

Definition of Terms

Relations

- Schema: Collection of attributes (table header)
- Degree/arity: number of attributes in the schema/number of columns
- Cardinality: number of rows
- Constraints: Ensuring the validity of the instance
- Relational database schema: A collection of all schemas

Keys

- Superkey: A set of attributes that can uniquely identify rows in a relation
- Key: Minimal superkey; cannot remove extra attributes from the superkey
- Candidate keys: all possible keys
- Prime attribute: an attribute within any of the candidate keys
- Primary key: the chosen candidate key
- Foreign key: If (A, B) refers to (C, D), then (C, D)
 - Must be a candidate key and
 - (a, b or both are NULL) OR ((a, b) exists in (C, D))

NULL

- Unknown value: neither true nor false
- NULL and NULL = NULL; NULL or NULL = NULL
- NULL or FALSE = NULL; NULL and TRUE = NULL
- NULL + x = NULL; NULL > x = NULL
- (NULL == NULL) = NULL; (NULL != NULL) = NULL
- (NULL === NULL) = TRUE (not distinct from); (NULL !== NULL) = FALSE (distinct from)

Relational Algebra

- Selection, sigma ($\sigma_{condition}$): filters rows
- Projection, pi ($\pi_{col1,col2}(relation)$): chooses columns
- Renaming, rho ($\rho_{newName}(relation)$): renames tables/columns

Table Creation

Create table

```
CREATE TABLE table1 (
  col1 INTEGER PRIMARY KEY,
  col2 VARCHAR NOT NULL DEFAULT 'some default',
  col3 INTEGER REFERENCES table2(foreign_col),
  FOREIGN KEY (col1, col2) REFERENCES table3(col1, col2) ON
  DELETE CASCADE,
  UNIQUE (col1, col3),
  CHECK (col1 > 0)
);
```

Foreign key actions

- ON DELETE/UPDATE
 - CASCADE : propagates action to all referencing tuples
 - SET DEFAULT : set to default value if possible
 - SET NULL : set to NULL value if possible

Constraints reject on FALSE (accepts NULLs)

Conditions accept on TRUE (rejects NULLs)

Table Modification

Alter

```
ALTER TABLE table1
ADD COLUMN col4 INTEGER,
DROP COLUMN col3,
ADD UNIQUE (col4),      -- table constraint
DROP CONSTRAINT constraint_name;
```

Insert

```
INSERT INTO table1 (col1, col2, col3) VALUES (1, 'New value', 3),
(2, 'Second', 4);
```

Delete

```
DELETE FROM table1 WHERE col1=1 AND col2='New value';
DELETE FROM table1 WHERE col1 < 0;
```

Update

```
UPDATE table1 SET col2='Alice' WHERE col1=2;
```

Join Operations

Inner join ⋈

```
SELECT * FROM t1 INNER JOIN t2 ON t1.col1 = t2.col1;
```

- Selects records that have matching values

Natural join

```
SELECT * FROM t1 NATURAL JOIN t2;
```

- Selects records that have matching values, no need to specify which column and does not repeat joined column

Left outer join ⋈_L

```
SELECT * FROM t1 LEFT JOIN t2 ON col1=col2;
```

- Selects all records from left table, and matched records from right table, appends NULL values if no match in right table

Right outer join ⋈_R

- Opposite of left outer join

Full outer join ⋈_F

- Similar to other outer joins, puts NULL values on both left and right tables

Set Operations

Union/union all

- Combines the 2 result sets
 - Same number of columns, same or more rows
- UNION ALL: keeps duplicates

Intersect/intersect all

- Selects rows that are the same between 2 tables
 - Same number of columns, same or less rows
- INTERSECT ALL: keeps duplicates

Except/except all

- Selects rows that are in t1 but not t2
 - Same number of columns, same or less rows
- EXCEPT ALL: weird, don't really use it

Querying

Operators

+ - * / % ^ !	
& << >>	Bitwise expressions
/ / @	Square root, cube root, abs
> >= < <= == != or <>	Comparators
	String concatenation
char_length	Number of characters
substring(coll, start, end)	Extract a substring
AND OR NOT IS NULL IS NOT NULL	

