3	0.219517
34	-0.4998	3	0.233523
35	-0.5064	3	0.220221
36	-0.4933	3	0.226609
37	-0.4984	3	0.223676
38	-0.5014	3	0.215396

CPU times: total: 2min 7s

Wall time: 9.26 s



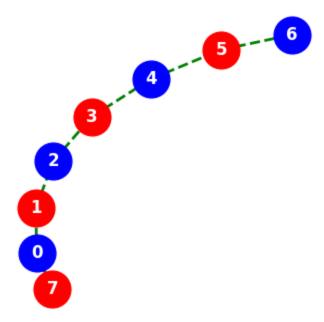
Check out your best / most frequent cut!

Following the variational quantum imaginary time evolution (vQITE) loop, we sample the quantum circuit to obtain classical bitstrings. The most frequent bitstring represents our solution, the final score though will take into account all of the right solutions...

```
In [148...
          from qiskit_aer import AerSimulator
          shots = 100_000
          backend = AerSimulator()
          # Sample your optimized quantum state using Aer for the tree
In [159...
          optimized_state_T = ansatz_T.assign_parameters(qit_evolver_T.param_vals[-1])
          optimized state T.measure all()
          counts_T = backend.run(optimized_state_T, shots=shots).result().get_counts()
          # Find the sampled bitstring with the largest cut value
          cut_vals_T = sorted(((bs, compute_cut_size(T, bs)) for bs in counts), key=lambda t:
          best_bs_T = cut_vals_T[-1][0]
          # Now find the most likely MaxCut solution as sampled from your optimized state
          # We'll leave this part up to you!!!
          most_likely_soln = ""
          print(counts_T)
```

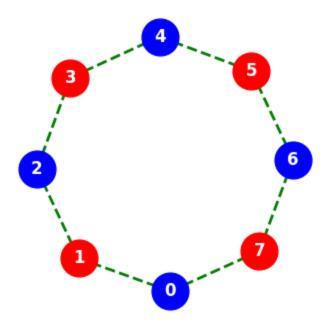
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```
interpret_solution(T, best_bs_T)
print("Cut value: "+str(compute_cut_size(T, best_bs_T)))
print(T, best_bs_T)
```



Cut value: 7
Graph with 8 nodes and 7 edges 01010101

```
In [161... # interpret the same solution, but with the whole graph instead of the tree
interpret_solution(graph, best_bs_T)
print("Cut value: "+str(compute_cut_size(graph, best_bs_T)))
print(graph, best_bs_T)
```



Cut value: 8
Graph with 8 nodes and 8 edges 01010101

```
In [162... # Sample your optimized quantum state using Aer for the tree

optimized_state_H = ansatz_H.assign_parameters(qit_evolver_H.param_vals[-1])
optimized_state_H.measure_all()
counts_H = backend.run(optimized_state_H, shots=shots).result().get_counts()
```

```
# Find the sampled bitstring with the largest cut value
cut_vals_H = sorted(((bs, compute_cut_size(H, bs)) for bs in counts), key=lambda t:
best_bs_H = cut_vals_H[-1][0]

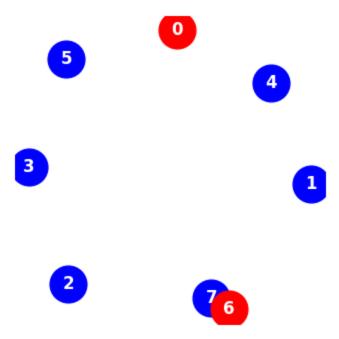
# Now find the most likely MaxCut solution as sampled from your optimized state
# We'll leave this part up to you!!!
most_likely_soln = ""

