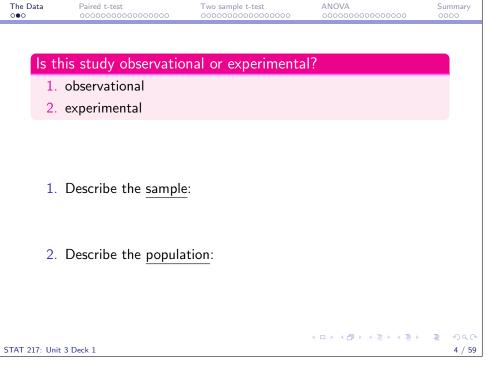


Beat the Blues
enrolled patients with depression/anxiety
randomly assigned them to Treatment as Usual (TAU) or BtheB, a new treatment delivery therapy via computers
measured depression via Beck Depression Inventory (BDI) at baseline (pre-treatment), and 2, 4, 6, and 8 month follow up
BDI scores range from 0 to 63 with higher scores indicating more severe depression



The first 6 observations in the data set

>	> head(BtheB)							
	drug	length	treatment	bdi.pre	bdi.2m	${\tt bdi.4m}$	${\tt bdi.6m}$	bdi.8m
1	No	>6m	TAU	29	2	2	NA	NA
2	Yes	>6m	BtheB	32	16	24	17	20
3	Yes	<6m	TAU	25	20	NA	NA	NA
4	No	>6m	BtheB	21	17	16	10	9
5	Yes	>6m	BtheB	26	23	NA	NA	NA
6	Yes	<6m	BtheB	7	0	0	0	0

 STAT 217: Unit 3 Deck 1
 5 / 59

The Data

Paired t-test

Two sample t-test

ANOVA

Summary

Two sample t-test

ANOVA

Summary

6 / 59

Summary

The Data

STAT 217: Unit 3 Deck 1

Paired t-test

00•0000000000000

Paired t-test

•00000000000000000

The research question: Do depression levels change from baseline (pre-treatment) to 2 months follow-up post treatment? le, regardless of treatment group, does participating in a clinical trial have an effect on depression levels?

First six observations:

1. What types of variables do we have?

	bdi.pre	bdi.2m
1	29	2
2	32	16
3	25	20
4	21	17
5	26	23
6	7	0

2. Are they "paired"?

3. How many groups are we studying?

4. How can we approach the problem?

Which scenarios represent paired measurements (or *dependent* samples)? Mark <u>all</u> that apply.

Two sample t-test

- 1. In order to study the efficacy of a new sunscreen, 50 volunteers put a standard sunscreen on their left arm and the new sunscreen on their right arm. After 3 hours, degree of redness was assessed for each arm.
- 2. Newer baseball stadiums are thought to attract more fans. Attendance records in the old stadium was compared to attendance records in the new stadium for 10 teams.
- 3. The General Social Survey (GSS) compared the number of hours worked per week among college graduates and non-college graduates.

STAT 217: Unit 3 Deck 1 8 / 59

★ロト ◆ ラト ◆ 恵ト ◆ 恵ト ◆ 恵ト ◆ 恵 ◆ へ ②STAT 217: Unit 3 Deck 17 / 59

The Data Paired t-test Two sample t-test Summary 00000000000000000 Parameter of interest: $\mu_d = \mu_{pre} - \mu_{2m} = \text{population mean}$ difference in depression scores between baseline and two month follow-up Three possible scenarios: ► No change: > BtheB\$diff2m<-BtheB\$bdi.pre-BtheB\$bdi.2m bdi.pre bdi.2m diff2m Improvement: 29 1 2 32 16 16 3 25 20 4 21 17 Worsening: 5 26 23 3 6 STAT 217: Unit 3 Deck 1 9 / 59

 The Data
 Paired t-test
 Two sample t-test
 ANOVA
 Summary

 000
 0000●0000000000
 0000000000000
 0000000000000
 0000

Answering the research question

We can answer the research question of interest with:

- \blacktriangleright A confidence interval for μ_d
- A hypothesis test of H_0 : $\mu_d = 0$ (this is the paired t-test)
- ► This is essentially the same inference about a mean that we have already learned

Conditions required for both the CI and HT:

- 1. independent observations
- 2. normal underlying population distribution OR $n \ge 30$

 ←□ ト ←□ ト ← □ ⊢ ← □ ⊢ ←

Checking condition 1: independent observations

dependent measurements made on the same person

	bdi.pre	bdi.2m	diff2m	
1	29	2	27 -	each person's change in
2	32	16	16 —	depression score is
3	25	20	5	independent from the nex
4	21	17	4	
5	26	23	3	
6	7	0	7	

The difference in depression scores between baseline and two month follow-up for person 1 is not related to the difference in depression scores between baseline and two month follow-up for person 2 (and for all other subjects in the study). This condition regarding independent observations is satisfied.

