ADTs

Stacks

Queues

Sets

COMP2521 24T3 Abstract Data Types

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abstraction abstract data types stacks and queues sets

ADTs

Stacks

Queues Sets

Abstraction

is the process of
hiding or generalising
the details of an object or system
to focus on its high-level meaning or behaviour

ADTs

Stacks

Queues

Sets

Assembly languages abstract away machine code

```
00000000000000000 <fn>:
  0: 55
                              push rbp
  1: 48 89 e5
                              mov rbp, rsp
  4: 89 7d ec
                              mov DWORD PTR [rbp-0x14], edi
  7: c7 45 fc 01 00 00 00
                              mov DWORD PTR [rbp-0x04], 0x1
  e: c7 45 f8 01 00 00 00
                              mov DWORD PTR [rbp-0x08], 0x1
 15: eb 0e
                              imp 25 < fn + 0x25 >
 17: 8b 45 fc
                                   eax, DWORD PTR [rbp-0x04]
                              mov
 1a: Of af 45 f8
                              imul eax, DWORD PTR [rbp-0x08]
 1e: 89 45 fc
                              mov DWORD PTR [rbp-0x04], eax
 21: 83 45 f8 01
                              add
                                   DWORD PTR [rbp-0x08], 0x1
 25: 8b 45 f8
                                   eax, DWORD PTR [rbp-0x08]
                              mov
 28: 3b 45 ec
                              cmp eax, DWORD PTR [rbp-0x14]
 2h: 7e ea
                              ile 17 <fn+0x17>
 2d: 8b 45 fc
                                   eax, DWORD PTR [rbp-0x04]
                              mov
 30: 5d
                                   rbp
                              pop
 31: c3
                              ret
```

Examples

Abstraction

ADTs

Stacks

Queues

Sets

Modern programming languages abstract away assembly code

```
push rbp
     rbp, rsp
mov
mov
    DWORD PTR [rbp-0x14], edi
mov DWORD PTR [rbp-0x04], 0x1
     DWORD PTR [rbp-0x08], 0x1
mov
                                 int fn(int n) {
    25 <fn+0x25>
jmp
                                     int res = 1;
     eax, DWORD PTR [rbp-0x04]
mov
                                     for (int i = 1; i <= n; i++) {
imul eax, DWORD PTR [rbp-0x08]
                                         res *= i:
     DWORD PTR [rbp-0x04], eax
mov
     DWORD PTR [rbp-0x08], 0x1
add
                                     return res:
     eax, DWORD PTR [rbp-0x08]
mov
    eax, DWORD PTR [rbp-0x14]
cmp
    17 <fn+0x17>
ile
     eax, DWORD PTR [rbp-0x04]
mov
     rbp
pop
ret
```

Examples

Abstraction ADTs

Stacks

Queues

Sets

A function abstracts away the details or steps of a computation

Abstraction Examples

Abstraction

ADTs

Stacks

Queues

Sets

We drive a car by using a steering wheel and pedals

We operate a television through a remote control

We deposit and withdraw money to/from our bank account via an ATM

ADTs Stacks

Queues

Sets

To use a system, it should be enough to understand what its components do without knowing how...

ADTs

Example Interface

Implementation
ADTs in C
Example - ban account

Stack

Queue

Sets

A data type is...

- a collection or grouping of values
 - could be atomic, e.g., int, double
 - could be composite/structured, e.g., arrays, structs
- a collection of operations on those values

Examples:

- int
 - operations: addition, multiplication, comparison
- array of ints
 - operations: index lookup, index assignment

ADTs

Example

Implementati

Example - ba

Other example

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Sets

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An abstract data type...

is a description of a data type from the point of view of a user, in terms of the operations on the data type and the behaviour of these operations.

Importantly, an ADT does not specify how the data type or operations should be implemented.

