

Assignment no.2

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Introduction

This project focuses on analyzing a large dataset using Spark. Here the project enabled us to load all the provided data, perform data transformation and analysis on them and finally train it using machine learning models for predicting outcome.

Now the dataset provided is of The New York City Taxi and Limousine Commission (TLC) which is responsible for licensing and regulating New York City's taxi cabs since 1971. The data provided were in parquet files from the years 2015 to 2022 And they were classified based on the taxi color green and yellow.

The project involved several steps starting from uploading all the data to the Azure container, then mounting Azure to the DataBricks environment, then reading the data, cleaning it, analyzing it and finally training it on two machine learning models (Linear Regression and Random Forest Regression) to predict the outcome of the total fare amount.

Methodology

The Data and Cloud Upload

For this project the dataset from the New York City Taxi and Limousine Commission (TLC) was used. There were 16 data files in parquet. The data files were classified according to the taxi cab color and the year of the ride. We had two taxi colors yellow and green and the year of ride ranged from 2015 to 2022. Apart from the 16 parquet data files there was another file in csv format which held the location details and the IDs.

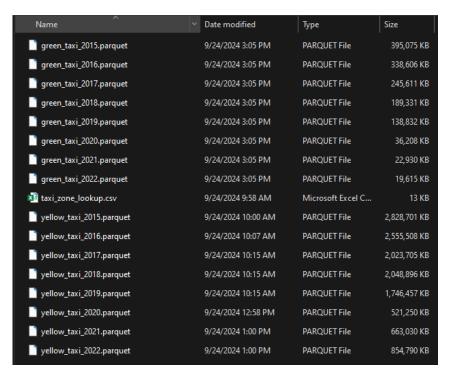


Figure 1: The .parquet and .csv data files

So, for this project we had to upload all 17 files to our Microsoft Azure Cloud container for future use of mounting it to the Databricks application.

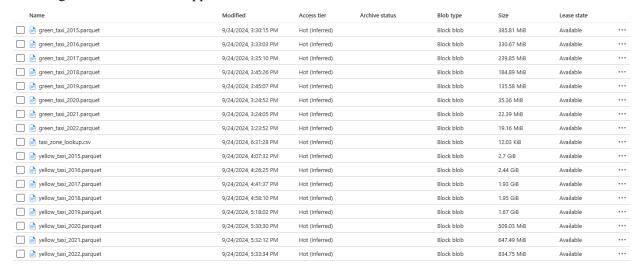


Figure 2: The .parquet and .csv data files uploaded to Azure Cloud container

All these files were uploaded into the Microsoft Azure container for future use in the time of data ingestion into Databricks The Storage Account Access key is the important credential needed for use in time of mounting the data in Databricks. This was found in the "Access Keys" tab under the storage account.



Figure 3: Access Key to Microsoft Azure Container

Azure mounting and Data Ingestion

As we sign in to our Community Edition of Databricks, we create a new notebook under Worksheet. This is the place where all of our codes and queries were written and ran.

The purpose of Microsoft Azure's mounting in the Databricks is to be able to access the data as if they were a part of Databrick's file system (DBFS).

```
storage_account_name = "shaqran39"
storage_account_access_key = "yQTb+AMZogT9ie2qeFSUIyKtrt/iPg7ZRPOiNFvwdboubyr4+cyf2uem9q57uUM01x7W803MNPDR+AStfpVP4g=="blob_container_name = "bde-assignment2"

dbutils.fs.mount[
source = f'wasbs://{blob_container_name}@{storage_account_name}.blob.core.windows.net',
mount_point = f'/mnt/{blob_container_name}/',
extra_configs = {'fs.azure.account.key.' + storage_account_name + '.blob.core.windows.net': storage_account_access_key}
}
```

Figure 4: Code to mount Microsoft Azure Container to the Databricks File System (DBFS)

After we have mounted, we read the files and put them in dataframes according to the colors and the csv is loaded to a separate dataframe.

Just so that our processing time is quicker we copy all the files from our mounted directory and copy them into Databrick's File System.



