

Part III: Normal Forms

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Database Design Theory

- General idea:
 - Express constraints on the data
 - Use these to decompose the relations
- Ultimately, get a schema that is in a “normal form” that guarantees good properties, such as no anomalies.
- “Normal” in the sense of conforming to a standard.
- The process of converting a schema to a normal form is called **normalization**.

Acknowledgements: M. Papagelis, R. Johnson

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Motivation for normal forms

- Identify a “good” schema
 - For some definition of “good”
 - Avoid anomalies, redundancy, etc.
- Many normal forms
 - 1st
 - 2nd
 - 3rd
 - Boyce-Codd
 - ... and several more we won’t discuss...

$$BCNF \subseteq 3NF \subseteq 2NF \subseteq 1NF$$

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1st Normal Form (1NF)

- No multi-valued attributes allowed
 - Imagine storing a list of values in an attribute
- Counter example
 - Course(name, instructor, [student,email]*)

Name	Instructor	Student Name	Student Email
CS 3DB3	Chiang	Alice	alice@gmail
		Mary	mary@mac
		Mary	mary@mac
SE 3SH3	Miller	Nilesh	nilesh@gmail

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2nd normal form (2NF)

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- Non-key attributes depend on candidate keys
 - Consider non-key attribute A
 - Then there exists an FD $X \rightarrow A$, and X is a candidate key
- Counter-example
 - Movies(title, year, star, studio, studioAddress, salary)
 - FD: title, year \rightarrow studio; studio \rightarrow studioAddress; star \rightarrow salary

Title	Year	Star	Studio	StudioAddr	Salary
Star Wars	1977	Hamill	Lucasfilm	1 Lucas Way	\$100,000
Star Wars	1977	Ford	Lucasfilm	1 Lucas Way	\$100,000
Star Wars	1977	Fisher	Lucasfilm	1 Lucas Way	\$100,000
Patriot Games	1992	Ford	Paramount	Cloud 9	\$2,000,000
Last Crusade	1989	Ford	Lucasfilm	1 Lucas Way	\$1,000,000

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3rd normal form (3NF)

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- Non-prime attr. depend *only* on candidate keys
 - Consider FD $X \rightarrow A$
 - Either X is a superkey OR A is *prime* (part of a key)
- Counter-example:
 - studio \rightarrow studioAddr
 - (studioAddr depends on studio which is not a candidate key)

Title	Year	Studio	StudioAddr
Star Wars	1977	Lucasfilm	1 Lucas Way
Patriot Games	1992	Paramount	Cloud 9
Last Crusade	1989	Lucasfilm	1 Lucas Way

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3NF, dependencies, and join loss

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- Theorem: always possible to convert a schema to lossless join, dependency-preserving 3NF
- Caveat: always *possible* to create schemas in 3NF for which these properties do not hold
- FD loss example 1:
 - MovieInfo(title, year, studioName)
 - StudioAddress(title, year, studioAddress)
 - => Cannot enforce studioName \rightarrow studioAddress
- Join loss example 2:
 - Movies(title, year, star)
 - StarSalary(star, salary)
 - => Movies \bowtie StarSalary yields additional tuples

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Boyce-Codd normal form (BCNF)

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- One additional restriction over 3NF
 - All non-trivial FDs have superkey LHS
- Counterexample
 - CanadianAddress(street, city, province, postalCode)
 - Candidate keys: {street, postalCode}, {street, city, province}
 - FD: postalCode \rightarrow city, province
 - Satisfies 3NF: city, province both prime
 - Violates BCNF: postalCode is not a superkey
 - => Possible anomalies involving postalCode

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Boyce-Codd Normal Form

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- We say a relation R is in **BCNF** if whenever $X \rightarrow A$ is a nontrivial FD that holds in R , X is a superkey.
 - Remember: *non-trivial* means A is not contained in X .

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Example: a relation not in BCNF

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Drinkers(name, addr, beersLiked, manf, favBeer)

FD's: $\text{name} \rightarrow \text{addr}$, favBeer , $\text{beersLiked} \rightarrow \text{manf}$

- Only key is {name, beersLiked}.
- In each FD, the left side is **not** a superkey.
- Any one of these FDs shows *Drinkers* is not in BCNF

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Another Example

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Beers(name, manf, manfAddr)

FD's: $\text{name} \rightarrow \text{manf}$, $\text{manf} \rightarrow \text{manfAddr}$

- **Beers** w.r.t. $\text{name} \rightarrow \text{manf}$ does not violate BCNF, but $\text{manf} \rightarrow \text{manfAddr}$ does.

In other words, BCNF requires that:
the only FDs that hold are the result of key(s).
Why does that help?

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Decomposition into BCNF

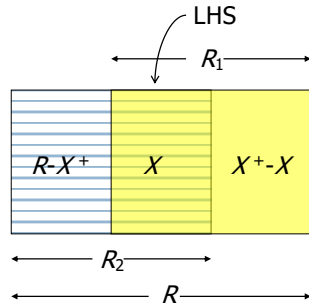
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- Given: relation R with FDs F
- Look among the given FDs for a BCNF violation $X \rightarrow Y$ (i.e., X is not a superkey)
- Compute X^+ .
 - Find $X^+ \neq X \neq$ all attributes, (o.w. X is a superkey)
- Replace R by relations with:
 - $R_1 = X^+$.
 - $R_2 = R - (X^+ - X) = R - X^+ \cup X$
- Continue to recursively decompose the two new relations
- **Project** given FDs F onto the two new relations.