Example

Interface Implementati

Example - ba

Other example

Stacks

Queues

Sets

Example of an ADT: Stack

A stack is a linear collection of items with two main operations:

push

adds an item to the top of the stack

pop

Example

Abstraction

Abstraction

ADTs Example

Interface

ADTs in C

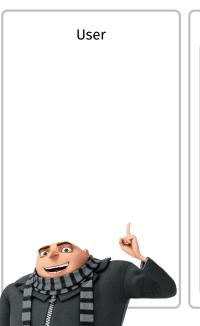
Example - bank account

Other exampl

Stacks

Queues

Sets



Stack

Operations

push

adds an item to the top of the stack $% \left(1\right) =\left(1\right) \left(1\right) \left($

pop

Example

Abstraction

ADTs Example

Interface

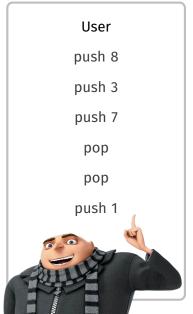
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ADTs in C Example - bank account

Stacks

Queues

Sets



Stack

Operations

push

adds an item to the top of the stack $% \left(1\right) =\left(1\right) \left(1\right) \left($

pop

Example

Abstraction

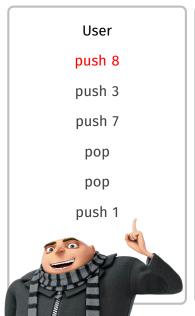
ADTs Example

ADTs in C Example - bank

Stacks

Queues

Sets



Stack

Operations

push

adds an item to the top of the stack

pop





Example

Abstraction

ADTs

Example

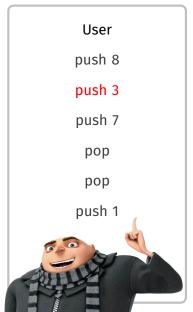
ADTs in C

Example - bank

Stacks

Queues

Sets



Stack

Operations

push

adds an item to the top of the stack

pop



Example

Abstraction

ADTS Example

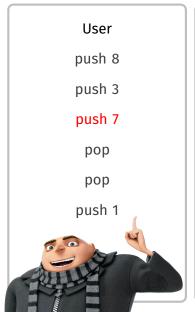
Example

Implementation ADTs in C Example - bank

Stacks

Queues

Sets



Stack

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Operations

push

adds an item to the top of the stack

pop

Example

Abstraction

ADTs Example

Interface

Implementa

ADTs in C Example - bank

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Stacks

Queues

Sets



Stack



Operations

push

adds an item to the top of the stack

pop

Example

Abstraction

ADTs Example

Interface

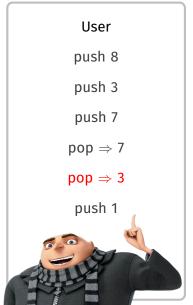
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Stacks

Queues

Sets



Stack



push

adds an item to the top of the stack

pop





Example

Abstraction

ADTs Example

Example

Implementati

Example - bank account

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Stacks

Queues

Sets

User push 8 push 3 push 7 $pop \Rightarrow 7$ $pop \Rightarrow 3$ push 1

Stack



Operations

push

adds an item to the top of the stack

pop



Interface

Abstraction

ADTs

Interface

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ADTS IN C

Other example

Stacks

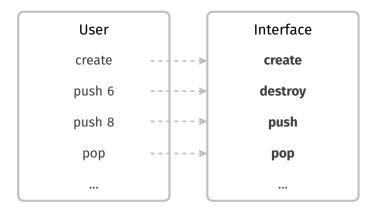
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Queues

Sets

The set of operations provided by an ADT is called the interface.

Users of an ADT only see and interact with the interface.



Interface

Abstraction

Example

Interface

ADTs in C

account

Other exampl

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Queues

Sate

An ADT interface must:

- clearly describe the behaviour of each operation
- 2. describe the conditions under which each operation can be used

Example:

pop

removes the item at the top of the stack

assumes that the stack is not empty

Implementation

Abstraction

ADTs

Example

Implementation

ADTs in C Example - bank account

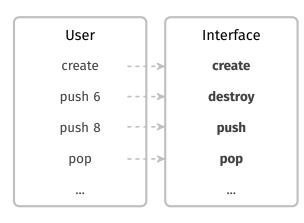
Other exan

Stacks

Queues

Sets

Builders of an ADT provide an implementation of its operations.



