

Statistical Modeling of Fatigue and Weakness in PLHIV: Ordinal, Multinomial, and Loglinear Approaches

Sharath Chandra Shankar - 2576017
Dec 2025



BE BOUNDLESS

W

Table of Contents

- Introduction
- Exploratory Data Analysis
- Game Plan
- Fatigue Prediction
- Weakness Prediction
- Loglinear Symptom Analysis
- Takeaways

Three-month trial of 609 PLHIV yielded 1,343 symptom reports on fatigue, weakness, and treatment

Setting the Background



The dataset under analysis comes from a longitudinal randomized controlled trial investigating the progression of fatigue and weakness among people living with HIV (PLHIV). A total of 609 HIV-positive participants were followed over a three-month period and asked to self-report the severity of two symptoms: fatigue and weakness.

Data Structure

Of the 609 individuals:

- 173 (28.41%) provided one symptom report
- 138 (22.66%) provided two reports
- 298 (48.93%) provided all three

After removing records with missing values, the final analytic dataset consists of 1,343 observations. Each record corresponds to a single individual at a single timepoint and includes their fatigue level, weakness level, and treatment group.



Contingency Table Framework

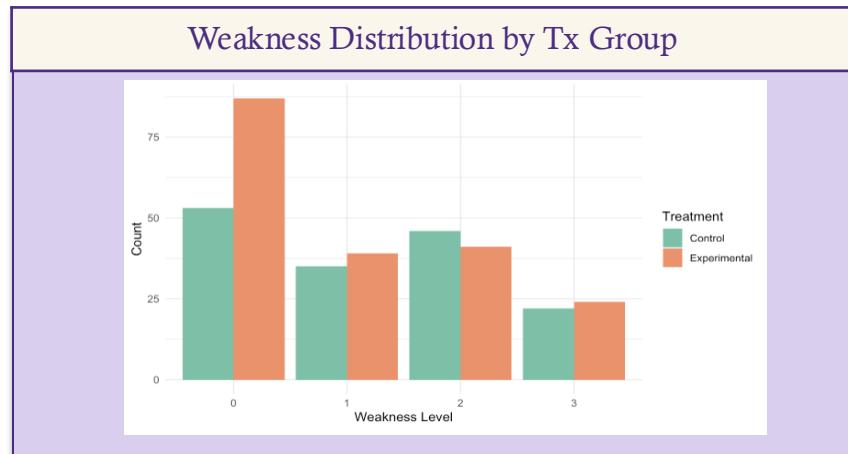
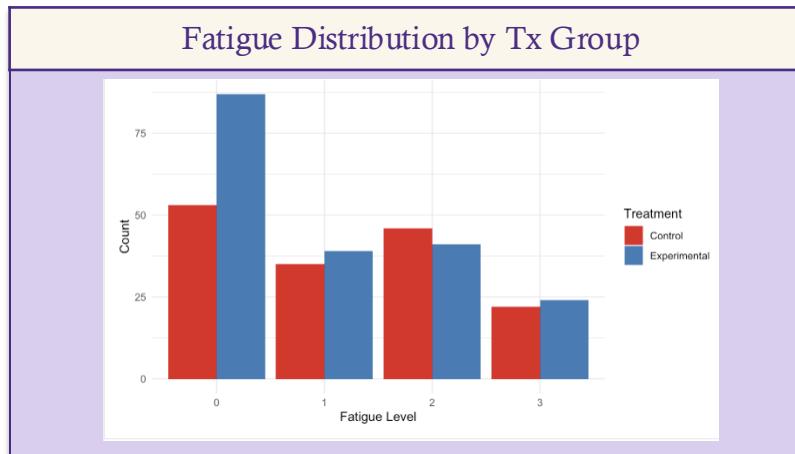
- The 1,343 observations can be arranged into a four-dimensional contingency table defined by SSC-F, SSC-W, TIME, and IC. This structure yields 96 possible cells ($4 \times 4 \times 3 \times 2$). Each cell count reflects the number of individuals in the control or intervention group who reported a specific combination of fatigue and weakness at a particular time point.
- For the purposes of this analysis, the TIME variable is disregarded.