print(counts_H)
```

```
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         284, '01110101': 241, '10001100': 263, '10011111': 264, '01101010': 276, '01001000':
         272, '01100010': 259}
          interpret_solution(H, best_bs_H)
In [163...
          print("Cut value: "+str(compute_cut_size(H, best_bs_H)))
```

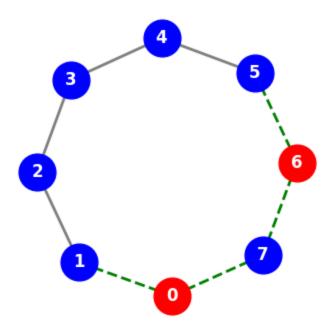
```
file:///C:/Users/akank/OneDrive/Documents/GitHub/2025-lonQ/lonQuHack2025_graph1.html
```

print(H, best_bs_H)



Cut value: 1
Graph with 8 nodes and 1 edges 10000010

interpret_solution(graph, best_bs_H)
print("Cut value: "+str(compute_cut_size(graph, best_bs_H)))
print(graph, best_bs_H)

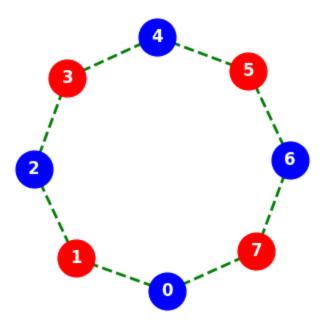


Cut value: 4
Graph with 8 nodes and 8 edges 10000010

```
In [165... # choose the better result from best_bs_T and best_bs_H
best_bs_final = best_bs_H if compute_cut_size(H, best_bs_H) > compute_cut_size(T, b
final_cut_value = compute_cut_size(graph, best_bs_final)

# choose the better result ansatz from ansatz_T and ansatz_H
ansatz_final = ansatz_H if compute_cut_size(H, best_bs_H) > compute_cut_size(T, bes
```

```
interpret_solution(graph, best_bs_final)
print("Cut value: "+str(final_cut_value))
print(graph, best_bs_final)
```



Cut value: 8
Graph with 8 nodes and 8 edges 01010101

```
In [166... # from qiskit_aer import AerSimulator

# shots = 100_000

# Sample your optimized quantum state using Aer
# backend = AerSimulator()
optimized_state = ansatz.assign_parameters(qit_evolver.param_vals[-1])
optimized_state.measure_all()
counts = backend.run(optimized_state, shots=shots).result().get_counts()

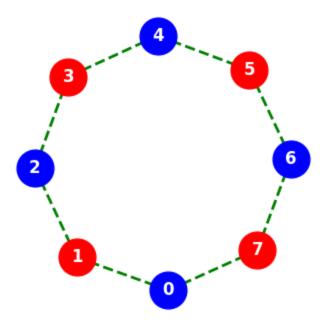
# Find the sampled bitstring with the largest cut value
cut_vals = sorted(((bs, compute_cut_size(graph, bs)) for bs in counts), key=lambda
best_bs = cut_vals[-1][0]

# Now find the most likely MaxCut solution as sampled from your optimized state
# We'll leave this part up to you!!!
most_likely_soln = ""