Implementation create(...) { ... } destroy(...) { ... } push(...) { ... } pop(...) { ... }

Implementation

Abstraction

ADTs Example

Implementation

ADTs in C Example - bank

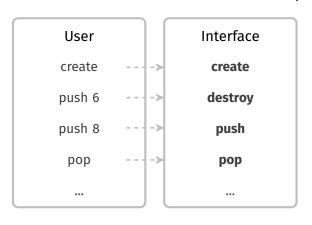
Other exam

Stacks

Queues

Sets

Users of an ADT do not see the implementation.



```
Implementation
    create(...) {
        ...
        destroy(...) {
            ...
        push(...) {
            ...
        }
        pop(...) {
            ...
        }
```

Abstraction

ADTs

Example

Implementati

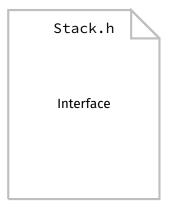
Example - ba

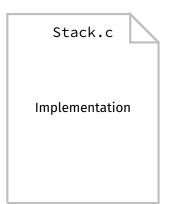
Other examp

Stacks

Queues Sets In C, abstract data types are implemented using two files:

a .h file that contains the interface a .c file that contains the implementation





Interface — , h file

Abstraction

ADTS

Sets

The interface includes:

- forward declaration of the struct for the concrete representation
 - via typedef struct t *T
 - the struct is not defined in the interface
- function prototypes for all operations
- clear description of operations
 - via comments
- a contract between the ADT and clients
 - documentation describes how an operation can be used
 - and what the expected result is as long as the operation is used correctly

Interface — . h file

Abstraction

Interface

Interrace

ADTs in C

ADTs

Example - bank account

Other exampl

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Queues

Sets

Stack.h

```
typedef struct stack *Stack;
/** Creates a new empty stack */
Stack StackNew(void);
/** Frees memory allocated to the stack */
void StackFree(Stack s);
/** Adds an item to the top of the stack */
void StackPush(Stack s, int item);
/** Removes the item at the top of the stack
   Assumes that the stack is not empty */
int StackPop(Stack s);
```

Implementation - .c file

Abstraction

Example

ADTs

Interface Implementation

Example - ba

Other example

Other example

Stacks Oueues

Queue

Sets

The implementation includes:

- concrete definition of the data structures
 - definition of struct t
- function implementations for all operations

Implementation — . c file

Abstraction

ADTs in C

ADTs

Example - bank

Stacks

Queues

Sets

Stack.c

```
struct stack {
};
Stack StackNew(void) {
    . . .
void StackFree(Stack s) {
    . . .
void StackPush(Stack s, int item) {
    . . .
int StackPop(Stack s) {
    . . .
```

Interface

ADTs

Implementa

Example - bank account

Other example

Stacks Oueues

Queues

A user of an ADT #includes the interface and uses the interface functions to interact with the ADT.

```
user.c
#include "Stack.h"

int main(void) {
    Stack s = StackNew();
    StackPush(s, 6);
    StackPush(s, 8);
    int item = StackPop(s);
    ...
}
```

Abstraction

ADTs

ADTs in C Example - bank

Stacks Queues

Sets

Users of an ADT only see and interact with the interface they do not see the implementation!

```
user.c
#include "Stack.h"
int main(void) {
    Stack s = StackNew();
    StackPush(s, 6);
    StackPush(s, 8);
    int item = StackPop(s);
```

```
Stack.h
typedef struct stack *Stack;
. . .
```

```
Stack.c
```

Abstraction

ADTs Example Interface

ADTs in C

Example - bank account

Other example

Stacks

Queues

Sets

Users of an ADT only see and interact with the interface — they do not see the implementation!

```
user.c
#include "Stack.h"
int main(void) {
    Stack s = StackNew();
    // this is not valid!
    s->...
```

```
Stack.h
typedef struct stack *Stack;
. . .
```

```
Stack.c
```

This means users cannot access the concrete representation (struct) directly.

COMP2521 Conventions

Abstraction

ADTs Example

ADTs in C

Example - bank account

Other examp

Stacks

Queue

Sets

Naming conventions:

- ADTs are defined in files whose names start with an uppercase letter
 - For example, for a Stack ADT:
 - The interface is defined in Stack.h
 - The implementation is defined in Stack.c
- ADT interface function names are in PascalCase and begin with the name of the ADT

Creating/Using Abstract Data Types

Abstraction

ADTS

Sets

- 1 Decide what operations you want to provide
 - Operations to create, query, manipulate
 - What are their inputs and outputs?
 - What are the conditions under which they can be used (if any)?
- Provide the function signatures and documentation for these operations in a . h file
- 3 The "developer" builds a concrete implementation for the ADT in a .c file
- 4 The "user" #includes the interface in their program and uses the provided functions

ADTs

Example - bank

account

Stacks

Queues

Sets

What operations can you perform on a simple bank account?

