# Compass TB1 Group Project: Lab Notebook

Euan Enticott, Daniel Ward, Shannon Williams

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## 1 Introduction

In this lab notebook we present the analyses undertaken as part of the Compass TB1 group project. We focus on a large, open source dataset provided by the City of Chicago consisting of reported incidents of crime from 2001 to present day, as reported by the Chicago Police Department. The dataset can be obtained from the website https://data.cityofchicago.org/Public-Safety/Crimes-2001-to-Present/ijzp-q8t2.

The notebook will be broken up into three sections:

- 1. Workflow and Computational Techniques: A summary of the approach used in the development of the **chigcrim** package.
- 2. Classification: Predicting whether a reported crime led to the arrest of a suspect. We consider three different discriminative classifiers: logistic regression, support vector machines, and random forests.
- 3. Prediction: Predicting the number of reported crimes which occur in a given region over a specified time period (of a given type, if desired), through interpolation. We consider kernel ridge regression and generalised additive models (GAMs).

## 2 Workflow and Computational Techniques

In the development of the package **chigcrim**, we utilised a number of computational techniques which are documented below. The package can be accessed on GitHub: https://github.com/shannon-wms/chicago-crime.

## 2.1 Object-Oriented Programming

We decided to use an object oriented approach to constructing models. In particular, we made use of the R6Class from the R6 package. R6 objects are mutable and use an object oriented approach similar to most programming languages (unlike the more basic S3 and S4 classes). R6 classes are very similar to reference classes, although generally R6 classes are preferred. This is for a variety of reasons, including the fact that R6 classes are much faster, and they handle fields in a neater way by putting them in a separate environment. More information on this can be found here. Notably, R6 classes support both public (available to the user) and private (not visible to the user) members.

Each of the models considered can be initialised with a call to model\$new(...), and then fitted using model\$fit(X, y) where X and y are our training data matrix and response vector, respectively. Predictions can then be made with model\$predict(X). The datasets, fitted model and predictions, along with other objects unique to the model, are then stored as fields accessed through model\$field.

It is worth noting that this use of fit and predict methods in object-oriented machine learning packages is used elsewhere, particularly in the **Python** package scikit-learn. The key advantage of this approach is that it abstracts away the underlying complexities, and creates a consistent structure that makes it easier to compare different models.

#### 2.2 Parallel Programming

Parallel programming was used to speed up slow code, utilising the package **doParallel** which calls the packages **parallel** and **foreach**. In particular, we implemented a parallel cross-validation function kfold\_cv, which facilitated more accurate and faster assessment of model performance.

#### 2.3 Documentation

In order to document functions in the package, we made use of **roxygen2**. This package automatically creates the .Rd documentation files for functions, classes and data, from comments added above the function definitions. In addition to being an efficient way to generate documentation, this allows the code and documentation to coexist, making it easier to remember to update the documentation.

#### 2.4 API Querying

The Chicago Crime dataset is updated on a daily basis and, at the time of writing, contains over 7 million rows of data. For each reported incident, a total of 22 features are recorded (for a full list of features and their descriptions see the City of Chicago website). We elected not to download the dataset in full and include this in the package as it would consume a significant amount of storage, and quickly become out of date.

Instead, we utilised the **RSocrata** package which allows easy interaction with the online open data portal. The wrapper load\_data allows the end user to directly download the dataset into the R environment, via the function read.socrata. load\_data provides functionality for filtering by year, limiting the number of data points received, and omitting missing/NA values.

#### 2.5 Testing and Continuous Integration

For tests, we used the **testthat** package. This simply creates a new directory ./tests/testthat/ in which the user can define tests for the package functions. Although the tests can be run alone, generally, we made use of the package rcmdcheck. This contains the function rcmdcheck, which not only runs the tests, but also carries out a more sophisticated check. Some examples of what is checked are listed below:

- Checks the package installs correctly.
- Checks for missing documentation.
- Automatically runs examples in documentation, to check they run successfully.
- Checks for undefined variables.
- Checks for missing dependencies.

In order to ensure that tests and checks were run on a regular basis, continuous integration was set up using Github Actions. This runs rcmdcheck() for each pull request and push to the main branch, thus limiting the possibility of unintentionally introducing any breaking changes.

## 3 Classification

In this section we consider the binary classification task of predicting whether a suspect is arrested, given data on the reported crime. Three models will be investigated: logistic regression, support vector machines and random forest classifiers.

#### 3.1 Assessing Performance

To assess performance, three metrics will be used:

- Overall accuracy: The proportion of correct predictions.
- Sensitivity: The proportion of positive observations correctly predicted.
- Specificity: The proportion of negative observations correctly predicted.

These metrics can be computed using the functions classification\_accuracy, classification\_sensitivity, and classification\_specifity, respectively, from the chigcrim package.

Note that logistic regression is a probabilistic classifier whereas support vector machines and random forests are non-probabilistic. As such, the output from logistic regression is a probability in [0,1] while the outputs from the other models are class predictions in  $\{0,1\}$ . In our analysis, the probabilities given by logistic regression are rounded to yield predictions that can be assessed using the metrics above. This facilitates the comparison of these results with the other two classifiers.

```
# Load required packages
library(chigcrim)
# Use seed to ensure reproducibility
set.seed(1)
```

For each classifier, we will use repeated k-fold cross validation to obtain mean values of the metrics. Specifically, 5-fold cross validation is repeated five times (run in parallel using the function kfold\_cv), and the metrics are averaged across the folds and repeats.