Two sample t-test

Checking condition 2

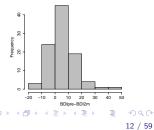
The differences in depression scores has a slight right skew; however, the sample size is n=97>30 so this condition is satisfied.

Summary data needed for both CI and HT:

n =

 $\bar{x}_d =$

 $s_d =$



Summarv

STAT 217: Unit 3 Deck 1 11 / 59 STAT 217: Unit 3 Deck 1

95% confidence interval for μ_d

$$\bar{x}_d \pm t^* imes rac{s_d}{\sqrt{n}}$$

based on a 95% conf. level and df = n - 1 = 97 - 1 = 96 $t^* = 1.98 \text{ (from R)}$

$$se = s_d / \sqrt{n} = 9.47 / \sqrt{97} = 0.96$$

$$6.23\pm1.98\times0.96$$

$$6.23 \pm 1.90$$

95% CI for
$$\mu_d$$
: (4.33,8.13)

What is the margin of error for this confidence interval?

- 1. 0.05
- 2. 0.96
- 3. 1.90
- 4. 1.98
- **5**. 3.80

13 / 59

Interpretation

The Data

- Literal interpretation of the interval:
- ▶ Does it include zero?
- ▶ What does that mean?
- ► Answer the research question:

STAT 217: Unit 3 Deck 1 14 / 59

The Data

Two sample t-test

Summary

Two sample t-test

Summary

Paired t-test

$$H_0$$
: $\mu_d = 0$ vs H_a : $\mu_d \neq 0$

Paired t-test

00000000000000000

$$t = \frac{\bar{x}_d - \mu_0}{s_d / \sqrt{n}} = \frac{6.23 - 0}{9.47 / \sqrt{97}} = 6.47$$

This t test statistic follows a t distribution with 96 (n-1) degrees of freedom. The p-value is found by a two-tailed area under the tdistribution.

STAT 217: Unit 3 Deck 1

000000000000000000

The 95% CI for μ_d is (4.33,8.33). Which of the following would be a *plausible* p-value when testing the hypotheses H_0 : $\mu_d = 0 \text{ vs } H_a$: $\mu_d \neq 0$?

- 1. 0.03
- 2. 0.23
- 3. 0.53
- 4. 0.73

STAT 217: Unit 3 Deck 1

5. not enough information to determine

◆□▶→□▶→□▶→□▶ □

15 / 59

4□▶ 4□▶ 4 = ▶ 4 = ▶ 9 < 0</p> STAT 217: Unit 3 Deck 1

Results in R

#These two commands give equivalent results. Why?

> t.test(BtheB\$diff2m,mu=0)

> t.test(BtheB\$bdi.pre,BtheB\$bdi.2m,paired=TRUE)

One Sample t-test

data: BtheB\$diff2m

t = 6.4836, df = 96, p-value = 3.869e-09

alternative hypothesis: true mean is not equal to 0

95 percent confidence interval:

4.327579 8.146647 sample estimates:

mean of x 6.237113

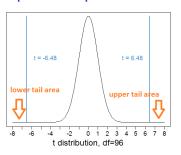
STAT 217: Unit 3 Deck 1

17 / 59

Interpret the p-value

Paired t-test

The Data



p-value = lower tail area + upper tail area

If there really was no difference in average depression scores between baseline and 2 months (ie, if H_0 true), then the probability that we would observe a test statistic less than -6.48 or greater than 6.48 is really small (3.869 \times 10⁻⁹). This presents evidence against H_0 .

Two sample t-test

Summary

STAT 217: Unit 3 Deck 1 18 / 59

Conclusion in context

- 1. Decision about H_0 :
- 2. Statement about the parameter tested in context of the research question:
- 3. Provide a deeper connection of how this relates to the research question:

 The Data on the Da

What type of error could we have committed here?