- Open an account
- Check balance
- Deposit money
- Withdraw money

Example - Bank Account

Interface (Account.h)

Abstraction

ADTs Example Interface

ADTs in C

Example - bank account

Other example:

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Sets

```
/** Opens a new account with zero balance */
Account AccountOpen(void);
/** Closes an account */
void AccountClose(Account acc);
/** Returns account balance */
int AccountBalance(Account acc);
/** Withdraws money from account
   Returns true if enough balance, false otherwise
   Assumes amount is positive */
bool AccountWithdraw(Account acc, int amount);
/** Deposits money into account
   Assumes amount is positive */
void AccountDeposit(Account acc, int amount);
```

typedef struct account *Account;

```
Abstraction
```

ADTs

Example - bank

int main(void) {

account

Queues

Sets

```
Account acc = AccountOpen();
printf("Balance: %d\n", AccountBalance(acc));
AccountDeposit(acc, 50);
printf("Balance: %d\n", AccountBalance(acc));
AccountWithdraw(acc, 20);
printf("Balance: %d\n", AccountBalance(acc));
AccountWithdraw(acc, 40);
printf("Balance: %d\n", AccountBalance(acc));
AccountClose(acc);
```

Example

Interface

ADTs in C Example - bank

account

Other example:

Stacks Oueues

Sets

Invalid usage of an ADT (breaking abstraction):

```
int main(void) {
    Account acc = AccountOpen();

    acc->balance = 1000000;

    // I'm a millionaire now, woohoo!
    printf("Balance: %d\n", AccountBalance(acc));

    AccountClose(acc);
}
```

Examples of ADTs

Abstraction

ADTs

ADTs in C

Example - bank

Other examples

Stacks Queues

Sets

- Stack
- Queue
- Set
- Multiset
- Map
- Graph
- Priority Queue

ADSTIACTION

ADTs Stacks

Example Usage Interface

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Queues Sets

A stack is a collection of items, such that the last item to enter is the first item to leave:

Last In, First Out (LIFO)

(Think stacks of books, plates, etc.)

ADTs Stacks

Queues Sets

A stack is a collection of items, such that the last item to enter is the first item to leave:

Last In, First Out (LIFO)

(Think stacks of books, plates, etc.)

- web browser history
- text editor undo/redo
- balanced bracket checking
- HTML tag matching
- RPN calculators (...and programming languages!)
- function calls

ADTs

Stacks

Interface

Queues

Queues

A stack supports the following operations:

push

add a new item to the top of the stack

pop

remove the topmost item from the stack

size

return the number of items on the stack

peek

get the topmost item on the stack without removing it

ADTs

Stacks Example Usage

Queues Sets

A Stack ADT can be used to check for balanced brackets.

Example of balanced brackets:

([{}])

Examples of unbalanced brackets!

```
([{}])]
```

ADTs

Stacks
Example Usage

Interface

Oueues

Sets

char	stack	check
		_
((_

ADTs

Stacks
Example Usage

Interface

Sets

Queues

Sample input: ($[\ \{\ \}\]$)

char	stack	check
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ADTs

Stacks
Example Usage

Interface Implementati

Queues

Sets

Sample input: ($[\{ \}])$

char	stack	check
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ADTs

Stacks Example Usage

Interface

Sets

Queues

char	stack	check
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}	([{ = }

ADTs

Stacks

Example Usage Interface

Queues Sets Sample input: ($[\ \{\ \}\]$)

char	stack	check
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}	([{ = }
]	([=]

Abstraction ADTs

Stacks Example Usage

Interface

Queues Sets

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ADTs

Stacks

Example Usage Interface

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Queues

Sets

char	stack	check
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	([_
{	([{	_
}	([{ = }
]	([=]
)		(=)
EOF		is empty

ADTs

Stacks
Example Usage

Interface

Implementation

Sets

Queues

Sample input: ($[\ \{\ \}\)\]$

char	stack	check
((-

ADTs

Stacks
Example Usage

Interface

Implementation

Queues

Sets

Sample input: ($[\ \{\ \}\)\]$

char	stack	check
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ADTs

Stacks Example Usage

Interface

Queues

Sets

char	stack	check
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Example Usage