Table of Contents

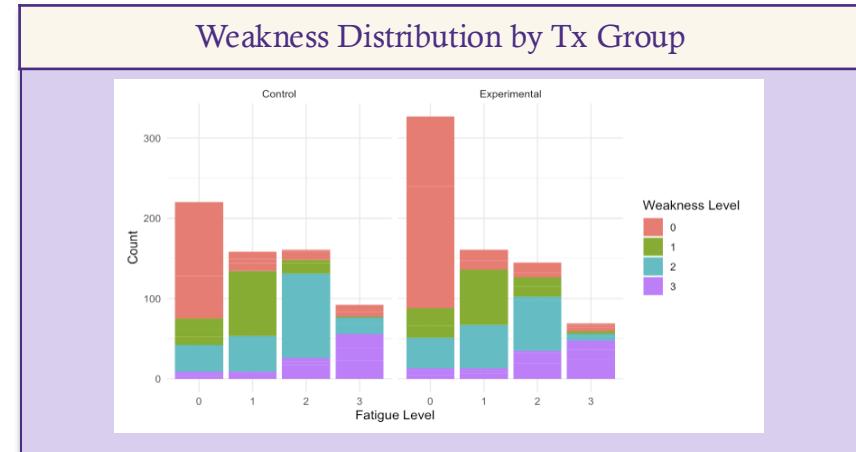
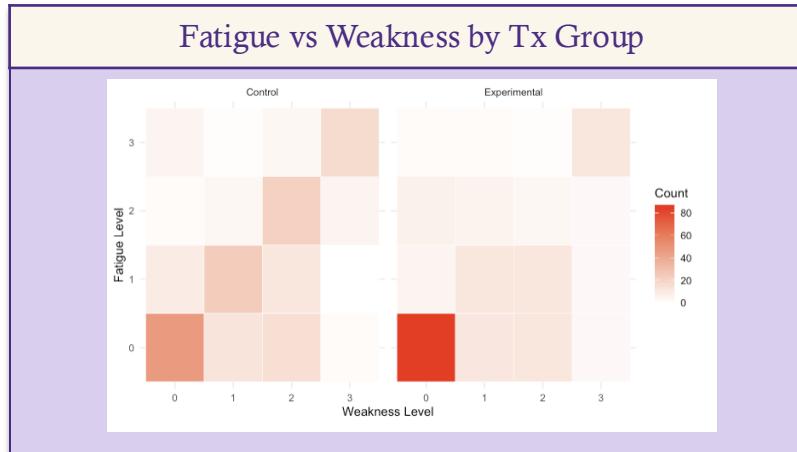
- Introduction
- Exploratory Data Analysis
- Game Plan
- Fatigue Prediction
- Weakness Prediction
- Loglinear Symptom Analysis
- Takeaways

Analyzing Symptom Distribution Shifts: The Impact of Experimental Treatment on Fatigue and Weakness



- The **Experimental** treatment group appears to experience a greater reduction in both **Fatigue** (more patients at Level 0) and **Weakness** (more patients at Level 0) compared to the **Control** group.
- However, the Experimental group also shows a higher count of patients at the maximum level (Level 3) for **Weakness**, suggesting the treatment's effect may be heterogeneous or have an inverse reaction in a small subset of patients.

Multivariate Analysis of Symptom Correlation: Treatment Efficacy on the Joint Distribution of Fatigue and Weakness



- The **Experimental** treatment group shows a much **stronger concentration** of patients experiencing both **no Fatigue (Level 0)** and **no Weakness (Level 0)** compared to the Control group. This suggests the treatment is highly effective at eliminating both symptoms simultaneously for a large subset of patients.
- Conversely, when **Fatigue is severe (Level 3)**, the distribution of Weakness is **less favorable** in the Experimental group, with a higher proportion of patients reporting **high Weakness (Levels 2 & 3)** compared to the Control group at the same Fatigue level. This reinforces the earlier finding that the treatment may have an inverse or non-responsive effect in a small, severely symptomatic subset.

Table of Contents

- Introduction
- Exploratory Data Analysis
- Game Plan
- Fatigue Prediction
- Weakness Prediction
- Loglinear Symptom Analysis
- Takeaways

Exploring 8 Modeling Approaches (Additive and Interaction) to Determine the Best-Fitting Model for Weakness and Fatigue

POLR (Proportional Odds / Ordinal Logistic Regression)

- Assumes the outcome is ordered (0 = absent, 1 = mild, 2 = moderate, 3 = severe).
- Models the cumulative odds of being at or above a certain fatigue level.
- Assumes the effect of predictors is consistent across thresholds (proportional odds).
- Produces interpretable odds ratios for moving to higher fatigue levels.

Multinomial Logistic Regression

- Treats the outcome as unordered categories.
- Models the odds of each category relative to a reference level.
- Does not use the ordering information, potentially losing efficiency.
- Requires estimating more parameters, especially for multiple predictors.

Why POLR may be preferred

- Fatigue is inherently ordered, so ignoring the order (as multinomial does) is less efficient.
- POLR provides simpler, more interpretable results with fewer parameters.
- Usually recommended when outcome is ordinal with few categories.

Why experiment with both anyway

- Multinomial can capture non-proportional effects if the proportional odds assumption is violated.
- Allows comparison of model fit (AIC/BIC, LRTs) to ensure POLR is adequate.
- Can validate robustness of conclusions across model types.

Conclusion

For this problem, POLR is theoretically more appropriate because fatigue levels are ordered, but we will also fit multinomial models to compare fit and ensure robustness.

