

Mechatronics (ROB-GY 5103 Section A)

- **Today's lecture:**
 - H-bridge
 - Control
 - Miscellaneous
- (See Topics #4 and #7 from Main Text for details)

Next Week

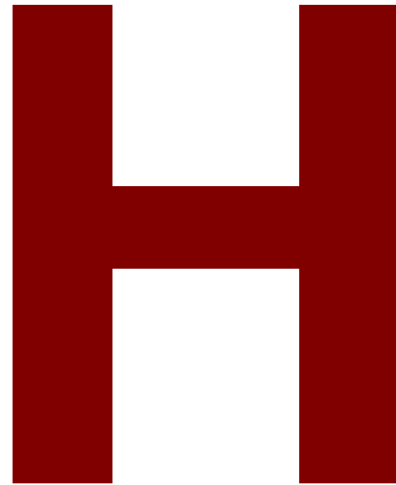
- **Final Exam (2:00 to 2:45)**
 - 45 minutes for 8 written questions
 - Only on content covered after midterm
- **Break/Intermission (2:45 to 3:00)**

Next Week

- **Early presentations (3:00 onwards)**
 - Presentations (~10-15 minutes followed by Q&A)
 - Must bring physical prototype to demonstrate
 - Submit your presentation files on Brightspace
 - I encourage you to present early!
 - [Sign up sheet here](#)
 - Indicate special accommodations
 - You can still submit project report on NYU Brightspace at the official deadline Dec 19.

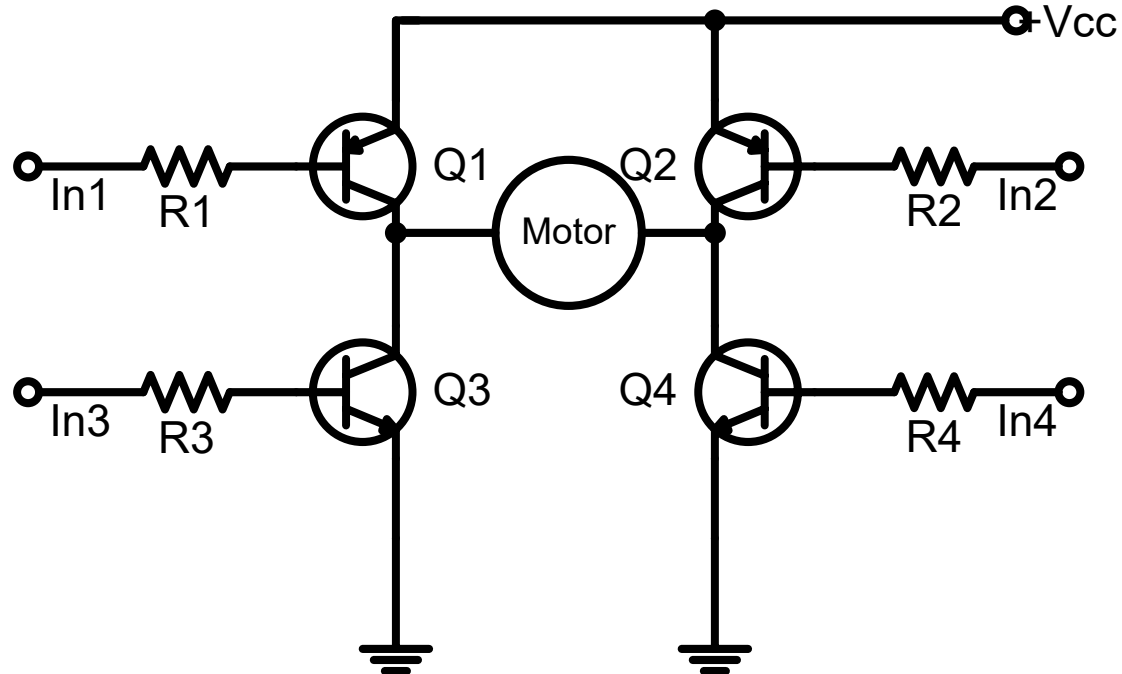
H-Bridge

- Why is it called an H-bridge (Full-bridge)?



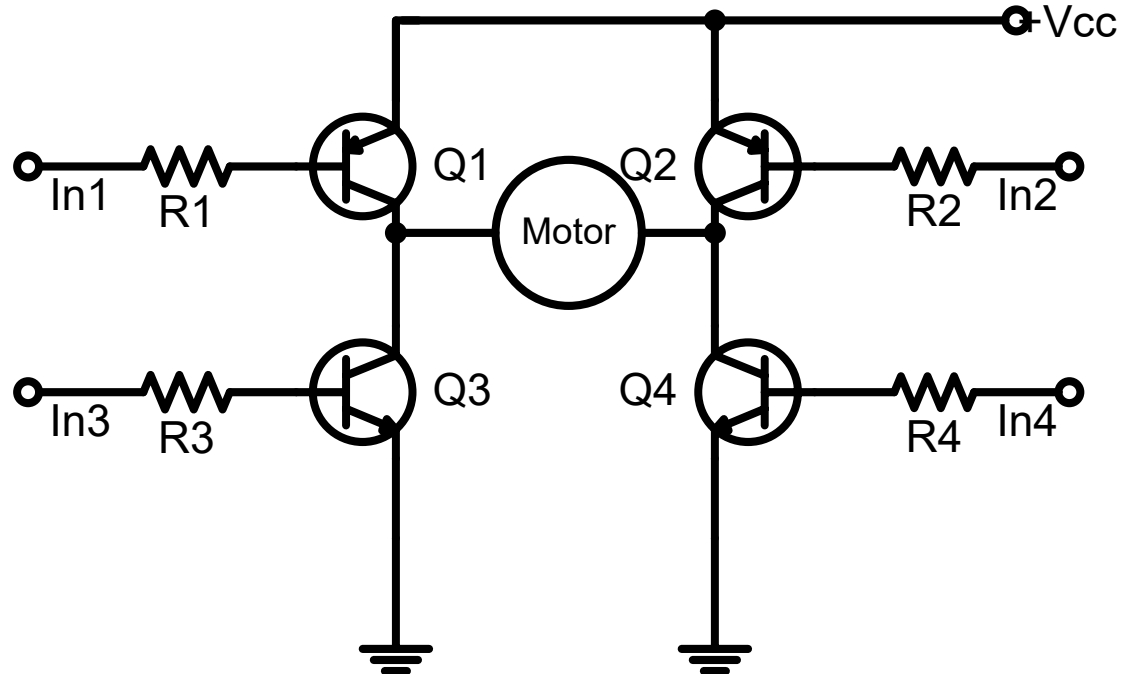
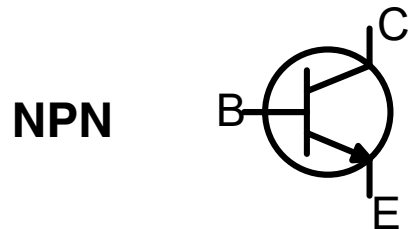
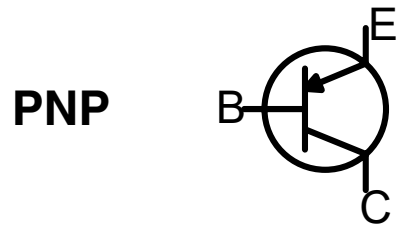
Full-Bridge: Version 1

- 4 BJTs, 1 voltage source, and a DC motor.
- Switches: transistors Q1-Q4.



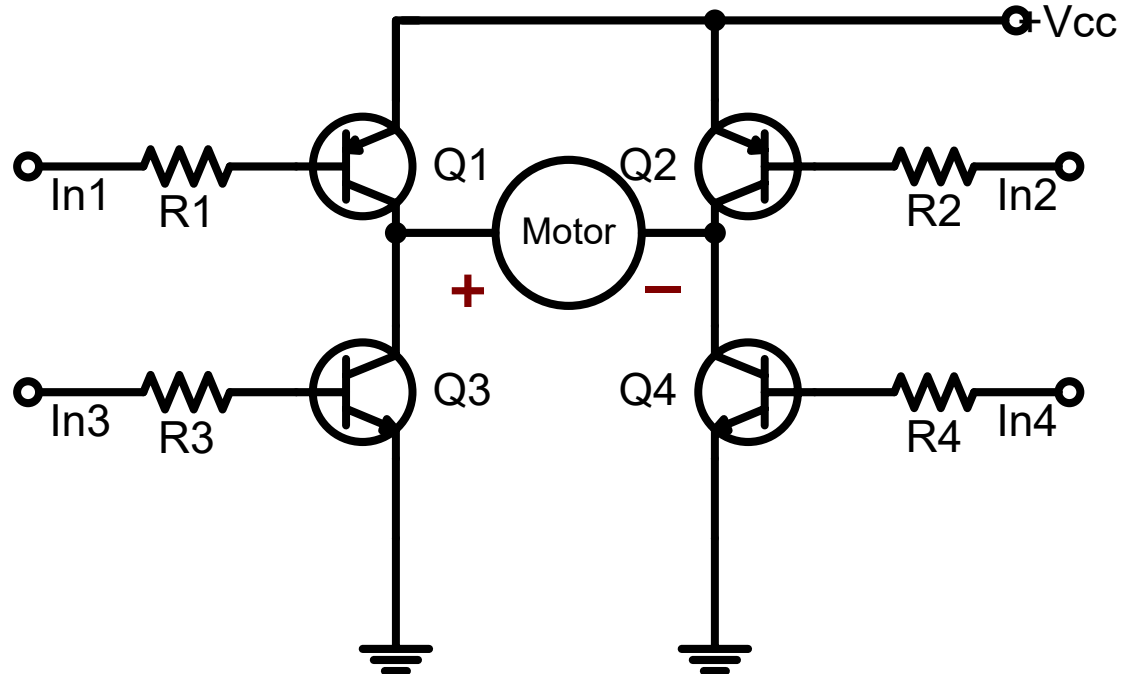
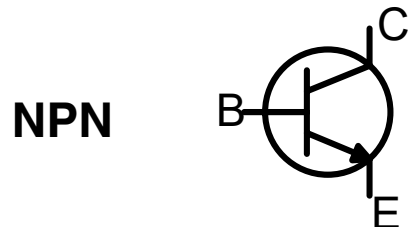
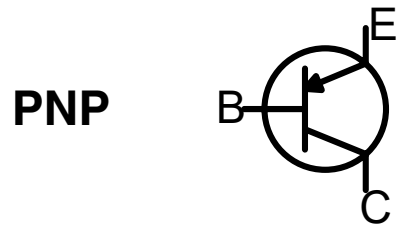
Full-Bridge: Version 1

- NPN transistor. **Normally off**. When base potential higher than emitter potential, collector-emitter pair conducts. $V_c > V_e$.
- PNP transistor. **Normally off**. When base potential is lower than emitter potential, emitter-collector pair conducts. $V_e > V_c$.



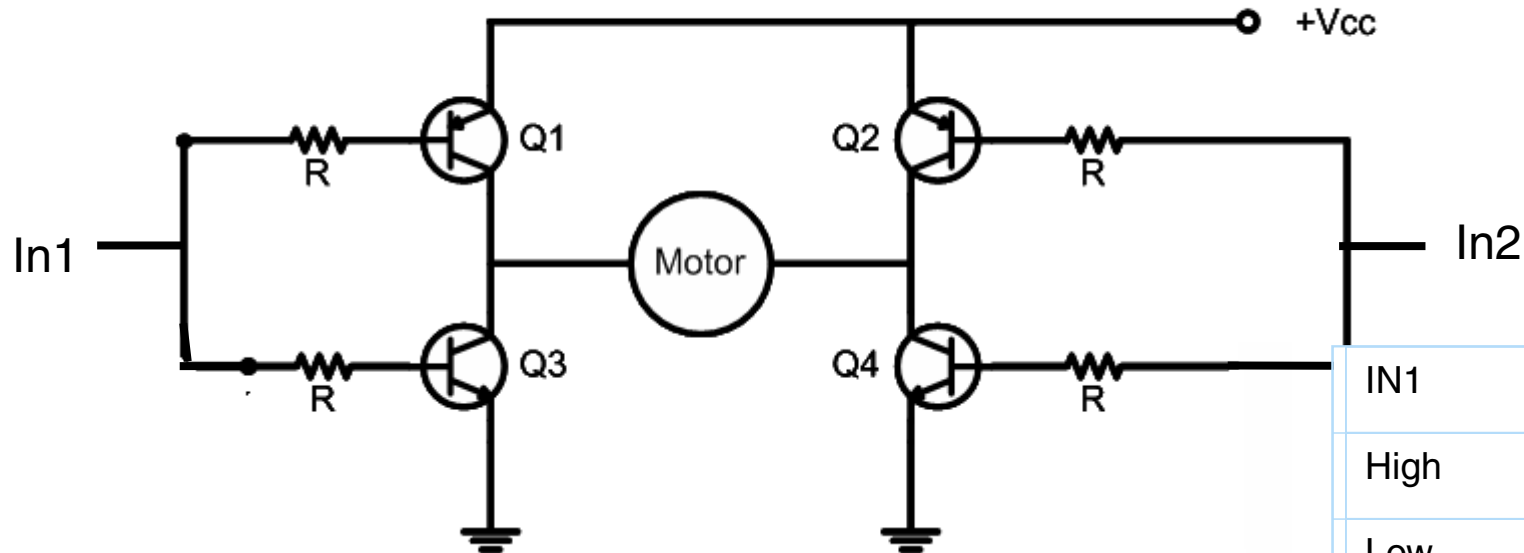
Full-Bridge: Version 1 (4 inputs)

- $V_{in1} \leq V_{cc} - 0.6V$ and $V_{in4} \geq 0.6V$: Motor turns forward.
- $V_{in2} \leq V_{cc} - 0.6V$ and $V_{in3} \geq 0.6V$: Motor turns backward.
- **4 inputs** are being used to appropriately switch the transistors.



Full-Bridge: Version 2 (2 inputs)

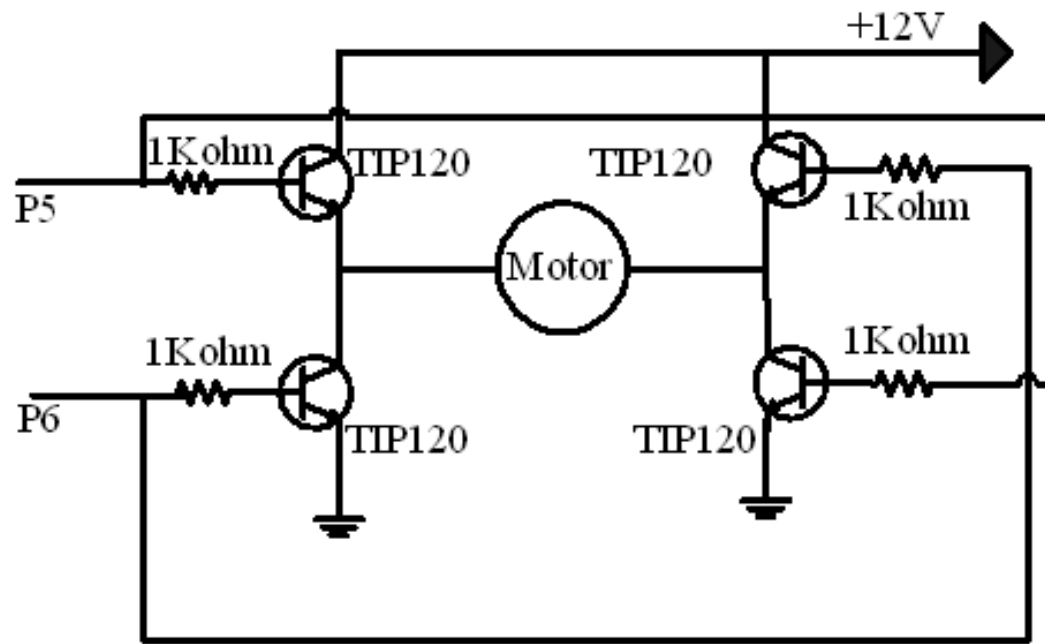
- **2 inputs** are being used to appropriately switch the transistors.