#### 3.2 Feature Selection

Due to the time and computational limitations involved in downloading, storing, and training models on the entire dataset, we shall train the models only on a subset of the data from the year 2019.

```
# Load 2019 data to build classification models
df <- load_data(year = 2019, strings_as_factors = FALSE)</pre>
```

```
print(as.data.frame(head(df)))
```

```
##
           id case_number
                                          date
                                                                   block iucr
## 1 11552577
                 JC100040 2019-01-01 00:31:00
                                                    032XX W LAWRENCE AVE 1310
## 2 11552587
                 JC100034 2019-01-01 00:05:00
                                                         006XX E 83RD PL 1310
## 3 11552596
                 JC100045 2019-01-01 00:03:00
                                                        001XX W HURON ST 0430
                 JC100030 2019-01-01 00:01:00
                                                  004XX N MONTICELLO AVE 143A
## 4 11552605
                 JC100028 2019-01-01 00:05:00 013XX S CENTRAL PARK AVE 0486
## 5 11552609
## 6 11552610
                 JC100044 2019-01-01 00:02:00
                                                         031XX W 25TH ST 1310
##
          primary_type
                                          description location_description arrest
                                          TO PROPERTY
## 1
       CRIMINAL DAMAGE
                                                                 RESTAURANT
                                                                              FALSE
## 2
       CRIMINAL DAMAGE
                                          TO PROPERTY
                                                                  RESIDENCE
                                                                             FALSE
               BATTERY AGGRAVATED: OTHER DANG WEAPON
## 3
                                                                HOTEL/MOTEL
                                                                              FALSE
## 4 WEAPONS VIOLATION
                             UNLAWFUL POSS OF HANDGUN
                                                                       ALLEY
                                                                               TRUE
## 5
               BATTERY
                              DOMESTIC BATTERY SIMPLE
                                                                  APARTMENT
                                                                              FALSE
## 6
       CRIMINAL DAMAGE
                                          TO PROPERTY
                                                                  RESIDENCE
                                                                              FALSE
##
     domestic beat district ward community_area fbi_code x_coordinate y_coordinate
## 1
        FALSE 1713
                          17
                               33
                                                        14
                                                                1153943
                                               14
                                                                              1931709
## 2
        FALSE 632
                           6
                                6
                                               44
                                                        14
                                                                1182085
                                                                              1849762
## 3
        FALSE 1832
                          18
                               42
                                               8
                                                       04B
                                                                1175159
                                                                              1905043
## 4
        FALSE 1122
                          11
                               27
                                               23
                                                                1151958
                                                        15
                                                                              1902815
## 5
         TRUE 1011
                          10
                               24
                                               29
                                                       08B
                                                                1152589
                                                                              1893426
## 6
        FALSE 1033
                          10
                               12
                                               30
                                                        14
                                                                1155950
                                                                              1887234
##
                   updated on latitude longitude
## 1 2019 2019-01-10 15:16:50 41.96844 -87.70934
## 2 2019 2019-01-10 15:16:50 41.74297 -87.60841
## 3 2019 2019-01-10 15:16:50 41.89482 -87.63213
## 4 2019 2019-01-10 15:16:50 41.88920 -87.71740
## 5 2019 2019-01-10 15:16:50 41.86342 -87.71533
## 6 2019 2019-01-10 15:16:50 41.84636 -87.70316
```

Below we outline our feature selection and data pre-processing choices. These decisions involved incorporating information from conducting exploratory data analysis (EDA), as well as considering what is computationally feasible.

- Encode the date as the day of the year, yday (an integer between 1-365, or 1-366 for leap years).
- Encode time of day as a floating point in 0-24 (time), as this showed promising results in our EDA.
- Drop year as we are only using data from 2019.
- Drop id as this is the unique key for each data point.
- We drop case number, as the values are almost all unique and are not informative.
- Drop primary\_type, description and iucr code. Keep fbi\_code as an indicator of crime type.

- Drop updated\_on as this only refers to when the data was last updated and is uninformative.
- Drop latitude and longitude, and keep x\_coordinate and y\_coordinate. Note that these coordinates are likely not particularly useful for linear classifiers, but should be useful for non-linear methods.
- Keep community\_area, but other areas (district, beat, ward and block) are dropped.
- Omit all NA values.
- Particularly rare factors will be grouped into a variable other (see ?otherise).

```
# Convert rarely used fbi categories to "OTHER"
df$fbi_code <- otherise(df$fbi_code, 500)</pre>
```

## 7 out of 26 categories were converted to OTHER corresponding to 0.51% ## of observations.

```
df$location_description <- otherise(df$location_description, 1000)</pre>
```

## 126 out of 155 categories were converted to OTHER corresponding to 10.82% ## of observations.

```
##
     location_description arrest domestic community_area fbi_code x_coordinate
## 1
               RESTAURANT FALSE
                                    FALSE
                                                       14
                                                                14
                                                                        1153943
## 2
                RESIDENCE FALSE
                                    FALSE
                                                       44
                                                                14
                                                                        1182085
## 3
              HOTEL/MOTEL FALSE
                                    FALSE
                                                       8
                                                               04B
                                                                        1175159
## 4
                                    FALSE
                                                       23
                    ALLEY
                            TRUE
                                                                15
                                                                        1151958
## 5
                APARTMENT
                          FALSE
                                     TRUE
                                                       29
                                                               08B
                                                                        1152589
                RESIDENCE FALSE
## 6
                                    FALSE
                                                       30
                                                                14
                                                                        1155950
    y_coordinate day
                            time
## 1
          1931709
                    1 0.51666667
## 2
          1849762
                    1 0.08333333
## 3
          1905043 1 0.05000000
          1902815 1 0.01666667
## 4
## 5
          1893426 1 0.08333333
## 6
          1887234
                  1 0.03333333
```

#### 3.3 Logistic Regression

We will first consider a logistic regression classifier, which is a linear classifier for binary data. We use our R6 class LogisticRegression which has methods fit and predict. fit calls the function optim() internally to minimize the cross-entropy/log-loss function using gradient-based optimisation methods (either BFGS, L-BFGS-B or CG); in our analysis we use BFGS as we don't run into memory issues.

	accuracy	sensitivity	specificity
1	0.8614	0.4347	0.9788
2	0.8613	0.4351	0.9786
3	0.8613	0.4345	0.9787
4	0.8613	0.4341	0.9789
5	0.8612	0.4346	0.9786

#### 3.4 Support Vector Machines

As the support vector machine (SVM) allows use of a kernel function, it should be able to capture non-linear relationships in the original feature space (given an appropriate kernel). As the relationship between the features and the class is unknown, a radial basis function kernel is used. The R6 class SupportVectorMachine, again with fit and predict methods, is a wrapper of the function svm from the dedicated SVM package e1071. Unfortunately, support vector machines do not scale well to large data sets, so here we will only use 30,000 rows.

```
# Subset the data randomly
index <- sample(1:nrow(df), 30000)
X_subset <- X[index, ]
y_subset <- y[index]</pre>
```

In order to obtain optimal values for cost and gamma to be provided to svm for training the SVM, we utilise the built-in generic function tune from e1071 which performs a grid search over given parameter ranges.

svm\_tuned

```
##
## Parameter tuning of 'e1071::svm':
##
## - sampling method: 5-fold cross validation
##
## - best parameters:
## cost gamma
## 16 0.03125
##
## - best performance: 0.128
```