The final model choice will depend on statistical performance (AIC/BIC, likelihood ratio tests) and interpretability.

Fatigue Prediction

| Model | Game Plan |
|------------------------------|---|
| Ordinal with Weakness | Ordinal logistic regression predicting fatigue (SSC-F) from weakness (SSC-W) only. |
| Ordinal with Treatment | Ordinal logistic regression predicting fatigue from treatment group (control vs intervention) only. |
| Ordinal Additive | Ordinal logistic regression predicting fatigue from both weakness and treatment (additive model). |
| Ordinal with Interaction | Ordinal logistic regression predicting fatigue from weakness, treatment, and their interaction. |
| Multinomial with Weakness | Multinomial logistic regression predicting fatigue from weakness only (ignores ordering). |
| Multinomial with Treatment | Multinomial logistic regression predicting fatigue from treatment only (ignores ordering). |
| Multinomial Additive | Multinomial logistic regression predicting fatigue from weakness and treatment (additive). |
| Multinomial with Interaction | Multinomial logistic regression predicting fatigue from weakness, treatment, and their interaction. |

Weakness Prediction

| Model | Game Plan |
|------------------------------|--|
| Ordinal with Fatigue | Ordinal logistic regression predicting weakness (SSC-W) from fatigue (SSC-F) only. |
| Ordinal with Treatment | Ordinal logistic regression predicting weakness from treatment group (control vs intervention) only. |
| Ordinal Additive | Ordinal logistic regression predicting weakness from both fatigue and treatment (additive model). |
| Ordinal with Interaction | Ordinal logistic regression predicting weakness from fatigue, treatment, and their interaction. |
| Multinomial with Fatigue | Multinomial logistic regression predicting weakness from fatigue only (ignores ordering). |
| Multinomial with Treatment | Multinomial logistic regression predicting weakness from treatment only (ignores ordering). |
| Multinomial Additive | Multinomial logistic regression predicting weakness from both fatigue and treatment (additive). |
| Multinomial with Interaction | Multinomial logistic regression predicting weakness from fatigue, treatment, and their interaction. |

Table of Contents

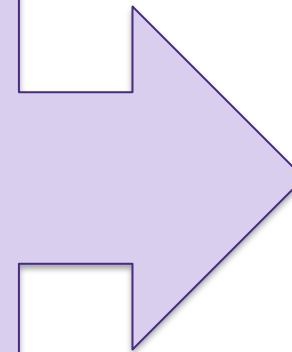
- Introduction
- Exploratory Data Analysis
- Game Plan
- Fatigue Prediction
- Weakness Prediction
- Loglinear Symptom Analysis
- Takeaways

Additive models with Weakness and Tx provide the best fit; interactions are unnecessary, and ordinal RG is preferred for interpretability.

| | Ordinal Regression (POLR) | Multinomial Regression |
|---|---|---|
| With Weakness | <ul style="list-style-type: none"> Provides a baseline for how much fatigue can be explained by weakness alone. LRT shows that adding treatment improves fit, so this model is incomplete. | <ul style="list-style-type: none"> Predicts fatigue without assuming ordering. Captures category-specific effects of weakness. LRT comparing to additive model: treatment adds modest improvement (LR stat = 12.81, p = 0.005). Interpretation: Weakness is still the dominant predictor. |
| With Treatment | <p>LRT shows weakness dramatically improves model fit (LR stat = 627.47, p < 0.0001), indicating treatment alone is a weak predictor compared to weakness.</p> | <ul style="list-style-type: none"> Predicts fatigue based on treatment alone. LRT comparing to additive model: weakness dramatically improves fit (LR stat = 785.08, p < 0.0001). Interpretation: Treatment-only model is insufficient; weakness drives fatigue levels. |
| With Interaction (Weakness × Treatment) | <ul style="list-style-type: none"> Adds an interaction term to the additive model. LRT vs additive model: LR stat = 5.96, p = 0.11 → interaction not statistically significant. Interpretation: The effect of weakness on fatigue does not vary by treatment group; additive model is sufficient. | <ul style="list-style-type: none"> Captures category-specific additive effects of weakness and treatment. Best-fitting multinomial model among main effects. Provides slightly better AIC/BIC than interaction model. Interpretation: Weakness remains the strongest predictor; treatment adds modest improvements. |
| Additive (Weakness + Treatment) | <ul style="list-style-type: none"> Models fatigue as a function of both weakness and treatment. Both predictors are included additively. LRT comparing this to Weakness-only: LR stat = 11.66, p = 0.00064 → treatment adds a small but significant improvement. Interpretation: Weakness dominates; treatment provides a modest additive effect. | <ul style="list-style-type: none"> Includes interactions for each fatigue category. LRT vs additive model: LR stat = 11.95, p = 0.216 → interaction not significant. Interpretation: The effect of weakness on each fatigue category does not meaningfully differ by treatment. Additional parameters increase model complexity without improving fit. |