IN1	IN2	Motor	Notes
High	Low	Forward	
Low	High	Backward	
Low	Low	No motion	
High*	High*	*	Forbidden

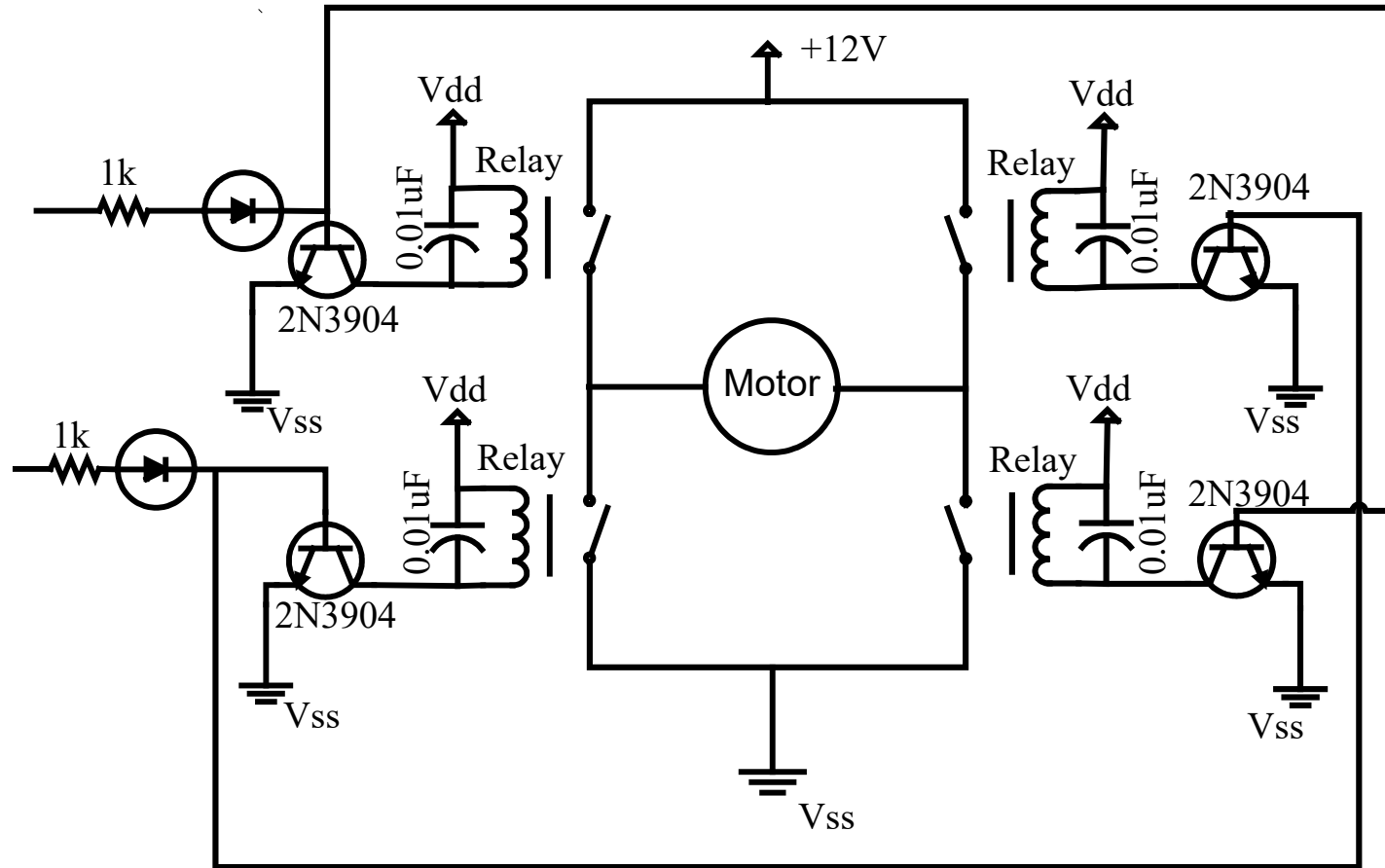
Full-Bridge: Version 3 (2 inputs)

- **2 inputs** are being used to appropriately switch the transistors.
 - Only NPN transistors



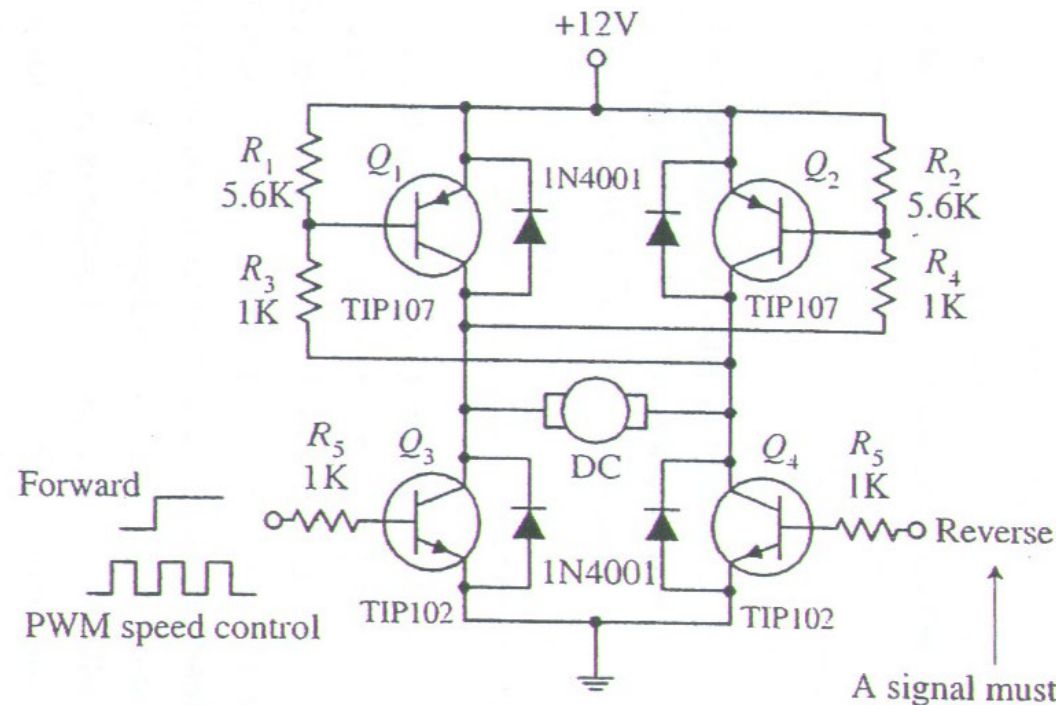
P5	P6	Motor	Notes
Positive	Ground	Forward	
Ground	Positive	Backward	
Ground	Ground	No motion	
Positive	Positive	*	Forbidden

H-bridge: Relays



H-bridge: BJTs

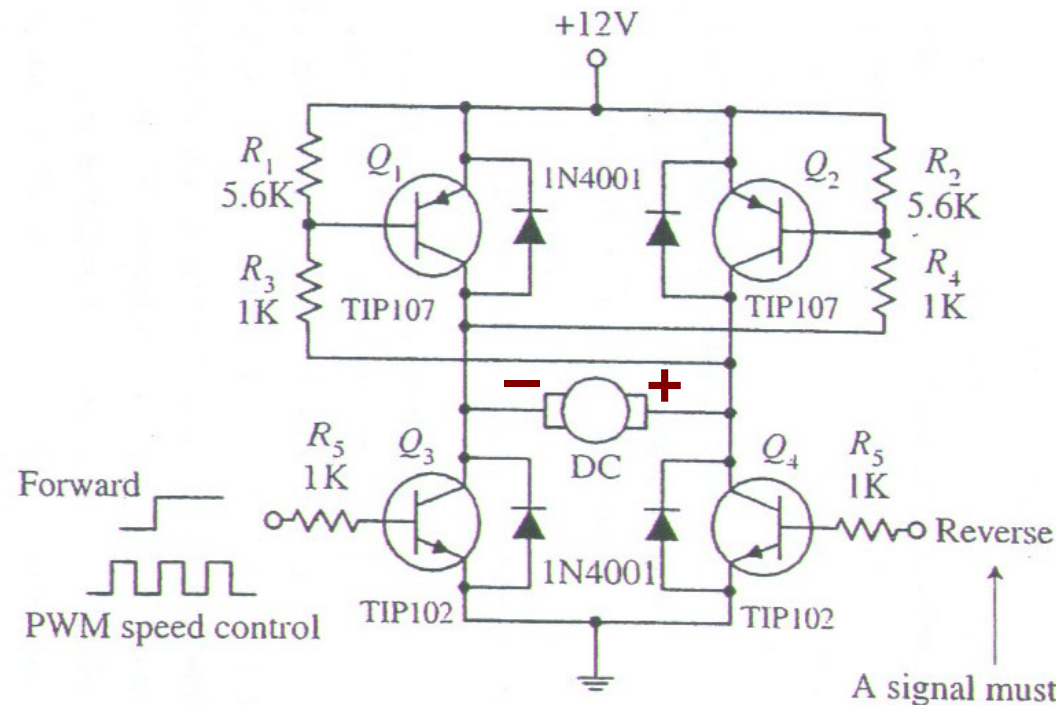
- Diodes are being used to prevent BJTs being damaged by inductive kickback.



A signal must not be applied here when a signal is being applied to the forward lead.

H-bridge: BJTs

- High signal enters Q3's base, Q3 conducts, which allows Q2 to conduct.
 - Current flows from +12 V supply through the motor from right to left (forward).
- To reverse the direction, remove High signal from Q3, and apply to Q4 instead.

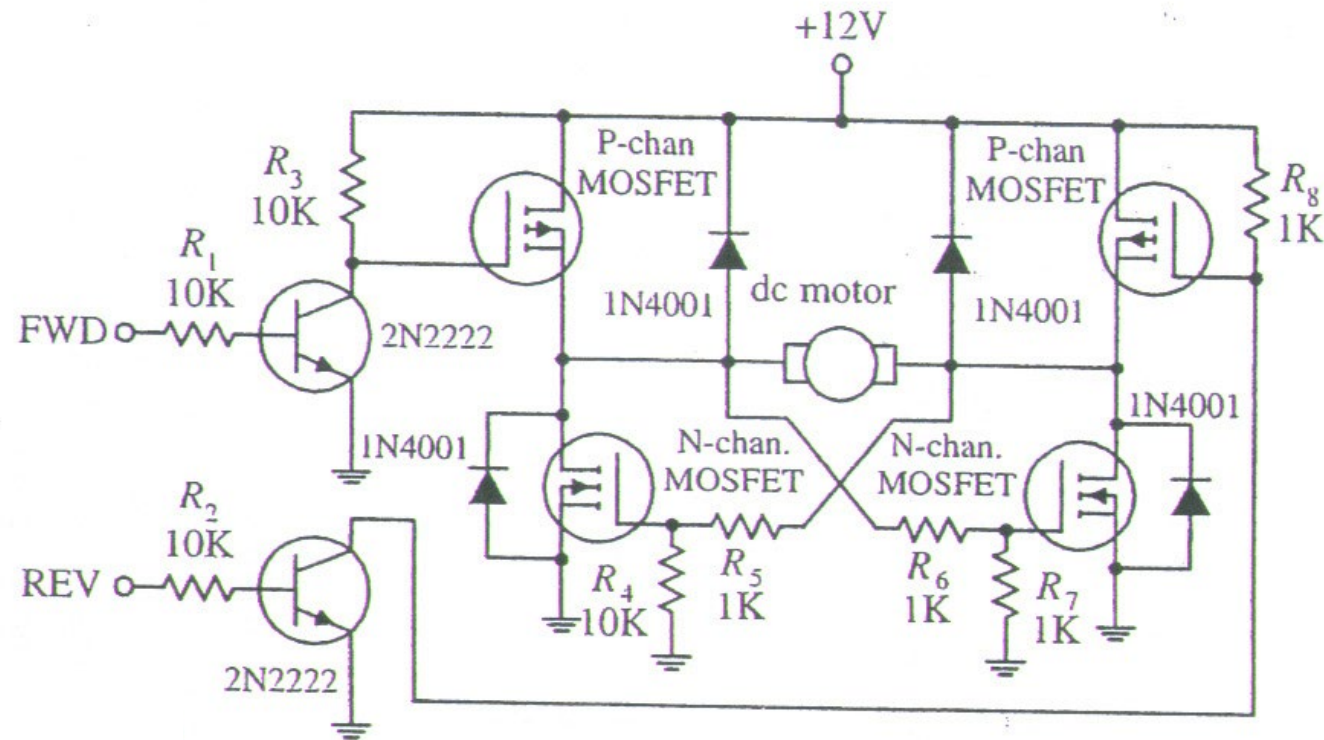


A signal must not be applied here when a signal is being applied to the forward lead.

A signal must r

H-bridge: MOSFETs

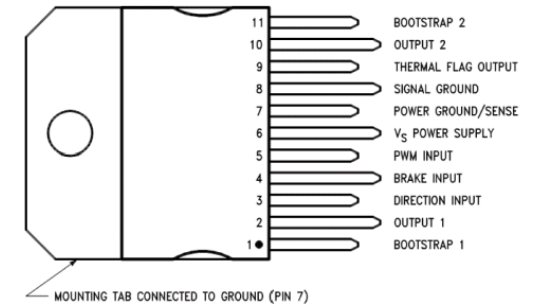
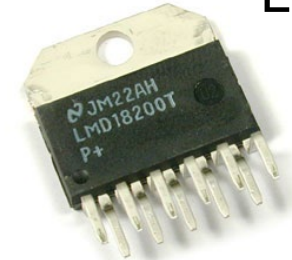
MOSFET H-Bridge



H-Bridge Motor Driver ICs

- Common H-Bridge solutions include:
 - National Semiconductor's LMD18200, LMD18201, LM15200
- LMD18200
 - High-current, easy-to-use H-bridge chip (3A, 12-55V).
 - TTL and CMOS compatible.
 - Comes with clamping diodes, shorted load protection, and a thermal warning interrupt output lead.
- L293D (Unitrode)
 - Very easy to use, cheaper than LMD18200
 - Can't handle as much current
 - Not many functions available.

LMD18200



LMD18201



L293D

Speed Control

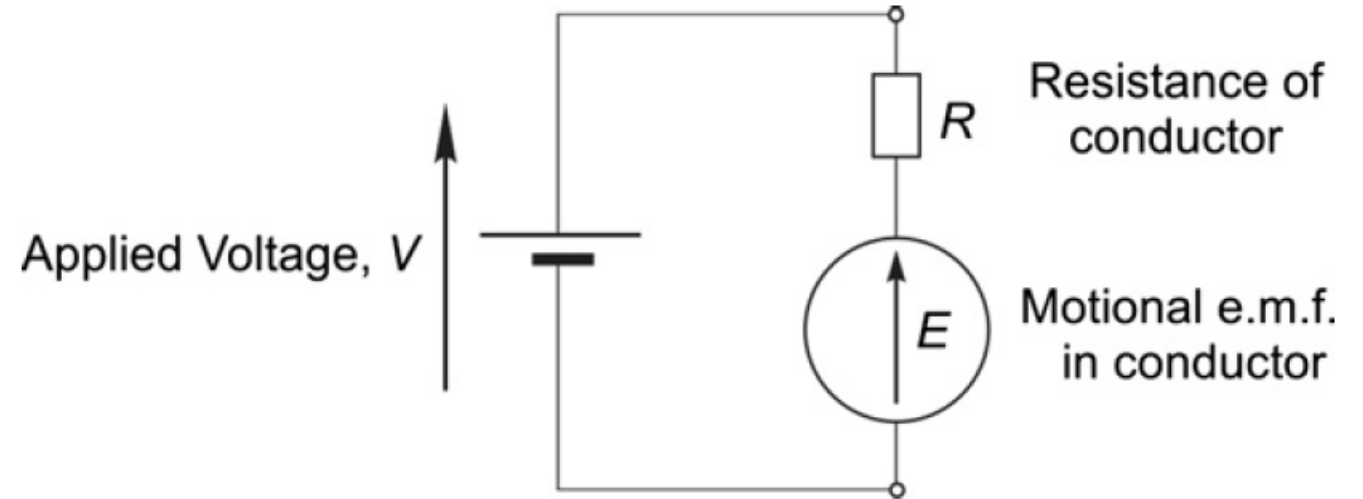
- Apply voltage to motor:
 - Lower than the nominal voltage → motor runs slower.
 - Larger than nominal voltage → motor runs faster.

