Introductory Scientific Computing with Python

More on numpy arrays

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Outline

- Matrices
- Least Squares Fit
- Random numbers
- Summary

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Matrices: Introduction

All matrix operations are done using arrays



Matrices: Initializing

```
In []: c = array([[11,12,13]],
                    [21, 22, 23],
                    [31,32,33]])
In []: c
Out[]:
array([[11, 12, 13],
        [21, 22, 23],
        [31, 32, 3311)
```

Initializing some special matrices

```
In []: ones((3,5))
Out[]:
array([[ 1., 1., 1., 1., 1.],
       [ 1., 1., 1., 1., 1.],
       [ 1., 1., 1., 1., 1.]])
In []: ones like([1, 2, 3, 4])
Out[]: array([1, 1, 1, 1])
In []: identity(2)
Out[]:
array([[ 1., 0.],
       [0., 1.11)
Also available zeros, zeros_like, empty, empty_like
```

Accessing elements

```
In []: c
Out[]:
array([[11, 12, 13],
       [21, 22, 23],
       [31, 32, 33]])
In []: c[1][2]
Out[]: 23
In []: c[1,2]
Out[]: 23
In []: c[1]
Out[]: array([21, 22, 23])
```

Changing elements

```
In []: c[1,1] = -22
In []: c
Out[]:
array([[ 11, 12, 13],
       [ 21, -22, 23],
       [ 31, 32, 33]])
In []: c[1] = 0
In []: c
Out[]:
array([[11, 12, 13],
       [ 0, 0, 0],
       [31, 32, 33]])
```

How do you access one column?



Slicing

```
In []: c[:,1]
Out[]: array([12, 0, 32])
In []: c[1,:]
Out[]: array([0, 0, 0])
In []: c[0:2,:]
Out[]:
array([[11, 12, 13],
       [0, 0, 0]
In []: c[1:3,:]
Out[]:
array([[ 0, 0, 0],
       [31, 32, 3311)
```

Slicing ...

```
In []: c[:2,:]
Out[]:
array([[11, 12, 13],
       [0, 0, 0]
In []: c[1:,:]
Out[]:
array([[ 0, 0, 0],
       [31, 32, 33]])
In []: c[1:,:2]
Out[]:
array([[ 0, 0],
       [31, 3211)
```

Striding

```
In []: c[::2,:]
Out[]:
array([[11, 12, 13],
        [31, 32, 33]])
In []: c[:,::2]
Out[]:
array([[11, 13],
        [ 0, 0],
        [31, 3311)
In []: c[::2,::2]
Out[]:
array([[11, 13],
        [31, 3311)
```

Shape of a matrix

Shape specifies shape or dimensions of a matrix

Elementary image processing

```
In []: a = imread('lena.png')
In []: imshow(a)
Out[]: <matplotlib.image.AxesImage object at 0xa0
imread returns an array of shape (512, 512, 4) which
represents an image of 512x512 pixels and 4 shades.
imshow renders the array as an image.</pre>
```

Slicing & Striding Exercises

- Crop the image to get the top-left quarter
- Crop the image to get only the face
- Resize image to half by dropping alternate pixels

Solutions

In []: imshow(a[:256,:256])

In []: imshow(a[200:400,200:400])

```
Out[]: <matplotlib.image.AxesImage object at 0xb7</pre>
In []: imshow(a[::2,::2])
Out[]: <matplotlib.image.AxesImage object at 0xb7</pre>
```

Out[]: <matplotlib.image.AxesImage object at 0xb6

Transpose of a Matrix

```
In []: a = array([[1, 1, 2, -1]],
                  [2, 5, -1, -9],
  . . . :
                  [2, 1, -1, 3],
  . . . :
                  [1, -3, 2, 7]
  . . . :
In []: a.T
Out[]:
array([[ 1, 2, 2, 1],
       [1, 5, 1, -3],
       [2, -1, -1, 2],
       [-1, -9, 3, 711)
```

Matrix Addition

```
In []: b = array([[3,2,-1,5]],
                [2, -2, 4, 9],
                [-1, 0.5, -1, -7]
                [9, -5, 7, 311)
In []: a + b
Out[]:
array([[ 4., 3., 1., 4.],
      [ 4., 3., 3., 0.],
      [1., 1.5, -2., -4.],
      [10., -8., 9., 10.]
```

Elementwise Multiplication

Matrix Multiplication

Inverse of a Matrix

Determinant and sum of all elements

```
In []: det(a)
Out[]: 80.0
```

```
In []: sum(a)
```