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Decomposition on $X \rightarrow Y$

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Example: BCNF Decomposition

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- Drinkers**(name, addr, beersLiked, manf, favBeer)
- $F = \{\text{name} \rightarrow \text{addr}, \text{name} \rightarrow \text{favBeer}, \text{beersLiked} \rightarrow \text{manf}\}$
- Key = name, beersLiked
- Pick BCNF violation name \rightarrow addr.
 - Closure: $\{\text{name}\}^+ = \{\text{name}, \text{addr}, \text{favBeer}\}$.
 - Decomposed relations:
 - **Drinkers1**(name, addr, favBeer)
 - **Drinkers2**(name, beersLiked, manf)

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Example -- Continued

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- We are not done; we need to check **Drinkers1** and **Drinkers2** for BCNF.
- Projecting FDs is easy here.
- For **Drinkers1**(name, addr, favBeer), relevant FDs are name \rightarrow addr and name \rightarrow favBeer.
 - ▣ Thus, {name} is the only key and **Drinkers1** is in BCNF.

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Example -- Continued

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- For **Drinkers2**(name, beersLiked, manf), the only FD is beersLiked \rightarrow manf, and the only key is {name, beersLiked}.
 - ▣ Violation of BCNF.
- $\text{beersLiked}^+ = \{\text{beersLiked}, \text{manf}\}$, so we decompose **Drinkers2** into:
 - **Drinkers3**(beersLiked, manf)
 - **Drinkers4**(name, beersLiked)

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Example -- Concluded

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- The resulting decomposition of *Drinkers* :
 - *Drinkers1*(name, addr, favBeer)
 - *Drinkers3*(beersLiked, manf)
 - *Drinkers4*(name, beersLiked)
- Notice: *Drinkers1* tells us about drinkers, *Drinkers3* tells us about beers, and *Drinkers4* tells us the relationship between drinkers and the beers they like.

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What we want from a decomposition

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- **Lossless Join** : it should be possible to project the original relations onto the decomposed schema, and then reconstruct the original, i.e., get back exactly the original tuples.
- **No anomalies**
- **Dependency Preservation** : All the original FDs should be satisfied.

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What we get from a BCNF decomposition

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- **Lossless Join** : ✓
- **No anomalies** : ✓
- **Dependency Preservation** : ✗

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Example: Failure to preserve dependencies

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- Suppose we start with $R(A, B, C)$ and FDs
 - $AB \rightarrow C$ and $C \rightarrow B$.
- There are two keys, $\{A, B\}$ and $\{A, C\}$.
- $C \rightarrow B$ is a BCNF violation, so we must decompose into AC, BC .

The problem is that if we use AC and BC as our database schema, we cannot enforce the FD $AB \rightarrow C$ in these decomposed relations.

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3NF: Helps Us Avoid this Problem

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- **3rd Normal Form** (3NF) modifies the BCNF condition so we do not have to decompose in this problem situation.
- An attribute is **prime** if it is a member of any key.
- $X \rightarrow A$ violates 3NF if and only if X is not a superkey, and also A is not prime.
- i.e., it's ok if X is not a superkey, as long as A is prime.

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Example: 3NF

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- In our problem situation with FDs $AB \rightarrow C$ and $C \rightarrow B$, we have keys AB and AC .
- Thus A , B , and C are each prime.
- Although $C \rightarrow B$ violates BCNF, it does not violate 3NF.

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What we get from a 3NF decomposition

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- **Lossless Join** : ✓
- **No anomalies** : ✗
- **Dependency Preservation** : ✓

Why?

Unfortunately, neither BCNF nor 3NF can guarantee all three properties we want.

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3NF Synthesis Algorithm

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- We can always construct a decomposition into 3NF relations with a lossless join and dependency preservation.
- Need **minimal basis** for the FDs (same as used in projection)
 - Right sides are single attributes.
 - No FD can be removed.
 - No attribute can be removed from a left side.

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3NF Synthesis – (2)

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- One relation for each FD in the minimal basis.
 - ▣ Schema is the union of the left and right sides.
- If no key is contained in an FD, then add one relation whose schema is some key.

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Example: 3NF Synthesis

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- Relation $R = ABCD$.
- FDs $A \rightarrow B$ and $A \rightarrow C$.
- **Decomposition:** AB and AC from the FDs, plus AD for a key.

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Limits of decomposition

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- Pick two...
 - Lossless join
 - Dependency preservation
 - Anomaly-free
- 3NF
 - Provides lossless join and dependency preserving
 - May allow some anomalies
- BCNF
 - Anomaly-free, lossless join
 - Sacrifice dependency preservation

Use domain knowledge to choose 3NF vs. BCNF

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