Speed Control: DC motor dynamics

- Equivalent Circuit Model

$$V = E + IR$$

$$\tau = kI \quad E = k\omega$$



- E: Motional EMF or electromotive force)
- R: Motor Resistance
- I: Motor Current
- k: motor (torque) constant
- V: Applied Voltage (at motor terminals)

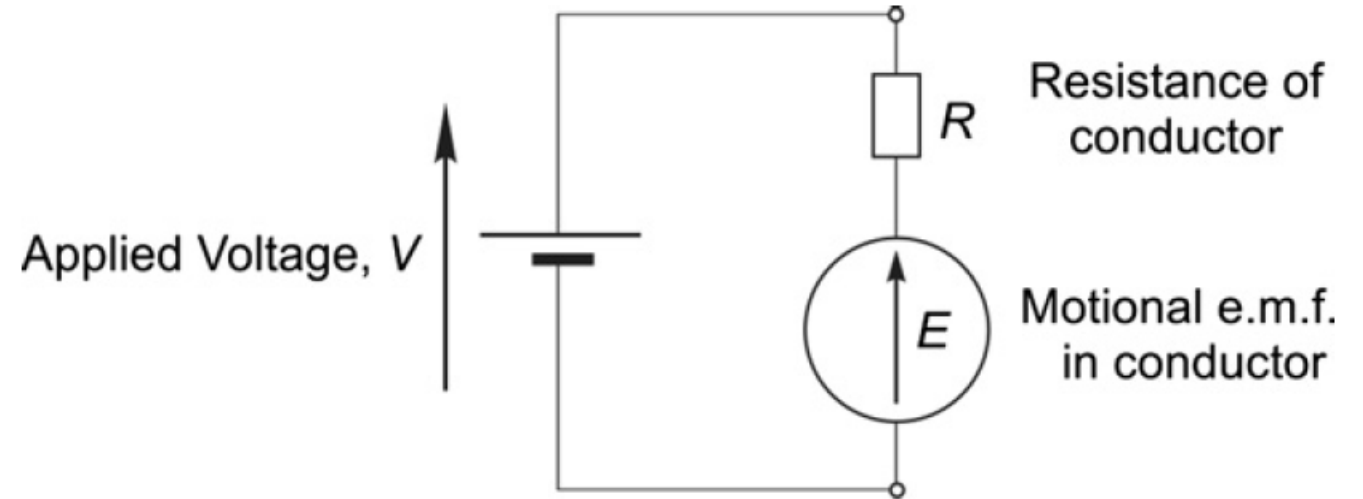
Speed Control: DC motor dynamics

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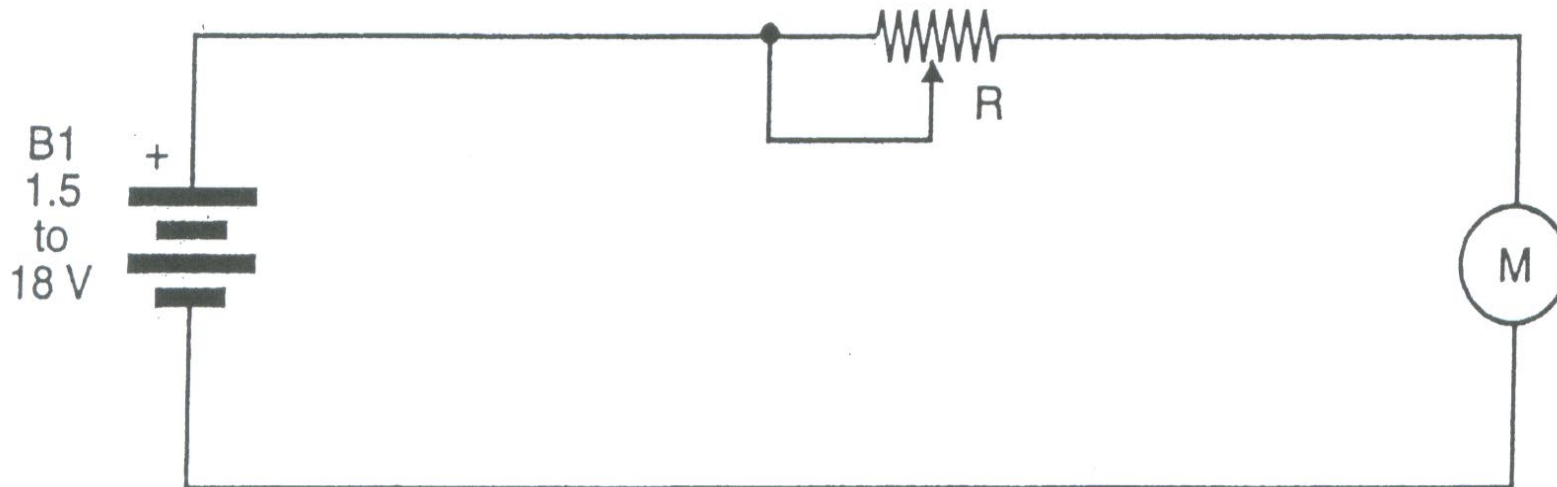
Lorenz Force **Faraday's law of induction**



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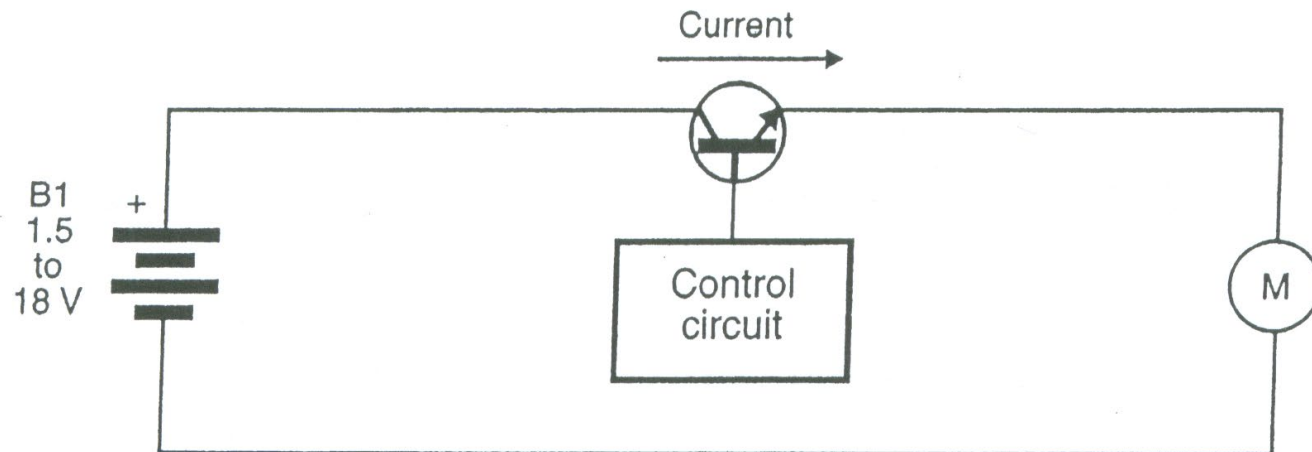
Speed Control: Potentiometer

- Despite the linearity of the control, don't do this. Not recommended.
- Highly inefficient:
 - Resistance wastes energy
- Use of pot as described does not allow soft start of the motor while keeping the torque constant. It leads to a hard start which may induce jerk behavior.



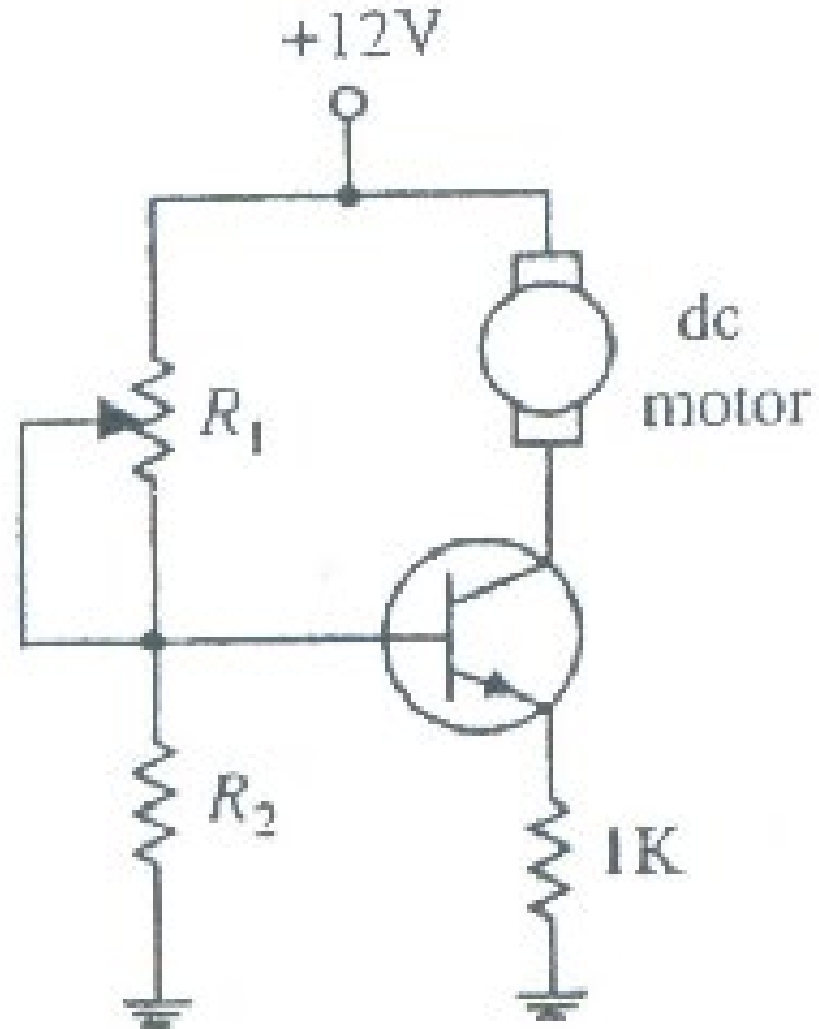
Speed Control: BJT

- Don't do this. Not recommended.
 - Base voltage/current changes the resistance across collector-emitter pair thus varying the current flow through the circuit connected through collector-emitter pair.
 - Now the BJT must dissipate heat.
 - Power dissipated by transistor = (voltage drop across transistor) x (current flow through the transistor)



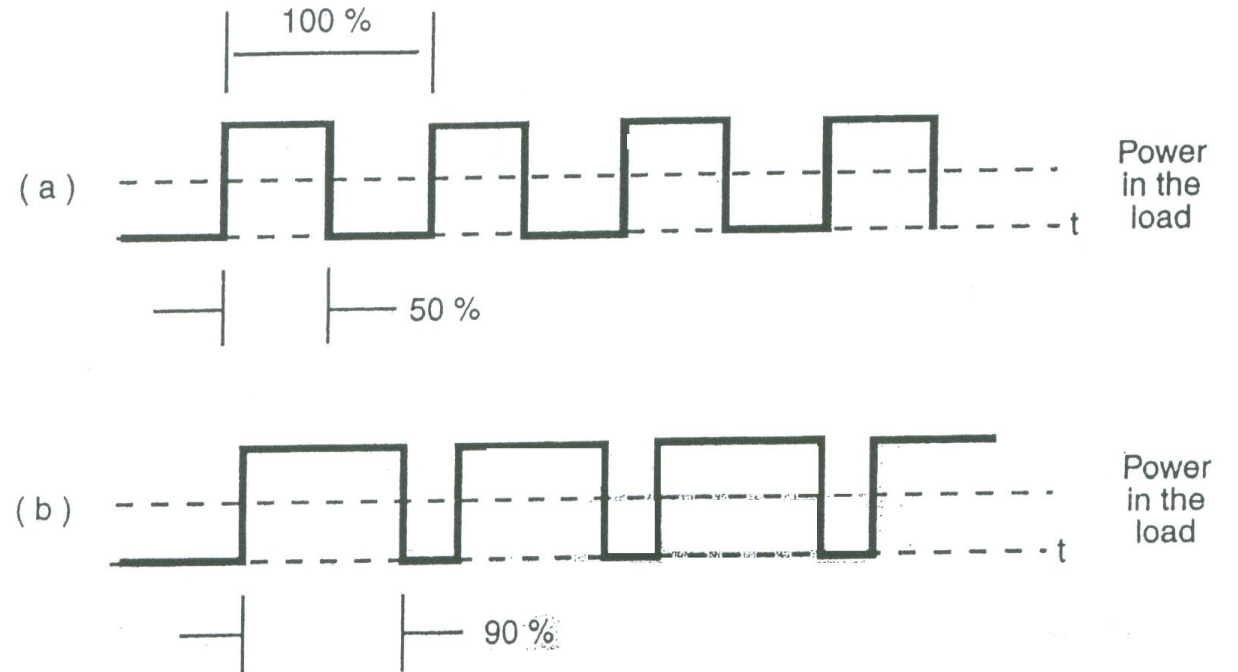
Speed Control: Potentiometer BJT

- Don't do this. Not recommended.