We obtain optimal values of 2<sup>4</sup> for cost and 2<sup>5</sup> for gamma, which we use to train our SVM.

```
# Initialise new SupportVectorMachine object
svm <- SupportVectorMachine$new(kernel = "radial")</pre>
```

```
# Export results for use in report
tab <- xtable::xtable(as_tibble(svm_results), digits = 4)
print(tab, type = "latex", comment = FALSE)</pre>
```

	accuracy	sensitivity	specificity
1	0.8624	0.4076	0.9870
2	0.8627	0.4091	0.9870
3	0.8626	0.4087	0.9870
4	0.8622	0.4067	0.9870
5	0.8619	0.4052	0.9870

#### 3.5 Random Forests

The random forest trains multiple decision trees using a subset of features to create each tree. Decision trees are an ordered set of rules defined on the feature values that attempt to split the data into classes. As decision trees have a tendency to overfit, the random forest attempts to overcome this by growing multiple trees on different features within the dataset. In the classification case, a prediction is made by predicting from each decision tree separately and finding the most common predicted class. This is a black-box method but has the potential for good predictive performance.

Our R6 class RandomForest is a wrapper for the function randomForest from the randomForest package. Due to the high computational cost involved in fitting random forest models we again use a smaller subset of the data. Here we use the same dataset used to fit the SVM, with the factor community\_area removed as the algorithm for fitting the model cannot handle such a large number of factors.

```
# Export results for use in report
tab <- xtable::xtable(as_tibble(rf_results), digits = 4)
print(tab, type = "latex", comment = FALSE)</pre>
```

	accuracy	sensitivity	specificity
1	0.8762	0.5258	0.9722
2	0.8780	0.5293	0.9736
3	0.8762	0.5299	0.9712
4	0.8775	0.5293	0.9729
5	0.8761	0.5259	0.9721

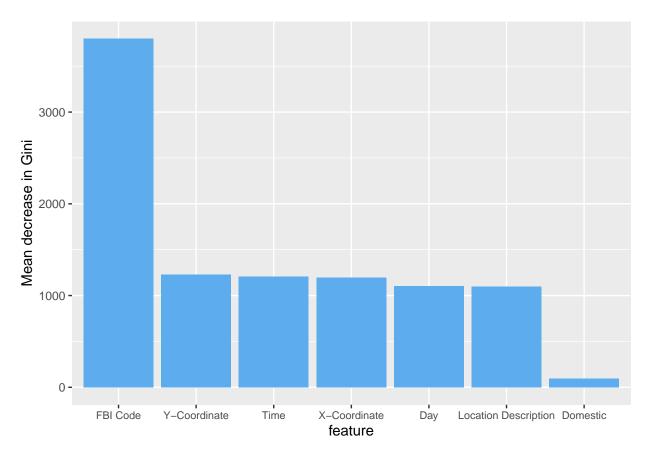
#### 3.6 Model Comparisons

The models all performed quite similarly. Unsurprisingly, the support vector machine and the random forest classifier performed best, due to their ability to capture non-linear relationships. It is worth noting that this difference is surprisingly small, although this could be related to the fact that the logistic regression model was trained on a larger dataset. Alternatively, the SVM results could suggest that encoding the community areas as factors was sufficient to capture much of the spatial aspect of the crimes in logistic regression.

Logistic regression had higher sensitivity than the support vector machine, and thus could be viewed as a preferable option if false negatives are particularly detrimental. It is worth noting however that both support

vector machines and logistic regression can be adjusted to reflect unbalanced costs associated with incorrect predictions.

Being an ensemble model, the random forest unsurprisingly performed the best based on all three metrics. It is likely that the random forest could be improved by training on a larger subset of the data and optimising the hyperparameters. The downside of using a random forest is that, as a black-box method, it does not provide any inference as to how the features are used within the model. We are at least able to look at how many times each feature was chosen as a splitting point in all of the trees, providing us with some information as to the importance of each of the features.



The plot suggests that the most "important" feature is fbi\_code, which is somewhat unsurprising as this tells us what type of crime was reported. This would intuitively have a significant impact on whether the incident report led to a suspect being arrested. Note that none of the models achieved an accuracy greater than 90%.

## 4 Prediction

In this section we consider the regression tesk of predicting the number of reported incidents of crime in a given region over a specified time period. We will look at a kernel ridge regression model before moving on to generalised additive models.

#### 4.1 Assessing Performance

To assess performance, two metrics will be used: the root mean squared error (RMSE) and R-squared ( $R^2$ ). These metrics can be computed using the functions rmse\_loss and r\_squared, respectively, from the **chigcrim** package.

```
# List of metrics used to evaluate regression models
metrics <- list(rmse = rmse_loss, r2 = r_squared)</pre>
```

Repeated k-fold cross validation is used, and hyperparameters are chosen based on the RMSE metric. In particular, we will use 5 repetitions of 5-fold cross validation at each parameter value using the  $kfold_cv$  function.

#### 4.2 Kernel Ridge Regression

The R6 class KernelRegression fits a kernel ridge regression model with a specified kernel: one of "linear" (equivalent to ridge regression), "polynomial", or "radial" (radial basis kernel).

As the relationship between the data and response is complex and non-linear, only the radial basis kernel will be considered here. This implicitly induces an extremely flexible infinite-dimensional feature transform. Note that we fix the regularisation parameter lambda as 0.001 in the ensuing analysis.

```
# Load required packages
library(rgdal)
library(sf)
library(ggmap)
# Use seed to ensure reproducibility
set.seed(1)
```

#### 4.2.1 Weekly Predictions

We first consider a simple, single-dimensional model, using only the number of crimes per week as the predictor.

```
df <- load_data(select = "date")</pre>
```

```
df %<>%
  mutate(date = date(date), week = week(date), year = year(date)) %>%
  filter(week < 53) %>%
  group_by(week, year) %>%
  mutate(week_start = min(date)) %>%
  ungroup() %>%
  count(week, week_start, year) %>%
  arrange(year, week) %>%
  mutate(cumulative_week = 1:nrow(.))
print(as.data.frame(head(df)))
```

