# Compass TB1 Group Project: Lab Notebook

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25/01/2021

### Introduction

In this lab notebook we present the analyses undertaken as part of the Compass TB1 group project. We focus on a large, open source dataset provided by the City of Chicago consisting of reported incidents of crime from 2001 to present day, as reported by the Chicago Police Department. The dataset can be obtained from the website https://data.cityofchicago.org/Public-Safety/Crimes-2001-to-Present/jjzp-q8t2.

The notebook will be broken up into three sections:

- 1. Workflow and Computational Techniques: A summary of the approach used in the development of the **chigcrim** package.
- 2. Classification: Predicting whether a reported crime led to the arrest of a suspect. We consider three different discriminative classifiers: logistic regression, support vector machines, and random forests.
- 3. Prediction: Predicting the number of reported crimes which occur in a given region over a specified time period (of a given type, if desired), through interpolation. We consider kernel ridge regression and generalised additive models (GAMs).

## Workflow and Computational Techniques

In the development of the package for this project, we utilised many computational techniques, that are outlined below.

#### **Object-Oriented Programming**

We decided to use an object oriented approach to constructing models. Specifically, we made use of the R6Class from the R6 package. R6 objects are mutable and use an object oriented approach similar to most programming languages (unlike the more basic S3 and S4 classes). R6 classes are very similar to reference classes, although generally R6 classes are preferred. This is for a variety of reasons, including the fact that R6 classes are much faster, and they handle fields in a neater way by putting them in a separate environment. More information on this can be found here. When building models, a model could be fitted using model\$fit(X, y), and predictions made with model\$predict(X). It is worth noting that this use of fit and predict methods in object-oriented machine learning packages is used elsewhere, particularly in the Python package scikit-learn. The key advantage of this approach is that it abstracts away the underlying complexities, and creates a consistent structure that makes it easier to compare different models.

#### Parallel Programming

Parallel programming was used to speed up slow code, utilising the package **doParallel** which calls the packages **parallel** and **foreach**. In particular, we implemented a parallel cross-validation function kfold\_cv, which facilitated more accurate and faster assessment of model performance.

#### Documentation

In order to document functions in the package, we made use of **roxygen2**. This package automatically creates the .Rd documentation files for functions (or classes), from comments added above the function definitions. As well as being efficient, this allows the code and documentation to coexist, meaning it is easier to remember to update the documentation.

### **API Querying**

The Chicago Crime dataset is updated on a daily basis and, at the time of writing, contains over 7 million rows of data. For each reported incident, a total of 22 features are recorded (for a full list of features and their descriptions see the City of Chicago website). We elected not to download the dataset in full and include this in the package as it would consume a significant amount of storage, and quickly become out of date. Instead, we utilised the **RSocrata** package which allows easy interaction with the online open data portal. The wrapper load\_data allows the end user to directly download the dataset into the R environment, via the function read.socrata. load\_data provides functionality for filtering by year, limiting the number of data points received, and omitting missing/NA values.

### Testing and Continuous Integration

For tests, we used the **testthat** package. This simply creates a new directory ./tests/testthat/ in which the user can define tests for the package functions. Although the tests can be run alone, generally, we made use of the package rcmdcheck. This contains the function rcmdcheck, which not only runs the tests, but also carries out a more sophisticated check. Some examples of what is checked are listed below:

- Checks the package installs correctly.
- Checks for missing documentation.
- Automatically runs examples in documentation, to check they run successfully.
- Checks for undefined variables.
- Checks for missing dependencies.

In order to make sure that tests and checks were run on a regular basis, continuous integration was set up using github actions. This runs rcmdcheck() for each pull request and push to the main branch. This limits the possibility of unintentionally introducing breaking changes.

### Classification

```
# Load required packages
library(chigcrim)

## Warning: replacing previous import 'magrittr::set_names' by 'rlang::set_names'
## when loading 'chigcrim'

# Use seed to ensure reproducibility
set.seed(1)
```

In this section we consider the binary classification task of predicting whether a suspect is arrested, given data on the reported crime. Three models will be investigated: logistic regression, support vector machines and random forest classifiers.

### **Assessing Performance**

To assess performance, three metrics will be used: the overall accuracy, the sensitivity and the specificity. These are defined as follows:

- Overall accuracy: The proportion of correct predictions.
- Sensitivity: The proportion of positive observations correctly predicted.
- Specificity: The proportion of negative observations correctly predicted.

These metrics can be computed using the functions classification\_accuracy, classification\_sensitivity, and classification\_specifity, respectively, from the **chigcrim** package.

Note that as logistic regression is a probabilistic classifier whereas support vector machines and random forests are not. As such, the output from logistic regression is a probability in [0, 1]. In our analysis, these probabilities are rounded to yield predictions that can be assessed with the metrics above to facilitate the comparison with the results of the other two classifiers.

For each classifier, we will use repeated k-fold cross validation to obtain mean values of the metrics. Specifically, 5-fold cross validation is repeated five times (run in parallel using the function  $kfold_cv$ ), and the metrics are averaged across the folds and repeats.

#### Feature selection

## 3 11552596

## 4 11552605

## 5 11552609

Due to the time and computational limitations involved, we shall train the models on a subset of the data from the year 2019.

```
# Load 2019 data to build classification models
df <- load_data(year = 2019, strings_as_factors = FALSE)

print(as.data.frame(head(df)))

## id case_number date block iucr
## 1 11552577 JC100040 2019-01-01 00:31:00 032XX W LAWRENCE AVE 1310
## 2 11552587 JC100034 2019-01-01 00:05:00 006XX E 83RD PL 1310</pre>
```