print(counts)
```

{'01011100': 19, '10110110': 337, '10011001': 25, '10101010': 25299, '01010101': 255 53, '11010010': 1549, '10010101': 1515, '11101010': 1455, '01110111': 5, '01001011': 384, '00010101': 1563, '01010100': 1521, '10111010': 320, '00101001': 1458, '1100111 0': 23, '00101011': 1490, '00110101': 1475, '10111100': 12, '01010110': 1516, '01010 010': 1517, '00101101': 1580, '00110011': 26, '01011010': 1567, '10110100': 400, '01 101010': 1450, '10101101': 1553, '01110001': 8, '01001101': 345, '11010100': 1572, '10101100': 371, '10100100': 377, '11010110': 1510, '11001000': 20, '10101111': 18, '10100010': 359, '01101101': 370, '10101011': 1568, '11011010': 1495, '10010100': 34 7, '00111011': 26, '00100101': 1485, '01010001': 371, '10111101': 15, '10010110': 35 3, '01110100': 23, '01001010': 1516, '10100001': 20, '01101011': 379, '01001001': 34 0, '10100110': 389, '11001010': 1525, '10011010': 383, '10101001': 1507, '01101001': 363, '10110101': 1515, '10101110': 353, '10100101': 1484, '11010000': 27, '0111010 1': 398, '10111111': 1, '01010011': 369, '10110001': 21, '01011101': 350, '1011011 1': 20, '01011011': 365, '10110010': 353, '01100101': 343, '10101000': 372, '0101011 1': 343, '10111011': 22, '10010010': 374, '01000101': 345, '10011011': 19, '0101100 1': 355, '11101100': 21, '10001010': 360, '01110110': 24, '01001100': 26, '0010101 0': 20, '11101110': 21, '00001011': 16, '00010111': 23, '10100011': 20, '10010111': 27, '10001011': 21, '10100111': 21, '00000101': 20, '00001101': 25, '11111010': 22, '01111001': 3, '00100111': 24, '10110011': 18, '01011111': 5, '00111001': 17, '01001 000': 22, '00111101': 16, '00100011': 19, '10110000': 3, '01011110': 22, '11100100': 16, '10010001': 31, '10011100': 7, '01101100': 17, '01111011': 2, '01000111': 8, '01 101111': 6, '10001001': 22, '01100011': 5, '00010011': 36, '11010101': 20, '0100111 0': 24, '01100010': 23, '11001100': 13, '11110010': 21, '11000100': 18, '01100110': 16, '00110111': 17, '01000110': 17, '01111100': 1, '11101101': 2, '11000110': 21, '1 1110110': 21, '01101110': 26, '10011000': 6, '01001111': 5, '01110011': 4, '1011100 1': 23, '10001110': 8, '10011101': 17, '01100001': 7, '11011000': 21, '10010011': 2 9, '11101000': 18, '01010000': 18, '101111110': 5, '001111111': 1, '00100001': 27, '00 011001': 17, '11000010': 20, '10111000': 9, '11011110': 19, '11100010': 14, '1000110 0': 2, '10001101': 26, '01000010': 30, '01111010': 16, '01000100': 24, '11110100': 2 1, '00110001': 21, '00101111': 14, '00100100': 1, '01011000': 24, '00011101': 15, '0 1000001': 7, '01111101': 3, '10100000': 5, '00001001': 28, '01110010': 25, '1000010 1': 16, '01000011': 3, '11011100': 24, '01101000': 18, '00010001': 21, '111111100': 2, '01100100': 14, '10011110': 5, '10000110': 3, '011111110': 1, '11001101': 1, '1110 0110': 12, '10000010': 5, '00011011': 21, '01100111': 3, '10001000': 2, '10010000': 3, '00010100': 1, '11010111': 1, '01100000': 1, '11100101': 1, '10000100': 2, '11101 011': 1, '11001011': 1, '00111010': 1, '11111000': 2, '11010011': 1, '10011111': 1, '00010010': 1}

```
interpret_solution(graph, best_bs)
print("Cut value: "+str(compute_cut_size(graph, best_bs)))
print(graph, best_bs)
```



Cut value: 8
Graph with 8 nodes and 8 edges 01010101

Drumroll please... the scores!