Speed Control: PWM

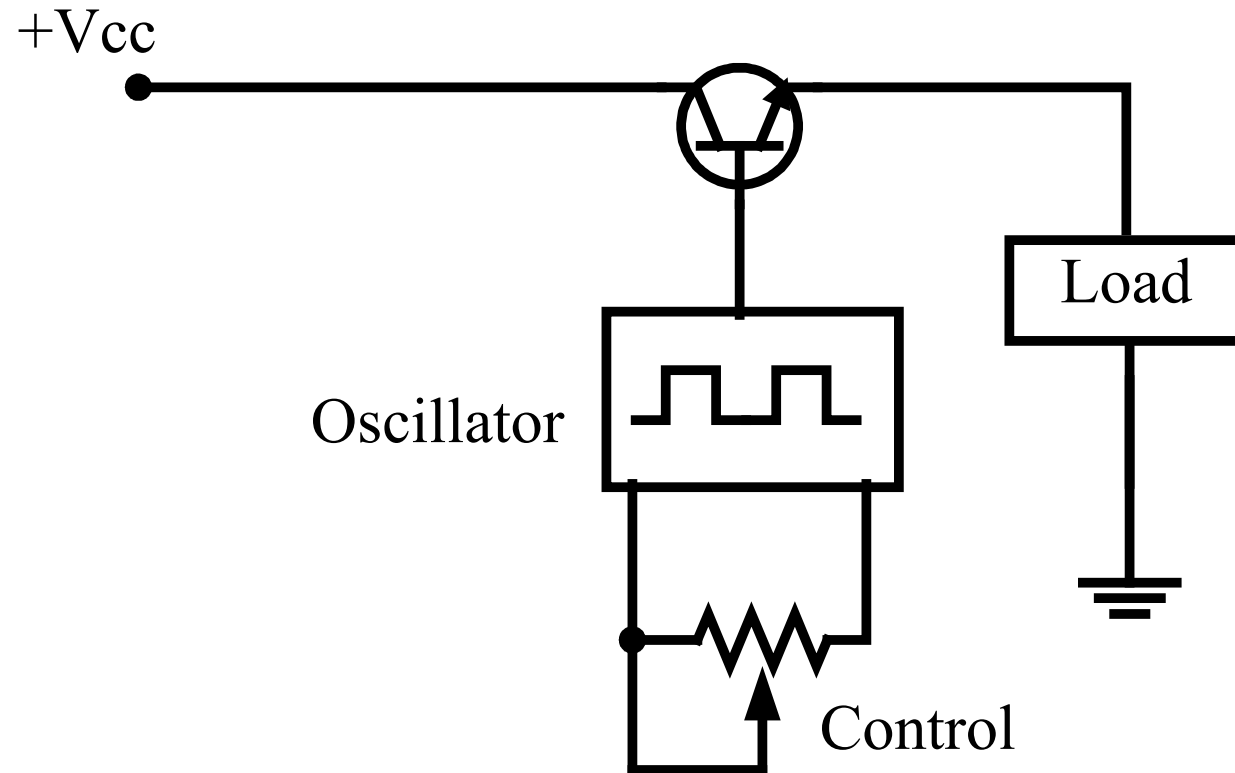
- Yes, please do this.
Recommended



The power depends on the pulse width

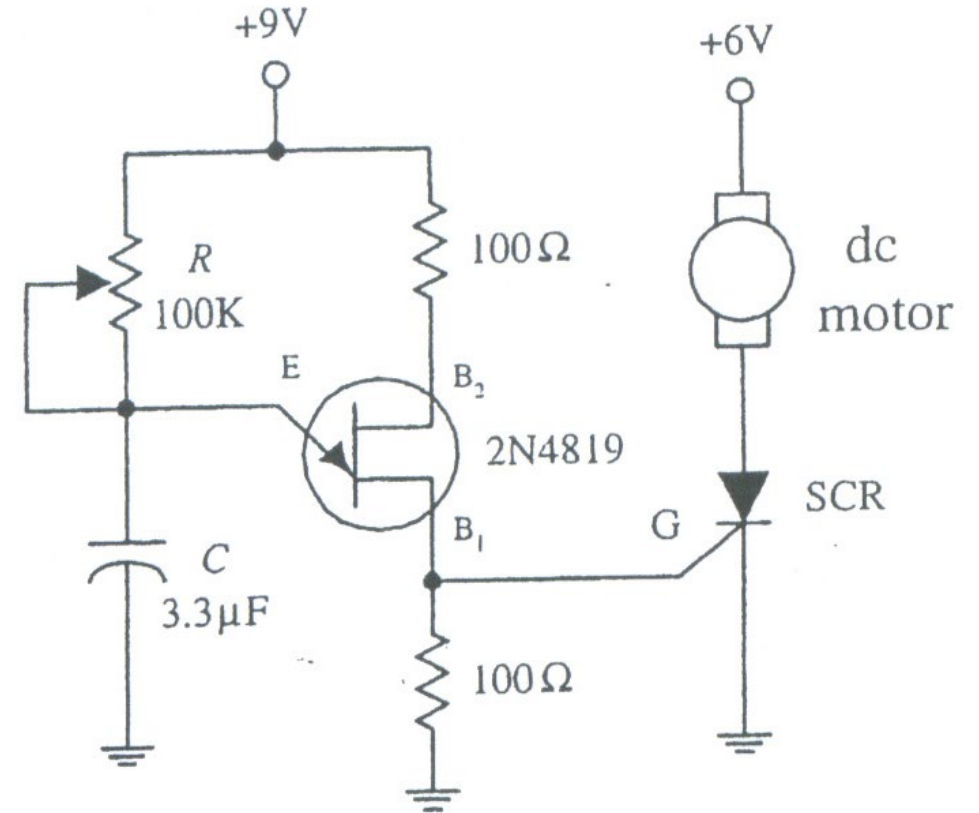
Pulse Width Modulator

- The output of a variable duty oscillator is fed to the control lead “base” of a power transistor.



DC Motor Speed Control using PWM: Version 1

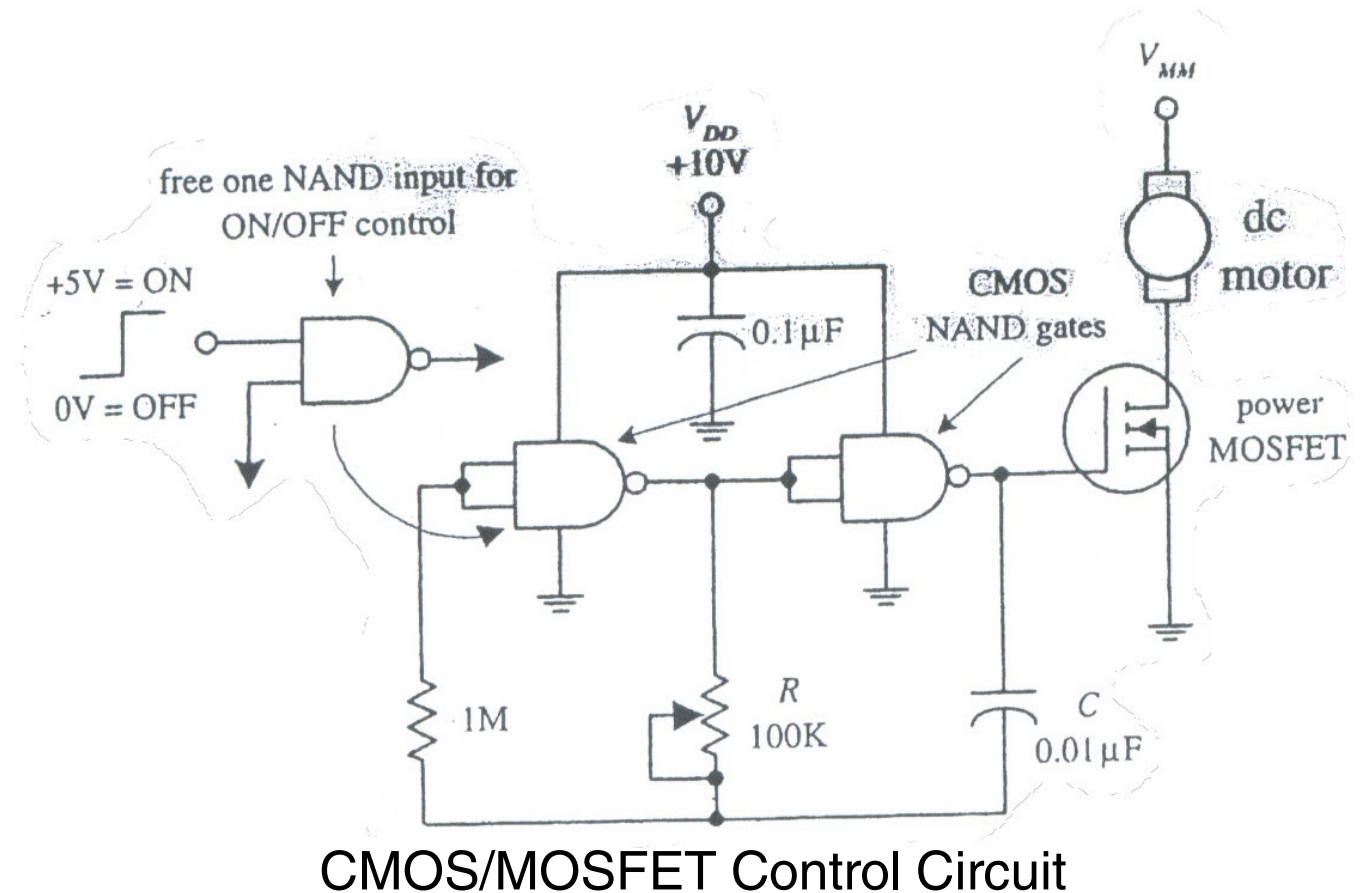
- Here a UJT relaxation oscillator is used to generate a series of pulses that drive an SCR on and off.
- To vary the speed of the motor, the UJT oscillator's frequency is adjusted by changing the RC time constant.



UJT/SCR Control Circuit

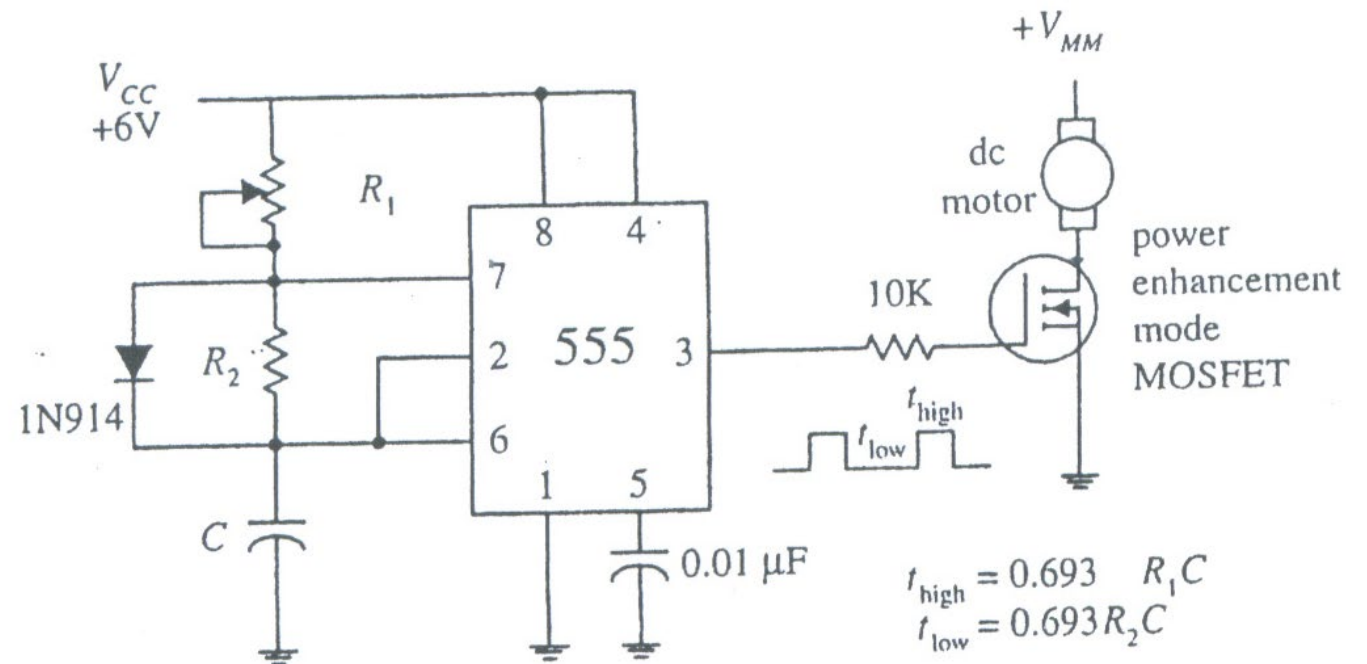
DC Motor Speed Control using PWM: Version 2

- A pair of NAND gates make up the relaxation oscillator section, while an enchantment-type power MOSFET is used to drive the motor.
- Like the preceding circuit, the speed of the motor is controlled by the oscillator's RC time constant.



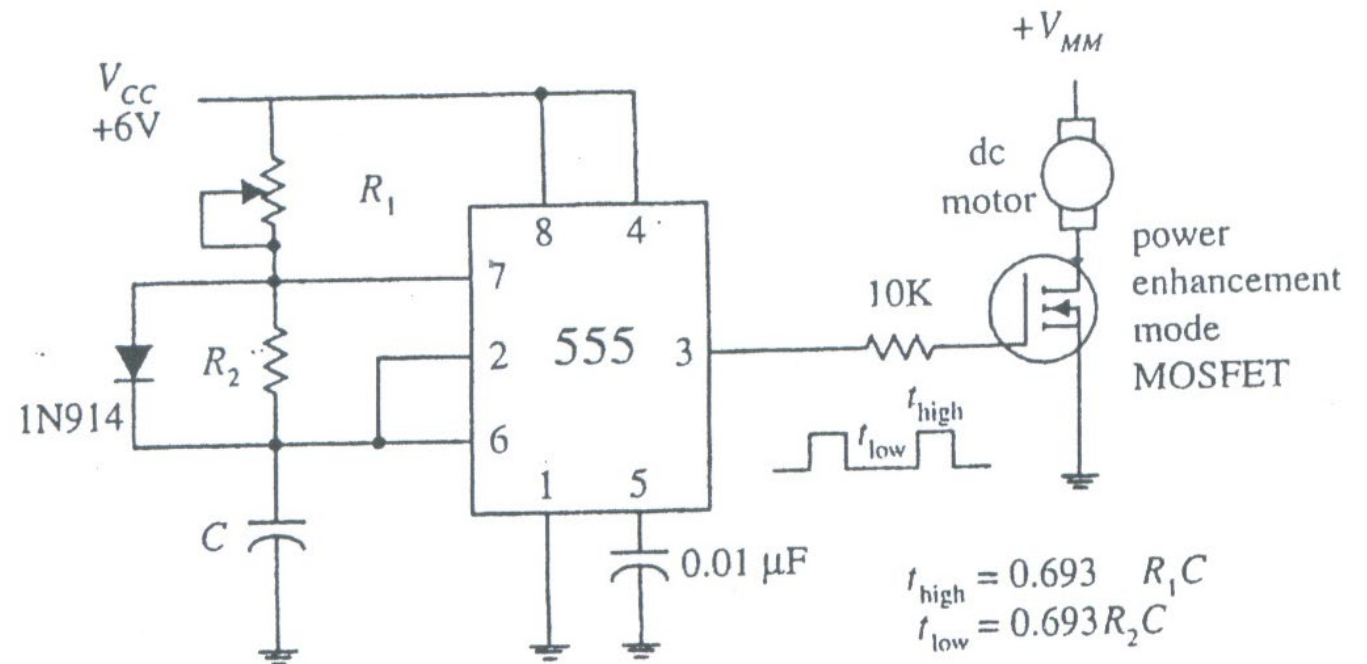
DC Motor Speed Control using PWM: Version 3

- 555 timer in astable mode to generate pulses that drive a power MOSFET.
- By inserting a diode between pins 7 and 6, as shown, the 555 timer is placed into low-duty cycle operation.
 - R_1 , R_2 , and C set the frequency and on/off duration of the output pulses



DC Motor Speed Control using PWM: Version 3

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- By inserting a diode between pins 7 and 6, as shown, the 555 timer is placed into low-duty cycle operation.
 - R_1 , R_2 , and C set the frequency and on/off duration of the output pulses



Without diode, $t_{high} = 0.693 (R_1 + R_2) C$

Interfacing DC Motor with BS2: On/Off Control Circuit #1

- Interface an N-channel MOSFET IRF511 to BS2 as shown.
- Interface the motor between the +5V of power supply and the drain of MOSFET, with MOSFET source connected to ground.
- Place a 1N4001 diode in reverse biased mode parallel to motor.
- With BS2 o/p high on P0 → MOSFET gate is driven positive relative to source of MOSFET.
 - The drain source pair of the MOSFET conducts and motor turns on.
- With BS2 o/p low on P0 → MOSFET stops conducting, a reverse voltage spike is generated in the motor which conducts through a diode.
- A low voltage (5VDC) motor is being used in this circuit.