001XX W HURON ST 0430

004XX N MONTICELLO AVE 143A

JC100045 2019-01-01 00:03:00

JC100030 2019-01-01 00:01:00

JC100028 2019-01-01 00:05:00 013XX S CENTRAL PARK AVE 0486

```
## 6 11552610
                 JC100044 2019-01-01 00:02:00
                                                         031XX W 25TH ST 1310
##
                                           description location_description arrest
          primary_type
       CRIMINAL DAMAGE
## 1
                                           TO PROPERTY
                                                                 RESTAURANT
## 2
       CRIMINAL DAMAGE
                                           TO PROPERTY
                                                                   RESIDENCE FALSE
## 3
               BATTERY AGGRAVATED: OTHER DANG WEAPON
                                                                HOTEL/MOTEL
                                                                              FALSE
## 4 WEAPONS VIOLATION
                             UNLAWFUL POSS OF HANDGUN
                                                                       ALLEY
                                                                               TRUE
                              DOMESTIC BATTERY SIMPLE
## 5
               BATTERY
                                                                   APARTMENT
                                                                             FALSE
## 6
       CRIMINAL DAMAGE
                                           TO PROPERTY
                                                                   RESIDENCE FALSE
##
     domestic beat district ward community_area fbi_code x_coordinate y_coordinate
## 1
        FALSE 1713
                          17
                               33
                                               14
                                                        14
                                                                 1153943
                                                                              1931709
## 2
        FALSE 632
                           6
                                6
                                               44
                                                        14
                                                                 1182085
                                                                              1849762
        FALSE 1832
                          18
                               42
                                                8
                                                       04B
                                                                 1175159
## 3
                                                                              1905043
## 4
        FALSE 1122
                          11
                               27
                                               23
                                                        15
                                                                 1151958
                                                                              1902815
## 5
                                                                              1893426
         TRUE 1011
                          10
                               24
                                               29
                                                       08B
                                                                 1152589
## 6
        FALSE 1033
                          10
                                                        14
                                                                 1155950
                                                                              1887234
                               12
                                               30
##
                   updated_on latitude longitude
     year
## 1 2019 2019-01-10 15:16:50 41.96844 -87.70934
## 2 2019 2019-01-10 15:16:50 41.74297 -87.60841
## 3 2019 2019-01-10 15:16:50 41.89482 -87.63213
## 4 2019 2019-01-10 15:16:50 41.88920 -87.71740
## 5 2019 2019-01-10 15:16:50 41.86342 -87.71533
## 6 2019 2019-01-10 15:16:50 41.84636 -87.70316
```

Below we outline our feature selection and data pre-processing choices. These decisions involved incorporating information from conducting exploratory data analysis (EDA), as well as considering what is computationally feasible.

- Encode the date as the day of the year (an integer between 1-365, or 1-366 for leap years).
- Encode time of day as a floating point in 0-24, as this showed promising results in our EDA.
- Drop year as we are only using data from 2019.
- Drop id as this is the unique key for each data point.
- We drop case\_number, as the values are almost all unique and are not informative.
- Drop primary\_type, description and iucr code. Keep fbi\_code as an indicator of crime type.
- Drop updated\_on as this only refers to when the data was last updated and is uninformative.
- Drop latitude and longitude, and keepx\_coordinate and y\_coordinate. Note that these coordinates likely not particularly useful for linear classifiers, but should be useful for non-linear methods.
- Keep community\_area, but other areas (district, beat, ward and block) are dropped.
- Omit all NA values.
- Particularly rare factors will be grouped into a variable other (see ?otherise).

```
# Convert rarely used fbi categories to "OTHER"

df$fbi_code <- otherise(df$fbi_code, 500)

## 7 out of 26 categories were converted to OTHER corresponding to 0.51%

## of observations.

df$location_description <- otherise(df$location_description, 1000)

## 126 out of 155 categories were converted to OTHER corresponding to 10.82%

## of observations.</pre>
```

```
# List of features for removal
remove_features <- c("id", "year", "case_number", "primary_type", "description",</pre>
                     "iucr", "updated on", "latitude", "longitude",
                     "date", "district", "beat", "ward", "block")
# Add more time features, remove missing values and convert columns to factor
df %<>% mutate(day = yday(df$date),
               time = hour(df$date) + minute(df$date) / 60) %>%
  select(-all of(remove features)) %>%
  filter(complete.cases(df)) %>%
  mutate(location_description = as.factor(location_description),
         fbi_code = as.factor(fbi_code),
         community_area = as.factor(community_area))
print(as.data.frame(head(df)))
     location_description arrest domestic community_area fbi_code x_coordinate
## 1
              RESTAURANT FALSE
                                    FALSE
                                                      14
                                                               14
                                                                       1153943
## 2
               RESIDENCE FALSE
                                    FALSE
                                                      44
                                                               14
                                                                       1182085
## 3
             HOTEL/MOTEL FALSE
                                                      8
                                                              04B
                                    FALSE
                                                                       1175159
## 4
                    ALLEY
                           TRUE
                                    FALSE
                                                      23
                                                               15
                                                                       1151958
## 5
               APARTMENT FALSE
                                    TRUE
                                                      29
                                                              08B
                                                                       1152589
## 6
               RESIDENCE FALSE
                                    FALSE
                                                      30
                                                               14
                                                                       1155950
    y_coordinate day
## 1
         1931709
                    1 0.51666667
## 2
          1849762 1 0.08333333
## 3
          1905043 1 0.05000000
## 4
         1902815 1 0.01666667
## 5
          1893426 1 0.08333333
## 6
          1887234 1 0.03333333
```

#### Logistic Regression

We will first consider a logistic regression classifier, which is a linear classifier for binary data. We use our R6 class LogisticRegression which has methods fit and predict. fit calls the function optim() internally to minimize the cross-entropy/log-loss function using gradient-based optimisation methods (either BFGS, L-BFGS-B or CG); in our analysis we use BFGS as we don't run into memory issues.

```
## % latex table generated in R 4.0.3 by xtable 1.8-4 package
## % Sun Jan 24 23:05:38 2021
## \begin{table}[ht]
## \centering
## \begin{tabular}{rrrr}
     \hline
##
    & accuracy & sensitivity & specificity \\
##
##
     \hline
## 1 & 0.8614 & 0.4347 & 0.9788 \\
     2 & 0.8613 & 0.4351 & 0.9786 \\
##
     3 & 0.8613 & 0.4345 & 0.9787 \\
     4 & 0.8613 & 0.4341 & 0.9789 \\
##
##
     5 & 0.8612 & 0.4346 & 0.9786 \\
##
      \hline
## \end{tabular}
## \end{table}
```

### **Support Vector Machines**

As the support vector machine (SVM) allows use of a kernel function, it should be able to capture non-linear relationships in the original feature space (given an appropriate kernel). As the relationship between the features and the class is unknown, a radial basis function kernel is used. The R6 class SupportVectorMachine, again with fit and predict methods, is a wrapper of the function svm from the dedicated SVM package e1071. Unfortunately, support vector machines do not scale well to large data sets, so here we will only use 30,000 rows.

```
# Subset the data randomly
index <- sample(1:nrow(df), 30000)
X_subset <- X[index, ]
y_subset <- y[index]</pre>
```

In order to obtain optimal values for cost and gamma to be provided to svm for training the SVM, we utilise the built-in generic function tune from e1071 which performs a grid search over given parameter ranges.

```
##
## Parameter tuning of 'e1071::svm':
##
## - sampling method: 5-fold cross validation
##
## - best parameters:
## cost gamma
## 16 0.03125
```

