Final Review and Practice Problems

Shannon Pileggi

STAT 217

Practice

Data

Overview

OUTLINE

Practice

Data

Review Slides

Review Slides

Final exam

The final exam is cumulative

- ightharpoonup ~ 20% Unit 1
- ► ~ 20% Unit 2
- ► ~ 60% Unit 3

Please bring your calculator! Questions?

Data

- ► Confidence Intervals Confidence intervals
- ► Hypothesis Tests (steps) (errors
- ► Different Methods overview tests calculations

Which of the following are true statements about *p*-values? Mark all that apply.

- 1. A nonsignificant difference (eg, p-value>0.05) means that the null hypothesis is true.
- 2. Sample size can affect your p-value.

Data

3. A scientific conclusion should be based solely on whether or not the p-value is significant.

Final Remarks

- quantitative methods/statistics are applied in all disciplines, regardless of whether you are in the humanities, social sciences, or natural sciences
- a p-value isn't the end of the story

Data

- association does not mean causation.
- a statistically significant result isn't always meaningful
- sometimes statistical analysis is the end result of the research, but sometimes it is just the beginning....

Practice

STAT 217: Unit 3 Deck 4

Data

Overview

Data

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Review Slides

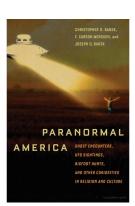


- established in 1991
- largest conference on UFOs in US
- registration \sim \$200

- >20 speakers discussing topics related to the UFO phenomenon including technology, government cover-ups, exopolitics, black projects, crop circles, alien visitation and more
- speakers include astrophysicists, nuclear physicists, abductees, and former top-secret-clearance military personnel

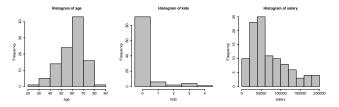
Overview

- ► Feb 21-27, 2010 in Laughlin, Nevada
- anonymous survey of conference attenders
- collected by the Dept of Sociology at Baylor University (Texas)
- 400 surveys distributed, 156 returned, 104 used
- 97 variables
 - UFO beliefs and theories
 - UFO experiences and beliefs about government conspiracies related to UFOs
 - non-UFO paranormal beliefs and experiences
 - religion
 - demographics



The data, n = 104

```
> summary(ufo)
      JOBTITLE
                                         beliefs
                                                    ufo_experience
                     age
          :20
                                 cosmic force:60
                Min.
                        :24.00
                                                    >=1:85
Retired
          :15
                1st Ou.:55.75
                                 aod
                                              :44
                                                    none:19
                Median:62.00
 RN
Teacher
                Mean
                       :60.62
Therapist: 2
                3rd Ou.:68.00
 (Other)
          :60
                Max.
                       :83.00
NA's
          : 2
believe_bigfoot
                                   kids
                                                  salary
                                                                 years_edu
                     sex
no :17
                 female:48
                                                                      :10.00
                              Min.
                                     :0.00
                                             Min.
                                                  : 6597
                                                               Min.
ves:87
                 male :56
                              1st Qu.:0.00
                                             1st Qu.: 33365
                                                               1st Qu.:14.00
                              Median:0.00
                                             Median: 53983
                                                               Median :16.00
                              Mean
                                     :0.25
                                                     : 69757
                                                                      :15.97
                                             Mean
                                                               Mean
                              3rd Ou.:0.00
                                             3rd Qu.: 96522
                                                               3rd Ou.:18.00
                              Max.
                                     :4.00
                                             Max.
                                                     :199258
                                                               Max.
                                                                      :22.00
```





Histogram of years edu

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Overview

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Research question 1

Which null hypothesis?

The average years of education of the general population is 13, whereas the average years of education among the 104 respondents is 16. Is average years of education for those interested in UFOs the same as the general population?

- 1. $H_0: \mu_1 = \mu_2$
- 2. $H_0: \bar{x}_1 = \bar{x}_2$
- 3. $H_0: \mu_0 = 13$
- 4. $H_0: \mu_0 = 16$
- 5. $H_0: \mu = 16$
- 6. $H_0: \mu = 13$
- 7. $H_0: \bar{x} = 13$
- 8. $H_0: \bar{x} = 16$

Research question 2

Which method?

Is whether or not an individual had a UFO experience associated with years of education?

- 1. one sample z-test
- 2. two sample z-test
- 3. chi-squared test
- 4. one sample t-test
- 5. two sample t-test
- 6. paired t-test
- 7. ANOVA
- 8. Linear regression



Is there an association between gender and belief in big foot?