- 1. a Type I error
- 2. a Type II error
- 3. either
- 4. neither

 ▼ロト・プト・モート 夏 ◆○○○

 STAT 217: Unit 3 Deck 1
 20 / 59

4 B > 4 B > 4 B > 4 B > 9 Q (연

19 / 59

Paired t-test

Two sample t-test

ANOVA

Summary

The Data

6.7).

Paired t-test

What can we infer from this CI?

treatment is effective

Two sample t-test

Suppose I am dealing with paired data from a randomized clinical

trial regarding weight before and after a treatment intending to assist in weight loss. μ_d represents the average of post-treatment

weight minus the pre-treatment weight. A 95% CI for μ_d is (0.5,

1. the treatment is not effective because the CI includes 1, indicating that

3. the treatment is not effective for weight loss because treatment is causing

there is no difference in weight loss before and after treatment

weights are on average less than the pre-treatment weights

patients to gain weight, rather than lose weight, on average 4. there is not enough information to determine whether or not the

2. the treatment is effective for weight loss because the post-treatment

ANOVA

Summary

Meaningful?

One Sample t-test

data: BtheB\$diff2m

t = 6.4836, df = 96, p-value = 3.869e-09

alternative hypothesis: true mean is not equal to 0

95 percent confidence interval:

4.327579 8.146647 sample estimates:

mean of x 6.237113

The results are statistically signficant. But is it meaningful?

STAT 217: Unit 3 Deck 1

40.40.45.45. 5 000

22 / 59

The Data Paired t-test Two sample t-test ANOVA Summary

The Data

STAT 217: Unit 3 Deck 1

Paired t-test

Two sample t-test

 $\Delta NOV\Delta$

Summary

The research question: Do depression levels differ at baseline (bdi.pre) between patients who were and were not already on antidepressant drugs (drugs)? OR: Is there an association between baseline depression scores and whether or not patients take antidepressant drugs?

First six observations:

	drug	bdi.pre
1	No	29
2	Yes	32
3	Yes	25
4	No	21
5	Yes	26
6	Yes	7

- 1. What types of variables do we have?
- 2. Are they "paired"?
- 3. How many groups are we studying?
- 4. How can we approach the problem?

4 □ ト 4 □ ト 4 亘 ト 4 □ Λ 1 □ Λ

23 / 59 STAT 217: Unit 3 Deck 1

STAT 217: Unit 3 Deck 1

24 / 59

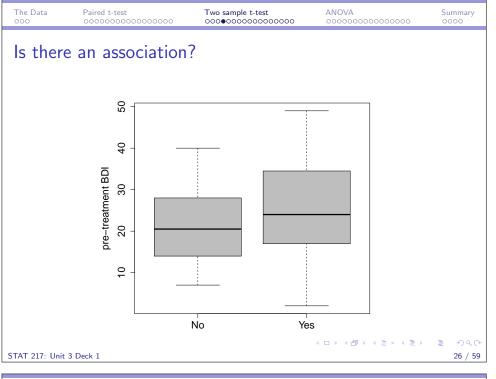
4日 > 4周 > 4 至 > 4 至 > 至

The Data Paired t-test Two sample t-test Summary 0000000000000000

Which figure would be appropriate to begin to visually assess if there is an association between depression scores and whether or not patients take antidepressant drugs?

- 1. dot plot
- 2. histogram
- 3. single boxplot
- 4. side by side boxplot
- 5. barplot

STAT 217: Unit 3 Deck 1 25 / 59



The Data Two sample t-test Summary 0000000000000000

Which of these scenarios represent a two sample comparison?

- 1. We take a random sample of 100 Cal Poly students and test if the average GPA differs from 3.3.
- 2. We take a random sample of 100 Cal Poly students and test if the average GPA differs between males and females.
- 3. We take a random sample of 100 Cal Poly students and test if the average GPA changes before and after attending a workshop on study habits.
- 4. We take a random sample of 100 Cal Poly students and test if the average GPA differs by political affiliation (democrat, republican, independent).