## - best performance: 0.128

##

We obtain optimal values of 2<sup>4</sup> for cost and 2<sup>-5</sup> for gamma, which we use to train our SVM.

```
# Initialise new SupportVectorMachine object
svm <- SupportVectorMachine$new(kernel = "radial")</pre>
# Run repeated 5-fold cross-validation to evaluate performance
svm_results <- kfold_cv(svm, X_subset, y_subset, metrics, k = 5,</pre>
                        n_reps = 5, parallel = FALSE,
                         n threads = 5, gamma = 2^-5, cost = 2^4)
# Export results for use in report
tab <- xtable::xtable(as_tibble(svm_results), digits = 4)</pre>
print(tab, type = "latex")
## \% latex table generated in R 4.0.3 by xtable 1.8-4 package
## % Sun Jan 24 17:13:56 2021
## \begin{table}[ht]
## \centering
## \begin{tabular}{rrrr}
##
    \hline
  & accuracy & sensitivity & specificity \\
##
##
     \hline
## 1 & 0.8624 & 0.4076 & 0.9870 \\
     2 & 0.8627 & 0.4091 & 0.9870 \\
##
##
     3 & 0.8626 & 0.4087 & 0.9870 \\
     4 & 0.8622 & 0.4067 & 0.9870 \\
##
     5 & 0.8619 & 0.4052 & 0.9870 \\
##
##
      \hline
## \end{tabular}
## \end{table}
```

#### Random Forest

The random forest trains multiple decision trees using a subset of features to create each tree. Decision trees are an ordered set of rules defined on the feature values that attempt to split the data into classes. As decision trees have a tendency to overfit, the random forest attempts to overcome this by growing multiple trees on different features within the dataset. In the classification case, a prediction is made by predicting from each decision tree separately and finding the most common predicted class. This is a black-box method but has the potential for good predictive performance.

Our R6 class RandomForest is a wrapper for the function randomForest from the randomForest package. Due to the high computational cost involved in fitting random forest models we again use a smaller subset of the data. Here we use the same dataset used to fit the SVM, with the factor community\_area removed as the algorithm for fitting the model cannot handle such a large number of factors.

## % latex table generated in R 4.0.3 by xtable 1.8-4 package

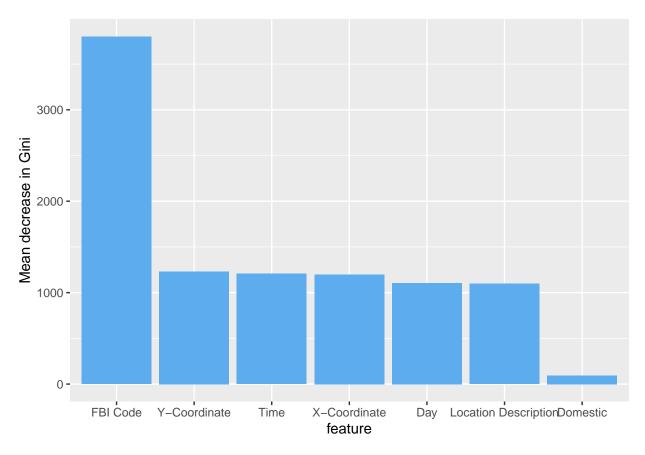
```
## % Sun Jan 24 17:13:56 2021
## \begin{table}[ht]
## \centering
## \begin{tabular}{rrrr}
##
     \hline
    & accuracy & sensitivity & specificity \\
##
##
     \hline
## 1 & 0.8762 & 0.5258 & 0.9722 \\
##
     2 & 0.8780 & 0.5293 & 0.9736 \\
##
     3 & 0.8762 & 0.5299 & 0.9712 \\
     4 & 0.8775 & 0.5293 & 0.9729 \\
     5 & 0.8761 & 0.5259 & 0.9721 \\
##
##
      \hline
## \end{tabular}
## \end{table}
```

### **Model Comparisons**

The models all performed very similarly. Unsurprisingly, the support vector machine and the random forest classifier performed better, due to their ability to capture non-linear relationships. It is worth noting that this difference is surprisingly small, although this could be related to the fact that the logistic regression model was trained on a larger dataset. Alternatively, the SVM results could suggest that encoding the community areas as factors was sufficient to capture much of the spatial aspect of the crimes in logistic regression.

Logistic regression had higher sensitivity than the support vector machine, and thus could be viewed as a preferable option if false negatives are particularly detrimental. It is worth noting however that both support vector machines and logistic regression can be adjusted to reflect unbalanced costs associated with incorrect predictions.

Being an ensemble model, the random forest unsurprisingly performed the best based on all three metrics. It is likely that the random forest could be improved by training on a larger subset of the data and optimising the hyperparameters. The downside of using a random forest is that, as a black-box method, it does not provide any inference as to how the features are used within the model. We are at least able to look at how many times each feature was chosen as a splitting point in all of the trees, providing us with some information as to the importance of each of the features.



The plot suggests that the most "important" feature is fbi\_code, which is somewhat unsurprising as this tells us what type of crime was reported. This would intuitively have a significant impact on whether the incident report led to a suspect being arrested. None of the models achieve an accuracy of more than 90%. The availability of more data, for example the demographic background of the suspect and whether they have been arrested previously, would likely allow for more accurate predictions.

### Prediction

In this section we consider the regression tesk of predicting the number of reported incidents of crime in a given region over a specified time period. We will look at a kernel ridge regression model before moving on to generalised additive models.

```
# Load required packages
library(chigcrim)
library(rgdal)
library(sf)
library(ggmap)
# Use seed to ensure reproducibility
set.seed(1)
```

### Assessing Performance

To assess performance, two metrics will be used: the root mean squared error (RMSE) and R-squared ( $R^2$ ). These are defined as follows:

- RMSE:
- R-squared:

These metrics can be computed using the functions rmse\_loss and r\_squared, respectively, from the chigcrim package.

```
# List of metrics used to evaluate regression models
metrics <- list(rmse = rmse_loss, r2 = r_squared)</pre>
```

Repeated k-fold cross validation is used, and hyperparameters are chosen based on the root mean square error metric. Specifically, we will use 5 repetitions of 5-fold cross validation at each parameter value (ran in parallel).

### Kernel Ridge Regression

The kernel ridge regression implementation includes a linear kernel (equivalent to ridge regression), a polynomial kernel, and a radial basis function kernel. As the relationship is complex and non-linear, only the radial basis function feature transform will be considered here, which implicitly induces an extremely flexible infinite dimensional feature transform.

### Weekly predictions

We first consider a simple, single-dimensional model, using only the number of crimes per week as the predictor.