Figure 5: Code to copy all the files from the mounted directory to a newly made directory inside DBFS

Reading the DBFS data

After the copying is done, we proceed to reading the files and putting them on dataframes and from this step onwards we will be using these dataframes for all the next parts of joining data, cleaning data, performing analysis and finally training the models.

```
# Reading Parquet files from DBFS (filtering by name)
green_taxi_df = spark.read.parquet("/dbfs/FileStore/Assignment2/green_taxi*.parquet")
yellow_taxi_df = spark.read.parquet("/dbfs/FileStore/Assignment2/yellow_taxi*.parquet")

# Reading the CSV file from DBFS
taxi_zone_lookup_df = spark.read.csv("/dbfs/FileStore/Assignment2/taxi_zone_lookup.csv", header=True, inferSchema=True)

* (4) Spark Jobs

| (4) Spark Jobs
| (5) green_taxi_df: pyspark.sql.dataframe.DataFrame = [VendorID: long, |pep_pickup_datetime: timestamp ... 18 more fields]
| (6) yellow_taxi_df: pyspark.sql.dataframe.DataFrame = [VendorID: long, tope_pickup_datetime: timestamp ... 17 more fields]
| (7) tope | taxi_zone_lookup_df: pyspark.sql.dataframe.DataFrame = [LocationID: integer, Borough: string ... 2 more fields]
```

Figure 6: Reading the files to dataframes from the Databrick's File System (DBFS)

After that we count the number of records for the green and yellow taxi dataframes. We find that

- Green taxi dataframe has 66,200,401 records and 20 features
- Yellow taxi dataframe has 663,055,251 records and 19 features

Figure 7: Counting the rows and columns of the tallow and green taxi dataframes

Converting a parquet file to a csv file

According to the project instruction, we were asked to convert the parquet file of green taxi data from the year 2015 and convert that into a csv file.

Figure 8: Reading the file and converting it to a csv file

Here, we are reading the saved file from the DBFS and then we are converting it to a csv file. As we convert the parquet file to a csv, the actual csv is found in the directory.

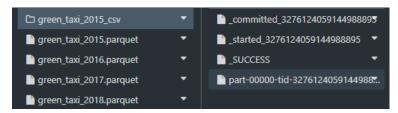


Figure 9: Browsing file directory to find the resultant csv file

After converting it we now check the file size and compare. We see that the newly made csv file has a size of 2078.17 MB where as the parquet file has a size of 385.81 MB.

```
# List the files and display the size of the newly created CSV file
files = dbutils.fs.ls("dbfs/FileStore/Assignment2/green_taxi_2015_csv/")

for file in files:
    if file.name.endswith(".csv"): # Only show CSV files
    print(f"File: {file.name}, Size: {file.size / (1024 * 1024):.2f} MB")

File: part-00000-tid-3276124059144988895-164cba59-c975-437c-ale1-cb171214afb2-8-1-c00
0.csv, Size: 2078.17 MB
```

Figure 10: Finding out the size of the newly made csv file

```
# List the files in the directory where the green_taxi_2015.parquet file is located parquet_files = dbutils.fs.ls("/dbfs/FileStore/Assignment2") # Replace with the actual path to your Parquet file

# Loop through the files and find the Parquet file
for file in parquet_files:
    if file.name == "green_taxi_2015.parquet": # Exact name of the Parquet file
        print(f"Parquet File: {file.name}, Size: {file.size / (1024 * 1024):.2f}
        MB")

Parquet File: green_taxi_2015.parquet, Size: 385.81 MB
```

Figure 11: Finding out the size of the newly made csv file

Combining the Dataframes

After we have successfully copied the files in the DBFS and read to the dataframes, the next job is to combine all the data from the green and yellow dataframes. We combine the two green and yellow taxi dataframes using their common columns. Also we added a new column "Taxi_color", depending upon from where the record is from.

Figure 12: Combining two dataframes together

After that we are to combine the resultant dataframe to the location dataframe.

Figure 13: Combining the above dataframe to the taxi zone lookup dataframe

The above code combines the combined_taxi_df by joining it with a location lookup table (taxi_zone_lookup_df) twice—once for pickup and once for dropoff locations. It adds details such as borough, zone, and service zone for both the pickup (PU_) and dropoff (DO_) locations, using their respective IDs.

Finally, we drop the redundant columns coming from the location lookup table.

Figure 14: Dropping the redundant columns from the final dataframe.