- 1. one sample z-test
- 2. two sample z-test
- 3. one sample t-test
- 4. two sample t-test
- 5. paired t-test
- 6. ANOVA
- 7. Linear regression



Research question 4 Which method?

Is salary associated with years of education?

Data

- 1. one sample z-test
- 2. two sample z-test
- 3. chi-squared test
- 4. one sample t-test
- 5. two sample t-test
- 6. paired t-test
- 7. ANOVA
- 8. Linear regression



Research question 5

Data

Which method?

Suppose we categorize years of education as <high school, high school, and >high school, and we want to determine if there is an association between salary and level of education.

- 1. one sample z-test
- 2. two sample z-test
- 3. chi-squared test
- 4. one sample t-test
- 5. two sample t-test
- 6. paired t-test
- 7. ANOVA
- 8. Linear regression



Contingency tables

Overview

| | Beliefs | | |
|-------------|--------------|-----|-------|
| | Cosmic Force | God | Total |
| Bigfoot Yes | 51 | 36 | 87 |
| Bigfoot No | 9 | 8 | 17 |
| Total | 60 | 44 | 104 |

Which of the following is <u>false</u>?

- 1. Among those who believe in God, 36/44=81.8% believe in bigfoot.
- Among those who believe in cosmic force, 51/104=49.0% believe in bigfoot.
- 3. Overall, the proportion of individuals who believe in bigfoot is higher than the proportion of individuals who believe in God.
- 4. All of the above are true.

Review Slides

The correlation between years of education and salary is 0.22. This means that

- 1. As annual salary increases by \$1, education increases by 0.22 years.
- 2. As education increases by one year, annual salary increases by \$0.22.
- Since the correlation is not 0, we can predict a salary perfectly from years of education.
- 4. The relationship between salary and years of education follows a curve rather than a straight line.
- 5. As one of these variables increases, there is a tendency for the other variable to increase also.



What is the estimated regression equation to predict salary by years of

```
lm(formula = salary ~ years_edu)
Residuals:
```

Coefficients:

Call:

Overview

```
Estimate Std. Error t value Pr(>|t|) (Intercept) 5024 27855 0.180 0.8572 years_edu 4053 1720 2.356 0.0204 * --- Signif. codes: 0 '***' 0.01 '**' 0.01 '*' 0.05 '.' 0.1
```

Residual standard error: 47010 on 102 degrees of freedom Multiple R-squared: 0.05163, Adjusted R-squared: 0.04233 F-statistic: 5.553 on 1 and 102 DF, p-value: 0.02036

education ?

1.
$$\hat{y} = 5024 + 4053 \times years_edu$$

2.
$$\hat{y} = 5024 + 4053 \times salary$$

3.
$$\hat{y} = 4053 + 5024 \times salary$$

4.
$$\hat{y} = 4053 + 5024 \times years_edu$$

5.
$$\hat{y} = 27855 + 1720 \times years_edu$$

6.
$$\hat{y} = 1720 + 27855 \times salary$$

SLR

```
Call:
lm(formula = salarv ~ vears edu)
Residuals:
   Min
          10 Median
-64379 -31667 -17831 23038 137490
```

Coefficients:

Signif. codes:

```
Estimate Std. Error t value Pr(>|t|)
(Intercept)
                5024
                          27855
                                  0.180
                                          0.8572
                4053
                           1720
                                  2.356
                                          0.0204 *
vears_edu
---
               0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1
```

Residual standard error: 47010 on 102 degrees of freedom Multiple R-squared: 0.05163, Adjusted R-squared: 0.04233 F-statistic: 5.553 on 1 and 102 DF, p-value: 0.02036

What is the null hypothesis tested on the line where the p-value is 0.0204?

1.
$$H_0$$
: $\mu_d = 0$

2.
$$H_0$$
: $\beta_0 = 0$

3.
$$H_0$$
: $\beta_1 = 0$

4.
$$H_0$$
: $\mu_1 = \mu_2$

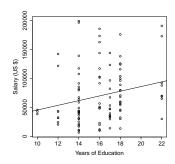
```
Overview
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```