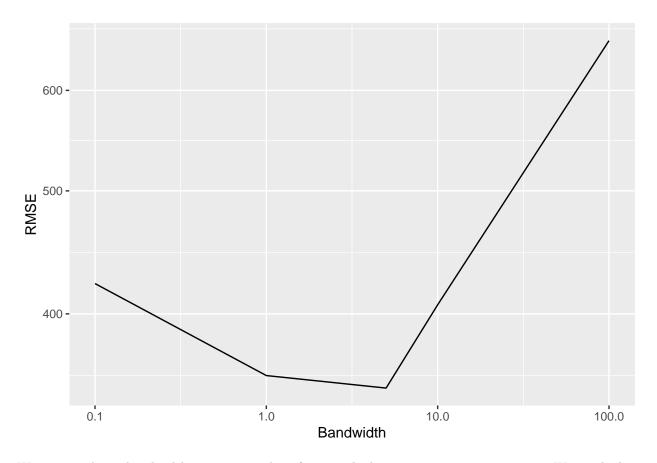
```
df <- load_data(select = "date")

df %<>%
    mutate(date = date(date), week = week(date), year = year(date)) %>%
    filter(week < 53) %>%
    group_by(week, year) %>%
    mutate(week_start = min(date)) %>%
    ungroup() %>%
    count(week, week_start, year) %>%
    arrange(year, week) %>%
    mutate(cumulative_week = 1:nrow(.))
print(as.data.frame(head(df)))
```

```
n cumulative_week
     week week_start year
## 1
       1 2001-01-01 2001 8942
## 2
        2 2001-01-08 2001 8589
                                              2
       3 2001-01-15 2001 8704
                                              3
## 3
## 4
       4 2001-01-22 2001 8300
                                              4
## 5
       5 2001-01-29 2001 8473
                                              5
       6 2001-02-05 2001 8418
```

We shall use a grid search with 5-fold cross validation to choose the bandwidth hyperparameter for the radial basis function kernel.

```
X <- as.matrix(df$cumulative_week)</pre>
X <- scale(X)</pre>
y <- df$n
# Candidate values for the bandwidth of the radial basis function
bandwidth \leftarrow c(0.1, 1, 5, 10, 100)
# Initisalise vector of RMSE
rmse_vec <- c()</pre>
# Conduct a grid search with 5-fold CV
for (i in 1:length(bandwidth)){
  kr = KernelRidge$new("rbf", lambda = 0.001, bandwidth[i])
  cv_results <- kfold_cv(kr, X, y, metrics, 5, n_reps = 5,</pre>
                           parallel = TRUE, n_threads = 5)
  mean rmse <- mean(cv results$rmse)</pre>
  rmse_vec <- c(rmse_vec, mean_rmse)</pre>
  # If mean RMSE is better than for the last best model clone and treat as best
  if (mean_rmse == min(rmse_vec)){
    # Clone the model and save
    kr best <- kr$clone(deep = TRUE)</pre>
    # Update the best results
    cv_results_best <- cv_results</pre>
}
rbf_results <- data.frame(bandwidth, rmse = rmse_vec)</pre>
bandwidth_plot <- ggplot(rbf_results) +</pre>
  geom_line(aes(x = bandwidth, y = rmse)) +
  scale_x_log10() +
  scale_y_log10() +
  xlab("Bandwidth") + ylab("RMSE")
bandwidth_plot
```



We can see that a bandwidth parameter value of 5 gave the lowest root mean square error. We can look at the results for the three repeats of 5-fold cross-validation for this model:

```
tab <- xtable::xtable(as_tibble(cv_results_best), digits = 4)</pre>
print(tab, type = "latex")
## % latex table generated in R 4.0.3 by xtable 1.8-4 package
## % Sun Jan 24 23:05:55 2021
## \begin{table}[ht]
## \centering
## \begin{tabular}{rrr}
##
     \hline
    & rmse & r2 \\
##
     \hline
##
   1 & 353.3775 & 0.9627 \\
##
     2 & 347.7463 & 0.9640 \\
##
     3 & 351.1616 & 0.9635 \\
##
     4 & 346.9327 & 0.9646 \\
##
     5 & 348.7730 & 0.9642 \\
##
##
      \hline
## \end{tabular}
## \end{table}
```

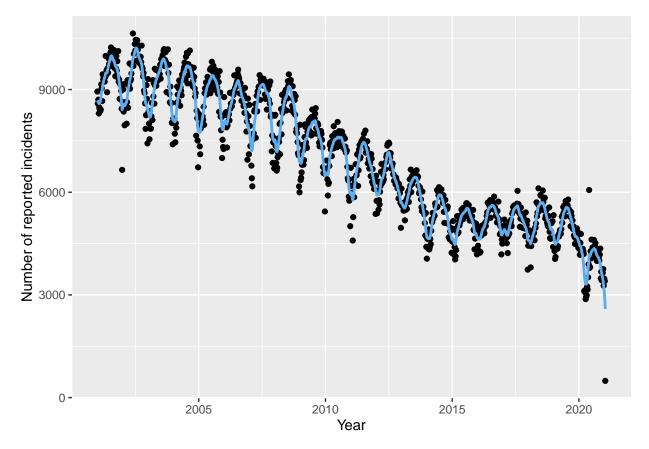
The model performs very well, explaining 96.38 % of the variance on average.

As this is single-dimensional, we can plot the prediction function for the best model.

```
# Fit the final kernel ridge regression model
kr_best$fit(X, y)
# Obtain predictions on the dataset
y_hat <- kr_best$predict(X)

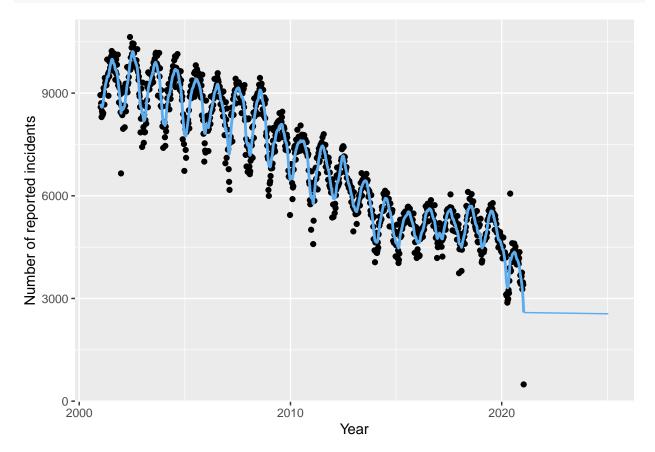
# Plot output
df$y_hat <- y_hat

week_plot <- ggplot(df) +
    geom_point(aes(x = week_start, y = n)) +
    geom_line(aes(x = week_start, y = y_hat), colour = "steelblue2", size = 1) +
    labs(x = "Year", y = "Number of reported incidents")
week_plot</pre>
```



The plot suggests a cyclic pattern over years, so naturally we proceed to consider using a trigonometric transformation of the data (taking year as the period), in the hope that we can capture this periodicity with a simpler model. Note that, whilst kernel ridge regression is useful for interpolation, this model with a radial basis kernel actually has limited utility for forecasting reported crime counts into the future. We illustrate this point by attempting to extrapolate from this model.

```
extra_X <- start_week_int:(start_week_int + length(extra_dates) - 1)
extra_X <- (extra_X - attributes(X)$`scaled:center`) /
   attributes(X)$`scaled:scale`
# Predict using our fitted model
extra_y_hat <- kr_best$predict(as.matrix(extra_X))
# Attach these values to the data frame
extra_df <- tibble(extra_dates, extra_y_hat)
week_plot + geom_line(data = extra_df, aes(extra_dates, extra_y_hat), colour = "steelblue2")</pre>
```



The cycles are captured solely due to being able to interpolate locally between points. When extrapolating with a radial basis function kernel, no cycles are predicted, so the out-of-sample accuracy drops substantially. The cross-validation error found is only applicable if the new data followed the same distribution, and this is simply not the case when considering future data.