Exporting the Combined Dataframe to a parquet file

For quicker computation time and easy data retrieval we are to export the combined dataframe to the Databrick's File System and as a parquet file.

```
1 combined_taxi_df.write.mode("overwrite").parquet("/dbfs/FileStore/tables/combined_taxi_data.parquet")
2
3
(2) Spark Jobs
```

Figure 15: Converting the combined dataframe as a parquet file and putting it in the DBFS

Data Cleaning

The data cleaning is one the most important parts of any data project. The large dataset we had involving the taxi ride records, we needed to make sure all the data were meaningful. For the entire data cleaning part, 6 steps of cleaning were performed:

a. We made sure that no records were there where the trip start time and end time were wrong. We made sure, that there were no records with trip finish time was earlier than trip start time.

```
    ▶ ▼ ✓ Showrsago (<1s)

# Step 1: Remove trips where dropoff is before pickup combined_taxi_df = combined_taxi_df.filter(combined_taxi_df.tpep_dropoff_datetime >= combined_taxi_df.tpep_pickup_datetime)

| ■ combined_taxi_df: pysparksql.dataframe.DataFrame = [VendorID: long, tpep_pickup_datetime: timestamp ... 23 more fields]
```

Figure 16: Filtering out only the records that have trip drop-off time greater than pickup time

b. We made sure that the pickup and drop-off datetime were within the range. Here we have data from 2015 to 2022. So, all of the data we have needs to be within that time.

```
from pyspark.sql.functions import year

# Filter the DataFrame to keep only rows where the pickup and dropoff dates are between 2015 and 2022
# Filter the DataFrame to keep only rows where the pickup and dropoff dates are between 2015 and 2022
combined_taxi_df = combined_taxi_df.filter(
    (year(combined_taxi_df['tpep_pickup_datetime']) >= 2015) &
    (year(combined_taxi_df['tpep_dropoff_datetime']) <= 2022) &
    (year(combined_taxi_df['tpep_dropoff_datetime']) <= 2022)
}</pre>
```

Figure 16: Filtering out only the records that are within the years 2015 to 2022

c. We made sure that there were no records of trips with negative speed. For this we first made a column "speed_mph", we chose miles as unit of distance as it was an American based data source. So, after making the column we filtered it and removed trip with zero or negative speed.

Figure 16: Creating a new column speed_mph and then filtering out values which are zero or negative

d. We filtered out trips with very high speed. We first calculated the record with the highest speed. And found that it was 3079127441.7391305 mph.

```
max_speed = combined_taxi_df.agg(F.max("speed_mph")).collect()[0][0]

# Display the maximum speed
print(f"The highest speed in the dataset is: {max_speed} mph")

> (2) Spark Jobs

The highest speed in the dataset is: 3079127441.7391305 mph
```

Figure 17: Finding out trip with the highest speed

After this we found out that NYC highways has the highest speed of 65mph. So, we filtered out records above 65mph.

```
combined_taxi_df = combined_taxi_df.filter(F.col("speed_mph") <= 65)</pre>
combined_taxi_df: pyspark.sql.dataframe.DataFrame = [VendorID: long, tpep_pickup_datetime: timestamp ... 25 more fields]
```

Figure 18: Filtering the dataset and keeping only the records with speed equal or below 65mph

e. We filtered out trip which are too short and which are too long(distance wise). Here we will be keeping records which are at least of 0.1 miles and equal or below 100 miles.

```
# Step 8: Remove trips that are too short or too long (distance-wise)

# Assume trips less than 0.1 miles or greater than 100 miles are unrealistic

combined_taxi_df = combined_taxi_df.filter((F.col("trip_distance") >= 0.1) & (F.col("trip_distance") <= 100))

| Step 8: Remove trips that are too short or too long (distance-wise)

# Assume trips less than 0.1 miles or greater than 100 miles are unrealistic

combined_taxi_df = combined_taxi_df.filter((F.col("trip_distance") >= 0.1) & (F.col("trip_distance") <= 100))
```

Figure 19: Filtering the dataset and keeping only the records with trip distance from 0.1 miles up to 100miles

f. We filtered out trip which are too short and which are too long(duration wise). Here we will be keeping the data which are equal or above 1 min in trip duration and ranges till 2 hours.

```
# Step 6: Remove trips that are too short or too long (duration-wise)

# Assume trips less than 1 minute or greater than 2 hours are unrealistic

combined_taxi_df = combined_taxi_df.filter((F.col("trip_duration_hours") >= 1/60) & (F.col("trip_duration_hours") < 2))

| Combined_taxi_df: pyspark.sql.dataframe.DataFrame = [VendorID: long, tpep_pickup_datetime: timestamp ... 25 more fields]
```

Figure 20: Filtering the dataset and keeping only the records with trip duration from 1 minute to up to 2 hours

After cleaning we find that the column had a total of 719568021 rows and 21 features. We will be analyzing this dataset in the next steps and training machine learning models on it.