```
In [168...
          %%time
          # Brute-force approach with conditional checks
          verbose = False
          G = graph
          n = len(G.nodes())
          w = np.zeros([n, n])
          for i in range(n):
              for j in range(n):
                  temp = G.get_edge_data(i, j, default=0)
                   if temp != 0:
                      w[i, j] = 1.0
          if verbose:
              print(w)
          best_cost_brute = 0
          best_cost_balanced = 0
          best_cost_connected = 0
          for b in range(2**n):
              x = [int(t) for t in reversed(list(bin(b)[2:].zfill(n)))]
              # Create subgraphs based on the partition
              subgraph0 = G.subgraph([i for i, val in enumerate(x) if val == 0])
              subgraph1 = G.subgraph([i for i, val in enumerate(x) if val == 1])
              bs = "".join(str(i) for i in x)
```

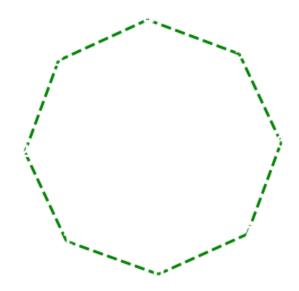
```
# Check if subgraphs are not empty
if len(subgraph0.nodes) > 0 and len(subgraph1.nodes) > 0:
    cost = 0
    for i in range(n):
        for j in range(n):
            cost = cost + w[i, j] * x[i] * (1 - x[j])
    if best_cost_brute < cost:</pre>
        best_cost_brute = cost
        xbest brute = x
        XS_brut = []
    if best_cost_brute == cost:
        XS_brut.append(bs)
    outstr = "case = " + str(x) + " cost = " + str(cost)
    if (len(subgraph1.nodes)-len(subgraph0.nodes))**2 <= 1:</pre>
        outstr += " balanced"
        if best_cost_balanced < cost:</pre>
            best_cost_balanced = cost
            xbest balanced = x
            XS_balanced = []
        if best_cost_balanced == cost:
            XS_balanced.append(bs)
    if nx.is connected(subgraph0) and nx.is connected(subgraph1):
        outstr += " connected"
        if best_cost_connected < cost:</pre>
            best_cost_connected = cost
            xbest\_connected = x
            XS_connected = []
        if best cost connected == cost:
            XS connected.append(bs)
    if verbose:
        print(outstr)
```

CPU times: total: 15.6 ms Wall time: 59.7 ms

```
In [169... # This is classical brute force solver results:
    interpret_solution(graph, xbest_brute)
    print(graph, xbest_brute)
    print("\nBest solution = " + str(xbest_brute) + " cost = " + str(best_cost_brute))
    print(XS_brut)

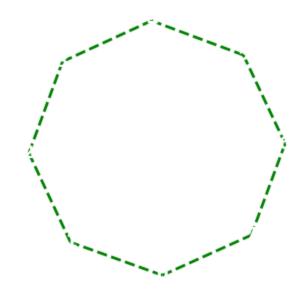
interpret_solution(graph, xbest_balanced)
    print(graph, xbest_balanced)
    print("\nBest balanced = " + str(xbest_balanced) + " cost = " + str(best_cost_balanced)

interpret_solution(graph, xbest_connected)
    print(graph, xbest_connected)
    print("\nBest connected = " + str(xbest_connected) + " cost = " + str(best_cost_connected)
    print("\nBest connected = " + str(xbest_connected) + " cost = " + str(best_cost_connected)
    plt.show()
```



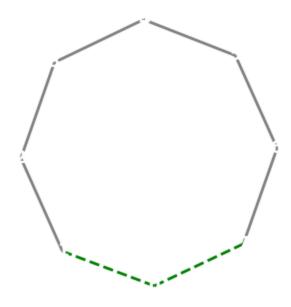
Graph with 8 nodes and 8 edges [1, 0, 1, 0, 1, 0, 1, 0]

Best solution = [1, 0, 1, 0, 1, 0, 1, 0] cost = 8.0 ['10101010', '01010101']



Graph with 8 nodes and 8 edges [1, 0, 1, 0, 1, 0, 1, 0]

Best balanced = [1, 0, 1, 0, 1, 0, 1, 0] cost = 8.0 ['10101010', '01010101']



Graph with 8 nodes and 8 edges [1, 0, 0, 0, 0, 0, 0]

```
Best connected = [1, 0, 0, 0, 0, 0, 0, 0] cost = 2.0
['10000000', '01000000', '11000000', '00100000', '01100000', '11100000', '00010000', '00110000', '01111000', '01111000', '01111000', '01111000', '01111100', '01111100', '01111100', '01111100', '01111110', '01111110', '01111110', '01111110', '01111110', '01111110', '111111110', '011000001', '10000001', '11000001', '11100001', '11110001', '11111001', '11111101', '011111', '01100011', '11110011', '11111011', '01100011', '11111011', '11111111', '0111111', '11000111', '11110111', '11000111', '11110111', '0111111', '0111111']
```