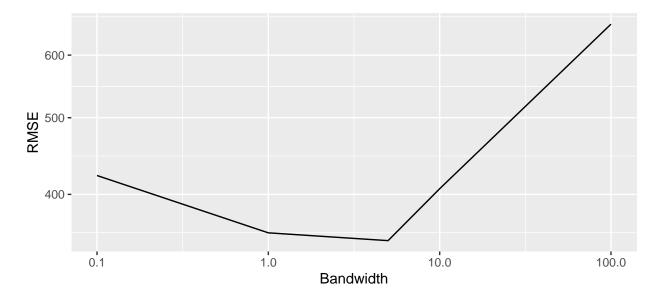
```
##
     week week_start year
                              n cumulative_week
## 1
        1 2001-01-01 2001 8942
## 2
        2 2001-01-08 2001 8589
                                               2
        3 2001-01-15 2001 8704
                                               3
## 3
## 4
        4 2001-01-22 2001 8300
                                               4
## 5
        5 2001-01-29 2001 8473
                                              5
## 6
        6 2001-02-05 2001 8418
                                               6
```

We shall use a grid search with 5-fold cross validation, repeated 5 times to obtain a robust average for RMSE, in order to choose the bandwidth hyperparameter for the radial basis kernel.

```
X <- as.matrix(df$cumulative_week)
X <- scale(X)
y <- df$n</pre>
```

```
# Candidate values for the bandwidth of the radial basis function
bandwidth <- c(0.1, 1, 5, 10, 100)
# Initisalise vector of RMSE</pre>
```

```
rmse_vec <- c()
# Conduct a grid search with 5-fold CV
for (i in 1:length(bandwidth)){
  kr = KernelRidge$new("rbf", lambda = 0.001, bandwidth[i])
  cv_results <- kfold_cv(kr, X, y, metrics, k = 5, n_reps = 5,</pre>
                          parallel = TRUE, n_threads = 5)
  mean_rmse <- mean(cv_results$rmse)</pre>
  rmse_vec <- c(rmse_vec, mean_rmse)</pre>
  # If mean RMSE is better than for the last best model clone and treat as best
  if (mean_rmse == min(rmse_vec)){
    # Clone the model and save
    kr_best <- kr$clone(deep = TRUE)</pre>
    # Update the best results
    cv_results_best <- cv_results</pre>
  }
}
# Save as data frame and plot results
rbf_results <- data.frame(bandwidth, rmse = rmse_vec)</pre>
bandwidth_plot <- ggplot(rbf_results) +</pre>
  geom_line(aes(x = bandwidth, y = rmse)) +
  scale_x_log10() +
  scale_y_log10() +
  xlab("Bandwidth") + ylab("RMSE")
bandwidth_plot
```



We find that a bandwidth parameter value of 5 provided the lowest RMSE value. We can look at the results for the 5 repeats of 5-fold cross-validation for this model:

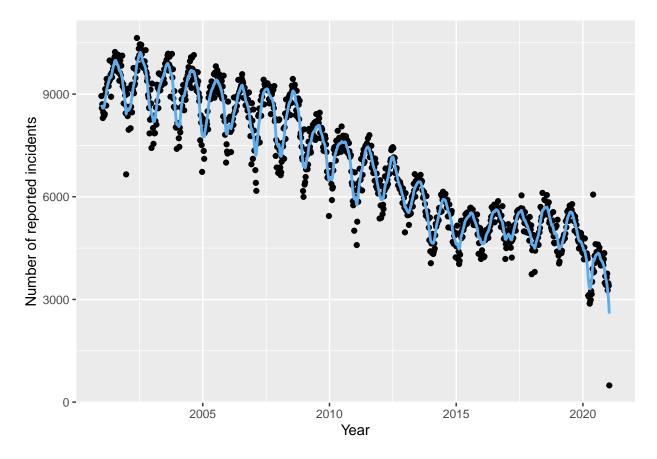
```
tab <- xtable::xtable(as_tibble(cv_results_best), digits = 4)
print(tab, type = "latex", comment = FALSE)</pre>
```

The model performs very well, explaining 96.38 % of the variance on average.

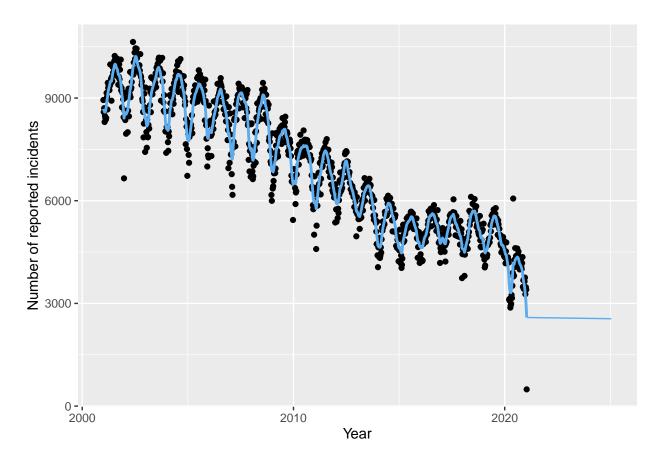
As this is single-dimensional, we can plot the prediction function for the model.

	rmse	r2
1	353.3775	0.9627
2	347.7463	0.9640
3	351.1616	0.9635
4	346.9327	0.9646
5	348.7730	0.9642

```
# Fit the final kernel ridge regression model
kr_best$fit(X, y)
# Obtain predictions on the dataset
y_hat <- kr_best$predict(X)
# Plot predictions
df$y_hat <- y_hat
week_plot <- ggplot(df) +
    geom_point(aes(x = week_start, y = n)) +
    geom_line(aes(x = week_start, y = y_hat), colour = "steelblue2", size = 1) +
    labs(x = "Year", y = "Number of reported incidents")
week_plot</pre>
```



The plot suggests a cyclic pattern over years, so naturally we proceed to consider using a trigonometric transformation of the data (taking year as the period), in the hope that we can capture this periodicity with a simpler model. Note that, whilst kernel ridge regression is useful for interpolation, this model with a radial basis kernel actually has limited utility for forecasting reported crime counts into the future. We illustrate this point by attempting to extrapolate from this model.



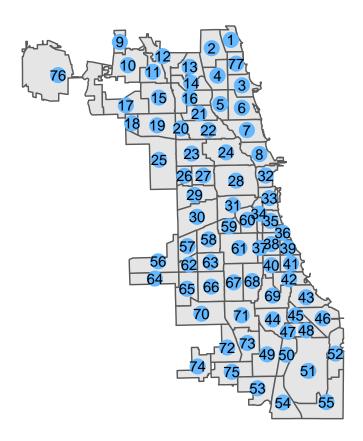
The cycles are captured solely due to being able to interpolate locally between points. When extrapolating with a radial basis function kernel, no cycles are predicted, so the out-of-sample accuracy drops substantially. The cross-validation error found is only applicable if the new data followed the same distribution, and this is simply not the case when considering future data.