Basic query

```
SELECT DISTINCT t1.col1 AS first, t2.col1 AS second
FROM table1 t1, table2 t2
WHERE t1.col1 = t2.col2
AND t1.col1 > 3;
```

Pattern matching

```
SELECT * WHERE col1 LIKE '_ab%'
```

- _ matches 1 char length
- % matches 0 or more characters
- 'ab' matches exact characters

Null if

```
SELECT NULLIF(col1, 3), col2 FROM table1;
```

- Returns NULL if col1=3, else it returns the value of col1

Coalesce

```
SELECT COALESCE(col1, col2, col3) FROM table1;
```

- Returns the first non-null attribute

Case analysis

Syntax

```
CASE
  WHEN col1 < 0 THEN 'sm'
  WHEN col1 < 3 THEN 'md'
  ELSE 'lg'
END;
```

Example in Select

```
SELECT OrderID,
CASE
  WHEN Quantity > 30 THEN 'Quantity is greater than 30'
  ELSE 'Quantity is less than or equal to 30'
END AS Description
FROM Orders;
```

Example in Order By

```
SELECT Name, Gender
FROM Customers
ORDER BY
  CASE WHEN Gender = 'F' THEN Name END DESC,
  CASE WHEN Gender = 'M' THEN Name END ASC;
```

Aggregate functions

```
SELECT MIN(coll) AS Minimum, MAX(coll) AS Maximum FROM table1;
```

function	If empty	If all NULL	meaning
MIN(A)	NULL	NULL	Min value of A
MAX(A)	NULL	NULL	Max value of A
SUM(A)	NULL	NULL	Sum of all values in A
COUNT(A)	NULL	NULL	Count of non-NULL values
AVG(A)	0	0	Average of values (sum/count)
COUNT(*)	0	N	Number of rows in the table
AVG(DISTINCT A)			Average of distinct values in A
SUM(DISTINCT A)			Sum of distinct values in A
COUNT (DISTINCT A)			Count of distinct, non-NULL values

Grouping (with aggregate function)

```
SELECT * FROM table1 GROUP BY col1, col2;
```

- Divides rows into groups where all values on (col1, col2) are the same; on each group
- Use HAVING instead of WHERE (if using aggregate functions in conditions)
 - HAVING is computed after the GROUP BY function; WHERE is computed before
- Restrictions
 - Either a candidate key appears in GROUP BY, or
 - For each attribute A in the SELECT statement, either
 - A appears in GROUP BY, or
 - A appears in an aggregate function in SELECT

Exists

```
SELECT * FROM table1
WHERE EXISTS (SELECT 1 FROM table2 WHERE col1=table1.col1);
```

- Exists returns TRUE as long as the result of the query is non-empty (at least 1 row)
- Opposite: NOT EXISTS

In

```
SELECT * FROM table1
WHERE col1 IN (SELECT col1 FROM table2);
```

- Returns TRUE if the value of col1 is in the result of the query

Any

```
SELECT * FROM table1
WHERE col1 < ANY (SELECT col1 FROM table2);
```

- Returns TRUE if the value satisfies the relational operation with any of the results

All

```
SELECT * FROM table1
WHERE col1 < ALL (SELECT col1 FROM table2);
```

- Returns TRUE if the value satisfies the relational operation with all of the results

Sorting

```
SELECT * FROM *
ORDER BY col1 ASC, col2 DESC
OFFSET m
LIMIT n;
```

- Orders by col1 ASC overall, col2 DESC within each equal col1 block
- Shows from the mth result, limits to n results ([m, ..., m+n-1] results)

Order of operations

FROM, WHERE, GROUP BY, HAVING, SELECT, ORDER BY, LIMIT/OFFSET

- Subqueries can contain a reference to a result/alias in a parent statement

Common Table Expressions (CTEs)