Comparing Model Fit Using AIC and BIC: Additive Models with Weakness and Treatment Provide the Best Balance of Fit and Simplicity

- Among **ordinal regression models**, the additive model (**Weakness +Treatment**) has the lowest AIC/BIC, meaning it balances fit and simplicity.
- Adding an **interaction term** does not improve fit, as shown by slightly higher AIC/BIC.
- Among **multinomial models**, the additive model also performs best numerically, but multinomial ignores the natural ordering of fatigue levels.
- Models with only Weakness or only Treatment have higher AIC/BIC, reflecting **poorer explanatory power**.
- Overall, the additive models (**Weakness +Treatment**) are **preferred**, with **ordinal regression** being conceptually more appropriate.



| Model | AIC | BIC |
|------------------------------|---------|---------|
| Multinomial Additive | 2691.54 | 2769.47 |
| Multinomial with Interaction | 2697.59 | 2822.27 |
| Multinomial with Weakness | 2698.34 | 2760.69 |
| Ordinal Additive | 2833.57 | 2869.94 |
| Ordinal with Interaction | 2833.62 | 2885.57 |
| Ordinal with Weakness | 2843.23 | 2874.4 |
| Ordinal with Treatment | 3455.05 | 3475.83 |
| Multinomial with Treatment | 3458.62 | 3489.79 |

Final Takeaway



- The **ordinal additive model (Weakness + Treatment)** is selected because fatigue levels are naturally ordered (0–3).
- Weakness (SSC-W) is the strongest predictor, while treatment provides a modest additive effect.
- Interaction between weakness and treatment is not significant, so the model is **simple and interpretable**.
- Clinically, the model reflects that higher weakness consistently increases the odds of more severe fatigue, regardless of treatment group, while treatment slightly reduces fatigue severity.

Table of Contents

- Introduction
- Exploratory Data Analysis
- Game Plan
- Fatigue Prediction
- Weakness Prediction
- Loglinear Symptom Analysis
- Takeaways

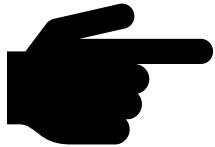
Additive models with Weakness and Tx provide the best fit; interactions are unnecessary, and ordinal RG is preferred for interpretability.

| | Ordinal Regression (POLR) | Multinomial Regression |
|--|--|--|
| With Fatigue | <ul style="list-style-type: none"> Baseline model with fatigue as the sole predictor. Captures the majority of predictive signal for weakness. Provides interpretable odds for moving to higher weakness levels. | <ul style="list-style-type: none"> Models fatigue as categorical predictor only (ignores ordering). Provides category-specific effects of fatigue on weakness. |
| With Treatment | <ul style="list-style-type: none"> Model with treatment only. LR test vs additive model: LR stat = 619.91, p < 0.0001 Interpretation: Fatigue is critical; treatment alone explains very little variation in weakness. | <ul style="list-style-type: none"> Treatment-only model. LR test vs additive: LR stat = 785.08, p < 0.0001 Interpretation: Fatigue overwhelmingly drives weakness; treatment alone insufficient. |
| With Interaction (Weakness × Treatment) | <ul style="list-style-type: none"> Combines fatigue and treatment additively. LR test vs fatigue-only: LR stat = 0.19, p = 0.66 Interpretation: Adding treatment does not significantly improve fit; fatigue dominates prediction. | <ul style="list-style-type: none"> Combines fatigue and treatment additively. LR test vs fatigue-only: LR stat = 10.22, p = 0.0168 Interpretation: Treatment adds a small but statistically significant improvement; fatigue remains the dominant predictor. |
| Additive (Weakness + Treatment) | <ul style="list-style-type: none"> Adds interaction to additive model. LR test: LR stat = 5.21, p = 0.16 Interpretation: Interaction is not significant; additive model is sufficient. Clinically: Effect of fatigue on weakness does not differ by treatment group. | <ul style="list-style-type: none"> Adds interaction to additive model. LR test: LR stat = 11.95, p = 0.216 Interpretation: Interaction is not significant; additive model is adequate. Clinically: Effect of fatigue on weakness is consistent across treatment groups. |

Comparing Model Fit Using AIC and BIC: Additive Models with Weakness and Treatment Provide the Best Balance of Fit and Simplicity

| Model | AIC | BIC | Key Interpretation |
|------------------------------|---------|---------|---|
| Multinomial Additive | 2785.39 | 2863.32 | Best-fitting model numerically; additive model captures main effects. |
| Multinomial with Fatigue | 2789.61 | 2851.95 | Slightly worse; treatment adds small improvement. |
| Multinomial with Interaction | 2791.43 | 2916.12 | Interaction unnecessary; adds complexity. |
| Ordinal with Fatigue | 2940.39 | 2971.57 | Captures ordering; baseline ordinal model. |
| Ordinal Additive | 2942.2 | 2978.57 | Slightly worse AIC/BIC than multinomial; additive model sufficient. |
| Ordinal with Interaction | 2942.99 | 2994.95 | Interaction unnecessary; increases complexity. |
| Multinomial with Treatment | 3552.47 | 3583.64 | Poor fit; ignores fatigue. |
| Ordinal with Treatment | 3556.11 | 3576.89 | Poor fit; ignores fatigue. |

