

Part A

Page rank

PageRank is a way of measuring the importance of website pages. Page Rank works by counting the number and quality of links to a page to determine a rough estimate of how important the website is. The underlying assumption is that more important websites are likely to receive more links from other websites. Our code has 4 major implementations

- Making the adjacency matrix
- Including the random teleportation
- Calculating rank vector using linear algebra packages
- Calculating rank vector using power iteration method

Inputs:

Takes in number of nodes and edges followed by the edges from one node to the next.

```
Number of nodes: 4
Number of edges: 6
1,2
2,1
2,3
3,2
3,4
4,3
```

The program then finds the rank matrix using two different method:

1. Using linear algebra packages

By calling the `pack()` function, with adjacency matrix as a parameter.

2. Using power iteration method

By calling the `powerIter()` function, with rank vector and adjacent matrix as parameters.

Each function also calls `randTele()` function which implements random teleportation with probability of random teleportation 0.1

Output:

Output is rank vector calculated by the two methods

```
Rank vector using power iteration: [0.17241379 0.32758621 0.32758621 0.17241379]
Rank vector using pakacges: [0.17241379 0.32758621 0.32758621 0.17241379]
```

Running time:

The running time is between 0.0025 to 0.003 seconds.

```
Runing time: 0.0026330947875976562
```

Part B

HITS

Our code returns the near-steady state values of the Hub & Authority scores of the nodes in the given web graph.

Our code performs following operations:

- **Preprocessing:** For preprocessing the graph dataset, we do stopwords removal, tokenization, and then followed by Porter Stemming.
- **Root set generation:** generates the root set by taking query as input parameter.
- **Base set generation:** generates the base set from the root set
- **Adjacency matrix for the base set:** We also show the adjacency matrix based upon the base set generated for a particular query.
- **Calculation of Hub and Authority score:** We finally calculate the hub and authority score vector for the nodes in the base set.

Algorithm we used for calculating hub and authority score :

$$\begin{aligned} a(0) &= (1, \dots, 1)^T, h(0) = (1, \dots, 1)^T \\ h(i+1) &= A a(i) \\ h(i+1) &= h(i+1) / \|h(i+1)\| \text{ // re-normalize } h \\ a(i+1) &= A^T h(i) \\ a(i+1) &= a(i+1) / \|a(i+1)\| \text{ // re-normalize } a \end{aligned}$$

When the code is run, the user enters a single word query . Based on the query root set and base set is generated.

The execution time for our algorithm is(including time taken to input query):

```
Execution time : 2.478200912475586 seconds
```

Overall, we use 3 functions in our implementation (apart from main):

- 1) makeBaseSet(): finds the base set
- 2) makeRootSet(): finds the root set
- 3) out_edges(): finds the list of outgoing edges