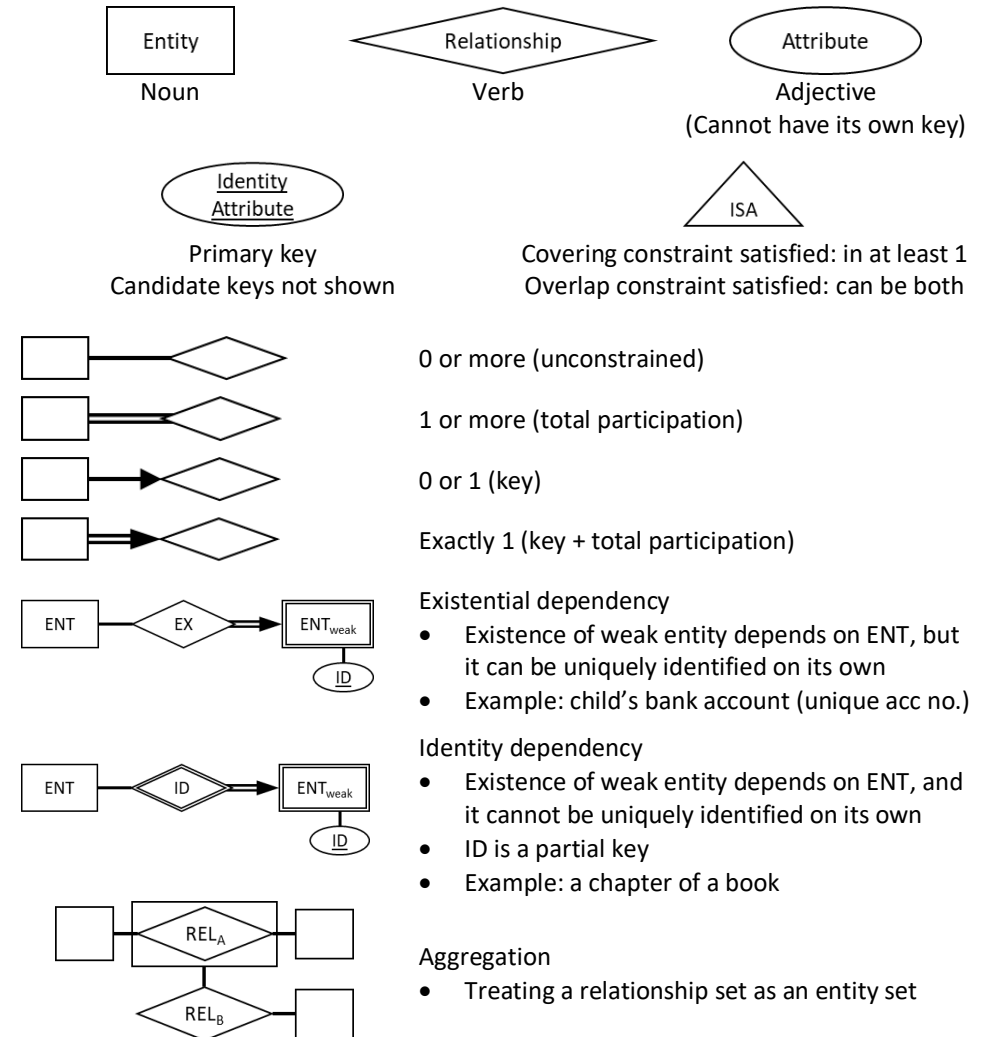
```
WITH
    table1 AS (SELECT * FROM ...),
    table2 AS (SELECT * FROM ...)
SELECT * FROM table1, table2;
```

- Declarative way of computing and storing queries sequentially

Views

- Used only for querying
 - Can be for privacy reasons, can be to compute attributes dynamically, can be for computing ISA (students view where students = undergrads + grads)
 - A virtual table that is dynamically computed each time
- ```
CREATE VIEW view1(first, second) AS
 SELECT col1, col2 FROM table1;
```