Out[]: 12



Eigenvalues and Eigen Vectors

```
In []: e = array([[3,2,4],[2,0,2],[4,2,3]])
In []: eig(e)
Out[]:
(array([-1., 8., -1.]),
 array([[-0.74535599, 0.66666667, -0.1931126],
        [0.2981424, 0.33333333, -0.78664085],
        [ 0.59628479, 0.66666667, 0.5864330311)
In []: eigvals(e)
Out[]: array([-1., 8., -1.])
```

Computing Norms

```
In []: norm(e)
```

Out[]: 8.1240384046359608



Singular Value Decomposition

```
In []: svd(e)
Out[]:
(array(
[[-6.6666667e-01, -1.23702565e-16, 7.4535599]
 [-3.33333333e-01, -8.94427191e-01, -2.9814239]
 [ -6.6666667e-01, 4.47213595e-01, -5.9628479
 array([ 8., 1., 1.]),
 array([[-0.66666667, -0.33333333, -0.66666667],
           , 0.89442719, -0.4472136 ],
        1−0.
        [-0.74535599, 0.2981424, 0.59628479]])
```

25 m

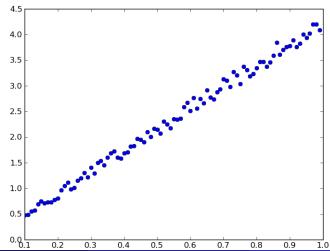


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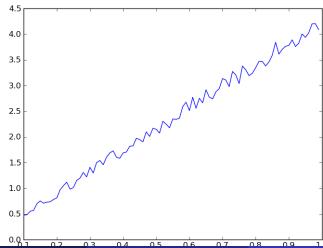
L vs. T² - Scatter

Linear trend visible.



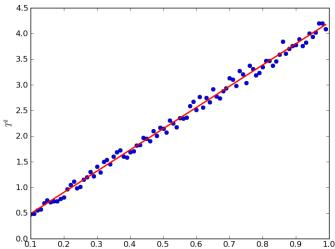
L vs. T^2 - Line

This plot is not a straight line, can we do better?



L vs. T² - Least Square Fit

This is what our intention is.



Matrix Formulation

- We need to fit a line through points for the equation $T^2 = m \cdot L + c$
- In matrix form, the equation can be represented as $T_{sq} = A \cdot p$,
- We need to find p to plot the line



$$\begin{bmatrix} T_1^2 \\ T_2^2 \\ \vdots \\ T_N^2 \end{bmatrix} = \begin{bmatrix} L_1 & 1 \\ L_2 & 1 \\ \vdots & \vdots \\ L_N & 1 \end{bmatrix} \cdot \begin{bmatrix} m \\ c \end{bmatrix}$$
 (1)

Or

$$T_{sq} = A \cdot p$$



Getting L and T^2

Generating A

```
In []: A = array([L, ones_like(L)])
In []: A = A.T
```

lstsq...

- Now use the lstsq function
- Along with a lot of things, it returns the least squares solution

```
In []: result = lstsq(A,tsq)
In []: coef = result[0]
```

Least Square Fit Line ...

We get the points of the line from coef

```
In []: Tline = coef[0]*L + coef[1]
```

```
In []: Tline.shape
```

 Now plot Tline vs. L, to get the least squares fit line.

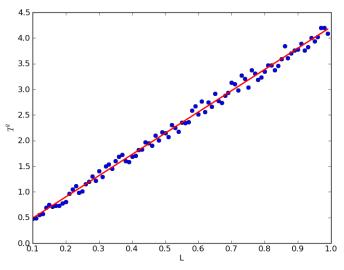
```
In []: plot(L, Tline, 'r')
```

```
In []: plot(L, tsq, 'o')
```

35 m



Least Squares Fit



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numpy.random

Easy random number generation

```
Or:
In []: import numpy
```

In []: random?

- In []: numpy.random
 - random.random: produces uniform deviates in (0, 1)
 - random.normal: draws random samples from a Gaussian distribution
 - Useful to create a random matrix of any shape

Using the random module

```
In []: x = random.random(size=100)
In []: y = random.random(size=100)
In []: scatter(x, y) # Scatter plot it.

In []: x,y = random.normal(size=(2,100))
In []: clf()
In []: scatter(x, y)
Note that size can be a tuple.
```

Using the random module

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What did we learn?

- Matrices
- Least Squares
- Random numbers

45 m