#### Monthly Predictions with a Spatial Component

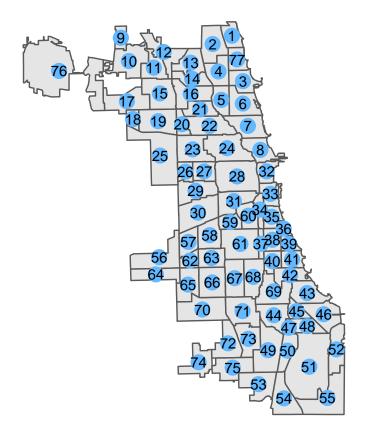
The previous example aggregated counts of reported crime over weeks, and as such used only a single-dimensional feature vector. We look at extending this analysis by aggregating over an additional spatial component. In the ensuing analysis, we consider predicting the reported crime counts over a month, aggregated over the community areas.

The positions of the community areas will be represented by the coordinates of their centroids, which are extracted from their shapefiles.

```
data("community_bounds")
centroids <- community_bounds %>%
    arrange(as.integer(area_numbe)) %>%
```

```
st_centroid() %>%
st_coordinates() %>%
as_tibble() %>%
mutate(community_area = 1:nrow(.))

centroids_plot <- ggplot() +
    geom_sf(data = community_bounds) +
    geom_point(data = centroids, aes(X, Y), size = 5, colour = "steelblue1") +
    geom_text(data = centroids, aes(X, Y, label = community_area)) +
    theme_void()
centroids_plot</pre>
```



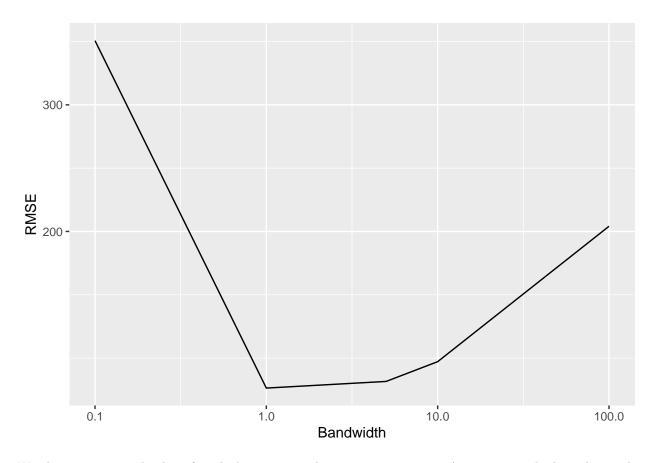
We shall consider data from the years 2016 to 2020.

```
df <- load_data(c(2016, 2020), strings_as_factors = FALSE, na_omit = TRUE)

df %<>% select(date, community_area) %>%
  mutate(date = date(date), year = year(date), month = month(date)) %>%
  group_by(year, month) %>%
  mutate(date = min(date)) %>%
  group_by_all() %>%
  summarise(n = n()) %>%
  left_join(centroids, by = "community_area")
```

In order to choose a suitable bandwidth parameter for the radial basis function, we perform repeated 5-fold cross-validation.

```
# Obtain data matrix for fitting the model
X <- df %>% ungroup() %>%
  select(-community_area, -date, -n) %>%
  as.matrix()
# Scale the parameters
X <- scale(X)</pre>
y \leftarrow df n
# Bandwidth candidates
bandwidth \leftarrow c(0.1, 1, 5, 10, 100)
rmse_vec <- c()</pre>
# Set new seed for reproduciblility
set.seed(3)
for (i in 1:length(bandwidth)){
  kr <- KernelRidge$new("rbf", lambda = 0.001, bandwidth[i])</pre>
  cv_results <- kfold_cv(kr, X, y, metrics, k = 5, n_reps = 5,</pre>
                           parallel = TRUE, n_threads = 5)
  mean_rmse <- mean(cv_results$rmse)</pre>
  rmse_vec <- c(rmse_vec, mean_rmse)</pre>
  # Save best model
  if (mean_rmse == min(rmse_vec)){
    kr_best <- kr$clone(deep=TRUE)</pre>
    cv_results_best <- cv_results</pre>
  }
}
rbf_results <- data.frame(bandwidth, rmse = rmse_vec)</pre>
band_plot <- ggplot(rbf_results) +</pre>
  geom_line(aes(x = bandwidth, y = rmse)) +
  scale_x_log10() +
  scale_y_log10()
band_plot
```

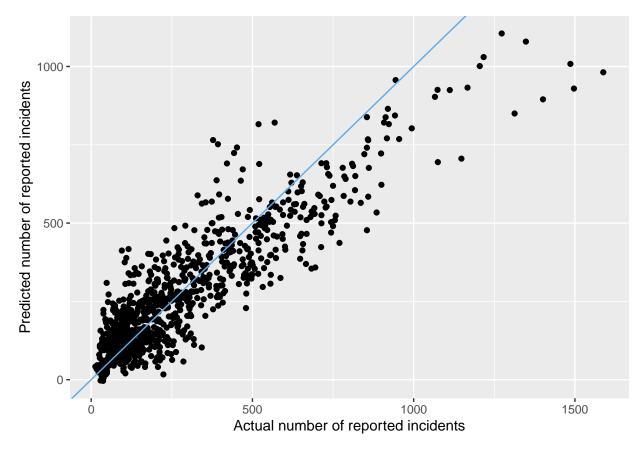


We obtain an optimal value of 1 which minimises the mean square error. Again, we can look at the results for the three repeats of 5-fold cross-validation for this model:

```
tab <- xtable::xtable(as_tibble(cv_results_best))</pre>
print(tab, type = "latex")
## % latex table generated in R 4.0.3 by xtable 1.8-4 package
## % Sun Jan 24 23:06:12 2021
## \begin{table}[ht]
## \centering
## \begin{tabular}{rrr}
##
     \hline
    & rmse & r2 \\
##
     \hline
##
   1 & 122.86 & 0.75 \\
##
     2 & 120.33 & 0.76 \\
##
     3 & 119.14 & 0.77 \\
##
     4 & 122.10 & 0.75 \\
##
     5 & 121.17 & 0.76 \\
##
##
      \hline
## \end{tabular}
## \end{table}
```

On average, this model explained 75.73% of the variance. Note the lower  $R^2$  value: in contrast to the weekly model, observations were not averaged over the whole of Chicago.

Although being higher dimensional so difficult to plot, we can plot the predicted values against the observed values on a held out data set:



The plot illustrates strong predictive power, particularly when the number of reported incidents is smaller. We do note the drop-off at the higher end of actual reported incidents, suggesting the model tends to under-predict in these cases. This is to be expected somewhat, as extremely high counts are rare and the model has not been trained on a dataset containing such high counts.