#### 4.2.2 Monthly Predictions with a Spatial Component

The previous example aggregated counts of reported crime over weeks, and as such used only a single-dimensional feature vector. We look at extending this analysis by aggregating over an additional spatial component. In the ensuing analysis, we consider predicting the reported crime counts over a month, aggregated over the community areas.

The positions of the community areas will be represented by the coordinates of their centroids, which are extracted from their shapefiles. These shapefiles are included in the package for ease.

```
data("community_bounds")
centroids <- community_bounds %>%
    arrange(as.integer(area_numbe)) %>%
    st_centroid() %>%
    st_coordinates() %>%
    as_tibble() %>%
    mutate(community_area = 1:nrow(.))
# Plot the locations of centroids on map
centroids_plot <- ggplot() +
    geom_sf(data = community_bounds) +
    geom_point(data = centroids, aes(X, Y), size = 5, colour = "steelblue1") +
    geom_text(data = centroids, aes(X, Y, label = community_area)) +
    theme_void()
centroids_plot</pre>
```



We shall consider data from the years 2016 to 2020.

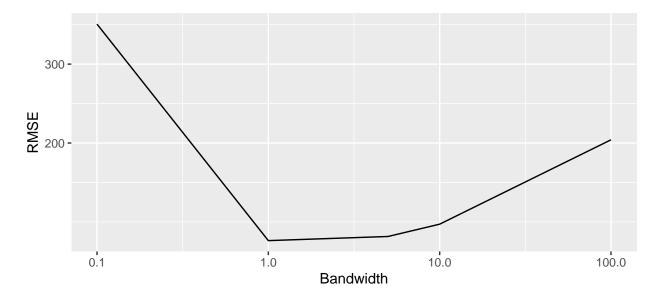
```
df <- load_data(c(2016, 2020), strings_as_factors = FALSE, na_omit = TRUE)

df %<>% select(date, community_area) %>%
   mutate(date = date(date), year = year(date), month = month(date)) %>%
   group_by(year, month) %>%
   mutate(date = min(date)) %>%
   group_by_all() %>%
   summarise(n = n()) %>%
   left_join(centroids, by = "community_area")
```

In order to choose a suitable bandwidth parameter for the radial basis function, we again perform repeated 5-fold cross-validation.

```
# Obtain data matrix for fitting the model
X <- df %>% ungroup() %>%
   select(-community_area, -date, -n) %>%
   as.matrix()
# Scale the parameters
X <- scale(X)
y <- df$n</pre>
```

```
# Bandwidth candidates
bandwidth \leftarrow c(0.1, 1, 5, 10, 100)
# Initialise vector for storing RMSE values
rmse_vec <- c()
# Set new seed for reproduciblility
set.seed(3)
for (i in 1:length(bandwidth)){
  kr <- KernelRidge$new("rbf", lambda = 0.001, bandwidth[i])</pre>
  cv_results <- kfold_cv(kr, X, y, metrics, k = 5, n_reps = 5,</pre>
                           parallel = TRUE, n_threads = 5)
  mean_rmse <- mean(cv_results$rmse)</pre>
  rmse_vec <- c(rmse_vec, mean_rmse)</pre>
  # Save best model
  if (mean_rmse == min(rmse_vec)){
    kr_best <- kr$clone(deep=TRUE)</pre>
    cv_results_best <- cv_results</pre>
  }
}
# Store as data frame and plot
rbf_results <- data.frame(bandwidth, rmse = rmse_vec)</pre>
band_plot <- ggplot(rbf_results) +</pre>
  geom_line(aes(x = bandwidth, y = rmse)) +
  scale_x_log10() +
  scale_y_log10()
band_plot
```



We obtain an optimal value of 1 which minimises the mean square error. Again, we can look at the results for the three repeats of 5-fold cross-validation for this model:

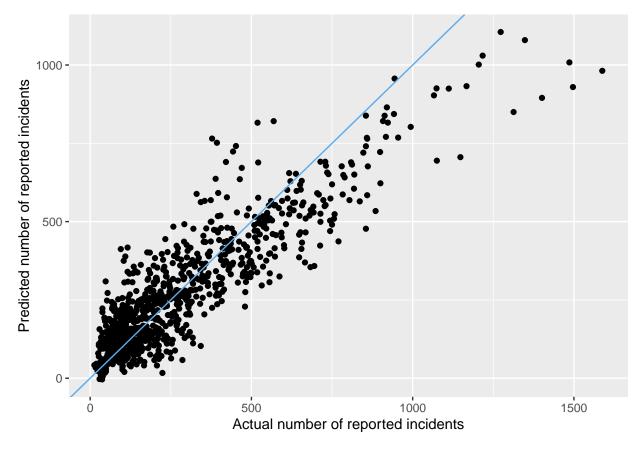
```
tab <- xtable::xtable(as_tibble(cv_results_best))
print(tab, type = "latex", comment = FALSE)</pre>
```

	rmse	r2
1	122.86	0.75
2	120.33	0.76
3	119.14	0.77
4	122.10	0.75
5	121.17	0.76

On average, this model explained 75.73% of the variance. Note the lower  $R^2$  value: in contrast to the weekly model, observations were not averaged over the whole of Chicago.

We can plot the predicted values against the observed values on a held out data set to observe the predictive power of the model:

```
scale_y_continuous(breaks = seq(0, 2000, by = 500))
pred_plot
```



The plot illustrates strong predictive power, particularly when the number of reported incidents is smaller. We do note the drop-off at the higher end of actual reported incidents, suggesting the model tends to underpredict in these cases. This is to be expected somewhat, as extremely high counts are rare and the model has not been trained on a dataset containing such high counts.

We conclude this section by noting that kernel ridge regression can provide prediction functions that explain a high proportion of the variance. However, a major limitation of this method in our case is that it would be primarily be useful for interpolation, rather than extrapolation, for the reasons outlined above.

In the subsequent section, we explore generalised additive models, which form a more principled approach for forecasting the number of crimes.

#### 4.3 Generalised Additive Models

Our R6 class PoissonGAM is a wrapper

A little about PoissonGAM and mgcv.