Figure 21: Counting the total number of rows and columns of the final dataset

Business Questions

Trip Analysis by Year and Month

In this query we had to go through the entire dataset and calculate the total number of trips per month providing insights. The query also had important rows like day of the week, hour of the day with most trips, average number of passengers per trip, average amount paid per trip, average amount paid per passenger.



Figure 22: Table from business question no1

The table above shows the total number of trips for each month. It indicates the day of the week which had the highest number of trips in each month. The first day 1= Monday and last day of the week is consider 7=Sunday. And the hour of the day shows the hour with the most trips. This is set in a 24hour format.

Trip Duration, Distance, and Speed by Taxi Color (Yellow and Green)

In this query we calculate the average, median, minimum and maximum trip duration, trip distance and speed in kmph for the two colored taxi cabs.



Figure 23: Table from the business question no2

The analysis of journey length, distance traveled, and speed for yellow and green cabs is shown in this table:

- Yellow taxis had slightly longer trips—14.41 minutes—than green taxis, which have an average travel duration of 13.96 minutes.
- Average Travel Time (min): The average travel time for yellow and green taxis is 11.28 and 10.72 minutes, respectively.
- Maximum Trip Time (min): For both kinds of trips, the maximum time is 119.98 minutes.
- The average trip distance (kilometers) traveled by green taxis is 3.06, which is somewhat greater than the 3.03 kilometers traveled by yellow taxis.

- Minimum and Maximum Trip Distance (km): The range of excursions for both taxi kinds is from 0.1 km to around 99.9 km.
- Yellow taxis average 18.74 km/h, slightly slower than green taxis' average of 20.27 km/h.
- Median Speed (km/h): The median speed for green taxis is greater (18.36 km/h) than for yellow taxis (16.44 km/h).
- Maximum Speed (km/h): The top speed attained by both varieties of taxis was 104.61 km/h.

This information offers a thorough analysis of the variations in journey duration and speed between different colored taxi. Although the maximum trip lengths and distances for both types of taxis are quite comparable, green taxis appear to run at slightly quicker rates on average.

Trips by Pickup and Dropoff Locations (Boroughs)

Through this query, for each pair of pickup and dropoff locations we found out the total number of trips, average distance, average amount paid per trip, total amount paid. Here we used the Borough information for the pickup and dropoff location.

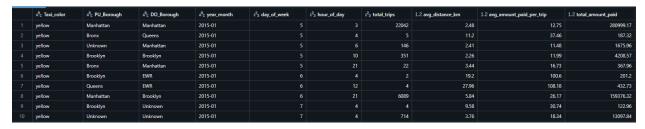


Figure 24: Table outcome for business question no 3

This table analyzes yellow and green taxi journeys between several boroughs, providing financial data and trip details:

The starting and finishing boroughs for each trip are indicated by the boroughs PU_Borough (Pickup Borough) and DO_Borough (Dropoff Borough).

Month and Year: Monthly grouping of the data begins in January 2015 (2015-01).

Day of the Week: Shows which day of the week is busiest for each combination of boroughs (1 = Monday, 7 = Sunday).

Hour of the Day: Displays the hour when every pair of pickup and drop-off locations had the most journeys.

Total Trips: The quantity of travels made for every combination of boroughs. For instance, in January 2015, 22,042 journeys were place inside Manhattan.

Percentage of Trips with Tips

Through this query we calculated the percentage of trip where the tips were given. From the final dataset as we analyze we find that the percentage is 63.54%

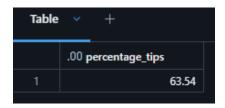


Figure 25: Table outcome for business question no4

Percentage of Trips with Tips of at Least \$5

For this query we go through the trips with tips again and calculate the percentage of those where the tip amount was at least 5\$.