Interface

Implementation

Queues

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ADTs

Abstraction

Stacks
Example Usage

Interface

Implementation

Queues

Sets

char	stack	check
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{	}])	_
}	([{ = }
)	([≠)

ADTs

Stacks Example Usage

Interface

Queues

Sets

char	stack	check
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{	[[_
}	([{ = }
)	([\neq)
		fail!

```
Abstraction
ADTs
```

Stacks Example Usage Interface

Implementa
Queues

Sets

```
/** Creates a new, empty Stack */
Stack StackNew(void);
/** Frees memory allocated for a Stack */
void StackFree(Stack s);
/** Adds an item to the top of a Stack */
void StackPush(Stack s, Item it);
/** Removes an item from the top of a Stack
   Assumes that the Stack is not empty */
Item StackPop(Stack s);
/** Gets the number of items in a Stack */
int StackSize(Stack s);
/** Gets the item at the top of a Stack
   Assumes that the Stack is not empty */
Item StackPeek(Stack s);
```

typedef struct stack *Stack;

ADTs

Stacks

Example Usage Interface

Implementation

Array

Linked list

Sets

How to implement a stack?

array

linked list

ADSTRACTION

ADTs Stacks

Example Usage

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Sets

Dynamically allocate an array with an initial capacity

Fill the array sequentially -s[0], s[1], ...

Maintain a counter of the number of items on the stack

Array implementation

Abstraction

ADTs Stacks

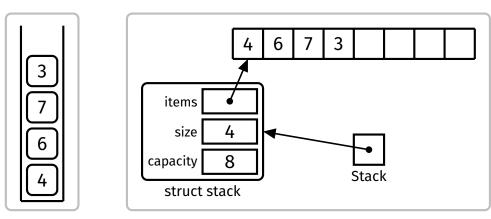
Example Usage Interface

Implementation Array

Linked list

Queues

Sets



User's view

ADTs

Stacks
Example Usage

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Array

Linked lis

Queues

Sets

Example

Perform the following operations:

 $\operatorname{push}(9)\text{, }\operatorname{push}(2)\text{, }\operatorname{push}(6)\text{, }\operatorname{pop, }\operatorname{pop, }\operatorname{push}(8)$

Array implementation

Abstraction

ADTs

Stacks
Example Usage

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Array

Queues

Sets

PUSH(9)PUSH(2)PUSH(6)PUSH(8)POP POP items size capacity 8 Stack struct stack

User's view

Array implementation

Abstraction

Stacks
Example Usage

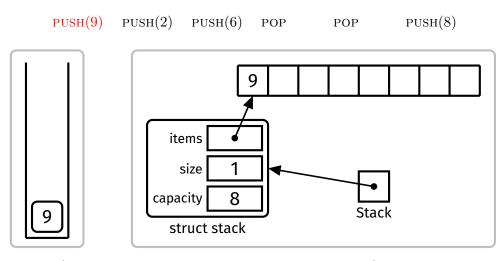
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Interface