For the training data we will use historical data between 2015 and 2018. We will then predict on the data from 2019 to test the model.

```
# Downoad training data
df_train <- load_data(c(2015, 2018), strings_as_factors = TRUE)
# Download test data
df_test <- load_data(2019, strings_as_factors = TRUE)</pre>
```

#### 4.3.1 Daily Predictions

As each row in the datasets represent a single reported crime incident, we need to sum the number of rows for each day in order to get the number of reported crimes for each day. We use **count** from **dplyr** to achieve this

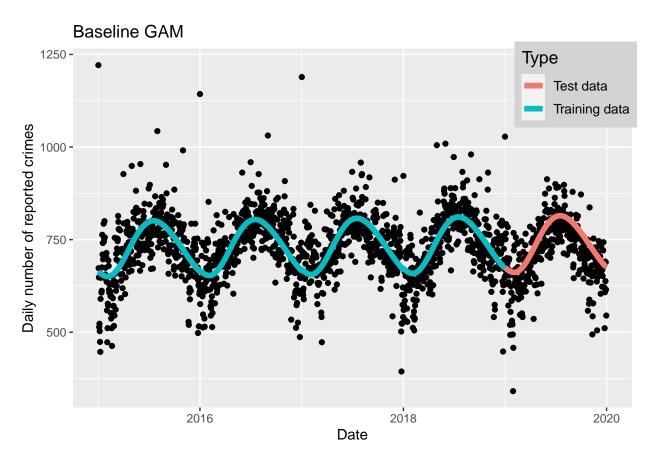
```
count_train <- gam_train %>% count(yday, year, date) %>% arrange(year, yday)
count_test <- gam_test %>% count(yday, year, date) %>% arrange(year, yday)
print(as.data.frame(head(count_train)))
```

```
## yday year date n
## 1 1 2015 2015-01-01 1221
## 2 2 2015 2015-01-02 673
## 3 3 2015 2015-01-03 648
## 4 4 2015 2015-01-04 514
## 5 5 2015 2015-01-05 523
## 6 6 2015 2015-01-06 503
```

We separate this dataset into a training set and a test set, and proceed to fit our baseline GAM which has the year and day of the year as predictors. We use a cyclic cubic smoother for the day of the year.

```
# Convert data to matrix and vector format for model training
X_train <- count_train %>% select(-n)
y_train <- count_train$n</pre>
```

```
X_test <- count_test %>% select(-n)
y_test <- count_test$n</pre>
# Fit the baseline GAM
gam1 <- PoissonGAM$new(time_period = "yday", region = NULL, crime_type = NULL,</pre>
                      include_nb = FALSE, include_year = TRUE)
gam1$fit(X = X_train, y = y_train, n_threads = 3)
gam1$fit summary
##
## Family: poisson
## Link function: log
##
## Formula:
## n ~ s(as.numeric(yday), bs = "cc") + as.numeric(year)
## Parametric coefficients:
                      Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                    -1.9118027 1.7432595 -1.097
                                                     0.273
## as.numeric(year) 0.0042184 0.0008645
                                           4.880 1.06e-06 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Approximate significance of smooth terms:
                        edf Ref.df Chi.sq p-value
                                8 5605 <2e-16 ***
## s(as.numeric(yday)) 5.74
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## R-sq.(adj) = 0.382 Deviance explained = 38.2\%
## UBRE = 5.3153 Scale est. = 1 n = 1461
pred <- gam1$predict(X = bind_rows(X_train, X_test))</pre>
# Store type of each data
count_train$Type <- "Training data"</pre>
count_test$Type <- "Test data"</pre>
all_dat <- bind_rows(count_train, count_test)</pre>
all_dat$Type <- as.factor(all_dat$Type)</pre>
# Create plot for baseline model
base_gam_plot <- ggplot(all_dat) +</pre>
  geom point(aes(date, n)) +
  xlab("Date") + ylab("Daily number of reported crimes") +
  geom_line(aes(date, pred, colour = Type), size = 2) +
  ggtitle("Baseline GAM") +
 theme(legend.position = c(0.9, 0.9),
        legend.background = element_rect(fill = "lightgrey", size = 0.5,
                                         linetype = "solid"),
        legend.title = element_text(size = 13),
        legend.text = element_text(size = 10))
base_gam_plot
```



```
# Obtain metrics on test data
pred_test <- gam1$predict(X = X_test)
# Initialise vectors for RMSE and R squared values
rmse <- c()
rsq <- c()
rmse[1] <- rmse_loss(pred_test, y_test)
rsq[1] <- r_squared(pred_test, y_test)</pre>
```

#### 4.3.2 Feature creation

There are several features that may be of interest, whether a day is a weekend or not, the number of crimes over the previous month, the number of crimes on the same day of the previous year.

We first summarise the dates on which the most and fewest crimes are reported, to gain some idea as to what factors might be influential.

```
most_crimes <- count_train %>% arrange(by = desc(n))
most_crimes$date <- as.character(most_crimes$date)

tab <- xtable::xtable(head(most_crimes[, -5]), )
print(tab, type = "latex", comment = FALSE)</pre>
```

	yday	year	date	n
1	1	2015	2015-01-01	1221
2	1	2017	2017-01-01	1189
3	1	2016	2016-01-01	1143
4	213	2015	2015-08-01	1043
5	245	2016	2016-09-01	1031
6	152	2018	2018-06-01	1009

```
least_crimes <- count_train %>% arrange(by = n)
least_crimes$date <- as.character(least_crimes$date)</pre>
```

```
tab <- xtable::xtable(head(least_crimes[, -5]), )
print(tab, type = "latex", comment = FALSE)</pre>
```

	yday	year	date	n
1	359	2017	2017-12-25	394
2	8	2015	2015-01-08	447
3	359	2018	2018-12-25	448
4	50	2015	2015-02-19	463
5	33	2015	2015-02-02	473
6	73	2017	2017-03-14	473

```
# Add features to training data
count_train_new <- count_train %>%
  mutate(week = week(date), month = month(date)) %>%
  add_prev_day() %>% add_dow() %>% add_is_fom() %>%
  add_is_christmas() %>% add_is_nyd()

# Add features to test data
count_test_new <- count_test %>%
  mutate(week = week(date), month = month(date)) %>%
  add_prev_day() %>% add_dow() %>% add_is_fom() %>%
  add_is_christmas() %>% add_is_nyd()

count_full <- bind_rows(count_train_new, count_test_new)</pre>
```

```
data_2014 <- load_data(2014, strings_as_factors = TRUE)
```