Final Takeaway



Best Model: Ordinal Regression (Fatigue-only) for Weakness

Respects Outcome Ordering

- Weakness (SSC-W) levels are **naturally ordered** from 0 (absent) → 3 (severe).
- Ordinal regression models the **cumulative odds** of being at or above a given weakness level.

Fatigue is the Dominant Predictor

- Likelihood ratio tests show **adding treatment does not significantly improve fit** (LR stat = 0.19, p = 0.66).
- This indicates that **fatigue alone captures most of the predictive signal** for weakness.

Clinical Interpretation

- Higher fatigue levels are associated with **higher likelihood of experiencing weakness**.
- Treatment does **not significantly alter this relationship**, suggesting weakness progression is largely driven by fatigue severity rather than intervention in this dataset.

Parsimony and Interpretability

- Fewer parameters than multinomial models.
- Produces **straightforward odds ratios**, making clinical interpretation simpler and robust.

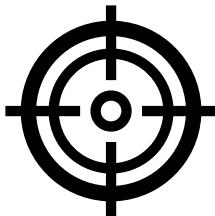
Key Takeaway:

- The **Ordinal Fatigue-only model** is **statistically appropriate, clinically intuitive, and parsimonious**.
- It clearly shows that **fatigue is the main driver of weakness**, and treatment has minimal direct effect in this context.

Table of Contents

- Introduction
- Exploratory Data Analysis
- Game Plan
- Fatigue Prediction
- Weakness Prediction
- Loglinear Symptom Analysis
- Takeaways

Exploring 8 Modeling Approaches (Additive and Interaction) to Determine the Best-Fitting Model for Weakness and Fatigue



| Variables |
|--|
| <ul style="list-style-type: none"> Weakness (SSC-W) – 4 levels Fatigue (SSC-F) – 4 levels Treatment (IC) – 2 levels |

| Method |
|--|
| <ul style="list-style-type: none"> Use loglinear models to model cell counts in the 3-way contingency table. Poisson regression on counts is mathematically equivalent to fitting a loglinear model. Goal: Identify which main effects and interactions significantly explain the observed counts. |

| Variables |
|--|
| <ul style="list-style-type: none"> Likelihood ratio test (G^2): Tests whether adding interactions significantly improves fit. AIC / BIC: Helps select the most parsimonious model balancing fit and complexity. |

| |
|--|
| <p>PLAN</p> <p>Independence model (no interactions)</p> <ul style="list-style-type: none"> Assumes all three variables are independent: Weakness $\perp\!\!\!\perp$ Fatigue $\perp\!\!\!\perp$ Treatment. Serves as a baseline model. <p>Additive model (main effects only)</p> <ul style="list-style-type: none"> Models the expected counts based on main effects: Weakness + Fatigue + Treatment. Tests whether main effects alone capture the structure of the data. <p>Two-way interaction model</p> <ul style="list-style-type: none"> Includes all pairwise interactions: Weakness \times Fatigue, Weakness \times Treatment, Fatigue \times Treatment. Evaluates whether associations exist between any two variables. <p>Saturated model (full three-way interaction)</p> <ul style="list-style-type: none"> Includes all main effects, two-way, and three-way interactions. Perfectly fits the observed counts; used as a reference for goodness-of-fit. |
|--|

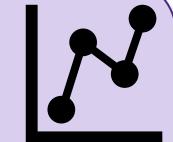
Loglinear Model Comparison: Residual Deviance, Degrees of Freedom, and Likelihood Ratio Test for Significance

| Model | Res. df | Res. Dev | ΔDf | ΔDev | p (Chi) |
|---|---------|----------|-------------------|--------------------|-------------|
| Independence (Weakness + Fatigue + Treatment) | 88 | 993.02 | – | – | – |
| Two-way interactions (all pairs) | 73 | 167.63 | 15 | 825.39 | < 2e-16 *** |
| Saturated (three-way) | 64 | 155.67 | 9 | 11.95 | 0.216 |

Statistical Interpretation

Independence model (Weakness + Fatigue + Treatment)

- Assumes no associations between any of the variables.
- Residual deviance is very high (993.02), indicating a poor fit.
- Clearly, the variables are not independent, so main effects alone are insufficient.



Two-way additive model (all pairwise interactions)

- Includes all main effects and pairwise interactions: Weakness × Fatigue, Weakness × Treatment, Fatigue × Treatment.
- Residual deviance drops dramatically to 167.63, G^2 test $p < 2e-16$, showing that adding interactions significantly improves fit.