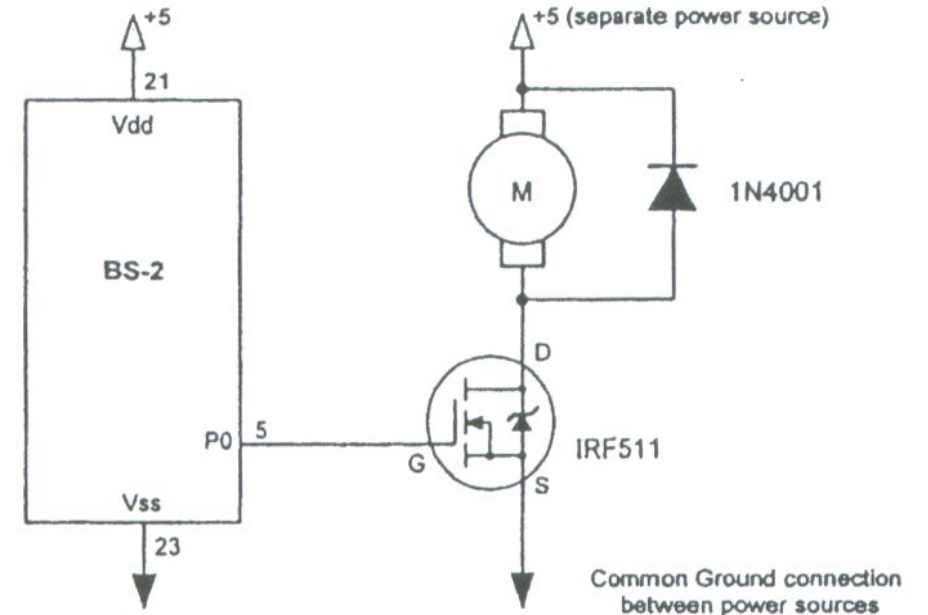
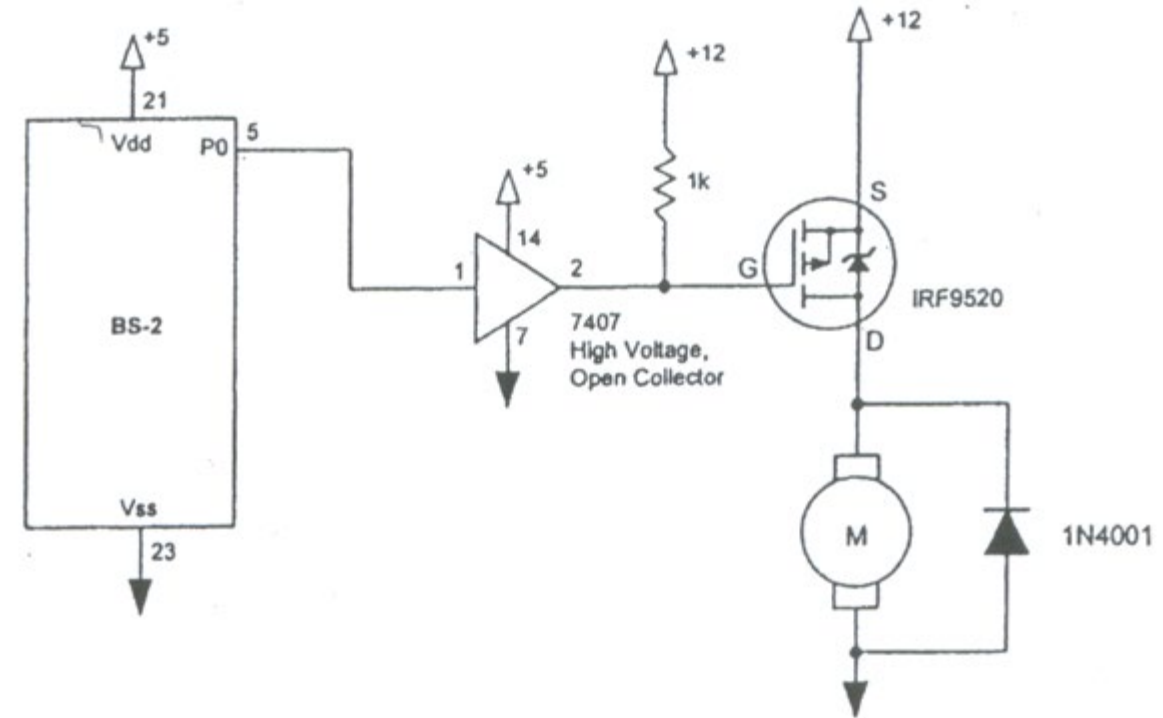


Figure
A simple DC motor driver circuit

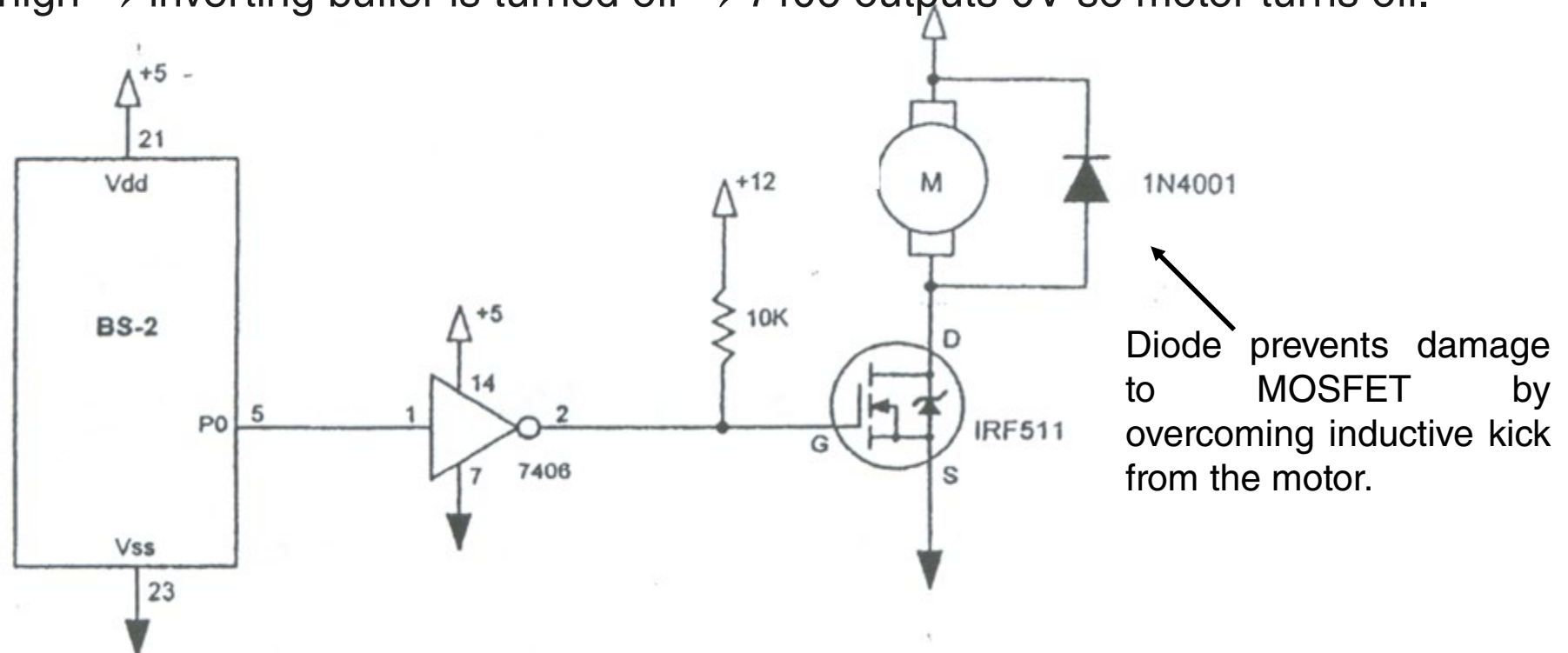
Interfacing DC Motor with BS2: On/Off Control Circuit #2

- BS2 drives the open collector, non-inverting buffer whose output is tied to 12VDC.
- When BS2 is low, 7407 buffer outputs 0V DC which drives a P-channel MOSFET.
- The 12VDC potential difference between source-gate yields higher drive capability.
- P0 low → motor turns on
P0 high → motor turns off.



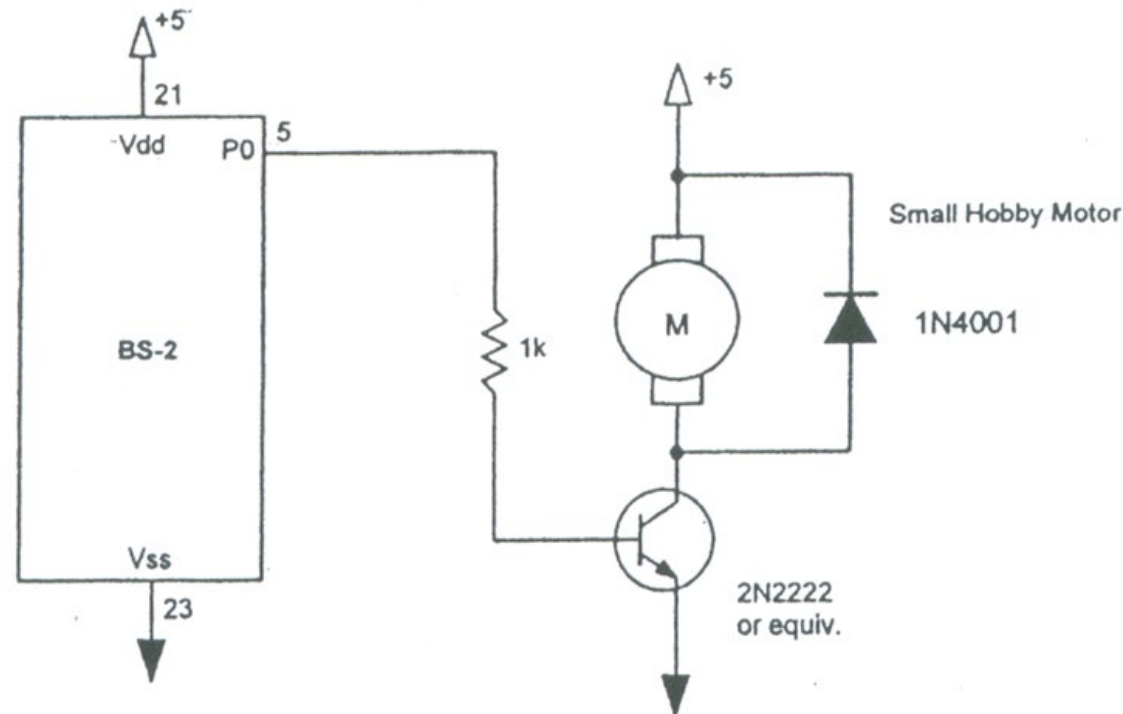
Interfacing DC Motor with BS2: On/Off Control Circuit #3

- In this circuit: P0 low → inverting buffer is turned on → 7406 outputs 12V which appears at the gate of an N-channel MOSFET IRF511.
 - The motor is turned on.
 - With $V_g - V_s = 12V$, the MOSFET provides high drive capability.
- With P0 high → inverting buffer is turned off → 7406 outputs 0V so motor turns off.



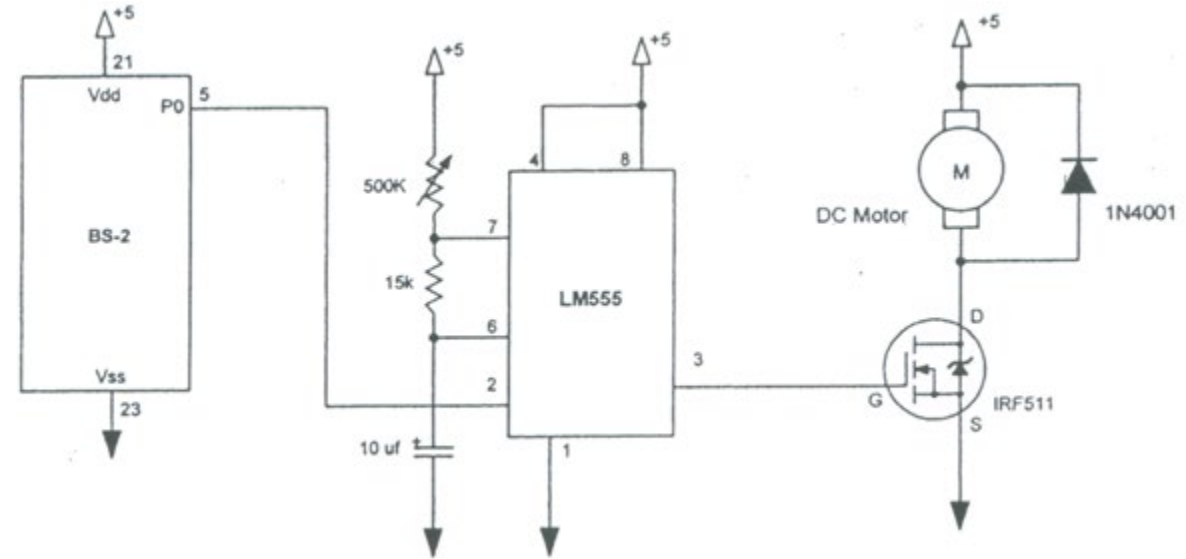
Interfacing DC Motor with BS2: On/Off Control Circuit #4

- In this circuit, an NPN BJT is used to turn on/off a low voltage, low current hobby motor.
- The current rating of BJT must be appropriately selected to provide the drive current required by the motor.



DC Motor: On-Time Control Circuit #1

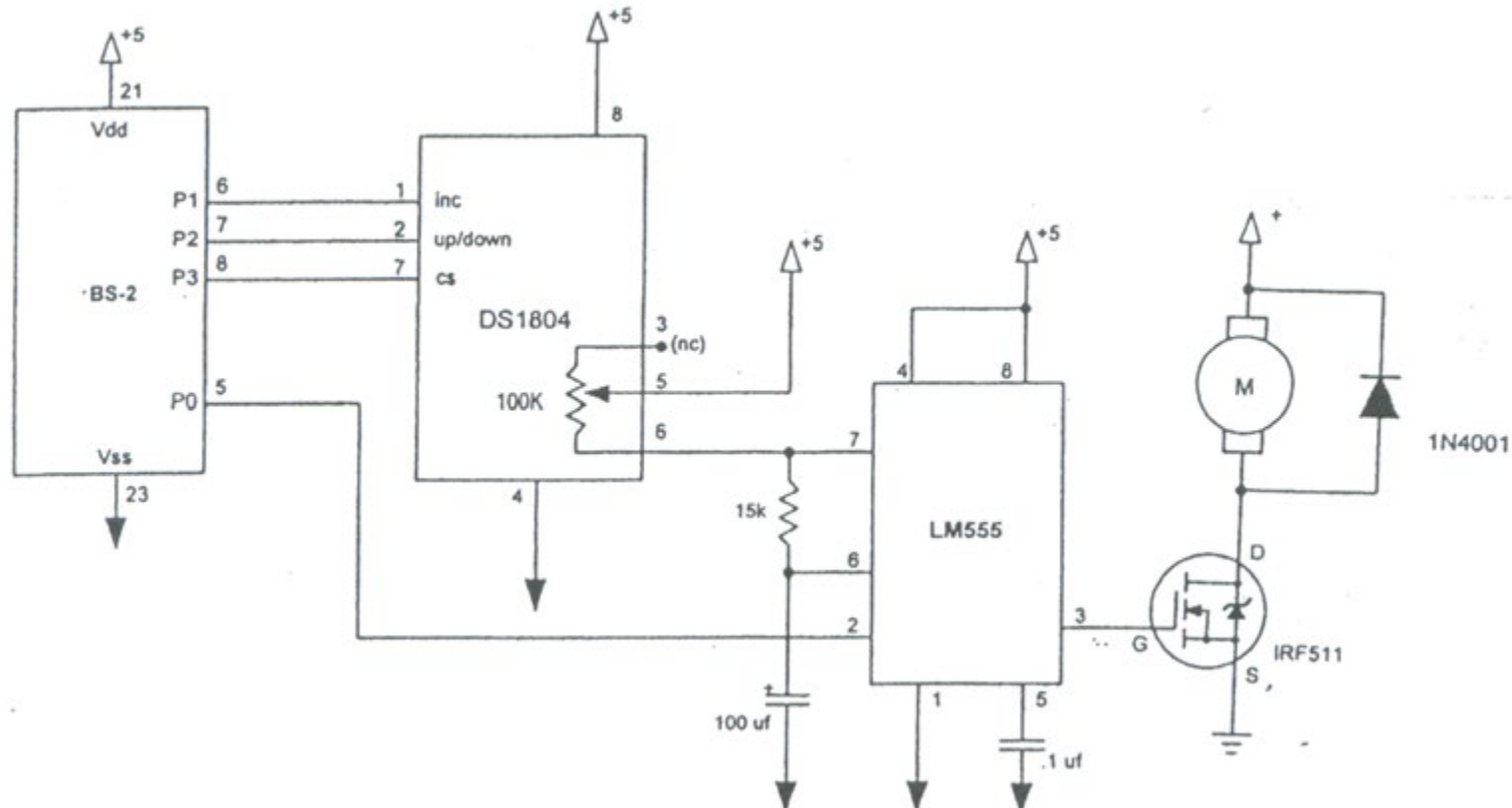
- DC motor is turned on for a period of time, determined by the 500k pot and 10 μ F capacitor.
- When a low going pulse appears at PIN2 of the LM555 timer, the IRF511 MOSFET is turned on which turns the motor on.
- PIN2 of LM555 timer should be turned high immediately after being turned low.
- This circuit allows us to off-load the task of running the motor for a certain period and then stopping it.
- BS2 simply turns the motor on, it does not have to monitor time to turn the motor off, since LM555 takes care of the timing issue (monostable operation mode).