Array

Queues

Sets



User's view

Array implementation

Abstraction

Stacks
Example Usage

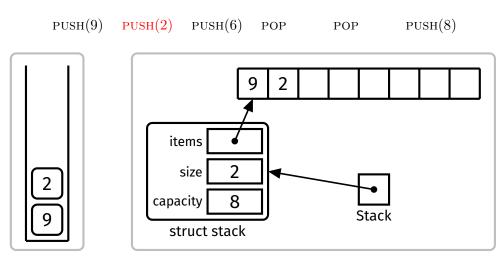
ADTs

Interface Implementation

Array Linked list

Queues

Sets



User's view

Array implementation

Abstraction

Stacks

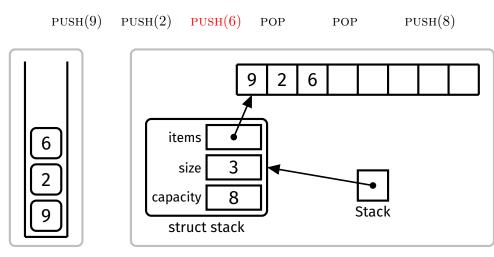
ADTs

Example Usage

Array

Queues





User's view

Concrete representation

Array implementation

Abstraction

ADTs Stacks

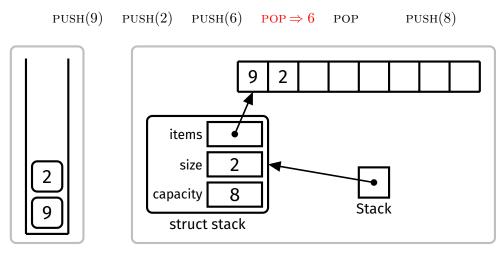
Example Usage

Implementation Array

Linked list

Queues

Sets



User's view

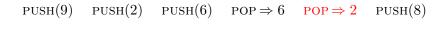
ADTs Stacks

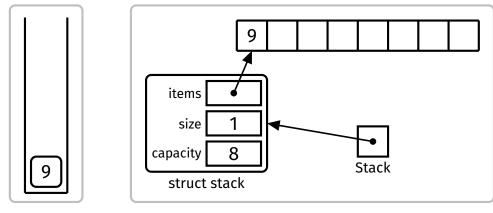
Example Usage

Array

Queues

Sets





User's view

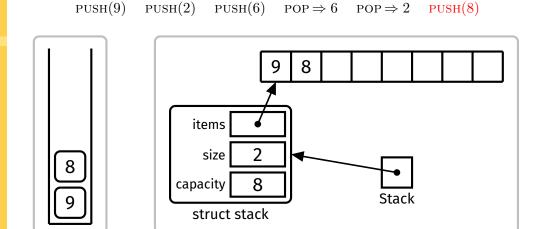
ADTs Stacks

Example Usage

Array

Queues

Sets



User's view

ADTs

Sets

Cost of push:

- Inserting item at index size is O(1)
- What if array is full?
 - If we double the size of the array with realloc(3) each time it is full, push will still be O(1) on average

Cost of pop:

• Accessing item at index (size -1) is O(1)

ADTs Stacks

> Example Usage Interface

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Linked list

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Sets

Store items in a linked list

To push an item, insert it at the beginning of the list

To pop an item, remove it from the beginning of the list

ADTs

Stacks
Example Usage

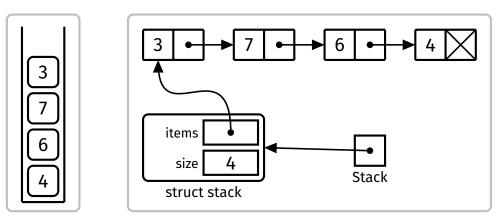
Interface

Array

Linked list

Queues

Sets



User's view

Concrete representation

ADTs Stacks

Example Usage

Implement

Array Linked list

Queues

Sets

Example

Perform the following operations:

 $\operatorname{PUSH}(9)$, $\operatorname{PUSH}(2)$, $\operatorname{PUSH}(6)$, POP , POP , $\operatorname{PUSH}(8)$