After going through the data we find that percentage was 12.23%.

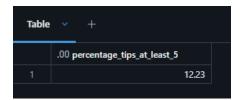


Figure 26: Table outcome for business question no5

Classifying Trips by Duration and Calculating Metrics

Through this query, trips were classified into bins. The following bins:

- Under 5 minutes
- From 5 to 10 minutes
- From 10 to 20 minutes
- From 20 to 30 minutes
- From 30 to 60 minutes
- At least 60 minutes

For each bin, the following were calculated:

- Average speed (km/h): Helps assess traffic conditions.
- Average distance per dollar (km/\$): Indicates fare efficiency.

Table · +				
	A ^B C duration_bin	1.2 avg_speed_kmph	1.2 avg_distance_per_dollar_km	
1	From 30 to 60 Mins	25.68	0.37	
2	At least 60 Mins	22.85	0.53	
3	From 10 to 20 Mins	17.72	0.26	
4	Under 5 Mins	19.57	0.16	
5	From 5 to 10 Mins	17.02	0.21	
6	From 20 to 30 Mins	21.25	0.31	

Figure 27: Table outcome for business question no6

- Duration Bin: Trips were grouped into 6 duration categories (e.g., "From 30 to 60 Mins," "From 10 to 20 Mins").
- Average Speed (km/h): The average speed of trips within each duration bin. Trips lasting from 30 to 60 minutes have the highest average speed (25.68 km/h), while shorter trips (e.g., under 5 minutes) tend to have lower speeds.
- Average Distance per Dollar (km/\$): This measures the fare efficiency by calculating how far the
 taxi travels per dollar. Longer trips (e.g., trips lasting at least 60 minutes) tend to offer more
 distance per dollar (0.53 km/\$), while shorter trips (e.g., under 5 minutes) have lower fare
 efficiency (0.16 km/\$).

This analysis suggests that longer trips are more cost-effective in terms of distance covered per dollar, while shorter trips are less efficient due to higher base fares. The optimal trip duration for balancing speed and fare efficiency is between 30 to 60 minutes.

Recommended Duration Bin for Maximizing Income

According to the previous business question we find that the optimal trip duration is between 30 to 60 minutes. But as we analyze to find the most rewarding trips, we see that the trips which are at least 60 minutes are the most rewarding.

	A ^B C duration_bin	1.2 median_total_amount
1	From 30 to 60 Mins	42.35
2	At least 60 Mins	64.34
3	From 10 to 20 Mins	14.76
4	Under 5 Mins	6.8
5	From 5 to 10 Mins	9.8
6	From 20 to 30 Mins	23.16

Figure 28: Table outcome for business question no7

Machine Learning

Baseline Model

For this project, the baseline model is a simple predictive model that uses historical averages to predict the total fare (total_amount) for each taxi trip. Instead of considering specific features like trip distance or duration to make predictions, the baseline model simply uses the average fare for similar trips based on factors such as:

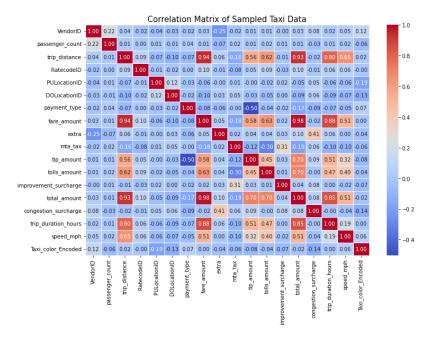
- Taxi color (yellow or green)
- Pickup and dropoff boroughs
- Month of the trip
- Day of the week
- Hour of the day

For every trip in the dataset, the baseline model assigns the average fare from trips with the same taxi color, boroughs, and time factors as the predicted fare (baseline_prediction). If no historical data is available for a specific combination of taxi color, borough, and time, a global average fare is used as the prediction.

The Root Mean Squared Error (RMSE) is computed by comparing the baseline predictions with the actual fare values (total_amount). RMSE provides a measure of the prediction error, where lower RMSE values indicate better performance. We got a RMSE score of 189.5.

Linear and Random Forest Regression

Before we ran the two models into the data. A lot of steps were taken. Since computational time was excessively high and as clusters collapsed and terminated many times, we chose 10000 random records to train the data. And before we trained our data we performed correlation matrix to find the relevant features for training. The following is the correlation matrix:



After that we chose the following as features and target:

The features were selected based upon the correlation scores with the target variable.