AIC = 586.42, BIC = 645.40, lowest among all models → best balance of fit and parsimony.

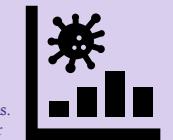
Saturated model (three-way interaction)

- Includes all main effects, pairwise, and the three-way interaction.
- Residual deviance decreases slightly to 155.67, but G^2 test $p = 0.216 \rightarrow$ adding the three-way interaction does not significantly improve fit.
- Higher BIC (674.52) penalizes complexity → not necessary for interpretation.

| Model | df | AIC | BIC |
|------------------|----|---------|---------|
| Independence | 8 | 1381.81 | 1402.32 |
| Two-way additive | 23 | 586.42 | 645.40 |
| Saturated | 32 | 592.46 | 674.52 |

Clinical Interpretation

- Fatigue and weakness are strongly associated in people living with HIV.
- Treatment group shows some association with these symptoms, but its effect does not modify the fatigue-weakness relationship (no significant three-way interaction).
- The two-way additive model captures all meaningful relationships.
- Clinicians can focus on the main effects and pairwise associations without overcomplicating with higher-order interactions.
- Clinically, this suggests that interventions targeting fatigue or weakness can be considered somewhat independently, as their relationship does not differ by treatment group.



The two-way additive loglinear model provides the simplest yet statistically robust description of the associations among weakness, fatigue, and treatment, making it both interpretable and clinically meaningful.

Table of Contents

- Introduction
- Exploratory Data Analysis
- Game Plan
- Fatigue Prediction
- Weakness Prediction
- Loglinear Symptom Analysis
- Takeaways

Multivariate Analysis of Symptom Correlation: Treatment Efficacy on the Joint Distribution of Fatigue and Weakness

Relationship Between Weakness and Fatigue

Ordinal Regression (POLR):

- Weakness is a strong and consistent predictor of fatigue.
- Likelihood ratio tests show adding treatment provides minimal additional predictive power once weakness is included.
- No significant interaction: the effect of weakness on fatigue does not differ across treatment groups, suggesting a stable, intrinsic association.
- Clinically, individuals with higher weakness scores are substantially more likely to report higher fatigue levels, regardless of intervention.

Multinomial Regression:

- Confirms POLR findings: weakness dominates fatigue prediction.
- Treatment alone has a small, sometimes statistically significant effect, but the overall pattern remains the same.
- Interaction is not significant, reinforcing that the additive model is sufficient.

Loglinear Models:

- Pairwise interactions (Weakness × Fatigue) are highly significant, reinforcing the strong statistical dependence.
- Three-way interaction (Weakness × Fatigue × Treatment) is not significant, confirming that treatment does not modify this relationship.

Effect of Intervention (Treatment)

Regression Models:

- Adding treatment to models with weakness provides a small but statistically detectable improvement in fit (more so in multinomial models).
- Ordinal models suggest that the clinical effect of treatment is modest and secondary to weakness.
- No significant interaction implies that the treatment effect does not amplify or reduce the association between weakness and fatigue.

Loglinear Models:

- Treatment shows some pairwise associations with fatigue or weakness individually, but no three-way interaction exists.
- Suggests that the intervention may have minor effects on symptom levels, but it does not substantially alter the fatigue-weakness relationship.

Clinical Insight: Treatment is not the primary driver of fatigue or weakness in this dataset. Interventions targeting symptom reduction may need to focus more directly on fatigue or weakness rather than expecting treatment group assignment alone to influence outcomes.

Consistency Across Methods

- Ordinal regression (POLR) is preferred for these data because it respects the ordered nature of fatigue and weakness, giving interpretable cumulative odds ratios.
- Multinomial regression supports the same qualitative conclusions, though it ignores ordering and requires more parameters.
- Loglinear models provide a complementary perspective, confirming the statistical dependence patterns among Weakness, Fatigue, and Treatment.

Overall Takeaways



- Weakness is strongly associated with fatigue—higher weakness levels predict higher fatigue levels.
- Treatment group has minimal impact, and it does not modify the weakness-fatigue relationship.
- Additive models (main effects + pairwise interactions) are sufficient; higher-order interactions are unnecessary.
- These conclusions are robust across multiple statistical approaches, supporting both statistical validity and clinical interpretability.