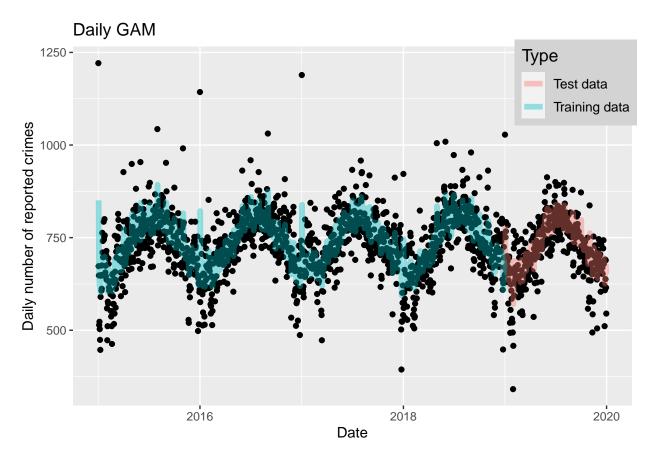
```
data_2014 <- data_2014 %>%
  convert_dates(exclude = "hour") %>%
  count(year, date) %>%
  arrange(year)

# Fill in previous year manually
count_train_new[1, "n_pre"] <- data_2014[data_2014$date == "2014-12-31", "n"][1,]
count_test_new[1, "n_pre"] <- count_train_new[count_train_new$date == "2018-12-31", "n"]
print(as.data.frame(head(count_train_new)))</pre>
```

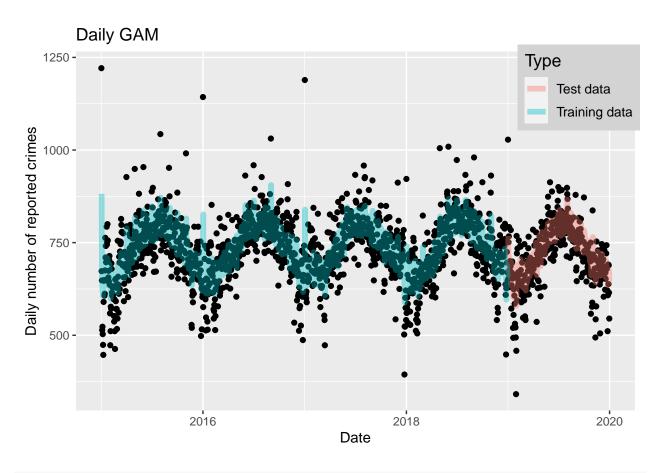
```
yday year
                                   Type week month n_pre dow is_fom
##
                  date
                         n
## 1 1 2015 2015-01-01 1221 Training data
                                        1
                                               1 585
                                                            TRUE
      2 2015 2015-01-02 673 Training data
                                               1 1221
                                                        6 FALSE
                                          1
                                        1
## 3 3 2015 2015-01-03 648 Training data
                                                  673 7 FALSE
```

```
4 2015 2015-01-04 514 Training data
                                           1
                                                   1
                                                       648
                                                             1 FALSE
## 5
       5 2015 2015-01-05 523 Training data
                                                   1
                                                       514
                                                             2 FALSE
                                             1
       6 2015 2015-01-06 503 Training data
                                                             3 FALSE
## 6
                                                       523
    is_christmas is_nyd
##
## 1
           FALSE TRUE
## 2
           FALSE FALSE
## 3
           FALSE FALSE
           FALSE FALSE
## 4
## 5
           FALSE FALSE
## 6
           FALSE FALSE
```

As PoissonGAM doesn't currently have functionality to support additional custom features, here we fit the GAM directly using gam from mgcv.

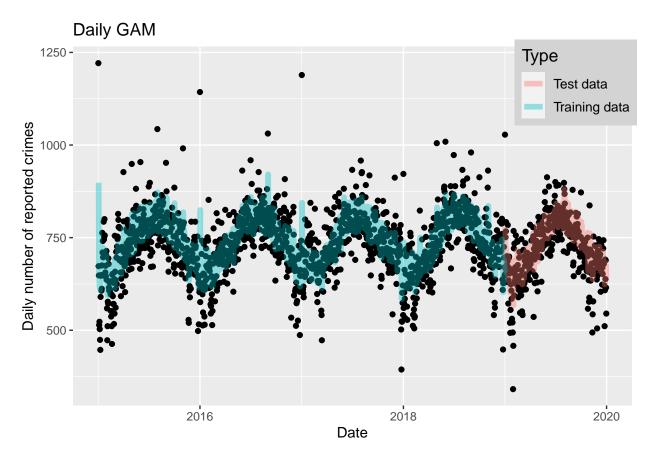


```
# Obtain metrics on test data
gam2_test <- predict(gam2, type = "response", newdata = count_test_new)
rmse[2] <- rmse_loss(gam2_test, count_test_new$n)
rsq[2] <- r_squared(gam2_test, count_test_new$n)</pre>
```



