

Lab 3

① tolerance = $10e^{-5}$
 root = 0.61906
 iterations = 4
 starting value = 0

iterations = 3
 starting value = 0.5

root = 1.51213
 iterations = 3
 starting value = 1.5

② Root close to 4.5 = 4.4936139
 tolerance = $10e^{-7}$
 iterations = 3

Root close to 7.7 = 7.72525183
 tolerance = $10e^{-7}$
 iterations = 4

③ $x_0 = 4.51$
 $x_1 = 4.5$

$x_0 = 7.69$
 $x_1 = 7.7$

tolerance = $10e^{-5}$
 iterations = 3

tolerance = $10e^{-7}$
 iterations = 5

root = 4.49309

root = 7.72525

④ ~~$2x^2 + 6e^{-x} - 4 = 0$~~
 ~~$-\ln(4 - 2x^2) = x$~~

(9) Forming a converging function

$$f(x) = 2x^2 + 6e^{-x} - 4 = 0.$$

$$\therefore g_1(x) = -\ln\left(\frac{4 - 2x^2}{6}\right)$$

$$g_2(x) = \sqrt{\frac{4 - 6e^{-x}}{2}}$$

$$|g_1'(x)| = \left| \frac{-6}{4 - 2x^2} \right|$$

$$|g_2'(x)| = \left| \frac{3e^{-x}}{\sqrt{2}\sqrt{4 - 6e^{-x}}} \right|$$

$$\text{tolerance} = 10e^{-7}$$

Using $g_1(x)$

$$x_0 = 0.5$$

$$\text{root} = \boxed{0.615373}$$

$$\text{iterations} = 83$$

$$x_0 = 0.7$$

$$\text{root} = \boxed{0.61538}$$

$$\text{iterations} = 82$$

Using $g_2(x)$

$$x_0 = 0.5$$

$$\text{root} = 0.8308 + i810e^{-7}$$

$$\text{iterations} = 47$$

$$x_0 = 0.7$$

$$\text{root} = \boxed{0.838079}$$

$$\text{iterations} = 44$$