APPENDIX

BE BOUNDLESS

W

R Studio Outputs: Fatigue Prediction

Ordinal regression LRTs:
Likelihood ratio tests of ordinal regression models

Response: Fatigue

| | Model | Resid. | df | Resid. | Dev | Test | Df LR stat. | Pr(Chi) |
|---|----------------------|--------|----------|--------|-----|------------|--------------|---------|
| 1 | Weakness | 1327 | 2831.232 | | | | | |
| 2 | Weakness + Treatment | 1326 | 2819.573 | 1 vs 2 | | 1 11.65922 | 0.0006388497 | |

Likelihood ratio tests of ordinal regression models

Response: Fatigue

| | Model | Resid. | df | Resid. | Dev | Test | Df LR stat. | Pr(Chi) |
|---|----------------------|--------|----------|--------|------------|------|-------------|---------|
| 1 | Treatment | 1329 | 3447.047 | | | | | |
| 2 | Weakness + Treatment | 1326 | 2819.573 | 1 vs 2 | 3 627.4747 | 0 | | |

Likelihood ratio tests of ordinal regression models

Response: Fatigue

| | Model | Resid. | df | Resid. | Dev | Test | Df LR stat. | Pr(Chi) |
|---|----------------------|--------|----------|--------|------------|-----------|-------------|---------|
| 1 | Weakness | 1329 | 3447.047 | | | | | |
| 2 | Weakness * Treatment | 1323 | 2813.617 | 1 vs 2 | 3 5.956141 | 0.1137637 | | |

Multinomial regression LRTs:
Likelihood ratio tests of Multinomial Models

Response: Fatigue

| | Model | Resid. | df | Resid. | Dev | Test | Df LR stat. | Pr(Chi) |
|---|----------------------|--------|----------|--------|------------|-----------|-------------|---------|
| 1 | Weakness + Treatment | 1326 | 2819.573 | | | | | |
| 2 | Weakness * Treatment | 1323 | 2813.617 | 1 vs 2 | 3 5.956141 | 0.1137637 | | |

Multinomial regression LRTs:
Likelihood ratio tests of Multinomial Models

Response: Fatigue

| | Model | Resid. | df | Resid. | Dev | Test | Df LR stat. | Pr(Chi) |
|---|----------------------|--------|----------|--------|------------|-----------|-------------|---------|
| 1 | Weakness | 1326 | 2819.573 | | | | | |
| 2 | Weakness + Treatment | 1323 | 2813.617 | 1 vs 2 | 3 5.956141 | 0.1137637 | | |

Response: Fatigue

| | Model | Resid. | df | Resid. | Dev | Test | Df LR stat. | Pr(Chi) |
|---|----------------------|--------|----------|--------|------------|-----------|-------------|---------|
| 1 | Treatment | 1326 | 2819.573 | | | | | |
| 2 | Weakness + Treatment | 1323 | 2813.617 | 1 vs 2 | 3 5.956141 | 0.1137637 | | |

Multinomial regression LRTs:
Likelihood ratio tests of Multinomial Models

Response: Fatigue

| | Model | Resid. | df | Resid. | Dev | Test | Df LR stat. | Pr(Chi) |
|---|----------------------|--------|----------|--------|------------|-----------|-------------|---------|
| 1 | Weakness + Treatment | 1326 | 2819.573 | | | | | |
| 2 | Weakness * Treatment | 1323 | 2813.617 | 1 vs 2 | 3 5.956141 | 0.1137637 | | |

Likelihood ratio tests of ordinal regression models

Response: Fatigue

| | Model | Resid. | df | Resid. | Dev | Test | Df LR stat. | Pr(Chi) |
|---|----------------------|--------|----------|--------|------------|------|-------------|---------|
| 1 | Weakness | 1327 | 2831.232 | | | | | |
| 2 | Weakness + Treatment | 1326 | 2819.573 | 1 vs 2 | 3 627.4747 | 0 | | |

Likelihood ratio tests of ordinal regression models

Response: Fatigue

| | Model | Resid. | df | Resid. | Dev | Test | Df LR stat. | Pr(Chi) |
|---|----------------------|--------|----------|--------|------------|------|-------------|---------|
| 1 | Treatment | 1329 | 3447.047 | | | | | |
| 2 | Weakness + Treatment | 1326 | 2819.573 | 1 vs 2 | 3 627.4747 | 0 | | |

Response: Fatigue

| | Model | Resid. | df | Resid. | Dev | Test | Df LR stat. | Pr(Chi) |
|---|----------------------|--------|----------|--------|------------|-----------|-------------|---------|
| 1 | Weakness | 1329 | 3447.047 | | | | | |
| 2 | Weakness * Treatment | 1323 | 2813.617 | 1 vs 2 | 3 5.956141 | 0.1137637 | | |

Likelihood ratio tests of ordinal regression models

| Model <chr> | AIC <dbl> | BIC <dbl> |
|----------------|--------------|--------------|
| Mult_Both | 2691.539 | 2769.467 |
| Mult_Int | 2697.585 | 2822.269 |
| Mult_Weak | 2698.344 | 2760.687 |
| Ord_Both | 2833.573 | 2869.939 |
| Ord_Int | 2833.617 | 2885.569 |
| Ord_Weak | 2843.232 | 2874.403 |
| Ord_Tx | 3455.047 | 3475.828 |
| Mult_Tx | 3458.619 | 3489.791 |