We conclude this section by noting that kernel ridge regression can provide prediction functions that explain a high proportion of the variance. However, a major limitation of this method in our case is that it would be primarily be useful for interpolation, rather than extrapolation, for the reasons outlined above. In the subsequent section, we explore generalised additive models, which form a more principled approach for forecasting the number of crimes.

#### Generalised Additive Models

A little about PoissonGAM and mgcv.

For the training data we will use historical data between 2015 and 2018. We will then predict on the data from 2019 to test the model.

```
# Downoad training data
df_train <- load_data(c(2015, 2018), strings_as_factors = TRUE)
# Download test data
df_test <- load_data(2019, strings_as_factors = TRUE)</pre>
```

#### **Daily Predictions**

As each row in the datasets represent a single reported crime incident, we need to sum the number of rows for each day in order to get the number of reported crimes for each day. We use **count** from **dplyr** to achieve this.

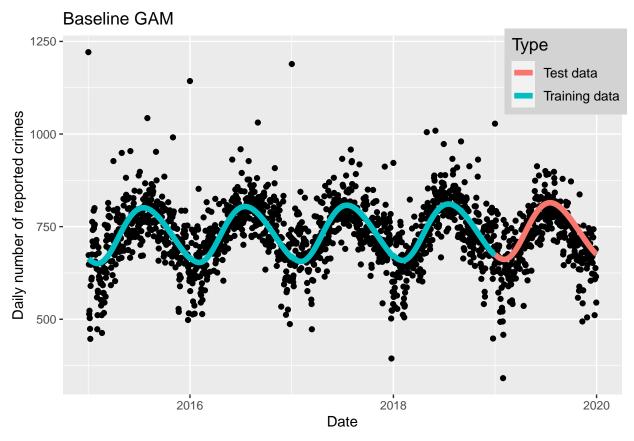
```
count_train <- gam_train %>% count(yday, year, date) %>% arrange(year, yday)
count_test <- gam_test %>% count(yday, year, date) %>% arrange(year, yday)
print(as.data.frame(head(count_train)))
```

We separate this dataset into a training set and a test set, and proceed to fit our baseline GAM which has the year and day of the year as predictors. We use a cyclic cubic smoother for the day of the year.

```
# Convert data to matrix and vector format for model training
X_train <- count_train %>% select(-n)
y_train <- count_train$n
X_test <- count_test %>% select(-n)
y_test <- count_test$n

# Fit the baseline GAM
gam1 <- PoissonGAM$new(time_period = "yday", region = NULL, crime_type = NULL,</pre>
```

```
include_nb = FALSE, include_year = TRUE)
gam1$fit(X = X_train, y = y_train, n_threads = 3)
gam1$fit_summary
## Family: poisson
## Link function: log
##
## Formula:
## n ~ s(as.numeric(yday), bs = "cc") + as.numeric(year)
## Parametric coefficients:
##
                      Estimate Std. Error z value Pr(>|z|)
                    -1.9118027 1.7432595 -1.097
## (Intercept)
## as.numeric(year) 0.0042184 0.0008645 4.880 1.06e-06 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Approximate significance of smooth terms:
                        edf Ref.df Chi.sq p-value
## s(as.numeric(yday)) 5.74
                                 8
                                    5605 <2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## R-sq.(adj) = 0.382 Deviance explained = 38.2\%
## UBRE = 5.3153 Scale est. = 1
pred <- gam1$predict(X = bind_rows(X_train, X_test))</pre>
# Store type of each data
count_train$Type <- "Training data"</pre>
count_test$Type <- "Test data"</pre>
all_dat <- bind_rows(count_train, count_test)</pre>
all_dat$Type <- as.factor(all_dat$Type)</pre>
# Create plot for baseline model
base_gam_plot <- ggplot(all_dat) +</pre>
 geom_point(aes(date, n)) +
  xlab("Date") + ylab("Daily number of reported crimes") +
  geom_line(aes(date, pred, colour = Type), size = 2) +
  ggtitle("Baseline GAM") +
  theme(legend.position = c(0.9, 0.9),
        legend.background = element_rect(fill = "lightgrey", size = 0.5,
                                         linetype = "solid"),
        legend.title = element_text(size = 13),
        legend.text = element_text(size = 10))
base gam plot
```



```
# Obtain metrics on test data
pred_test <- gam1$predict(X = X_test)
# Initialise vectors for RMSE and R squared values
rmse <- c()
rsq <- c()
rmse[1] <- rmse_loss(pred_test, y_test)
rsq[1] <- r_squared(pred_test, y_test)</pre>
```

#### Feature creation

There are several features that may be of interest, whether a day is a weekend or not, the number of crimes over the previous month, the number of crimes on the same day of the previous year.

We first summarise the dates on which the most and fewest crimes are reported, to gain some idea as to what factors might be influential.

```
most_crimes <- count_train %>% arrange(by = desc(n))
most_crimes$date <- as.character(most_crimes$date)
tab <- xtable::xtable(head(most_crimes[, -5]), )
print(tab, type = "latex")

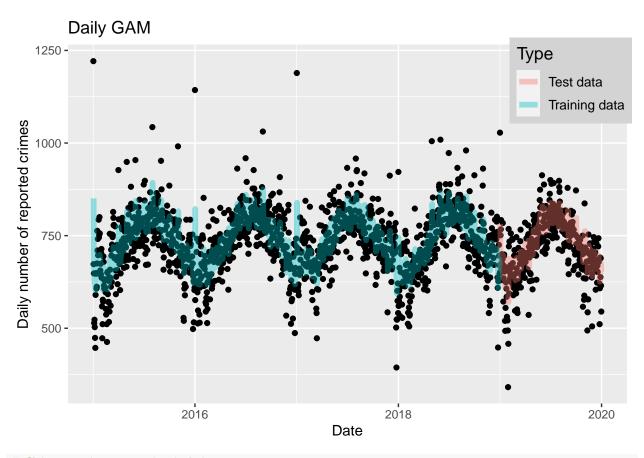
## % latex table generated in R 4.0.3 by xtable 1.8-4 package
## % Sun Jan 24 23:07:03 2021

## \begin{table}[ht]
## \centering
## \begin{tabular}{rrrlr}
## \hline
## & yday & year & date & n \\</pre>
```