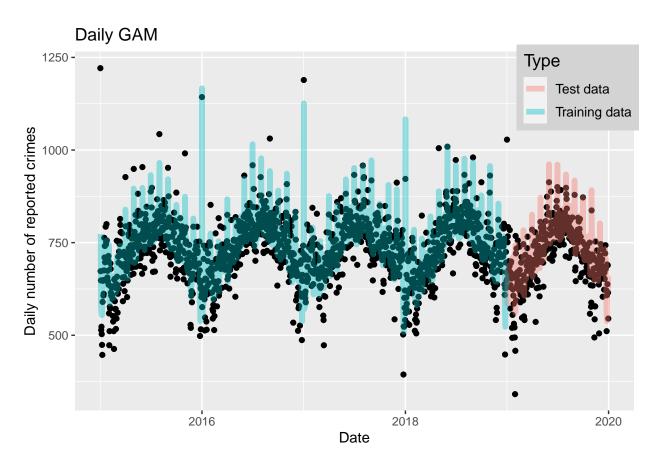
```
# Obtain metrics on test data
gam3_test <- predict(gam3, type = "response", newdata = count_test_new)
rmse[3] <- rmse_loss(gam3_test, count_test_new$n)
rsq[3] <- r_squared(gam3_test, count_test_new$n)</pre>
```

```
# Fit GAM
gam4 <- gam(n ~ s(as.numeric(yday), bs = "cc") +</pre>
              as.factor(dow) + n_pre,
            data = count_train_new, family = "poisson")
# Predict on entire dataset
gam4_pred <- predict(gam4, type = "response", newdata = count_full)</pre>
# Plot predictions
gam4_plot <- ggplot(all_dat) +</pre>
 geom_point(aes(date, n)) +
 xlab("Date") + ylab("Daily number of reported crimes") +
 geom_line(aes(date, gam4_pred, colour = Type), size = 2, alpha = 0.4) +
 ggtitle("Daily GAM") +
  theme(legend.position = c(0.9, 0.9),
        legend.background = element_rect(fill = "lightgrey", size = 0.5,
                                          linetype = "solid"),
        legend.title = element_text(size = 13),
        legend.text = element_text(size = 10))
gam4_plot
```



```
# Obtain metrics on test data
gam4_test <- predict(gam4, type = "response", newdata = count_test_new)
rmse[4] <- rmse_loss(gam4_test, count_test_new$n)
rsq[4] <- r_squared(gam4_test, count_test_new$n)</pre>
```

```
gam5 <- gam(n ~ s(as.numeric(yday), bs = "cc") + as.factor(dow) + n_pre +
              is_fom + is_christmas + is_nyd + as.factor(week),
            data = count_train_new, family = "poisson")
# Predict on entire dataset
gam5_pred <- predict(gam5, type = "response", newdata = count_full)</pre>
# Plot predictions
gam5_plot <- ggplot(all_dat) +</pre>
  geom_point(aes(date, n)) +
  xlab("Date") + ylab("Daily number of reported crimes") +
  geom_line(aes(date, gam5_pred, colour = Type), size = 2, alpha = 0.4) +
 ggtitle("Daily GAM") +
  theme(legend.position = c(0.9, 0.9),
        legend.background = element_rect(fill = "lightgrey", size = 0.5,
                                          linetype = "solid"),
        legend.title = element_text(size = 13),
        legend.text = element_text(size = 10))
gam5_plot
```



```
# Obtain metrics on test data
gam5_test <- predict(gam5, type = "response", newdata = count_test_new)
rmse[5] <- rmse_loss(gam5_test, count_test_new$n)
rsq[5] <- r_squared(gam5_test, count_test_new$n)
gam_metrics <- data.frame(RMSE = rmse, R2 = rsq)

tab <- xtable::xtable(gam_metrics)
print(tab, type = "latex", comment = FALSE)</pre>
```

	RMSE	R2
1	68.72	0.45
2	61.65	0.50
3	59.30	0.54
4	58.49	0.55
_5_	55.04	0.61

#### 4.3.3 Adding Spatial Data

```
# Construct training data set
spatial_train <- gam_train %>%
  get_count_data(time_period = "month", region = "community_area")
# Construct test data set
```

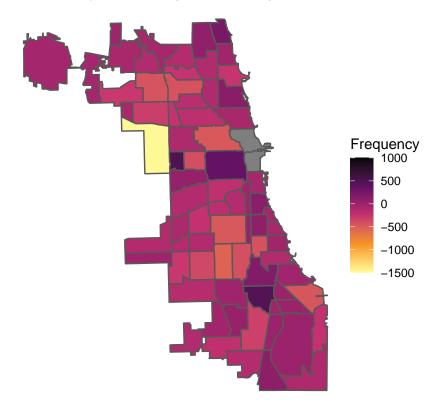
```
spatial_test <- gam_test %>%
  get_count_data(time_period = "month", region = "community_area")
# Split into data matrix and reponse vector
X_train <- spatial_train %>% select(-n)
y_train <- spatial_train$n</pre>
X_test <- spatial_test %>% select(-n)
metrics <- list(rmse = rmse_loss, r2 = r_squared)</pre>
# Initialise PoissonGAM object
mgam <- PoissonGAM$new(time_period = "month", region = "community_area",</pre>
                       crime_type = NULL, include_nb = TRUE)
# Find CV error for given metrics
mgam_results <- kfold_cv(mgam, X = X_train, y = y_train,</pre>
                           error_funcs = metrics, k = 5, n_reps = 5,
                           parallel = TRUE, n_threads = 5)
names(mgam_results) <- c("RMSE", "R2")</pre>
tab <- xtable::xtable(as_tibble(mgam_results), digits = 3)</pre>
print(tab, type = "latex", comment = FALSE)
                                            RMSE
                                                      R2
                                        1 40.991 0.974
                                        2 \quad 40.795 \quad 0.974
                                        3 \quad 40.599 \quad 0.974
                                        4 \quad 41.220 \quad 0.974
                                        5 \quad 40.934 \quad 0.974
# Re-fit model
mgam$fit(X_train, y_train, n_threads = 7)
```

```
# Summary of the fit
mgam$fit_summary
```

```
## Family: poisson
## Link function: log
##
## Formula:
## n ~ s(as.numeric(month), bs = "cc") + s(community_area, bs = "mrf",
##
      xt = list(nb = self$nb_list))
##
## Parametric coefficients:
              Estimate Std. Error z value Pr(>|z|)
## (Intercept) 5.313327 0.001396 3806 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Approximate significance of smooth terms:
                         edf Ref.df Chi.sq p-value
## s(as.numeric(month)) 7.974
                                8 7145 <2e-16 ***
```

	RMSE	R2
1	38.83	0.98

## Residuals produced by Community Area



#### 4.3.4 Adding Categorical Data

```
tab <- xtable::xtable(as_tibble(mgam_fbi_results), digits = 4)
print(tab, type = "latex", comment = FALSE)</pre>
```

	RMSE	R2
1	16.8159	0.7177
2	16.8304	0.7167
3	16.8168	0.7166
4	16.8706	0.7156
5	16.8499	0.7165

```
# Fit full model
mgam_com_fbi$fit(X_train, y_train, n_threads = 7)
```

```
spatial_fbi_test$predicted <- mgam_com_fbi$predict(X = X_test)</pre>
```

```
# Compute evaluation metrics
rmse <- rmse_loss(spatial_fbi_test$n, spatial_fbi_test$predicted)
rsq <- r_squared(spatial_fbi_test$n, spatial_fbi_test$predicted)
tab <- xtable::xtable(data.frame("RMSE" = rmse, "R2" = rsq))
print(tab, type = "latex", comment = FALSE)</pre>
```

	RMSE	R2
1	17.63	0.70

# Residuals produced by Community Area