```
In [170...
          # And this is how we calculate the shots counted toward scores for each class of th
          sum counts = 0
          for bs in counts:
              if bs in XS_brut:
                   sum_counts += counts[bs]
          print(f"Pure max-cut: {sum_counts} out of {shots}")
          sum_balanced_counts = 0
          for bs in counts:
              if bs in XS balanced:
                   sum_balanced_counts += counts[bs]
          print(f"Balanced max-cut: {sum_balanced_counts} out of {shots}")
          sum_connected_counts = 0
          for bs in counts:
              if bs in XS_connected:
                   sum_connected_counts += counts[bs]
```

print(f"Connected max-cut: {sum_connected_counts} out of {shots}")

Pure max-cut: 50852 out of 100000
Balanced max-cut: 50852 out of 100000
Connected max-cut: 10 out of 100000

```
In [171... | def final_score(graph, XS_brut,counts,shots,ansatz,challenge):
              if(challenge=='base'):
                  sum_counts = 0
                  for bs in counts:
                      if bs in XS_brut:
                           sum_counts += counts[bs]
              elif(challenge=='balanced'):
                  sum balanced counts = 0
                  for bs in counts:
                      if bs in XS_balanced:
                           sum_balanced_counts += counts[bs]
                  sum_counts = sum_balanced_counts
              elif(challenge=='connected'):
                  sum connected counts = 0
                  for bs in counts:
                      if bs in XS_connected:
                           sum_connected_counts += counts[bs]
                  sum_counts = sum_connected_counts
              transpiled_ansatz = transpile(ansatz, basis_gates = ['cx','rz','sx','x'])
              cx_count = transpiled_ansatz.count_ops()['cx']
              score = (4*2*graph.number_of_edges())/(4*2*graph.number_of_edges() + cx_count)
              return np.round(score,5)
          print("Base score: " + str(final_score(graph, XS_brut, counts, shots, ansatz, 'base')))
In [172...
          print("Balanced score: " + str(final_score(graph,XS_brut,counts,shots,ansatz,'balan
          print("Connected score: " + str(final_score(graph,XS_brut,counts,shots,ansatz,'conn
         Base score: 0.40682
         Balanced score: 0.40682
         Connected score: 8e-05
In [173...
          # calculate our version of the score for the final solution
          print("Base score: " + str(final_score(graph,XS_brut,counts,shots,ansatz_H,'base'))
          print("Balanced score: " + str(final_score(graph,XS_brut,counts,shots,ansatz_H,'bal
          print("Connected score: " + str(final_score(graph,XS_brut,counts,shots,ansatz_H,'co
         Base score: 0.49311
         Balanced score: 0.49311
         Connected score: 0.0001
          # calculate our version of the score for the final solution
In [174...
          print("Base score: " + str(final_score(graph,XS_brut,counts,shots,ansatz_T,'base'))
          print("Balanced score: " + str(final_score(graph,XS_brut,counts,shots,ansatz_T,'bal
          print("Connected score: " + str(final_score(graph, XS_brut, counts, shots, ansatz_T, 'co
         Base score: 0.41725
         Balanced score: 0.41725
         Connected score: 8e-05
```

This is the main challenge: design optimal ansatz generators and Hamiltonians for the maxcut problem, subject to three specific conditions. Solutions for each condition can be submitted independently; however, a unified approach applicable to all three conditions will receive additional credit.

Submit your results

I guess this is the most important part. You probably want to report your results.

Please, follow the link: https://forms.gle/gkpSCe7HGr7QHZXQ6

Let's revisit the problem statement. **This is important!!!** We have three scoring methods to report:

- 1. Counts shots achieving the optimal max-cut value. Sorry, no approximation value this time.
- 2. Adds a balance constraint—subgraphs must have equal cardinality.
- 3. Requires connected subgraphs—all vertices within a subgraph must be mutually reachable.

For **in-person participants**: Prepare a presentation that explains your research and demonstrates the value of your proposed solution.

Can you solve this? Good luck!

Feedback

If you have any suggestions or recommendations abou the hackathon challange, please, don't hesitatate to leave your comment here: https://iter.ly/u42um



In []: