

CS-201
Computational Physics

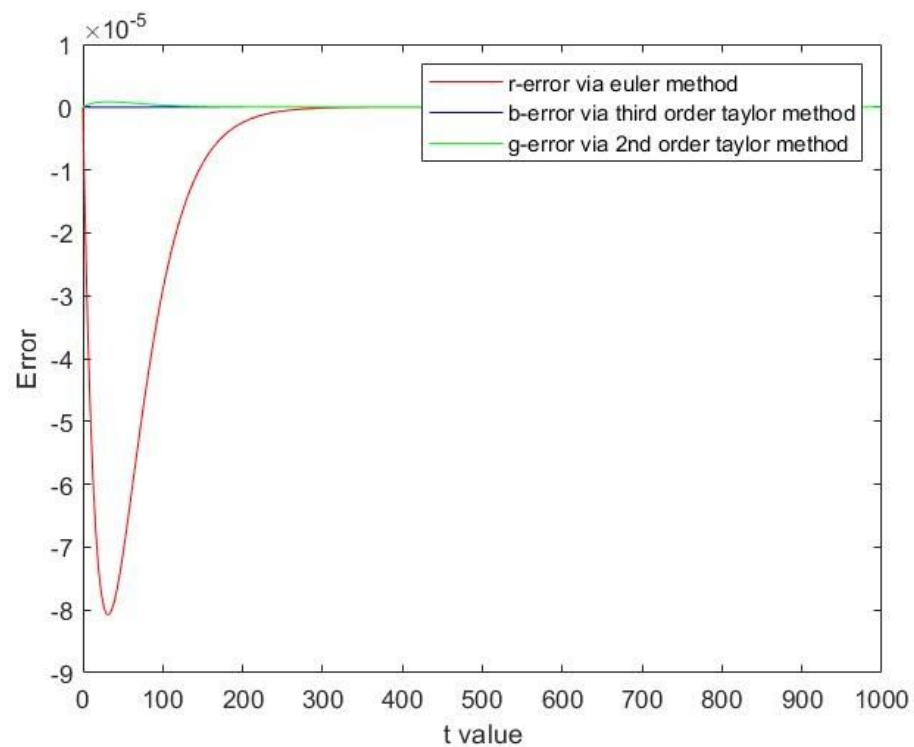
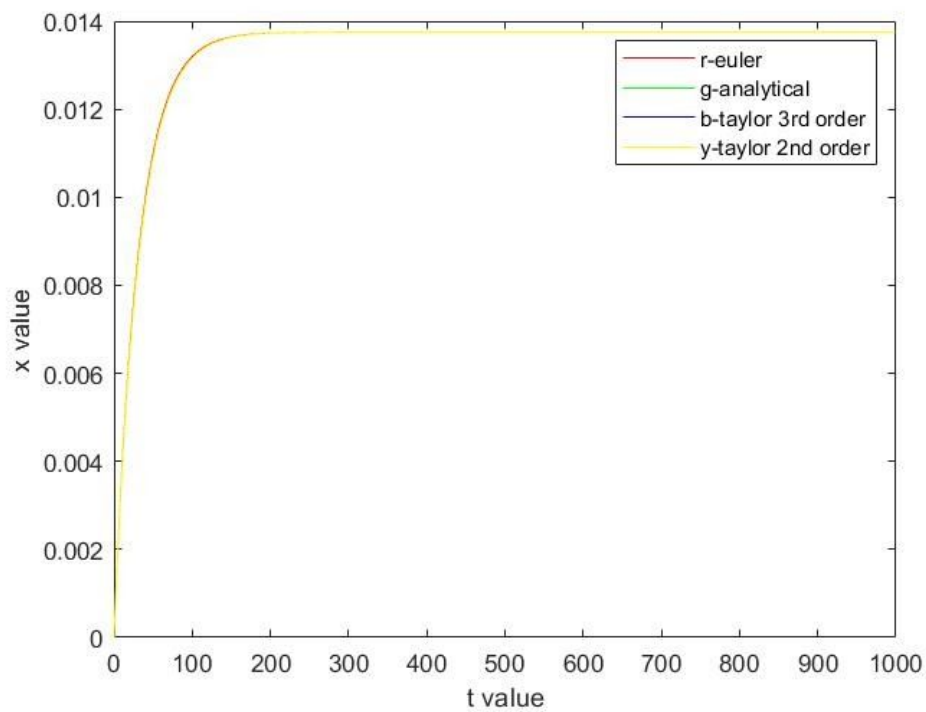
Lab-3
14 . 02 . 2020

Arkaprabha Banerjee 201801408
Shantanu Tyagi 201801015

3 Growth and it's Saturation

3.1 $f(x) = 4.332 \cdot 10^{-4} - 0.0315 \cdot x$; $x(0) = 0$; $0 \leq t \leq 1000$, $\Delta t = 1$
 $r = 4.332 \cdot 10^{-4}$, $\lambda = 0.0315$

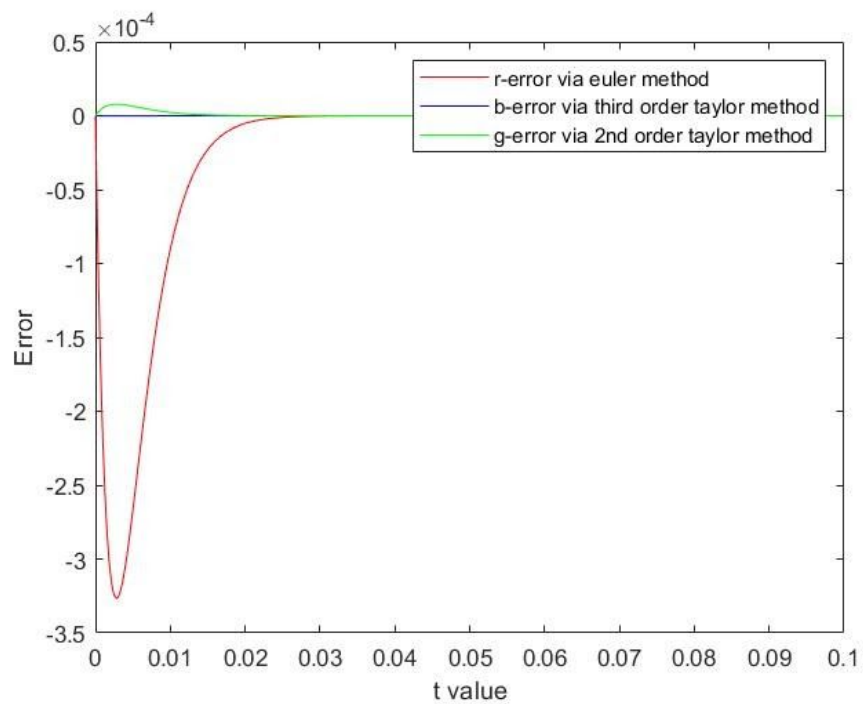
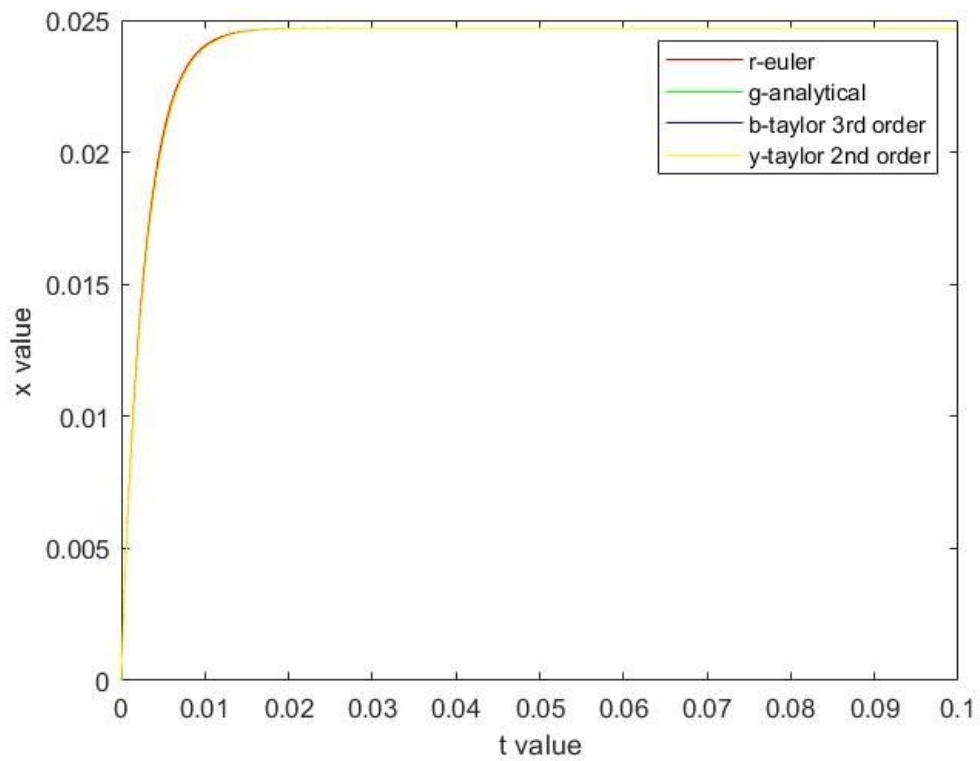
Analytical solution : $x(t) = 0.01375 \cdot (1 - e^{-0.0315 \cdot t})$



3.2 $f(v) = 8.6189 - 349.038 * x$; $v(0)=0$; $0 \leq t \leq 0.01$, $\Delta t = 2 * 10^{-4}$

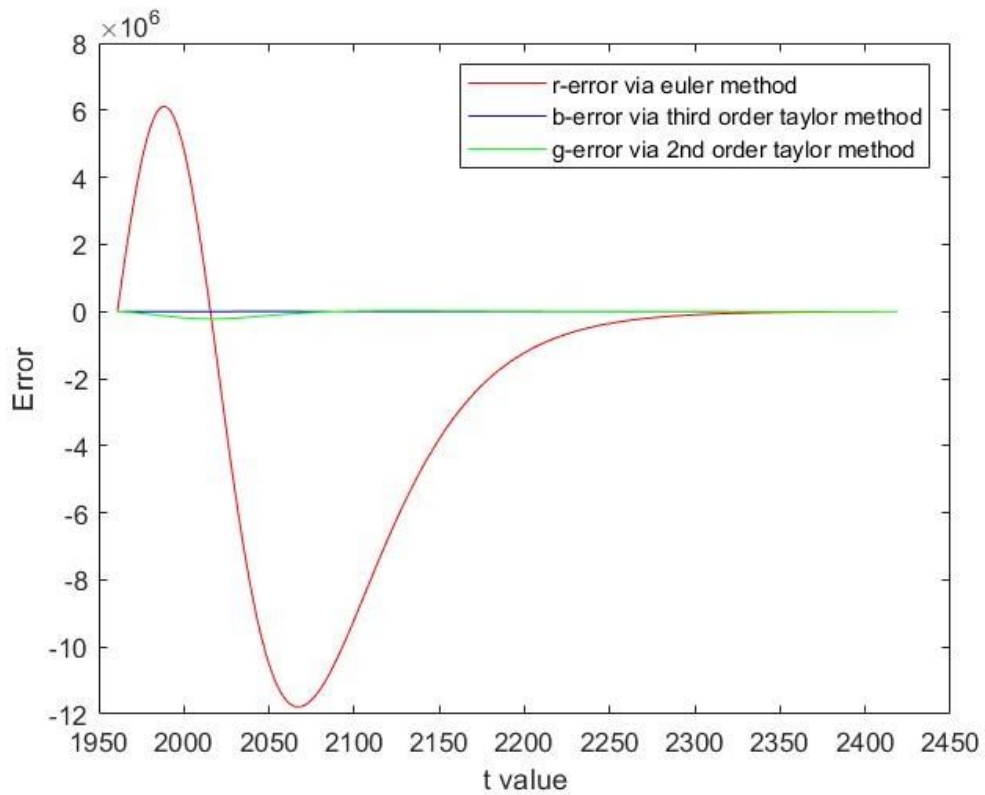
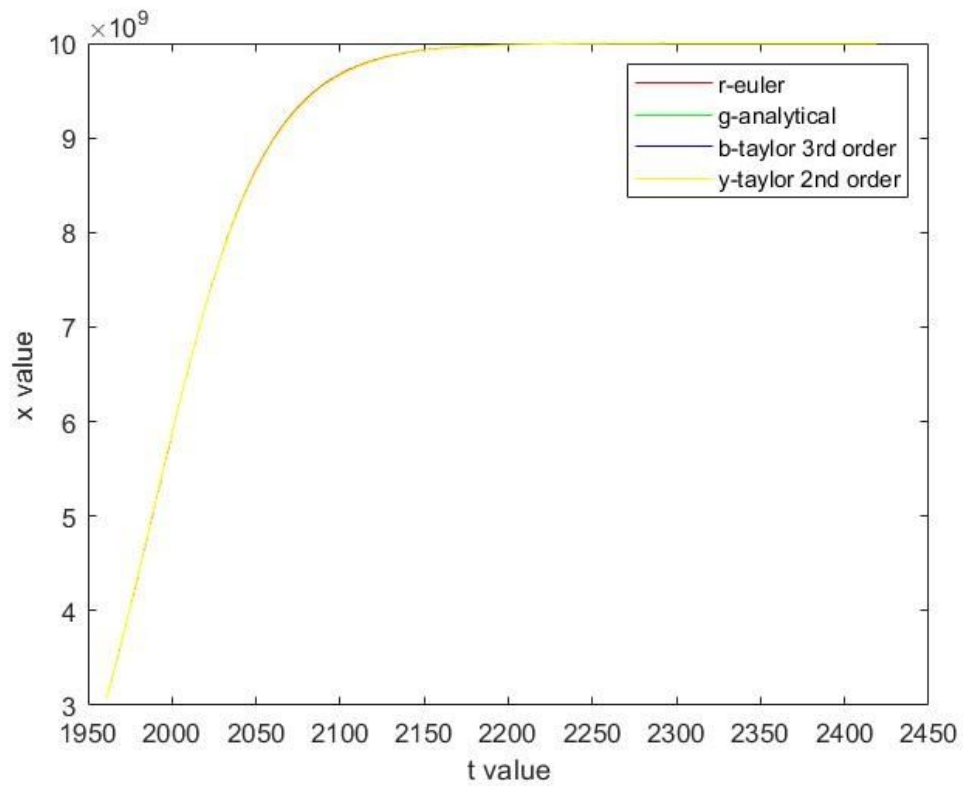
$A = 8.6189$, $B=349.038$

Analytical Solution : $v(t) = 2.469 * 10^{-2} * e^{-349.038*t}$



3.3 $f(x) = 0.03 * x - 3 * 10^{-12} * x^2$; $x(1961) = 3 * 10^9$; $1961 \leq t \leq 2500$, $\Delta t = 1$

Analytical Solution : $x(t) = (3.07 * 10^9 * e^{0.03 * (t - 1961)}) / (1 + 0.307 * (e^{0.03 * (t - 1961)} - 1))$



Limiting Population = 10^{10}

*Current Population (Via Analytical Equation) = $7.1623 * 10^9$*

*Current Population (Via Euler Approximation) = $7.1636 * 10^9$*

*Current Population (Via Taylor 2nd Order Approximation) = $7.1625 * 10^9$*

*Current Population (Via Taylor 3rd Order Approximation) = $7.1623 * 10^9$*

*Current Population (Actual) = $7.7642 * 10^9$*