## ER Diagrams



## Functional Dependencies (notation: A - single attribute, a - set)

### Definitions

- $a \rightarrow b$ 
  - a uniquely identifies all attributes in b for all valid relation instances
- Triviality of  $a \rightarrow b$ 
  - Trivial iff  $b \subseteq a$
  - Completely non-trivial if  $b \not\subseteq a$  AND  $a \cap b = \emptyset$
- Minimal cover
  - Minimal set of functional dependencies, with each in the form  $a \rightarrow A$
  - At least one FD always exists
  - Method of finding minimal cover
    - Remove attribute redundancy (removing A,  $(a - A) \rightarrow b$ , does not change F)
    - Remove FD redundancy (removing  $a \rightarrow b$  does not change F)

### Attribute closure

- $a^+ =$  attribute closure of a
  - All the attributes that can be uniquely identified by a
  - $a^+ = \{ A \text{ in relation } R \mid F \models a \rightarrow A \}$

### Armstrong's axioms

- Reflexivity
  - $a \rightarrow b$  for any  $b \subseteq a$
  - e.g.  $ABC \rightarrow AB$ ;  $A \rightarrow A$
- Augmentation
  - If  $a \rightarrow b$ , then  $ac \rightarrow bc$
- Transitivity
  - If  $a \rightarrow b$  AND  $b \rightarrow c$ , then  $a \rightarrow c$

### Extended Armstrong's axioms

- Union
  - If  $a \rightarrow b$  AND  $a \rightarrow c$ , then  $a \rightarrow bc$
- Decomposition
  - If  $a \rightarrow b$  AND  $c \subseteq b$ , then  $a \rightarrow c$
  - e.g.  $AB \rightarrow CDE$ , so  $AB \rightarrow C$

### Obtaining 3NF DP, LJ preserving decomposition from minimal cover

1. Create schema for each FD in minimal cover (eg  $A \rightarrow BC$ :  $R(ABC)$ )
2. Create i+1th schema for a key (eg if key is BD:  $R(BD)$ )
3. Remove schema subsets

## Schema Decomposition

### Definitions

- Decomposing relation R into fragments such that
  - $R = R_1 \cup R_2 \cup \dots \cup R_n$
- FD projection
  - $F[R_1] = \{ \text{all } a \rightarrow b \text{ in } F^+ \text{ of } R \mid ab \subseteq R_1 \}$

### Properties

- Lossless-join (LJ)
  - Information preserving join; after joining, will obtain original universal relation
  - Criteria for a lossless join decomp ( $R \rightarrow R_1, R_2$ )
    - If  $\text{attr}(R_1) \cup \text{attr}(R_2) = \text{attr}(R)$
    - If  $\text{attr}(R_1) \cap \text{attr}(R_2) \neq \emptyset$
    - If common attribute(s) are a superkey/key of either relation
  - For a completely non-trivial FD  $a \rightarrow b$ ,  $\{ R-b, ab \}$  is a LJ decomp (Corollary 1)
- Dependency preserving
  - After joining, all original FDs are preserved ( $F[R_1] \cup \dots \cup F[R_n] == F$ )

### Normal Forms

#### Boyce-Codd Normal Form (BCNF)

- No attribute is transitively dependent on any key
  - Every attribute is directly dependent on all keys
- R (or  $R_i$ ) is in BCNF if, for every  $a \rightarrow A$  in  $F^+$  (or  $F[R_i]$ )
  - $a \rightarrow A$  is trivial, or
  - a is a superkey
- Theorems
  - Any schema with exactly 2 attributes is in BCNF (Lemma 2)
  - There is always a valid LJ decomp where each fragment is in BCNF (Theorem 3)
  - There exists a schema that is not in BCNF which has no valid LJ + DP decomp such that each fragment is in BCNF (Theorem 4)
- To decompose to BCNF (only guaranteeing lossless)
  - Let  $a \rightarrow b$  be an FD that violates BCNF; decompose R to  $\{R_1(ab), R_2(R-b)\}$

#### Third Normal Form (3NF)

- No non-prime attribute is transitively dependent on any key
  - Every non-prime attribute is directly dependent on all keys
- R (or  $R_i$ ) is in 3NF if, for every  $a \rightarrow A$  in  $F^+$  (or  $F[R_i]$ )
  - It satisfies BCNF, or
  - A is a prime attribute
- Up to 3NF, it is always possible to get a valid LJ + dep preserving decomp (Theorem 5)