R Studio Outputs: Weakness Prediction

Ordinal Regression LRTs:
Likelihood ratio tests of ordinal regression models

Response: Weakness

| | Model | Resid. | df | Resid. | Dev | Test | Df | LR stat. | Pr(Chi) |
|---|---------------------|--------|----|----------|--------|------|-----------|------------|---------|
| 1 | Fatigue | 1327 | | 2928.394 | | | | | |
| 2 | Fatigue + Treatment | 1326 | | 2928.203 | 1 vs 2 | 1 | 0.1901051 | 0.66628292 | |

Likelihood ratio tests of ordinal regression models

Response: Weakness

| | Model | Resid. | df | Resid. | Dev | Test | Df | LR stat. | Pr(Chi) |
|---|---------------------|--------|----|----------|--------|------|----------|----------|---------|
| 1 | Treatment | 1329 | | 3548.110 | | | | | |
| 2 | Fatigue + Treatment | 1326 | | 2928.203 | 1 vs 2 | 3 | 619.9069 | 0 | |

Likelihood ratio tests of ordinal regression models

Response: Weakness

| | Model | Resid. | df | Resid. | Dev | Test | Df | LR stat. | Pr(Chi) |
|---|---------------------|--------|----|----------|--------|------|----------|-----------|---------|
| 1 | Fatigue + Treatment | 1326 | | 2928.203 | | | | | |
| 2 | Fatigue * Treatment | 1323 | | 2922.998 | 1 vs 2 | 3 | 5.205347 | 0.1573636 | |

Multinomial Regression LRTs:
Likelihood ratio tests of Multinomial Models

Response: Weakness

| | Model | Resid. | df | Resid. | Dev | Test | Df | LR stat. | Pr(Chi) |
|---|---------------------|--------|----|----------|--------|------|----------|------------|---------|
| 1 | Fatigue | 276 | | 2765.612 | | | | | |
| 2 | Fatigue + Treatment | 273 | | 2755.388 | 1 vs 2 | 3 | 10.22365 | 0.01675767 | |

Likelihood ratio tests of Multinomial Models

Response: Weakness

| | Model | Resid. | df | Resid. | Dev | Test | Df | LR stat. | Pr(Chi) |
|---|---------------------|--------|----|----------|--------|------|----------|----------|---------|
| 1 | Treatment | 282 | | 3540.469 | | | | | |
| 2 | Fatigue + Treatment | 273 | | 2755.388 | 1 vs 2 | 9 | 785.0803 | 0 | |

Likelihood ratio tests of Multinomial Models

Response: Weakness

| | Model | Resid. | df | Resid. | Dev | Test | Df | LR stat. | Pr(Chi) |
|---|---------------------|--------|----|----------|--------|------|----------|-----------|---------|
| 1 | Fatigue + Treatment | 273 | | 2755.388 | | | | | |
| 2 | Fatigue * Treatment | 264 | | 2743.434 | 1 vs 2 | 9 | 11.95422 | 0.2159027 | |

| | Model <chr> | AIC <dbl> | BIC <dbl> |
|------------------------------|------------------------------|--------------|--------------|
| Multinomial Additive | Multinomial Additive | 2785.388 | 2863.316 |
| Multinomial with Fatigue | Multinomial with Fatigue | 2789.612 | 2851.954 |
| Multinomial with Interaction | Multinomial with Interaction | 2791.434 | 2916.119 |
| Ordinal with Fatigue | Ordinal with Fatigue | 2940.394 | 2971.565 |
| Ordinal Additive | Ordinal Additive | 2942.203 | 2978.570 |
| Ordinal with Interaction | Ordinal with Interaction | 2942.998 | 2994.950 |
| Multinomial with Treatment | Multinomial with Treatment | 3552.469 | 3583.640 |
| Ordinal with Treatment | Ordinal with Treatment | 3556.110 | 3576.891 |

R Studio Outputs: Loglinear Symptom Analysis

Analysis of Deviance Table

```
Model 1: Count ~ Weakness + Fatigue + Treatment
Model 2: Count ~ (Weakness + Fatigue + Treatment)^2
Model 3: Count ~ Weakness * Fatigue * Treatment
Resid. Df Resid. Dev Df Deviance Pr(>Chi)
1      88    993.02
2      73   167.63 15   825.39  <2e-16 ***
3      64   155.67 9    11.95   0.2159
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

| | df <dbl> | AIC <dbl> |
|-------------|-------------|--------------|
| model_indep | 8 | 1381.8052 |
| model_2way | 23 | 586.4169 |
| model_sat | 32 | 592.4627 |

| | df <dbl> | BIC <dbl> |
|-------------|-------------|--------------|
| model_indep | 8 | 1402.3200 |
| model_2way | 23 | 645.3970 |
| model_sat | 32 | 674.5219 |