The Data Two sample t-test Summary 0000000000000000

Parameters of interest:

 $\mu_{\rm ves}$ =population mean baseline BDI score among patients who are on antidepressants

 μ_{no} =population mean baseline BDI score among patients who are not on antidepressants

Three possible scenarios:

No difference:

First six observations:

	drug	bdi.pre	
1	No	29	
2	Yes	32	
3	Yes	25	
4	No	21	
5	Yes	26	
6	Yes	7	

Difference:

Difference:

28 / 59

STAT 217: Unit 3 Deck 1 27 / 59 STAT 217: Unit 3 Deck 1

Paired t-test

Two sample t-test

ANOVA

Summary

Paired t-test

Two sample t-test

ANOVA

Summary

Answering the research question

We can answer the research question of interest with:

- ▶ A confidence interval for $\mu_{\textit{ves}} \mu_{\textit{no}}$
- A hypothesis test of H_0 : $\mu_{yes} = \mu_{no}$ (this is the two sample t-test)

Conditions required for both the CI and HT:

- 1. independent observations (in each of the two groups)
- 2. normal underlying population distribution OR $n \ge 30$ in each group



Possible outcomes

The Data

If we fail to reject H_0 : $\mu_1=\mu_2$ or if the 95% CI for $\mu_1-\mu_2$ includes 0, then

- What is the relationship between the population mean depression scores?
- ► Is there evidence of an association between pre-treatment BDI score and antidepressant drug use?

If we reject H_0 : $\mu_1=\mu_2$ or if the 95% CI for $\mu_1-\mu_2$ does not include 0, then

- ► What is the relationship between the population mean depression scores?
- ▶ Is there evidence of an association between pre-treatment BDI score and antidepressant drug use?

STAT 217: Unit 3 Deck 1

Paired t-test

Two sample t-test

Summary

STAT 217: Unit 3 Deck 1

The Data

Two sample t-test

ANOVA

Summary

The data

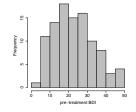
The Data

> favstats(BtheB\$bdi.pre~BtheB\$drug)
BtheB\$drug min Q1 median Q3 max mean sd n missing
 No 7 14 20.5 27.50 40 21.55357 8.974549 56 0
Yes 2 17 24.0 34.25 49 25.59091 12.577792 44 0

 $s_2 =$

Summary data needed for both CI and HT :

roup



Which of the following data would provide the *most* evidence against H_0 : $\mu_1 = \mu_2$?

1.
$$\bar{x}_1 = 25$$
, $\bar{x}_2 = 19$

2.
$$\bar{x}_1 = 25$$
, $\bar{x}_2 = 21$

3.
$$\bar{x}_1 = 25$$
, $\bar{x}_2 = 23$

4.
$$\bar{x}_1 = 25$$
, $\bar{x}_2 = 27$

5.
$$\bar{x}_1 = 25$$
, $\bar{x}_2 = 29$

STAT 217: Unit 3 Deck 1

31 / 59

Paired t-test

Two sample t-test 000000000000000000

Summary

The Data

Paired t-test

Two sample t-test 000000000000000000

Summary

95% confidence interval for $\mu_1 - \mu_2$

$$(ar{x}_1-ar{x}_2)\pm t^* imes se$$
 where $se=\sqrt{rac{s_1^2}{n_1}+rac{s_2^2}{n_2}}$

- \blacktriangleright The df for t^* is a complicated formula that you do not need to know. The t^* for a 95% CI with df = 74.9 is 1.99.
- ▶ We are calculating this CI under the assumption of unequal variances.

STAT 217: Unit 3 Deck 1

33 / 59

Hypothesis test of H_0 : $\mu_1 = \mu_2$

$$t = rac{(ar{x}_1 - ar{x}_2) - 0}{se}$$
 where $se = \sqrt{rac{s_1^2}{n_1} + rac{s_2^2}{n_2}}$

We are calculating this test statistic under the assumption of unequal variances.

> <ロ > < 回 > < 回 > < 巨 > く 巨 > 一 豆 | か へ 〇 34 / 59

Two sample t-test 000000000000000000

Summary

STAT 217: Unit 3 Deck 1

Two sample t-test 000000000000000000

Summary

Interpretation

Literal interpretation of the interval:

Does it include zero?

What does that mean?

Answer the research question:

Two sample t-test assuming unequal variances

 H_0 : $\mu_1 = \mu_2$ vs H_a : $\mu_1 \neq \mu_2$

> t.test(BtheB\$bdi.pre~BtheB\$drug)

Welch Two Sample t-test

data: BtheB\$bdi.pre by BtheB\$drug

t = -1.7995, df = 74.911, p-value = 0.07597

alternative hypothesis: true difference in means is not equal to 0 95 percent confidence interval:

-8.5069019 0.4322266

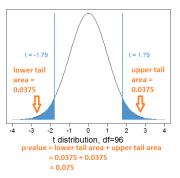
sample estimates:

mean in group No mean in group Yes 21.55357 25.59091

* Note the order of subtraction in the R output: R analyzes this as $\mu_{no} - \mu_{ves}$. You know this because the sample mean for group No is presented first, and the sample mean for group Yes_is presented second

36 / 59

Interpret the p-value



If average depression scores among patients who do and do not take anti-depressents really is the same (ie, if H_0 true), then the probability that we would observe a test statistic less than -1.79 or greater than 1.79 is 0.075. This probability isn't that small, and does not present evidence against H_0 .

