

## The Integrand in 3 Dimensions:

`In[ ]:= x[k_, l_] := k * l`

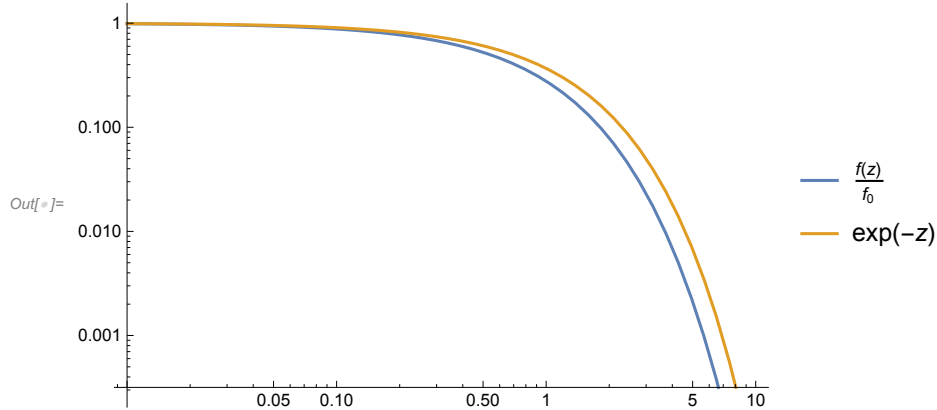
`In[ ]:= Rx[θ_] :=  $\left( (1.334 * E^{(-x / \cos[\theta])} * \cos[\theta]) / (1 - 1.334^2 * (\sin[\theta])^2)^{1/2} \right)$`

`In[ ]:= f[z_] := NIntegrate[2 * Pi * Sin[θ] * Rx[θ], {θ, 0, ArcSin[1/1.334]}] / (2 * Pi)`

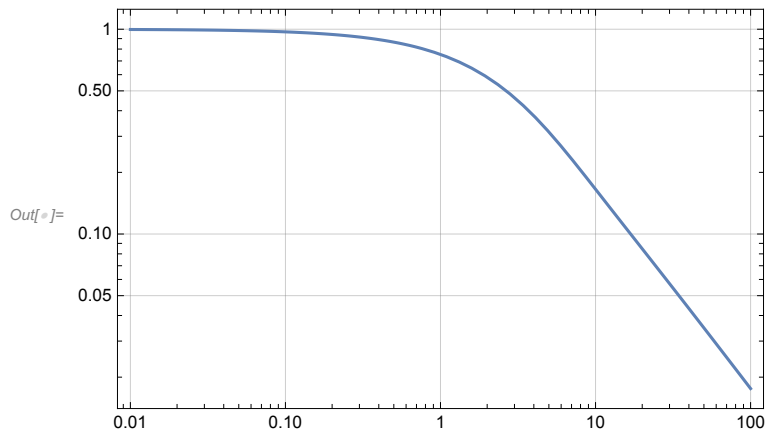
`In[ ]:= fθ = f[0]`

`Out[ ]:= 0.749625`

`In[ ]:= LogLogPlot[{f[z] / fθ, Exp[-z]}, {z, 0.01, 10}, PlotLegends → "Expressions"]`



`In[ ]:= LogLogPlot[(f[z] / fθ) / Exp[-z], {z, 0.01, 100}, Frame → True, GridLines → Automatic]`



`In[ ]:= a = Series[Cos[x], {x, 0, 6}]`

`Out[ ]:=  $1 - \frac{x^2}{2} + \frac{x^4}{24} - \frac{x^6}{720} + O[x]^7$`

`In[ ]:= b = Series[Sin[x], {x, 0, 7}]`

`Out[ ]:=  $x - \frac{x^3}{6} + \frac{x^5}{120} - \frac{x^7}{5040} + O[x]^8$`

In[ ]:= **c = Series[Exp[Cos[x]], {x, 0, 7}]**

$$\text{Out[ ]} = e - \frac{e x^2}{2} + \frac{e x^4}{6} - \frac{31 e x^6}{720} + O[x]^8$$

In[ ]:= **d = Exp[-1.334/a]**

$$\text{Out[ ]} = 0.263421 - 0.175702 x^2 - 0.0146126 x^4 + 0.00603081 x^6 + O[x]^7$$

In[ ]:= **e = (1.334 \* a)^2**

$$\text{Out[ ]} = 1.77956 - 1.77956 x^2 + 0.593185 x^4 - 0.0790914 x^6 + O[x]^7$$

In[ ]:= **integrand = (1.334 \* Pi \* a \* b \* d) / (1 - e)^0.5**

$$\text{Out[ ]} = (7.65621 \times 10^{-17} - 1.25035 i) x + (1.60054 \times 10^{-16} + 0.240413 i) x^3 + (3.51055 \times 10^{-16} - 0.717689 i) x^5 + (7.57894 \times 10^{-16} - 1.15189 i) x^7 + O[x]^8$$

In[ ]:= **CoefficientList[integrand, x]**

$$\text{Out[ ]} = \{0, 7.65621 \times 10^{-17} - 1.25035 i, 0, 1.60054 \times 10^{-16} + 0.240413 i, 0, 3.51055 \times 10^{-16} - 0.717689 i, 0, 7.57894 \times 10^{-16} - 1.15189 i\}$$

In[ ]:= **NIntegrate[(1.334 \* Pi \* a \* b \* d) / (1 - e)^0.5, {x, 0, ArcSin[1/1.334]}] / (2 \* Pi)**

**NIntegrate:** The integrand

$(7.65621 \times 10^{-17} - 1.25035 i) x + (1.60054 \times 10^{-16} + 0.240413 i) x^3 + (3.51055 \times 10^{-16} - 0.717689 i) x^5 + (7.57894 \times 10^{-16} - 1.15189 i) x^7 + O[x]^8$  has evaluated to Overflow, Indeterminate, or Infinity for all sampling points in the region with boundaries {{0, 0.847496}}.

$$\text{NIntegrate}\left[\frac{1.334 \pi a b d}{(1-e)^{0.5}}, \{x, 0, \text{ArcSin}\left[\frac{1}{1.334}\right]\}\right]$$

$$\text{Out[ ]} = \frac{\quad}{2 \pi}$$