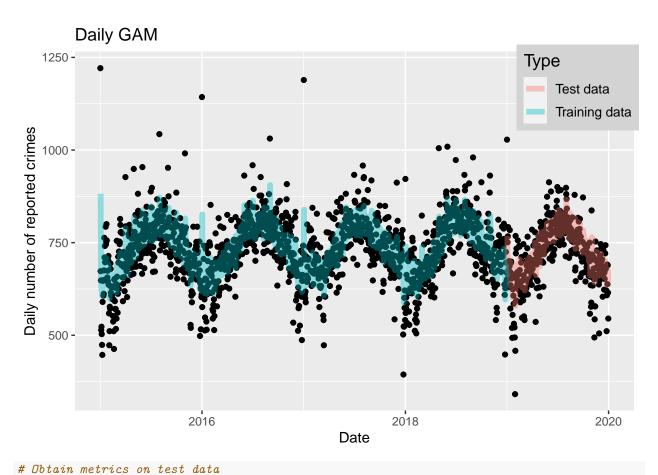
```
##
     \hline
## 1 & 1 & 2015 & 2015-01-01 & 1221 \\
          1 & 2017 & 2017-01-01 & 1189 \\
          1 & 2016 & 2016-01-01 & 1143 \\
##
    4 & 213 & 2015 & 2015-08-01 & 1043 \\
    5 & 245 & 2016 & 2016-09-01 & 1031 \\
##
     6 & 152 & 2018 & 2018-06-01 & 1009 \\
##
      \hline
## \end{tabular}
## \end{table}
least_crimes <- count_train %>% arrange(by = n)
least_crimes$date <- as.character(least_crimes$date)</pre>
tab <- xtable::xtable(head(least crimes[, -5]), )
print(tab, type = "latex")
## \% latex table generated in R 4.0.3 by xtable 1.8-4 package
## % Sun Jan 24 23:07:03 2021
## \begin{table}[ht]
## \centering
## \begin{tabular}{rrrlr}
##
    \hline
## & yday & year & date & n \\
   \hline
##
## 1 & 359 & 2017 & 2017-12-25 & 394 \\
    2 & 8 & 2015 & 2015-01-08 & 447 \\
##
    3 & 359 & 2018 & 2018-12-25 & 448 \\
##
   4 & 50 & 2015 & 2015-02-19 & 463 \\
   5 & 33 & 2015 & 2015-02-02 & 473 \\
##
##
    6 & 73 & 2017 & 2017-03-14 & 473 \\
##
      \hline
## \end{tabular}
## \end{table}
# Add features to training data
count_train_new <- count_train %>%
  mutate(week = week(date), month = month(date)) %>%
  add_prev_day() %>% add_dow() %>% add_is_fom() %>%
 add_is_christmas() %>% add_is_nyd()
# Add features to test data
count_test_new <- count_test %>%
  mutate(week = week(date), month = month(date)) %>%
  add_prev_day() %>% add_dow() %>% add_is_fom() %>%
  add_is_christmas() %>% add_is_nyd()
count_full <- bind_rows(count_train_new, count_test_new)</pre>
data_2014 <- load_data(2014, strings_as_factors = TRUE)</pre>
data_2014 <- data_2014 %>% convert_dates(exclude = "hour") %>% count(year, date) %>% arrange(year)
count_train_new[1, "n_pre"] <- data_2014[data_2014$date == "2014-12-31", "n"][1,] #fill in previous yea
count_test_new[1, "n_pre"] <- count_train_new[count_train_new$date == "2018-12-31", "n"] #fill in previ
print(as.data.frame(head(count_train_new)))
     yday year
                     date
                             n
                                        Type week month n_pre dow is_fom
## 1 1 2015 2015-01-01 1221 Training data
                                                1
                                                      1
                                                         585
```

```
## 2
       2 2015 2015-01-02 673 Training data
                                            1
                                                  1 1221
                                                            6 FALSE
## 3
       3 2015 2015-01-03 648 Training data
                                                  1
                                                      673
                                                            7 FALSE
                                            1
## 4
       4 2015 2015-01-04 514 Training data 1
                                                  1
                                                      648
                                                            1 FALSE
       5 2015 2015-01-05 523 Training data 1
                                                            2 FALSE
## 5
                                                  1
                                                      514
## 6
       6 2015 2015-01-06 503 Training data 1
                                                      523
                                                            3 FALSE
   is christmas is nyd
##
## 1
          FALSE
                 TRUE
          FALSE FALSE
## 2
## 3
          FALSE FALSE
## 4
           FALSE FALSE
## 5
           FALSE FALSE
           FALSE FALSE
## 6
```

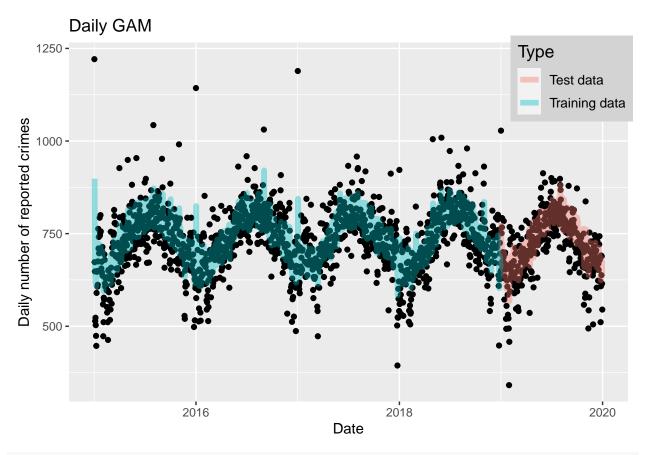
As PoissonGAM doesn't currently have functionality to support additional custom features, here we fit the GAM directly using gam from mgcv.