STAT 217: Unit 3 Deck 1 37 / 59

Conclusion in context

- 1. Decision about H_0 :
- 2. Statement about the parameter tested in context of the research question:
- 3. Provide a deeper connection of how this relates to the research question:

STAT 217: Unit 3 Deck 1 38 / 59

Which of the following are <u>true</u>? Mark <u>all</u> that apply.

- 1. We could have committed a Type I error.
- 2. We could have committed a Type II error.
- 3. There is evidence of an association between antidepressant drug use and depression scores.
- 4. There is no evidence of an association between antidepressant drug use and depression scores.
- 5. We have evidence that using antidepressant drugs causes people to have higher depression scores.

The Data

Paired t-test

Two sample t-tes

ANOVA

Summary

←□ト ← (型)ト ← (Z)ト ← (Z

Paired t-test

Two sample t-test

Summary

The Data

Paired t-test

Two sample t-test

The research question: Do patients' baseline depression levels differ by patient history? OR Is there an association between

baseline depression score and patient history?

ANOVA

Summary

A new variable

Suppose we create a variable defining patient history before they enrolled in the clinical trial. The variable is defined as:

- 1. history = 1: drug = no; length < 6m
- 2. history = 2: drug = no; length > 6m
- 3. history = 3: drug = yes; length < 6m
- 4. history = 4: drug = yes; length > 6m

	drug	length	bdi.pre	history
1	No	>6m	29	2
2	Yes	>6m	32	4
3	Yes	<6m	25	3
4	No	>6m	21	2
5	Yes	>6m	26	4
6	Yes	<6m	7	3

The history variable is...

- 1. quantitative
- 2. categorical

 4 □ > 4 □ > 4 □ > 4 □ > 4 □ > 4 □ > 4 □ > 4 □ > 4 □ > 4 □ > 4 □ > 4 □

 4 □ > 4 □ > 4 □ > 4 □ > 4 □ > 4 □ > 4 □ > 4 □ > 4 □ > 4 □ > 4 □

First six observations:

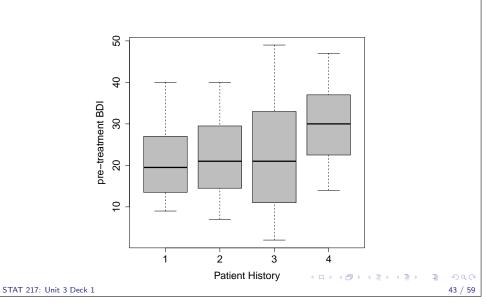
	drug	length	bdi.pre	history
1	No	>6m	29	2
2	Yes	>6m	32	4
3	Yes	<6m	25	3
4	No	>6m	21	2
5	Yes	>6m	26	4
6	Yes	<6m	7	3

- 1. What types of variables do we have?
- 2. Are they "paired"?
- 3. How many groups are we studying?
- 4. How can we approach the problem?

4□ > 4□ > 4□ > 4 ≣ > 4 ≣ > ■ 4 9 Q (~ 42 / 59

Is there an association?

STAT 217: Unit 3 Deck 1



Motivation

STAT 217: Unit 3 Deck 1

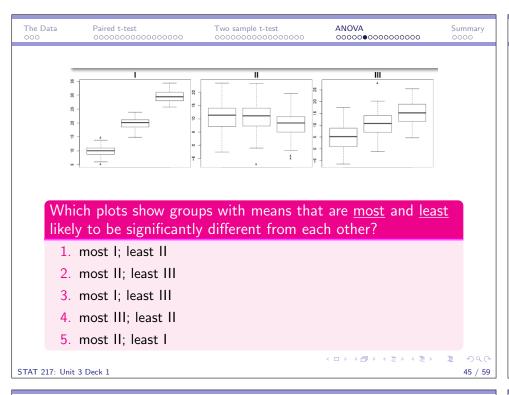
► We have already learned a hypothesis test for comparing two population means (two-sample *t*-test)

