

# Functional Programming

## Reflections

## Questions and Answers

## Course content

- Functions as first-class values.
- Algebraic and abstract data types.
- Polymorphism and classes.
- Testing functional programs.
- Lazy evaluations and infinite objects.
- Monads.

## Learning outcomes

- Write small to medium-sized functional programs for a variety of applications.
- Exploit a variety of programming techniques typical in functional programming, such as:
  - Use of recursion,
  - Modelling with recursive datatypes,
  - Abstraction and reuse with the help of higher order functions and monads.
- Appreciate the strengths and possible weaknesses of the functional programming paradigm.

# Functions as first class values

- This is a key aspect of functional programming.
- Higher order functions
  - Powerful way to build modular and reusable code.
    - Especially when combined with polymorphism.
- Using functions to represent data

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## Example: an abstract data type for sets

```
data Set a

empty      :: Set a
singleton  :: a -> Set a
insert     :: a -> Set a -> Set a

union, intersection, difference
          :: Set a -> Set a -> Set a

complement :: Set a -> Set a

member     :: a -> Set a -> Bool

toList     :: Set a -> [a]
```

- Probably need some constraints, **Eq** a or **Ord** a, depending on implementation.

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# How to represent sets

## Three possible representations

- Lists

```
data Set a = Set [a]
```

- Binary search trees

```
data Set a = Empty | Node a (Set a) (Set a)
```

- Functions

```
data Set a = Set (a->Bool)
```

- Which is easier?

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## Representing sets as lists

```
data Set a = Set [a] -- Invariant: no duplicates
```

```
empty = Set []
```

```
singleton x = Set [x]
```

```
insert x (Set xs) | x `elem` xs = Set xs
                  | otherwise   = Set (x:xs)
```

```
member x (Set xs) = x `elem` xs
```

```
union      (Set xs) (Set ys) = Set (xs++[y|y<-ys,y `notElem` xs])
```

```
intersection (Set xs) (Set ys) = Set [x|x<-xs,x `elem` ys]
```

```
difference  (Set xs) (Set ys) = Set [x|x<-xs,x `notElem` ys]
```

- Fairly easy. Only finite sets. Only types in the **Eq** class. No complement.
- Variant: keep the lists ordered for efficiency...

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# Representing sets as binary search trees

```

data Set a = Empty | Node a (Set a) (Set a)
-- Invariant: smaller elements to the left,
--            bigger to the right
empty = Empty
singleton x = Node x Empty Empty

insert x Empty = singleton x
insert x (Node y l r) | x==y = Node y l r
                      | x<y  = Node y (insert x l) r
                      | x>y  = Node y l (insert x r)

member x Empty = False
member x (Node y l r) = x==y ||
                        member x (if x<y then l else r)

```

- More complicated. Only finite sets. Only types in the **Ord** class. No complement.
- Even more complicated if we want to keep the trees balanced. ([Data.Set](#))

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# Representing sets as functions

```

data Set a = Set (a->Bool)

empty = Set (const False)
singleton x = Set (==x)
insert x s = union (singleton x) s

member x (Set f) = f x

```

```

union      (Set f) (Set g) = Set (\x->f x || g x)
intersection (Set f) (Set g) = Set (\x->f x && g x)
complement (Set f)         = Set (not . f)

difference s1 s2 = intersection s1 (complement s2)

```

- It's the easiest of the three! All operations are one-liners!
- Allows infinite sets and complement, but no `toList`, unlike the others.

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# Software prototyping experiment (1)

**Haskell vs. Ada vs. C++ vs. Awk vs. ...  
An Experiment in Software Prototyping Productivity**

**Paul Hudak and Mark P. Jones**

**Research Report YALEU/DCS/RR-1049  
October 1994**

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## Software prototyping experiment (2)