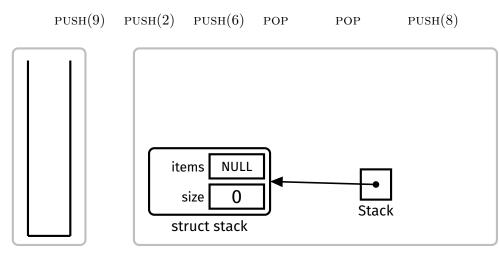
ADTs Stacks

Example Usage

Array Linked list

Queues

Sets



User's view

ADTs

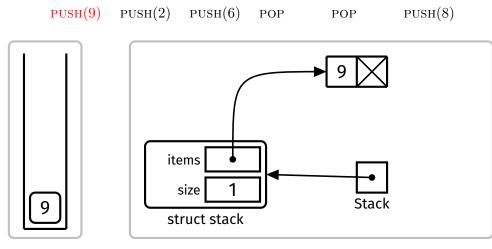
Stacks
Example Usage

Interface Implementation

Array Linked list

Queues

Sets



User's view

ADTs

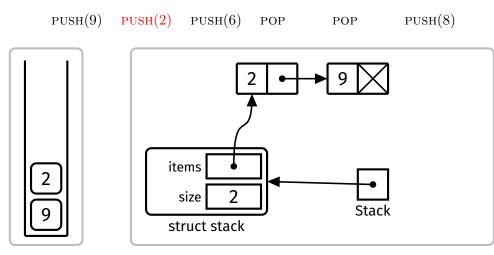
Stacks
Example Usage

Interface Implementatio Array

Linked list

Queues

Sets



User's view

ADTs

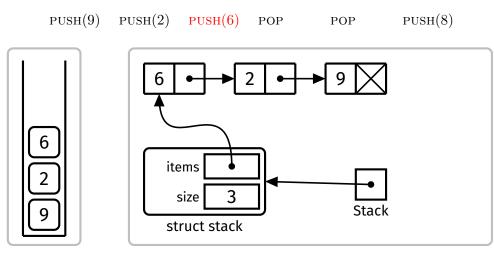
Stacks
Example Usage

Interface Implementation

Array Linked list

Queues

Sets



User's view

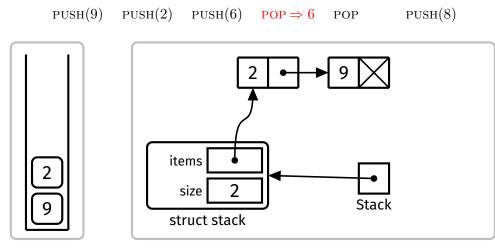
ADTs Stacks

Example Usage

Array Linked list

Queues

Sets



User's view

ADTs Stacks

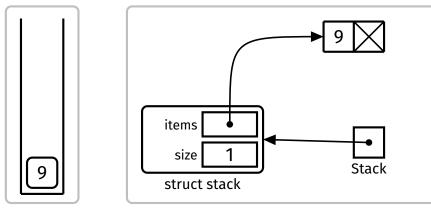
Example Usage

Array Linked list

Queues

Sets

$$PUSH(9)$$
 $PUSH(2)$ $PUSH(6)$ $POP \Rightarrow 6$ $POP \Rightarrow 2$ $PUSH(8)$



User's view

ADTs Stacks

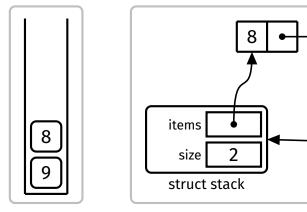
Example Usage

Array Linked list

Queues

Sets





User's view

Concrete representation

Stack

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ADTs Stacks

> Example Usage Interface

Array Linked list

Juene

Sets

Cost of push:

 \bullet Inserting at the beginning of a linked list is ${\cal O}(1)$

Cost of pop:

- Removing from the beginning of a linked list is ${\it O}(1)$

ADSTRACTION

ADTs Stacks

Oueues

Interrace

Sets

A queue is a collection of items, such that the first item to enter is the first item to leave:

First In, First Out (FIFO)

(Think queues of people, etc.)

ADTs Stacks

Queues

Sets

A queue is a collection of items, such that the first item to enter is the first item to leave:

First In, First Out (FIFO)

(Think queues of people, etc.)

- waiting lists
- call centres
- access to shared resources. (e.g., printers)
- processes in a computer

Queues

Sets

A queue supports the following operations:

enqueue

add a new item to the end of the queue

dequeue

remove the item at the front of the queue

size

return the number of items in the queue

peek

get the frontmost item of the queue, without removing it

Abstraction ADTs

Queues Interface

Sets

Stacks

```
typedef struct queue *Queue;
/** Create a new, empty Queue */
Queue QueueNew(void);
/** Free memory allocated to a Queue */
void QueueFree(Queue q);
/** Add an item to the end of a Queue */
void QueueEnqueue(Queue q, Item it);
/** Remove an item from the front of a Queue
   Assumes that the Queue is not empty */
Item QueueDequeue(Queue q);
/** Get the number of items in a Queue */
int QueueSize(Queue q);
/** Get the item at the front of a Queue
   Assumes that the Queue is not empty */
Item QueuePeek(Queue q);
```

ADTs Stacks

Queues

Interface

Implementation

Array

Sets

How to implement a queue?

array

linked list (easier)

ADTs Stacks

Queues Interface

Implementat

Avenue

Array

To enqueue an item, insert it at the end of the list

To dequeue an item, remove it from the beginning of the list

ADTs

Stacks

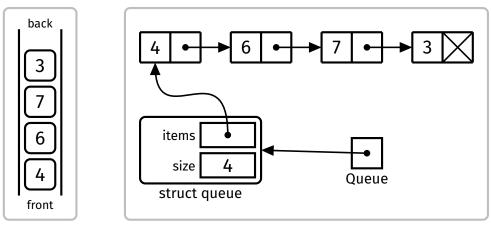
Interface

Linked list

Array

Sets

What's the problem with this design?