 $H_0: \mu_1 = \mu_2$ $H_a: \mu_1 \neq \mu_2$

► When we are interested in comparing >2 groups (and hence, >2 means) we can use ANOVA (analysis of variance)

 $H_0: \mu_1 = \mu_2 = \mu_3 = \dots \mu_g$ for g groups

 H_a : at least one mean is different than the others



ANOVA The Data Paired t-test Two sample t-test Summary 000000 0000000000

Conclusion

 $H_0: \mu_1 = \mu_2 = \mu_3 = \dots \mu_g$ vs

 H_a : at least one mean different than the others

If p-value $> \alpha$

- ightharpoonup fail to reject H_0
- there is not sufficient. evidence to suggest that population means differ significantly
- there is no evidence of an association between the two variables

If p-value $< \alpha$

- ightharpoonup reject H_0
- there is evidence that at least one population means differs from the others
- there is evidence of an association between the two variables
- cannot determine which population means differ (yet)

STAT 217: Unit 3 Deck 1

46 / 59

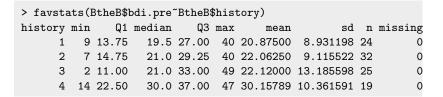
The Data Two sample t-test Summary 000000000000000

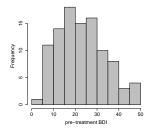
Conditions

- 1. observations are independent (in each of the g groups) This means that the baseline depression scores are independent from patient to patient within each of the four patient history groups.
- 2. normal underlying population distribution OR n > 30 in each group
 - This means that the baseline depression scores are approximately normally distributed OR $n \ge 30$ in each of the four patient history groups.
- 3. each group has (about) the same variability This means that the standard deviation of the baseline depression scores is about the same in each of the four patient history groups.

Two sample t-test Summary 000000000000000

Checking conditions





48 / 59 STAT 217: Unit 3 Deck 1

The Mechanics

For ANOVA...

you do need to know

- ▶ how to set up H_0 and H_a
- ▶ state a conclusion regarding H₀ and H_a based on the p-value

you don't need to know

- how to calculate the test statistic
- how to shade areas for the p-value



STAT 217: Unit 3 Deck 1

STAT 217: Unit 3 Deck 1

Two sample t-test AN

ANOVA 000000000000000000000 Summary

Multiple Comparisons

- When you reject $H_0: \mu_1 = \mu_2 = \mu_3$ in one-way ANOVA, it is of interest to determine exactly which means differ and to what extent they differ
- ► This results in *pairwise comparisons*. If you have 4 groups, there are 6 pairwise comparisons:
 - 1. group 1 vs group 2
 - 2. group 1 vs group 3
 - 3. group 1 vs group 4
 - 4. group 2 vs group 3
 - 5. group 2 vs group 4
 - 6. group 3 vs group 4
- For each comparison, we can answer this by either testing $H_0: \mu_1 = \mu_2$ or by calculating a confidence interval for $\mu_1 \mu_2$

Results in R

 $H_0: \mu_1 = \mu_2 = \mu_3 = \mu_4$ vs H_a : at least one mean differs

- > results <- aov(BtheB\$bdi.pre ~ BtheB\$history)
 > summary(results)
- Df Sum Sq Mean Sq F value Pr(>F)
 BtheB\$history 3 1118 372.8 3.404 0.0208
 Residuals 96 10516 109.5

The p-value is 0.0208. What is your conclusion?

- 1. reject H_0 ; we have evidence that the mean BDI differs in all 4 history groups
- 2. reject H_0 ; we have evidence that at least one mean BDI differs from the others
- 3. fail to reject H_0 ; we have evidence that the mean BDI is the same in all 4 history groups
- 4. fail to reject H_0 ; we do not have evidence that the mean BDI differs in the 4 history groups

50 / 59

52 / 59

The Data	Paired t-test	Two sample t-test	ANOVA	Summary
000	000000000000000	000000000000000	0000000000000000	0000

BUT...

