LAB-7

(1) " when x = [0 1 3 4 9]

P(M) = -0.2607x4 +3.58x3 - 13.95x2 +14.628x +8

(8 15 5 0) A when .

P(51) = 0.457x3 -4.828x2 + 8.371x +8

- When St. [0 1 8]

P(x): -0.719x2 +4.714x +8

(· [8 0]

- for two points ber obtain a linear line on including more points, was obtain more higher degree terms. The method followed is Lagrange's Interpolation.
- on increasing the no of points, we obtain a better approximation to the existing polynomial function. Here we can also expect lower error for higher number of points.
- . All graphs are altached at the end.

(02) · Via lagrangis Method:

 $p(x) = -0.00024x^{10} + 0.0023x^{9} - 0.012x^{8} + 0.0481x^{7} - 0.155x^{6} + 0.426x^{5} - 0.971x^{4} + 1.767x^{3} - 2.413x^{2} + 3.197x - 1$

· Via Mastor's Interpolation:

p(a) · 299x + 54

 $+ (5.0-10)(1.0-10) \times (5.0-10) \times (1.0-10) \times$

on expanding, both the polynomial toph out to be the

This can be seen from the Greage or well

- · On using Bisection Method for 30 itorations, we obtain a
- Another interesting observation is that, all 3 graphs
 almost coincide. This can be attailabled to the Jack that
 ame we have Il points between 0 to 1 (relatively high),
 hence we have a greater accuracy while approximating.
 [Al-though the above Jack is not always necessary Runge Phromison)
 Staff attacked at the tool.

. Graph attached at the end.

Os) Rung Phonominos is the problem of oscillation of the edges who using polynomial interpolation with polynomials g high degree. The above phonomenon can be clearly good from the graphs.

Observations:

A) Error Plots:

increase significantly, but the error at the midpoints docraces to a considerable extent.

This canbo way sean from the error plots

B) Palynamials.

The introductd polynomials (via Newton's Methods), also display a similal property like the error plots. Higher n'e polynomials oscillate willy at the edges, but have a better estimation in the mid part.

In contract lower in values, have low error at the edges, but have a pool estimation in the midpoints.
This can also be seen from the polynomial plot.

For n=5 & n=15, the interpolated & actual polynomial are technically supposed to meet at Dr x=0, and have only one intersection point but due to Matian's a accuracy Aprecision limitation, the interpolated polynomial graph shift slightly down and it now intersects with the actual graph at 1=-d to x=+of, leading to an extra intersection point (which should technically not be there).