- Sample code:
low 0
high 0
'(rest of the code here)

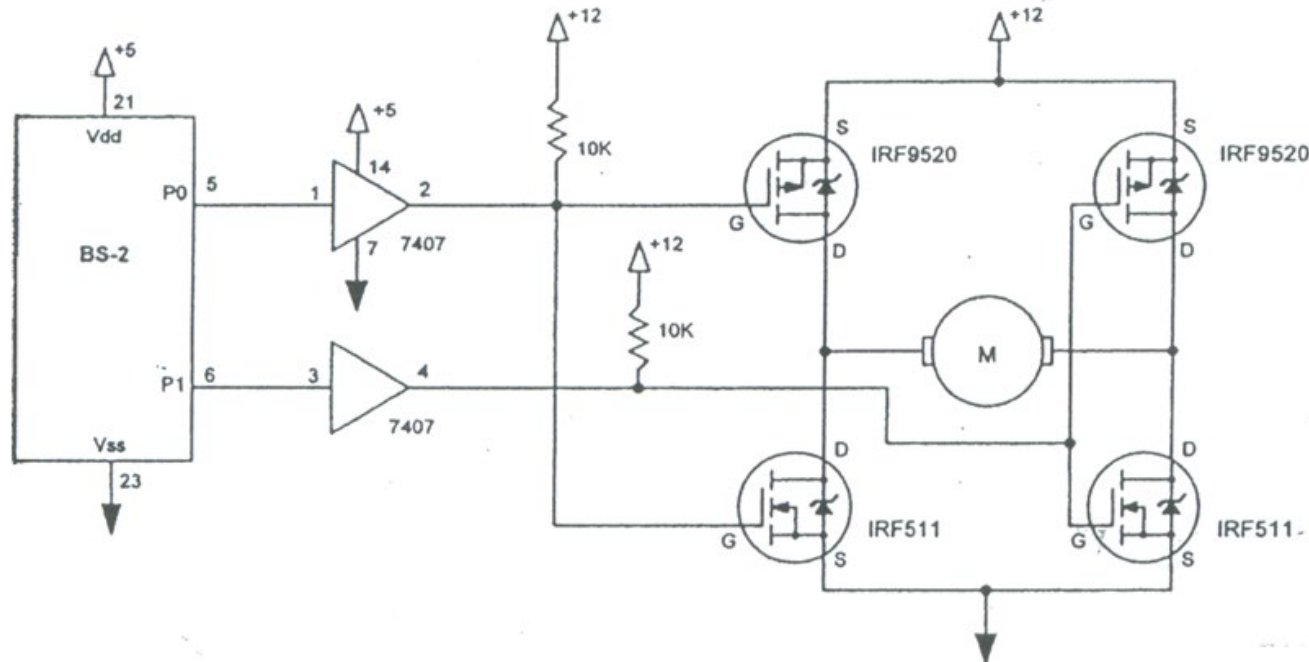
DC Motor: On-Time Control Circuit #2

- To allow automatic control of ON-time duration of motor, here a digital pot is used.
- By selecting a proper setting for solid state pot, the motor ON-time duration is controlled.



Interfacing DC Motor with BS2: H-Bridge Circuit

- MOSFET-based H-bridge for the direction control of a DC motor.
- The outputs from P0 and P1 of BS2 are processed by the 7407 non-inverting buffers. The buffer outputs control two pairs of two MOSFET's each to perform direction control.

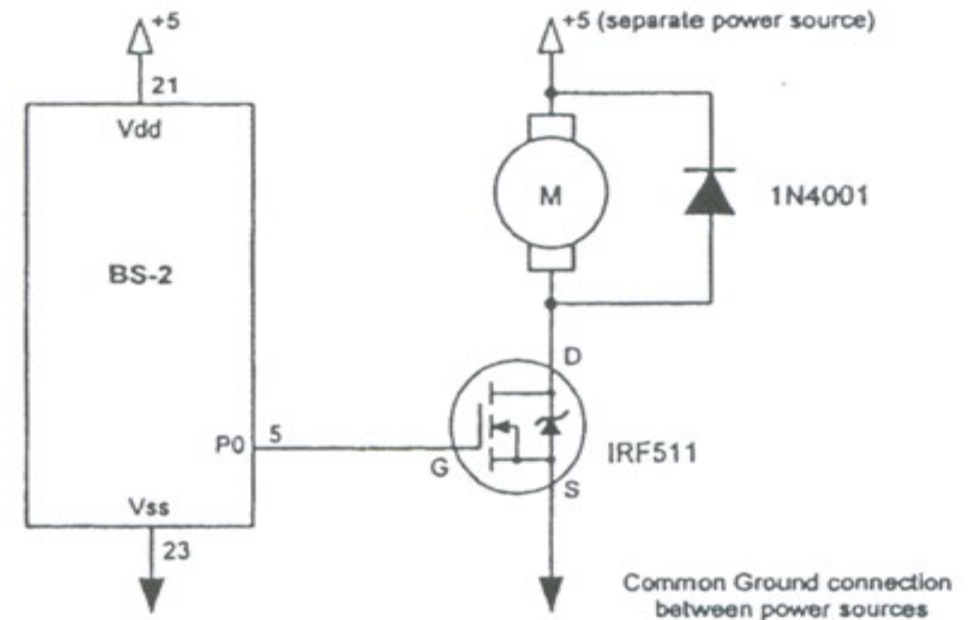


Sample Code:

```
loopstart:  
  high 0  
  low 1  
  pause 2000  
  low 0  
  high 1  
  pause 2000  
  goto loopstart
```

DC Motor Speed Control using PWM

- Consider DC Motor on/off control circuit #1 (reproduced below).
- We can use the PWM technique to control the speed of motor.
- Sample code shown below can be used to get:
 - Motor on at full speed (on all the time).
 - Motor on only 50% of time (slower speed compared to 100%).
 - Motor on only 25% of time (slower speed compared to 50%).
 - Motor accelerating

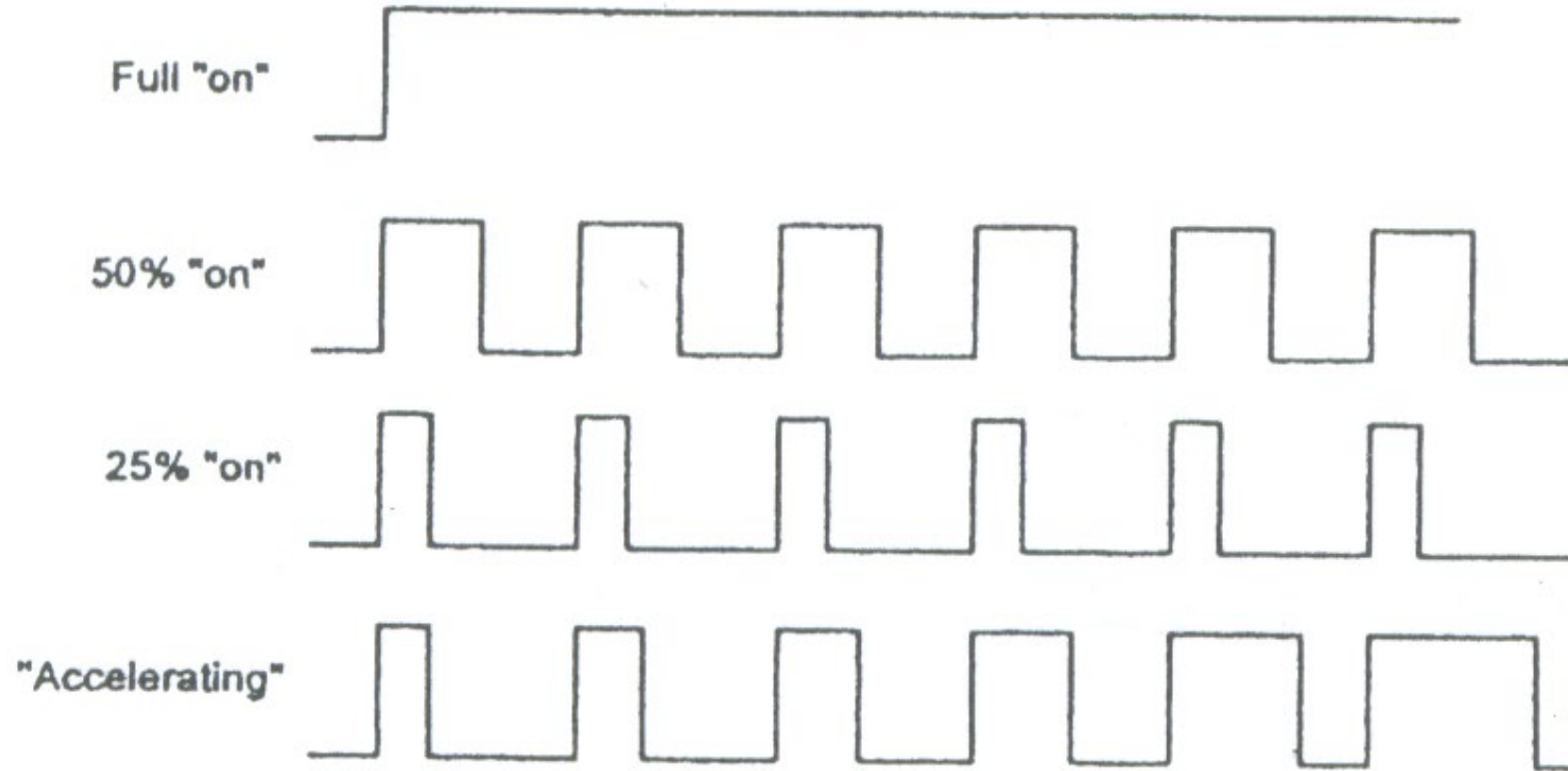


Sample PWM Code

```
x var word
y var word
here:
debug "This is full-on"
debug cr
high 0 'On all the time.
pause 2000
debug "This is 50% on"
debug cr
for x = 1 to 200
high 0
pause 5 'ON for 5 milliseconds
low 0
pause 5 'OFF for 5 milliseconds
next
```

```
debug "This is 25% on"
debug cr
for x = 1 to 100
high 0
pause 5 'ON for 5 milliseconds
low 0
pause 15 'OFF for 15
milliseconds
next
pause 2000
debug "This is accelerating"
debug cr
for y = 100 to 1
high 0
pause 15
low 0
pause y
next
goto here
```

PWM Signal Produced by the Sample Code



DC Motor Challenges

- Issues: rechargeability, energy density, capacity, voltage, internal resistance, etc.
- **Power supply noise:**
 - Current demand varies as motor starts or changes direction.
 - Commutator brush noise introduced due to breaking/making of contact that leads to inductive kickback.
 - PWM noise which also causes motor to turn on/off leading to inductive kickback.
 - **Advised to use separate power supplies or motor and microcontroller.**
- Electromagnetic interference may be produced as PWM pulses current in motor coil or as motor brushes make/break contact with the power supply.
- **Audible noise:**
 - When PWM frequency matches up with one of the resonant frequencies of motor structure (in the audible range).
 - Gearbox and other mechanical components.

Servomotor

- Position control rather than speed control
 - Servomechanism with feedback control
 - Example: potentiometer as angle sensor (encoder)

Parallax Standard Servo Motor

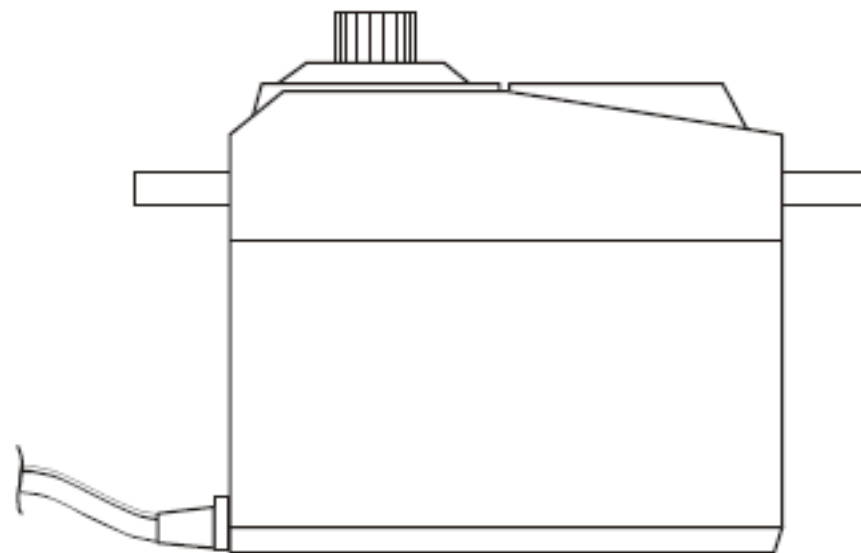
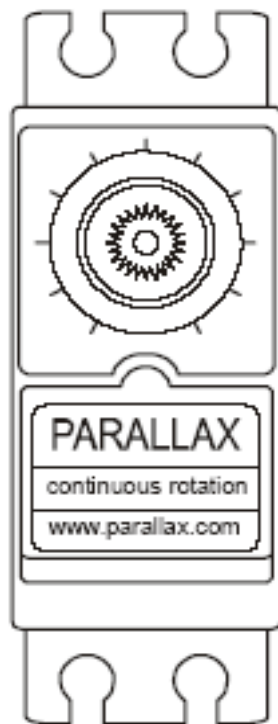
- DC motors with feedback position control
- As long as the coded signal exists on the input line, the servo will maintain the angular position of the shaft
- As the coded signal changes, the angular position of the shaft changes