STAT 217: Unit 3 Deck 1

But this means we are doing *multiple* testing, or calculating *multiple* confidence intervals

- ▶ this inflates the *overall* Type I error rate of the multiple tests taken together
- ▶ this deflates the *overall* coverage of the confidence intervals taken together

Number of tests	Chance of at least one Type I	error		
1	5%			-
3	14.3%			
5	22.6%			
10	40.1%			
20	64.2%			
50	92.3%			
100	99.4%			
	< □ > < ②		₽	990

The Data Paired t-test Two sample t-test ANOVA Summary 00000000000000000

Multiple testing techniques

- ▶ The goal of multiple testing/confidence interval techniques is to **control** the overall Type I error rate in a set of tests or the overall confidence level in a set of confidence intervals
- ► There are many techniques available
 - Fisher method
 - Bonferroni method
 - ► Tukey method
- ► For STAT 217, we will utilize the **Tukey method** for confidence intervals for pairwise comparisons.
 - gives overall confidence level very close to desired level
 - confidence intervals are slightly narrower than other methods
 - the formula is complex and you do not need to know it
 - you can get the results in R

200

53 / 59

Multiple Comparisons Results > TukeyHSD(results) > plot(TukeyHSD(results)) diff lwr upr p adj 2-1 1.187500 -6.2017875 8.576787 0.9749056 3-1 1.245000 -6.5750868 9.065087 0.9755714 4-1 9.282895 0.8797670 17.686022 0.0243165 3-2 0.057500 -7.2468503 7.361850 0.9999968 4-2 8.095395 0.1699716 16.020818 0.0433700 4-3 8.037895 -0.2906418 16.366431 0.0626362 How many pairwise comparisons indicate differences between the population means? 0 1 2 3 4 5 6

Two sample t-test

ANOVA

00000000000000000

Summary

54 / 59

The Data Two sample t-test Summary 000000000000000

4-1 Results

STAT 217: Unit 3 Deck 1

diff lwr p adj 4-1 9.282895 0.8797670 17.686022 0.0243165

We have evidence of a difference in mean BDI score among patients in history group 4 versus 1. But is this meaningful?



STAT 217: Unit 3 Deck 1

The Data

Paired t-test

Summary

∢ロト∢御ト∢差ト∢差ト 差 56 / 59 55 / 59 STAT 217: Unit 3 Deck 1

◆□▶◆御▶◆恵▶◆恵▶○恵

The Data Paired t-test Two sample t-test ANOVA Summary

Interpreting the p-value

The *p*-value represents the **strength** of the **evidence**:

- ► small *p*-values mean you have strong evidence of an association between two variables
- ► small *p*-values do not mean you have evidence of a strong association between two variables
- large *p*-values mean there is no evidence of an association

Other measures represent the **strength** of the **association**:

▶ difference of means: $(\bar{x}_1 - \bar{x}_2)$

The **strength** of the **association** can help you assess if an observed difference is meaningful.



The Data Paired t-test Two sample t-test ANOVA **Summary**

Different methods

STAT 217: Unit 3 Deck 1

STAT 217: Unit 3 Deck 1

Method	Use	Variables	Estimation	Testing
Single mean	quantitative response	one quantitative variable	CI for μ	H_0 : $\mu = \mu_0$
(one-sample t-test)	in single group			
*Two means	quantitative response	one quantitative variable and	CI for $\mu_1 - \mu_2$	H_0 : $\mu_1 = \mu_2$
(two-sample t-test)	in two groups	one categorical variable		
Dependent means	quantitative response	two paired	CI for μ_d	$H_0: \mu_d = 0$
(paired t-test)	measured on same observation	quantitative variables		
*ANOVA	quantitative response	one quantitative variable and	Tukey pairwise	$H_0: \mu_1 = \mu_2 = \cdots = \mu_g$
	in > 2 groups	one categorical variable	intervals	-

^{*}The starred methods can answer the question "Is there an association?" If we reject H_0 , then we conclude that some sort of association is present in the two variables.

4 D > 4 B > 4 E > 4 E > 9 C

The Data Paired t-test Two sample t-test ANOVA Summary

A researcher investigated if eye color of the mother (brown vs blue) is associated with birth weight of a baby (in pounds).

```
Two Sample t-test

data: dat$bwt by dat$eye
t = 2.7272, df = 29998, p-value = 0.006391
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval:
0.00888031 0.054255550
sample estimates:
mean in group blue mean in group brown
7.543471 7.511903
```

What is the best conclusion from this analysis? We (do/do not) have strong evidence that weight of babies differs by mother's eye color, and the effect of eye color is (strong/weak).

- 1. do; strong
- 2. do not; strong
- 3. do; weak
- 4. do not; weak

STAT 217: Unit 3 Deck 1 58 / 59