```
> cor(ufo$years_edu,ufo$salary)
[1] 0.2272182
```

```
Residuals:
           10 Median
   Min
                               Max
-64379 -31667 -17831 23038 137490
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept)
               5024
                          27855
                                  0.180
                                          0.8572
years_edu
               4053
                          1720
                                  2.356
                                         0.0204 *
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1
Residual standard error: 47010 on 102 degrees of freedom
Multiple R-squared: 0.05163, Adjusted R-squared: 0.04233
F-statistic: 5.553 on 1 and 102 DF. p-value: 0.02036
```

Which of the following statements is true?

- 1. We have evidence of an association between salary and years of education, and the association is strong.
- 2. Although we have evidence of an association between salary and years of education, the association is weak.
- 3. We do not have evidence between salary and years of education.



Which conditions of linear regression are not satisfied?

- 1. independence of observations
- 2. linear relationship between x and y
- 3. constant variability in *y* about the regression line
- 4. no conditions are violated

Overview

Review Slides

| | Df | Sum Sq | Mean Sq | F value | Pr(>F) |
|-----------|-----|--------|---------|---------|--------|
| source | 2 | 267 | 133.3 | 0.477 | 0.623 |
| Residuals | 101 | 15932 | 279.5 | | |

How can we interpret these ANOVA results?

- We have evidence that the mean salary is the same for all three levels of education.
- We have evidence that the mean salary is different for all three levels of education.
- We have evidence that the mean salary differs for at least two levels of education.
- 4. We do not have evidence that the mean salary differs by level of education.

```
Welch Two Sample t-test
```

```
data: years_edu by ufo_experience
t = -2.0956, df = 25.808, p-value = 0.04608
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval:
```

```
sample estimates:

mean in group >=1 mean in group none

15.70588 17.15789
```

What can we say about 95% CI for $\mu_1 - \mu_2$?

- 1. it would contain $\bar{x}_1 = 15.7$
- 2. it would contain p = 0.046
- 3. it would contain zero
- 4. it would not contain zero

Sampling Distributions

For which of the following scenarios is the sampling distribution of the sample mean approximately normally distributed?

- 1. Population is right skewed and n = 10
- 2. Population is left skewed and n = 40
- 3. Population is normal and n = 10

Data

- 4. 1, 2 and 3
- 5. 2 and 3 only

Descriptive statistics

- summarizing and visualizing categorical variables
- summarizing and visualizing quantitative variables
- statistics that are/are not robust to outliers

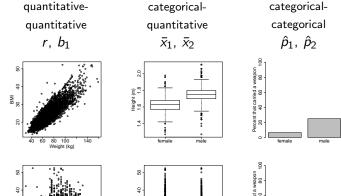


- recognizing observational vs experimental studies
- potential sources of bias in a study (sampling bias, nonresponse bias, response bias)
- recognizing types of observational study design (simple, stratified, cluster)
- recognizing response vs explanatory variables
- identifying potential confounding variables
- association does not imply causation





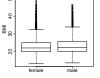
Associations



No association?

Association?







We need formal statistical tests to determine the direction, magnitude, and significance of the association!

Probability and Distributions

Distributions:

- ▶ normal/z, t
- ▶ 68 95 99.7 rule for normal

Interpreting a probability:

- ▶ is it large or small?
- would the event be likely to occur by random chance alone?

◆ Back

Sampling Distributions

- For a random sample of size n from a population with proportion p, then when $np \geq 10$ and $n(1-p) \geq 10$ the sampling distribution of the sample proportion is normally distributed with mean $(\hat{p}) = p$ and $\operatorname{sd}(\hat{p}) = \sqrt{\frac{p(1-p)}{n}}$.
- When underlying population distribution is normally distributed or sample size large enough such that $\overline{\text{CLT}}$ applies (n>30), then when sampling from a population with mean μ and standard deviation σ the **sampling distribution** of the **sample mean** is normally distributed with $\text{mean}(\bar{x}) = \mu$ and $\text{sd}(\bar{x}) = \frac{\sigma}{\sqrt{n}}$.

◆ Back



Confidence intervals

- used to estimate plausible values for a parameter of interest (like a mean or a proportion)
- Cls take the form

$$estimate \pm (z^* or \ t^*) \times se$$

- ▶ true meaning: in the long run, if we took many samples and calculated many confidence intervals, 95% of 95% Cls would actually capture the true parameter value
- know how to interpret
- understand how a confidence interval changes when n, s, or the confidence level changes





- 1. Define the parameter of interest
- 2. State the null and alternative hypotheses
- 3. Identify the appropriate test
- 4. State assumptions
- 5. Calculate the test statistic $test \ statistic = \frac{sample \ statistic null \ hypothesis \ value}{standard \ error \ of \ the \ sample \ statistic}$
- 6. Calculate the p-value (for STAT 217, provided by R!)
- 7. State your conclusion





Types of Errors

Table: Possible outcomes of a hypothesis test

Decision based on observed data Fail to reject H_0 Reject H_0

| Unknown Truth | | | |
|------------------|------------------|--|--|
| H_0 true | H_0 false | | |
| Correct Decision | Type II Error | | |
| Type I Error | Correct Decision | | |

Confidence intervals and hypothesis tests results should agree:

- ▶ When you reject H_0 , the corresponding CI **should not** include the null value tested in H_0 .
- ▶ When you fail to reject H_0 , the corresponding CI **should** include the null value tested in H_0 .



STAT 217: Unit 3 Deck 4

Overview of Statistical Methods

Quantitative variable - means

- one sample t-test
- paired t-test
- two sample t-test
- anova

Overview

Categorical variable - proportions

- one sample z-test
- ► N/A for STAT 217
- two sample z-test
- chi-squared test

Neither a mean or a proportion: simple linear regression.



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Different methods

| Method | Use | Variables | Estimation | Testing |
|---------------------|------------------------------|-------------------------------|------------------------|---------------------------------------|
| Single proportion | categorical response | one categorical variable | CI for p | $H_0: p = p_0$ |
| (one-sample z-test) | in single group | | | |
| *Two proportions | categorical response | two categorical variables | CI for $p_1 - p_2$ | $H_0: p_1 = p_2$ |
| (two-sample z-test) | in two groups | | | |
| *Chi-squared test | categorical response | two categorical variables | N/A | H ₀ : no association/ |
| | in ≥ 2 groups | | | vars independent |
| Single mean | quantitative response | one quantitative variable | CI for μ | $H_0: \mu = \mu_0$ |
| (one-sample t-test) | in single group | | | |
| *Two means | quantitative response | one quantitative variable and | CI for $\mu_1 - \mu_2$ | H_0 : $\mu_1 = \mu_2$ |
| (two-sample t-test) | in two groups | one categorical variable | | |
| *Dependent means | quantitative response | two paired | CI for μ_d | H_0 : $\mu_d = 0$ |
| (paired t-test) | measured on same observation | quantitative variables | | |
| *ANOVA | quantitative response | one quantitative variable and | Tukey pairwise | $H_0: \mu_1 = \mu_2 = \cdots = \mu_g$ |
| | in > 2 groups | one categorical variable | intervals | |
| *Linear regression | quantitative response and | 2 quantitative variables | CI for β_1 | $H_0: \beta_1 = 0$ |
| | a quantitative explanatory | | | |

*The starred methods can answer the question "Is there an association?" If we reject H_0 , then we conclude that some sort of association is present in the two variables.





Test statistics and Confidence Intervals

| Method | H ₀ | Test Statistic | Confidence Interval |
|-------------------|----------------------------------|--|--|
| Single proportion | $p = p_0$ | $z = \frac{\hat{p} - p_0}{\sqrt{\frac{p_0(1 - p_0)}{n}}}$ | $\hat{ ho}\pm z^*\sqrt{rac{\hat{ ho}(1-\hat{ ho})}{n}}$ |
| Two proportions | $p_1 = p_2$ | $z = \frac{\left(\hat{\rho}_1 - \hat{\rho}_2\right) - 0}{se}$ | $(\hat{ ho}_1 - \hat{ ho}_2) \pm z^* 	imes se$ |
| Chi-squared test | vars independent | $\chi^2 = \sum \frac{\text{(observed - expected)}^2}{\text{expected}}$ | N/A |
| Single mean | $\mu = \mu_0$ | $t = \frac{\bar{x} - \mu_0}{s / \sqrt{n}}$ | $\bar{x} \pm t_{df=n-1}^* \times s/\sqrt{n}$ |
| Two means | $\mu_1 = \mu_2$ | $t = \frac{(\bar{x}_1 - \bar{x}_2) - 0}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$ | $(\bar{x}_1 - \bar{x}_2) \pm t_{df=given}^* \times \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}$ |
| Dependent means | $\mu_d = 0$ | $t = \frac{\bar{x}_d - 0}{s_d / \sqrt{n}}$ | $\bar{x_d} \pm t_{df=n-1}^* \times s_d / \sqrt{n}$ |
| ANOVA | $\mu_1 = \mu_2 = \cdots = \mu_g$ | N/A | Tukey |
| Linear regression | $\beta_1 = 0$ | $t=rac{\widehat{eta}_1-0}{se_{\widehat{eta}_1}}$ | $\hat{eta}_1 \pm t^*_{df=n-2} 	imes se_{\hat{eta}_1}$ |

When performing a statistical analysis with data in R, R by default assumes the two-sided alternative hypotheses as presented above, and all p-values presented represent the final p-values (ie, no need to multiply by two).