Parallax Standard Servo Motor Specifications

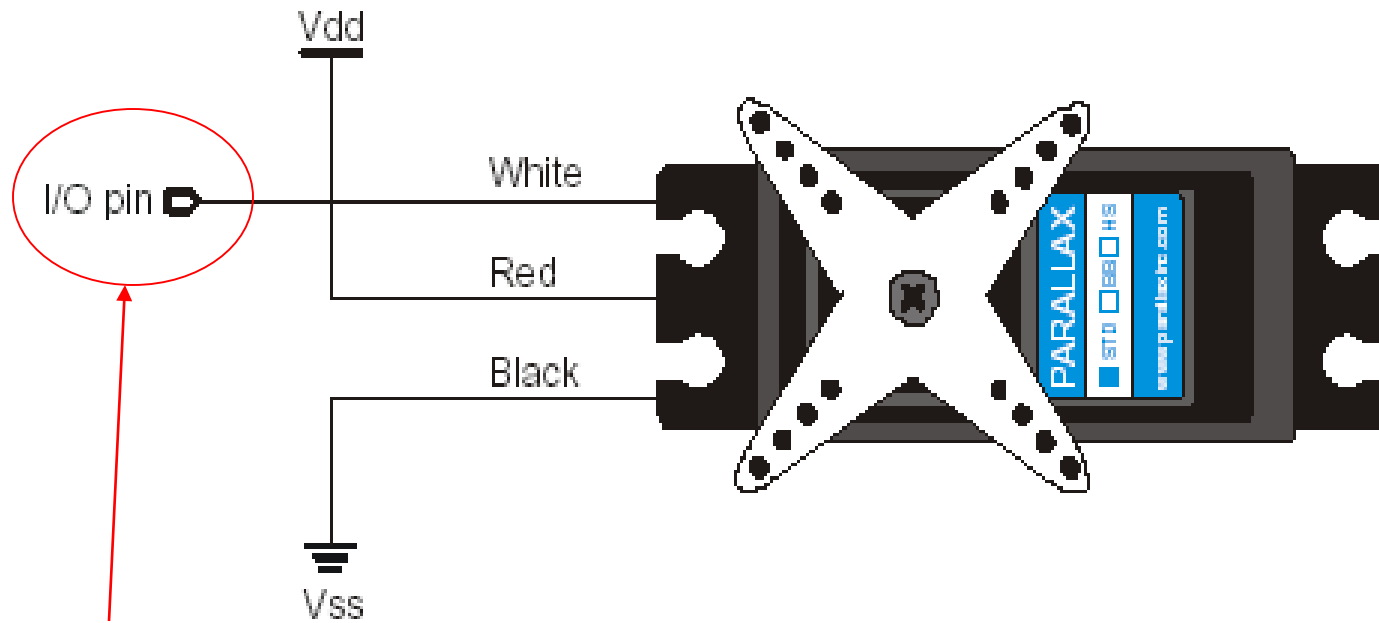
Technical Specifications

- > Power 6vdc max
- > Speed 0 deg to 180 deg in 1.5 seconds on average
- > Weight 45.0 grams/1.59oz
- > Torque 3.40 kg-cm/47oz-in
- > Size mm (L x W x H)
40.5x20.0x38.0
- > Size in (L x W x H)
1.60x.79x1.50



Servomotor Wiring

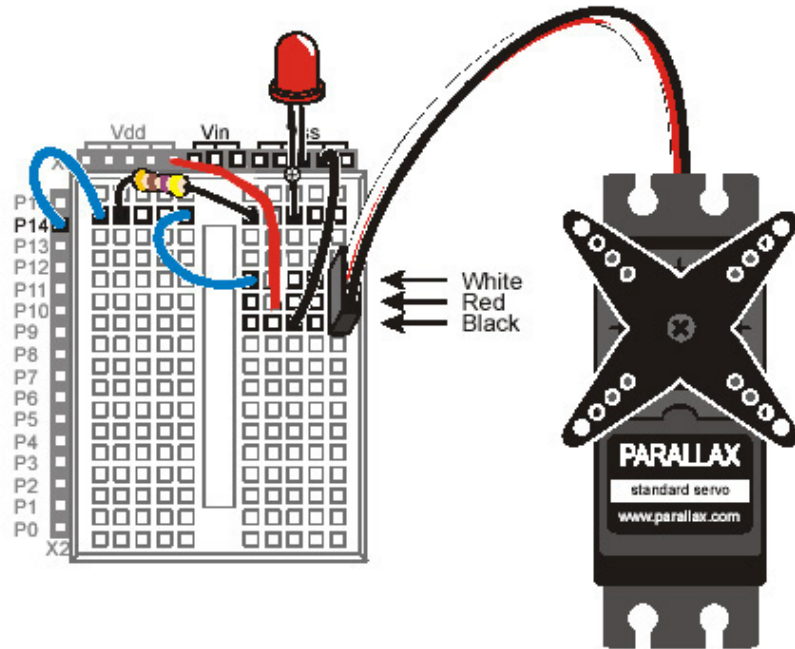
Wiring setup



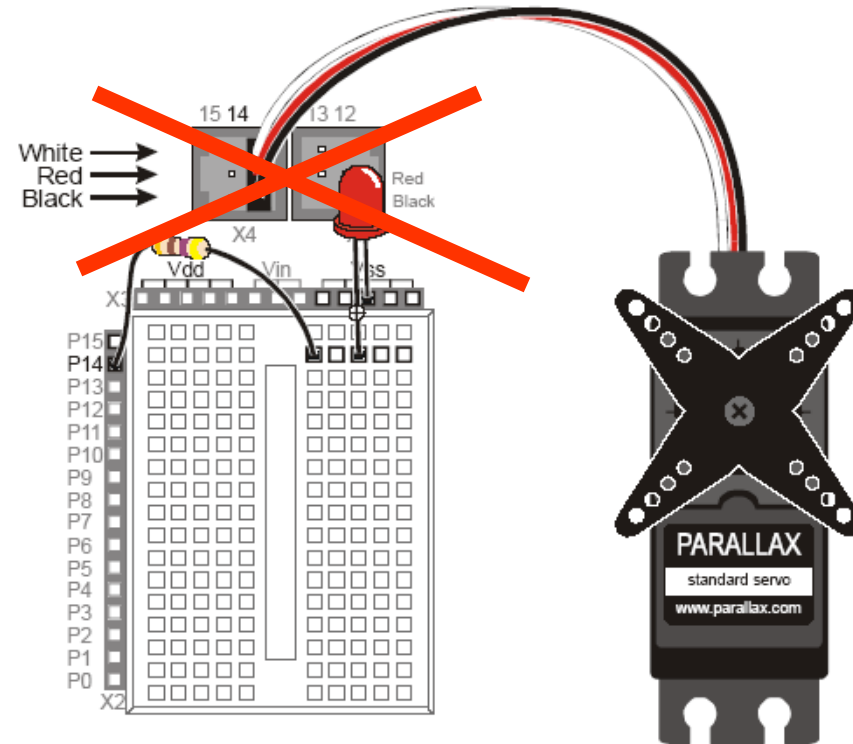
This pin can be any I/O pin

Servomotor with BS2

Board of Education Rev B



Caution: Do not connect servo here when using wall transformer or 9V battery. Servo is to be connected here only when using AA battery pack with $\leq 6V$.



When more than 2 servos are to be connected, need to use additional capacitors across V_{dd} and V_{ss} .

Servomotor with BS2: Code

X var byte
Output 12

Here:

```
For X = 1 to 100
```

```
Pulsout 12, 500
```

```
Pause 10
```

```
Next
```

```
Pause 500
```

```
For X = 1 to 100
```

```
Pulsout 12, 1000
```

```
Pause 10
```

```
Next
```

```
Pause 500
```

```
Goto Here
```

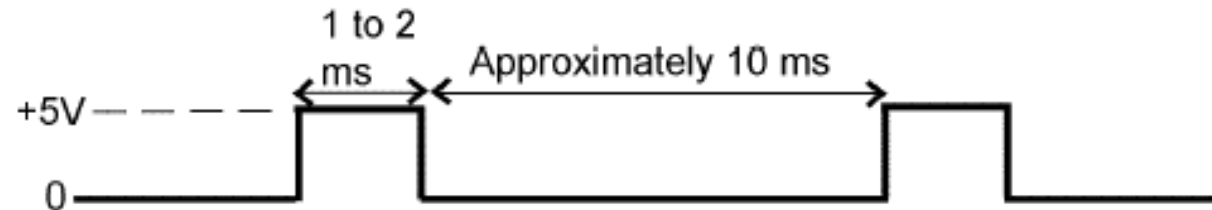
Pulsout Pin #, Duration

12 is pin number of BS2

500 means 1 millisecond

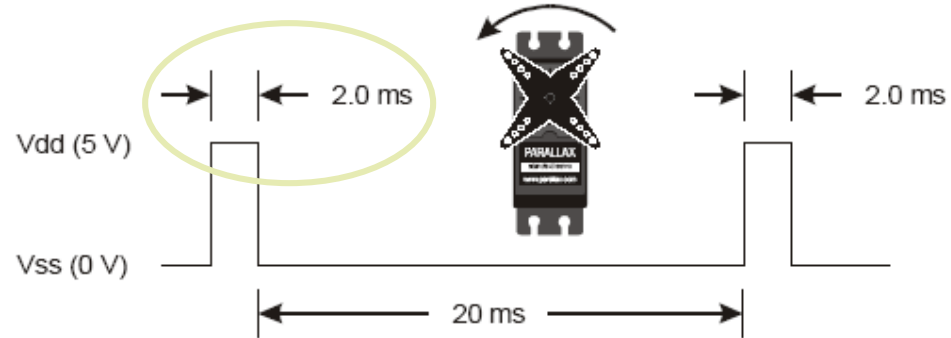
!! Caution

Fix the Duration
between 500 to
1000

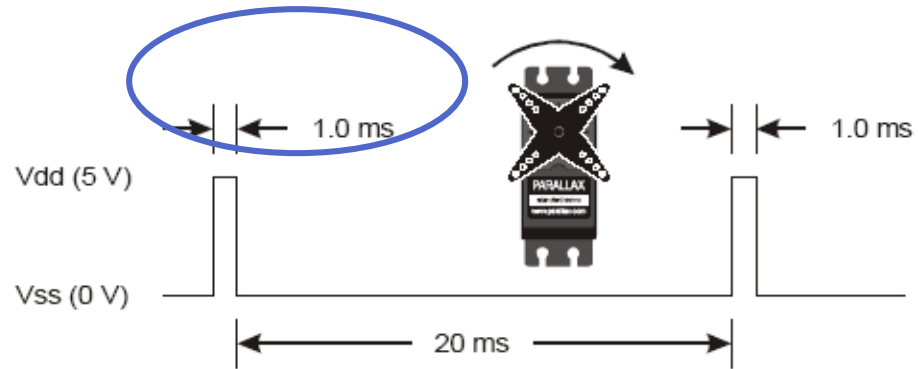


Servomotor with BS2: Code

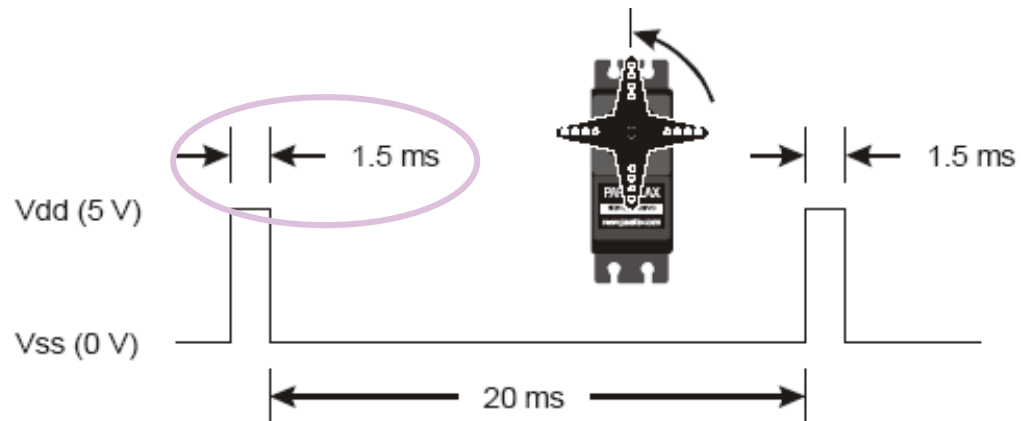
```
FOR counter = 1 to 150  
  pulsout 14, 1000  
  pause 20  
NEXT
```



```
FOR counter = 1 to 150  
  pulsout 14, 500  
  pause 20  
NEXT
```



```
FOR counter = 1 to 150  
  pulsout 14, 750  
  pause 20  
NEXT
```