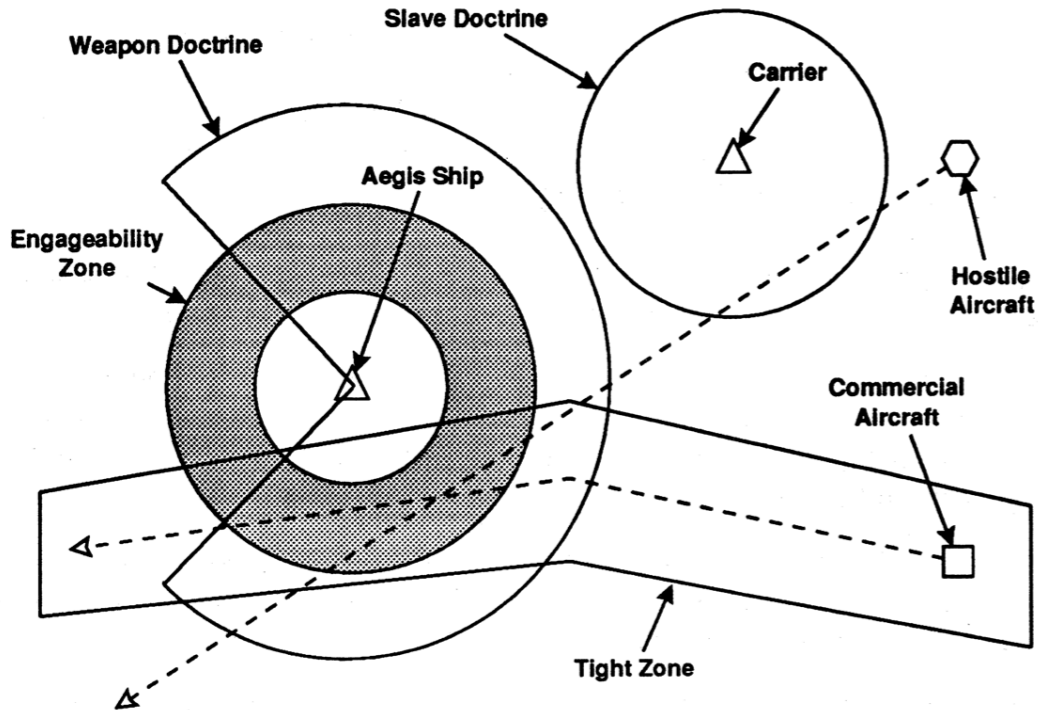


Figure 2: Geo-Server Input Data

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## Software prototyping experiment (3)

Language	Lines of code	Lines of documentation	Development time (hours)
(1) Haskell	85	465	10
(2) Ada	767	714	23
(3) Ada9X	800	200	28
(4) C++	1105	130	–
(5) Awk/Nawk	250	150	–
(6) Rapide	157	0	54
(7) Griffin	251	0	34
(8) Proteus	293	79	26
(9) Relational Lisp	274	12	3
(10) Haskell	156	112	8

Figure 3: Summary of Prototype Software Development Metrics

## Software prototyping experiment (4)

### Key design choice

```
type Region = Point -> Bool  
type Point = (Double, Double)
```

- This makes all operations on regions easy to define
  - Basic shapes: circles, rectangles, etc
  - Geometric transformations, e.g. moving, scaling & rotating regions
  - Unions, intersections, complements
  - Membership tests

## What can Haskell be used for?

### Examples

- GHC is implemented in Haskell.
- [Hackage](#): lots of free Haskell libraries and applications.
- Investment banking: financial modelling, quantitative analysis.
- Facebook: [HaXL](#), spam filtering.
- Keera Studios: game development, Android.
- More: [Haskell in Industry](#)
- [Haskell Communities and Activities Report](#), [November 2017 issue](#)

What can Haskell be used for? → Examples

From lwn.net: **Stephen Diehl: Reflecting on Haskell in 2017:**

- 14,000 new Haskell projects on Github!
- "It's really never been an easier and more exciting time to be programming professionally in the world's most advanced (yet usable) statically typed language."

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## Some Haskell software I have worked on

- These slides: formatting and syntax high-lighting.
- [WebFudgets](#).
- [Programatica](#): Haskell compiler front-end (2001-2006)
- [House](#): a prototype operating system in Haskell (2004-2006)
- Hardware emulation (6502 8-bit processor, used in C-64)
- An e-commerce system in Haskell (2006-2009)
- A web browser in Haskell (mid 1990s)
- [Alfa](#): GUI for the proof assistant Agda (mid 1990s)
- [Fudgets](#): GUI library in Haskell (early 1990s)

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## Questions and Answers

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## Recommended video

- [Keynote: Why Functional Programming Matters - John Hughes, Mary Sheeran](#) (Code Mesh, London 2015)

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## The End

- Good luck with your projects!
- See you next week!