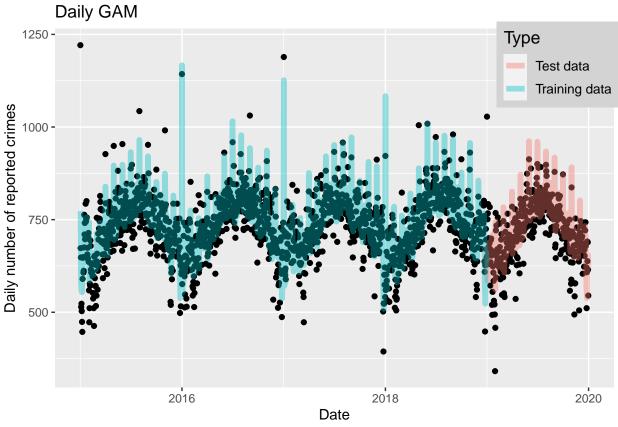
```
# Obtain metrics on test data
gam2_test <- predict(gam2, type = "response", newdata = count_test_new)</pre>
rmse[2] <- rmse_loss(gam2_test, count_test_new$n)</pre>
rsq[2] <- r_squared(gam2_test, count_test_new$n)</pre>
gam3 <- gam(n ~ s(as.numeric(yday), bs = "cc") +</pre>
              s(as.numeric(dow), bs = "cr", k = 5) + n_pre,
            data = count_train_new, family = "poisson")
gam3_pred <- predict(gam3, type = "response", newdata = count_full)</pre>
gam3_plot <- ggplot(all_dat) +</pre>
 geom_point(aes(date, n)) +
  xlab("Date") + ylab("Daily number of reported crimes") +
  geom_line(aes(date, gam3_pred, colour = Type), size = 2, alpha = 0.4) +
  ggtitle("Daily GAM") +
  theme(legend.position = c(0.9, 0.9),
        legend.background = element_rect(fill = "lightgrey", size = 0.5,
                                          linetype = "solid"),
        legend.title = element_text(size = 13),
        legend.text = element_text(size = 10))
gam3_plot
```



```
gam3_test <- predict(gam3, type = "response", newdata = count_test_new)</pre>
rmse[3] <- rmse_loss(gam3_test, count_test_new$n)</pre>
rsq[3] <- r_squared(gam3_test, count_test_new$n)</pre>
# Fit GAM
gam4 <- gam(n ~ s(as.numeric(yday), bs = "cc") +</pre>
              as.factor(dow) + n_pre,
            data = count_train_new, family = "poisson")
# Predict on entire dataset
gam4_pred <- predict(gam4, type = "response", newdata = count_full)</pre>
# Plot predictions
gam4_plot <- ggplot(all_dat) +</pre>
  geom_point(aes(date, n)) +
  xlab("Date") + ylab("Daily number of reported crimes") +
  geom_line(aes(date, gam4_pred, colour = Type), size = 2, alpha = 0.4) +
 ggtitle("Daily GAM") +
  theme(legend.position = c(0.9, 0.9),
        legend.background = element_rect(fill = "lightgrey", size = 0.5,
                                           linetype = "solid"),
        legend.title = element_text(size = 13),
        legend.text = element_text(size = 10))
gam4_plot
```



```
# Obtain metrics on test data
gam4 test <- predict(gam4, type = "response", newdata = count test new)
rmse[4] <- rmse_loss(gam4_test, count_test_new$n)</pre>
rsq[4] <- r_squared(gam4_test, count_test_new$n)</pre>
gam5 \leftarrow gam(n \sim s(as.numeric(yday), bs = "cc") + as.factor(dow) + n_pre +
              is_fom + is_christmas + is_nyd + as.factor(week),
            data = count_train_new, family = "poisson")
# Predict on entire dataset
gam5_pred <- predict(gam5, type = "response", newdata = count_full)</pre>
# Plot predictions
gam5_plot <- ggplot(all_dat) +</pre>
  geom_point(aes(date, n)) +
  xlab("Date") + ylab("Daily number of reported crimes") +
  geom_line(aes(date, gam5_pred, colour = Type), size = 2, alpha = 0.4) +
 ggtitle("Daily GAM") +
  theme(legend.position = c(0.9, 0.9),
        legend.background = element_rect(fill = "lightgrey", size = 0.5,
                                          linetype = "solid"),
        legend.title = element_text(size = 13),
        legend.text = element_text(size = 10))
gam5_plot
```



```
# Obtain metrics on test data
gam5_test <- predict(gam5, type = "response", newdata = count_test_new)</pre>
rmse[5] <- rmse_loss(gam5_test, count_test_new$n)</pre>
rsq[5] <- r_squared(gam5_test, count_test_new$n)</pre>
gam_metrics <- data.frame(RMSE = rmse, R2 = rsq)</pre>
tab <- xtable::xtable(gam_metrics)</pre>
print(tab, type = "latex")
## \% latex table generated in R 4.0.3 by xtable 1.8-4 package
## % Sun Jan 24 22:54:07 2021
## \begin{table}[ht]
## \centering
## \begin{tabular}{rrr}
     \hline
    & RMSE & R2 \\
##
##
     \hline
## 1 & 68.72 & 0.45 \\
##
     2 & 61.65 & 0.50 \\
     3 & 59.30 & 0.54 \\
##
##
     4 & 58.49 & 0.55 \\
     5 & 55.04 & 0.61 \\
##
      \hline
##
## \end{tabular}
## \end{table}
```

### Adding Spatial and Categorical Data

```
# Construct training data set
spatial_train <- gam_train %>%
  get_count_data(time_period = "month", region = "community_area",
                 crime_type = "fbi_code")
# Construct test data set
spatial_test <- gam_test %>%
  get_count_data(time_period = "month", region = "community_area",
                 crime_type = "fbi_code")
# Initisalise GAM
wgam_com <- PoissonGAM$new(time_period = "month", region = "community_area",</pre>
                     crime_type = "fbi_code", include_nb = FALSE)
# Fit using gam train as the dataset
X_train <- spatial_train %>% select(-n)
y_train <- spatial_train$n</pre>
X_test <- spatial_test %>% select(-n)
metrics <- list(rmse = rmse_loss, r2 = r_squared)</pre>
# Find CV error for given metrics
gam_results <- kfold_cv(wgam_com, X = X, y = y, error_funcs = metrics,</pre>
                        k = 5, n_reps = 5, parallel = TRUE, n_threads = 5)
names(gam_results) <- c("RMSE", "R2")</pre>
tab <- xtable::xtable(as_tibble(gam_results), digits = 4)</pre>
print(tab, type = "latex")
## \% latex table generated in R 4.0.3 by xtable 1.8-4 package
## % Sun Jan 24 23:07:07 2021
## \begin{table}[ht]
## \centering
## \begin{tabular}{rrr}
## \hline
## & RMSE & R2 \\
    \hline
##
## 1 & 16.8159 & 0.7177 \\
## 2 & 16.8304 & 0.7167 \\
   3 & 16.8168 & 0.7166 \\
   4 & 16.8706 & 0.7156 \\
##
    5 & 16.8499 & 0.7165 \\
##
      \hline
##
## \end{tabular}
## \end{table}
# Fit model and find validation error
wgam_comfit(X, y, n_threads = 7)
wgam_com$gam_fitted
##
## Family: poisson
## Link function: log
##
## Formula:
```

```
## n ~ s(as.numeric(month), bs = "cc") + fbi_code + community_area
##
## Estimated degrees of freedom:
## 7.95 total = 109.95
## UBRE score: 3.19414
spatial_test$predicted <- wgam_com$predict(X = X_test)</pre>
rmse_loss(spatial_test$n, spatial_test$predicted)
## [1] 17.63151
r_squared(spatial_test$n, spatial_test$predicted)
## [1] 0.7022976
com_area <- spatial_test %>% group_by(community_area) %>%
  summarise(n = sum(n), n_pred = sum(predicted))
com_area$residual <- (com_area$n - com_area$n_pred)</pre>
data("community_bounds")
community_bounds$residual <- com_area$residual</pre>
# Plot the residuals for each Community Area
by_area <- ggplot(community_bounds) +</pre>
  geom_sf(aes(fill = residual)) +
  ggtitle("Predicted Crime frequency by Community Area") +
  colorspace::scale_fill_continuous_sequential(5, palette = "Inferno") +
  theme_void() +
  guides(fill = guide_colorbar(title = "Frequency")) +
  scale_fill_gradientn(colors = colorspace::sequential_hcl(5, palette = "Inferno")[5:1],
                       breaks = seq(-1500, 1000, 500), limits = c(-1500, 1000))
by area
```

# Predicted Crime frequency by Community Area