For the training data and testing data we make sure we follow the assignment requirement.

That is we take all the data for the training data except those from October, November, December from 2022. And for testing data we only take the data from October, November, December of 2022.

After that we tried running the data through spark ML but failed so we tried using sklearn and implemented our models.

- For Linear Regression we got an RMSE score of 5.86
- For Random Forest Regression we got an RMSE score of 5.63

The Root Mean Squared Error (RMSE) values of 5.86 for Linear Regression and 5.6 for Random Forest suggest that both models are performing somewhat similarly, with Random Forest slightly outperforming Linear Regression.

Challenges and Resolutions

In this Big Data project, several technical and operational challenges arose during the analysis of a large taxi trip dataset, which consisted of millions of records. These challenges were primarily due to platform limitations, data size, and infrastructure constraints.

Platform Limitations Due to Free Subscriptions

Challenge: One of the primary challenges was the use of non-paid subscriptions for both Azure and Databricks. As a result, many of the platform features, such as higher compute resources, larger storage capacity, and more advanced analytics tools, were not fully accessible. This significantly limited the scalability of the project and the speed of processing.

Resolution: With the limitations of a free-tier subscription, we attempted to optimize queries and processes to make the best use of the available resources. For example, we carefully chose which portions of the data to analyze first and focused on sampling data where possible to reduce computational strain. However, without access to the full platform capabilities, performance remained a bottleneck.

Long Query Processing Times Due to Large Dataset

Challenge: The dataset contained millions of rows, which led to extremely long query execution times. Basic operations such as filtering, aggregating, and joining the data required significant amounts of processing power and time. The scale of the data overwhelmed the available compute resources, leading to delays in analysis.

Resolution: To mitigate the long processing times, we experimented with data sampling techniques, working with smaller chunks of data initially to test code and logic. This allowed for quicker iterations on queries before running the full dataset. Additionally, we leveraged PySpark optimizations where possible, including caching frequently used DataFrames to minimize repeated computations.

Frequent Cluster Termination and Short Idle Time

Challenge: The Databricks clusters frequently terminated due to inactivity or exceeded execution time limits. The idle time before the clusters automatically terminated was very short, which disrupted long-running queries and batch processes. This frequent downtime significantly affected productivity.

Resolution: We attempted to minimize the occurrence of idle time by scheduling jobs more frequently and closely monitoring cluster usage. Unfortunately, the frequent termination of clusters due to resource constraints limited our ability to efficiently manage long-running queries and processes.

Failure to Write Parquet File to CSV in Azure

Challenge: When attempting to write back the final dataset (which was in Parquet format) to CSV format in the Azure Blob Storage, multiple attempts resulted in write failures. These failures were likely caused by storage limitations or access restrictions in the free-tier Azure account.

Resolution: After several attempts, we explored alternative approaches, such as exporting smaller data chunks instead of the full dataset at once. Unfortunately, with the limited storage capacity and permissions, we were unable to successfully export the complete dataset as CSV. This highlighted the need for an upgraded Azure subscription with more robust storage options and permissions.

Failure to Copy the Final Dataset to DBFS (Databricks File System)

Challenge: A significant issue occurred when trying to copy the final dataset to DBFS (Databricks File System). Despite several attempts, the operation failed, most likely due to the large file size and storage restrictions in Databricks' free-tier environment.

Resolution: To overcome this, we performed the tasks by reading the datafiles again and again, combining and cleaning them on each resetting of the cluster.

Conclusion

This project utilized a large New York City taxi dataset with over 720 million rows to predict taxi fare amounts based on trip-related features such as trip distance, duration, and passenger count. After filtering the data and handling missing values, we developed and evaluated two models: Linear Regression and Random Forest Regression.

The Random Forest model outperformed Linear Regression, achieving an RMSE of 5.6 compared to 5.86 for Linear Regression, indicating that non-linear relationships between variables played a significant role in fare prediction. Despite the slight improvement, further optimizations such as hyperparameter tuning and feature engineering could enhance model performance.

Overall, the project demonstrated effective handling of big data, preprocessing techniques, and model building, providing useful insights into taxi fare prediction in a real-world context.

References

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