Control Theory

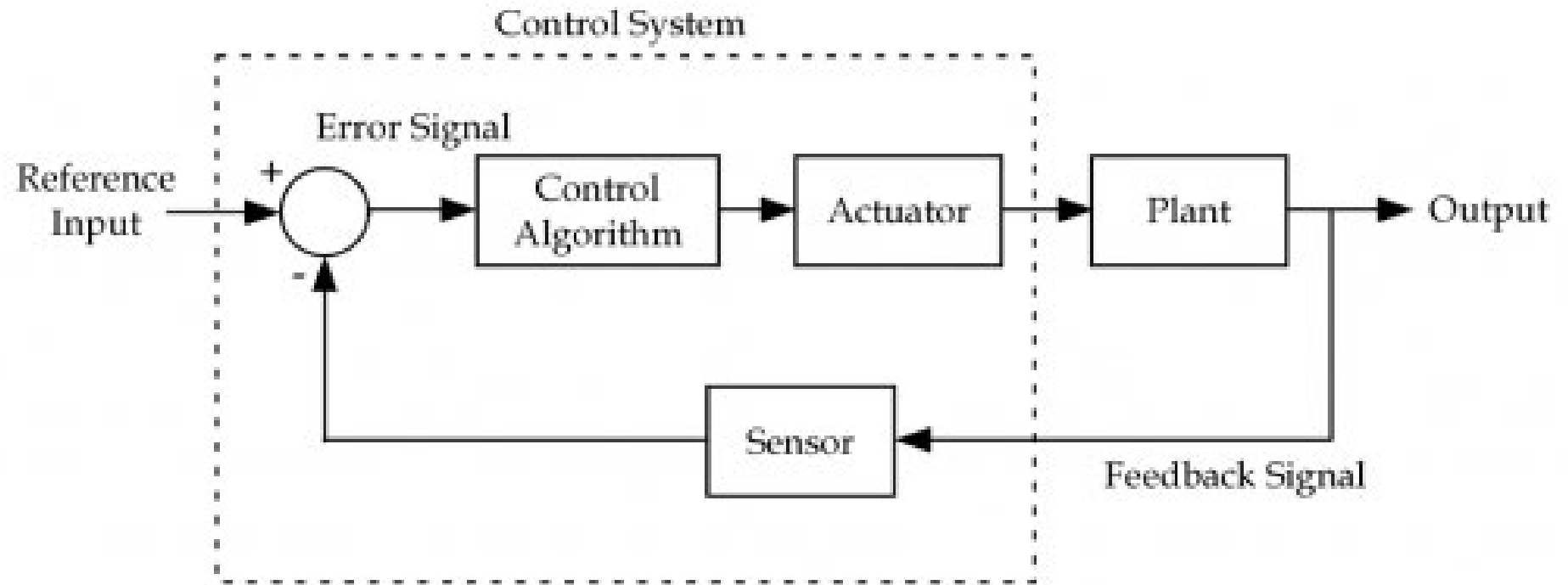
- How to ride a bike

PID Simulator

- <https://grauonline.de/alexwww/ardumower/pid/pid.html>

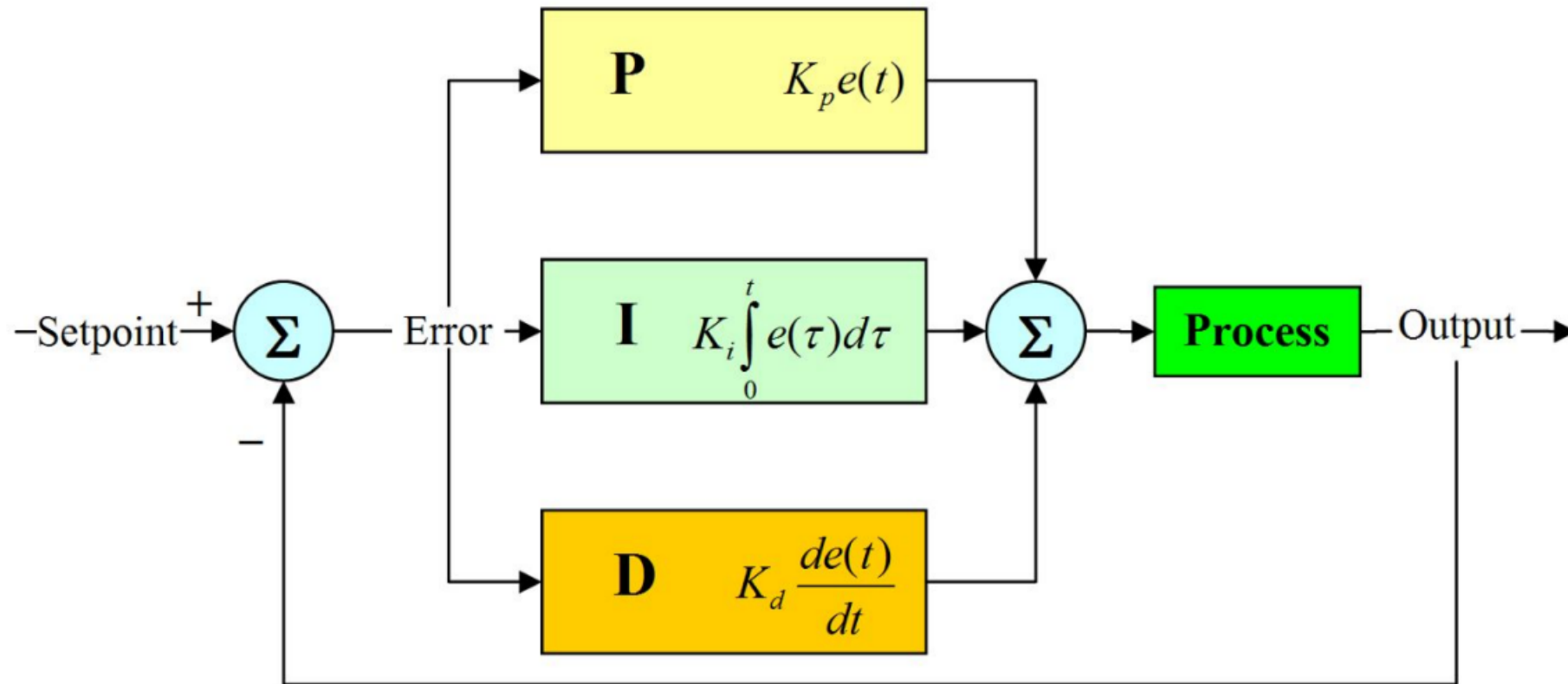
Control Theory

- Block diagram

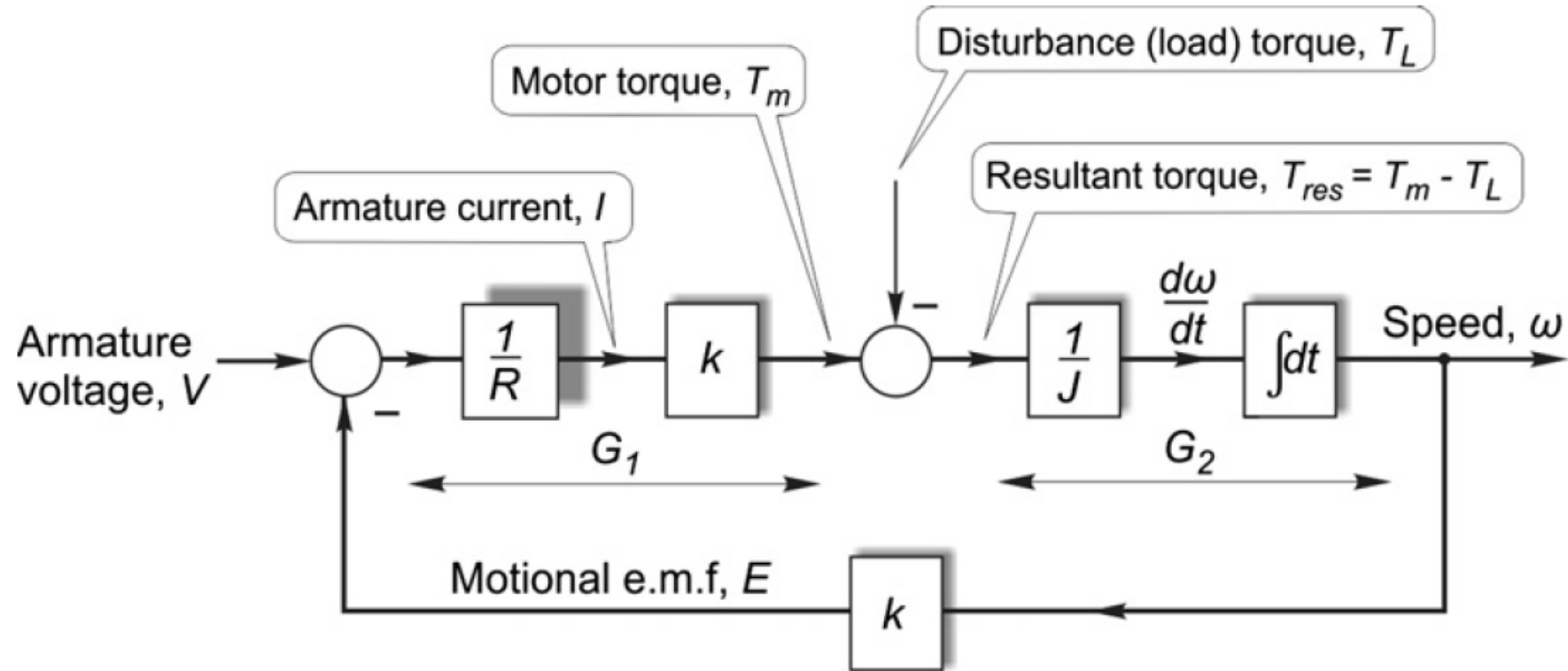


PID Control

- Proportional, Derivative, Integral Control



DC Motor Block Diagram



Miscellaneous

Dead Reckoning

- **Dead Reckoning:** derived from deduced reckoning of sailing days
 - Establish present location by advancing over a previous known position through known course and velocity information over a given length of time
- **Measure vehicle displacement:**
 - Wheel rotation (odometry using pot, encoder, magnetic/inductive proximity sensor, etc.).
 - Doppler navigation (motion relative to ground)
 - Inertial navigation (accelerometers)
- **Measure vehicle heading:**
 - Onboard steering
 - Magnetic compass
 - Rate gyro
 - Differential odometry

Doppler Effect

- Stationary Observer, moving source

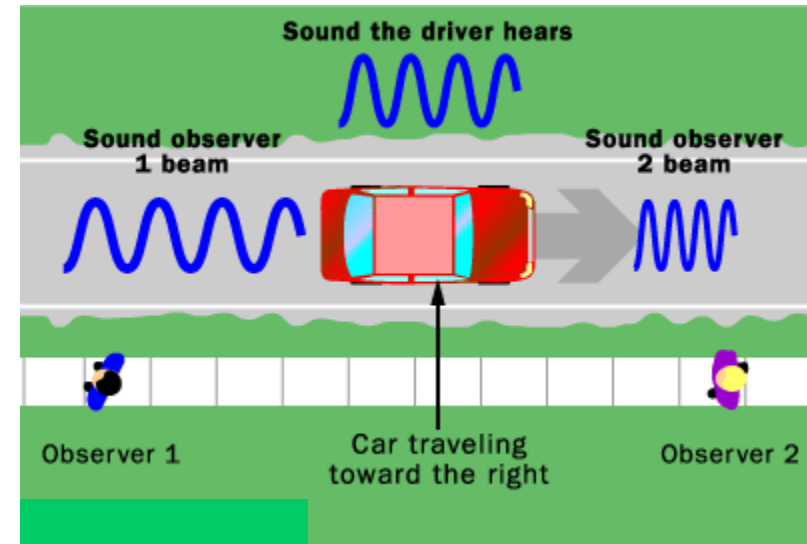
$$f_{\text{rec}} = f \left(\frac{s}{s \pm v_s} \right)$$

- f : source frequency, f_{rec} : frequency @ observer (Doppler frequency), s : speed of sound in air, v_s : velocity of source
- +/- sign: source moving away from/toward observer

- Moving observer, stationary source

$$f_{\text{rec}} = f \left(\frac{s \pm v_o}{s} \right)$$

- v_o : velocity of observer



- For reflected wave, instead of Doppler frequency, we consider the change in frequency (Doppler shift)

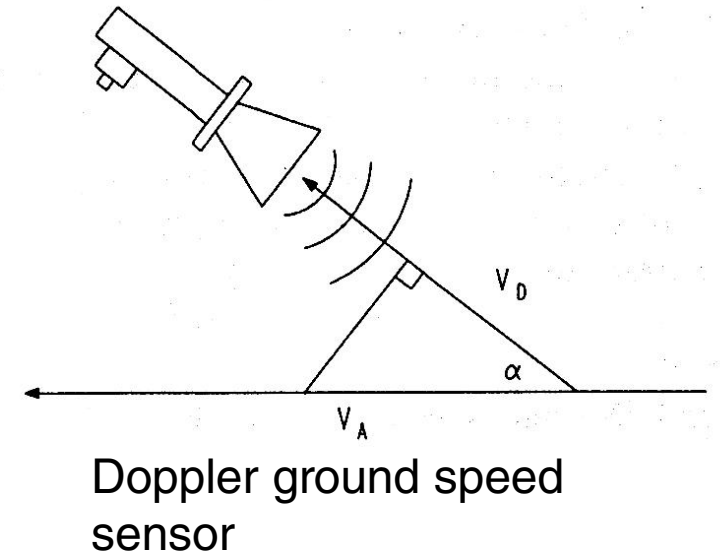
$$\Delta f = f - f_{\text{rec}} = \frac{2f v \cos \theta}{s}$$

- f : source frequency, f_{rec} : frequency received, s : speed of sound in air, v : velocity of target object, θ : relative angle between direction of motion and beam axis

Doppler Navigation

- Use ultrasonic sensor aimed downward at a prescribed angle to sense ground movement
- Use Doppler shift equation to determine the ground speed V_A of the vehicle as follows:

$$\Delta f = f - f_{rec} = \frac{2f V_D}{s}$$
$$\Rightarrow V_D = \frac{s \Delta f}{2f}$$
$$\Rightarrow V_A = \frac{V_D}{\cos \alpha} = \frac{s \Delta f}{2f \cos \alpha}$$



- f : transmitted frequency, Δf : Doppler shift, s : speed of sound in air, V_D : measured velocity, α : declination angle

Vehicle heading via Differential Odometry

- Displacement D of a differential-drive robot platform:

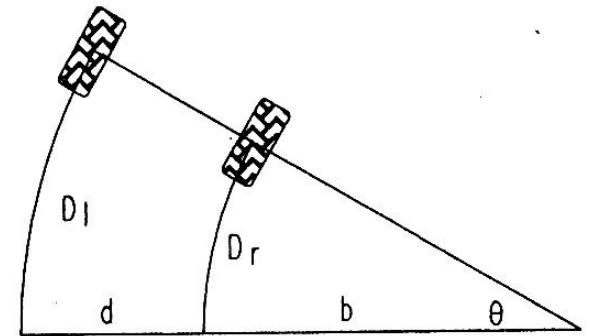
$$D = \frac{D_L - D_R}{2}$$

- D_L and D_R : displacements of left and right wheels, respectively
- D_L : portion of the circumference of a circle with radius $d+b$, $C_L = 2\pi(d+b)$
- D_R : portion of the circumference of a circle with radius b , $C_R = 2\pi b$
 - d : distance between left and right wheels, b : inner turn radius

- Moreover: $D_L = \left(\frac{C_L}{2\pi}\right)\theta \rightarrow C_L = \frac{2\pi D_L}{\theta} \rightarrow \theta = \frac{D_L}{d+b}$

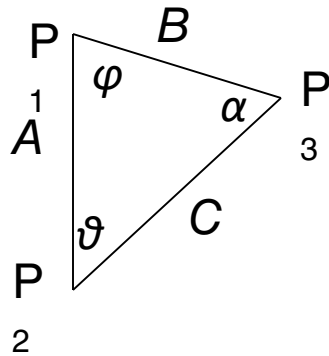
- Similarly, $D_R = \left(\frac{C_R}{2\pi}\right)\theta \rightarrow C_R = \frac{2\pi D_R}{\theta} \rightarrow \theta = \frac{D_R}{b} \rightarrow b = \frac{D_R}{\theta}$

- Finally, $\theta = \frac{D_L - D_R}{d}$



Triangulation Ranging

- Basis (Law of sines): If the sides of a triangle are a , b , and c and the angles opposite to those sides are α , θ , and φ , then



$$\frac{A}{\sin \alpha} = \frac{B}{\sin \theta} = \frac{C}{\sin \varphi}$$

$$\rightarrow B = A \frac{\sin \theta}{\sin \alpha} = A \frac{\sin \theta}{\sin(180 - \theta - \varphi)} = A \frac{\sin \theta}{\sin(\theta + \varphi)}$$

- Therefore, given the length of a side and two angles of a triangle, the length of the other two sides and the third angle can be determined.
- In ranging applications, length B represents the distance to the object of interest at point P_3 .
- In a passive ranging system, directional detectors can be placed at P_1 and P_2 to view the object point P_3 , forming an imaginary triangle.
- Measurement of angles θ and φ along with the known orientation and lateral separation of the detectors allows the calculation of range to the object at P_3 .

Time-of-Flight Ranging

Measure the round-trip time required for a pulse (burst) of emitted energy (acoustic, radio, or optical) to travel to an object and then reflect/echo back to a receiver.

Range to the object: $d=v(T/2)$, where v is the speed of the propagated wave, T =round-trip time of travel

Ultrasonic emitter/detector pairs (transceivers) are commonly used

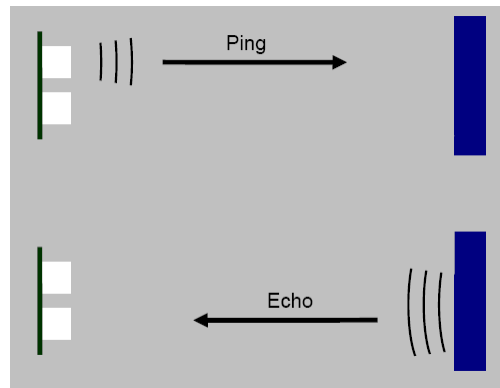
Common ultrasonic transducers: capacitive, electrostatic, and piezoelectric

Laser-based time-of-flight systems

Speed of sound $\approx 0.3\text{m/ms}$, speed of light $\approx 0.3\text{m/ns}$

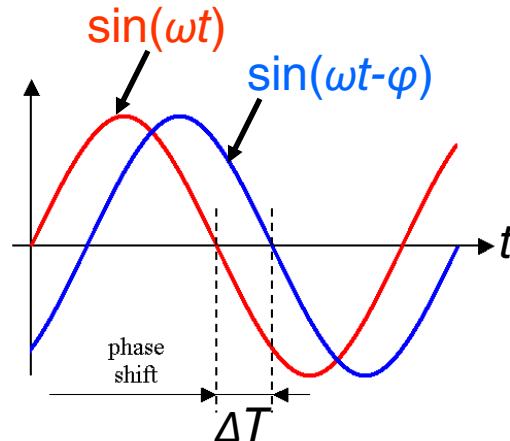
Time of flight for 3 meters: ultrasonic system: 10ms; laser system: 10ns

→ sophisticated timing circuitry necessitated in laser-based time-of-flight ranging instruments.



Ranging by Phase Shift Measurement

- A continuous-wave (e.g., amplitude-modulated laser, RF, or acoustic) energy source is directed towards a target.
- The reflected signal that strikes back at the detector is compared to a reference signal (tapped off from the transmitted signal).
- The relative phase shift between the reference and reflected signal is measured to determine the round-trip distance from the object.
- Notation: T : period (sec), f : frequency (Hz), ω : radial frequency (radian/sec), λ : wavelength (m), $\omega=2\pi f$, $\lambda=s/f$, s : speed of sound.



$$\begin{aligned}\phi &= \omega \Delta T = 2\pi f \Delta T = 2\pi \left(\frac{s}{\lambda} \right) \Delta T \\ &= \frac{2\pi}{\lambda} s \Delta T = \frac{2\pi(2d)}{\lambda} = \frac{4\pi d}{\lambda} \\ \Rightarrow d &= \frac{\phi \lambda}{4\pi}\end{aligned}$$

The End