User's view

Concrete representation

ADTs Stacks

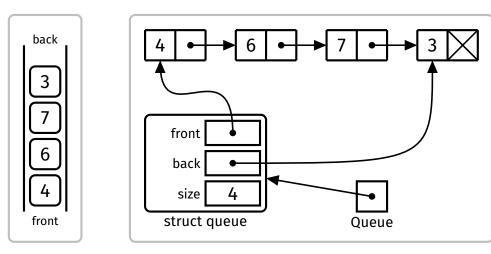
Oueues

Interface Implementatio

Linked list

Sets

Improved design



User's view

ADTs

Stacks

Queues

Implementati

Linked list

Array

Example

Perform the following operations:

 $\mathrm{enQ}(9)$, $\mathrm{enQ}(2)$, $\mathrm{enQ}(6)$, deQ , deQ , $\mathrm{enQ}(8)$

Linked list implementation

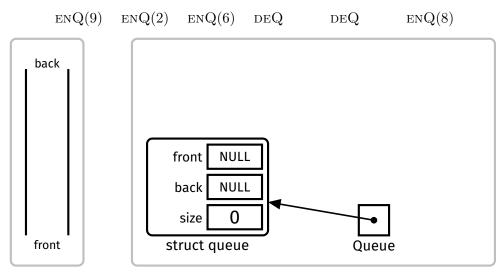
Abstraction

ADTs Stacks

Queues
Interface
Implementation
Linked list

Array

Sets



User's view

Linked list implementation

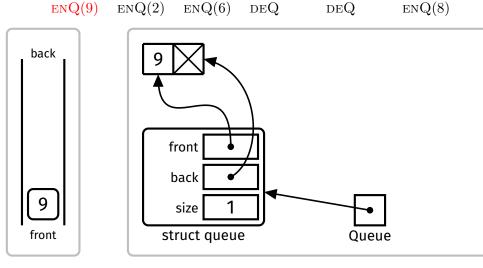
Abstraction

ADTs Stacks

Queues Interface Implementation

Linked list Array

Array



User's view

Linked list implementation

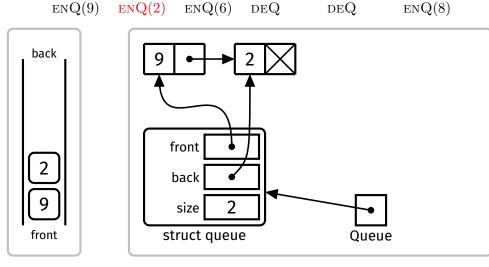
Abstraction

ADTs Stacks

Queues

Interface Implementation Linked list

Array Sets



User's view

Linked list implementation

Abstraction

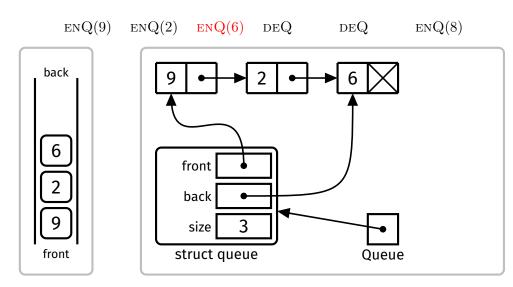
ADTs

Stacks

Queues
Interface
Implementatio
Linked list

Array

Sets



User's view

Linked list implementation

Abstraction

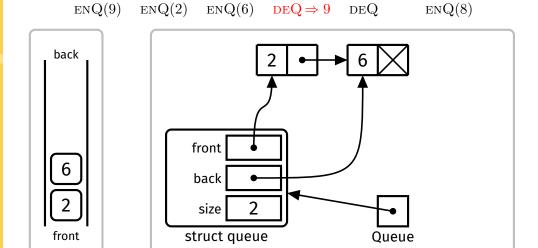
ADTs Stacks

Queues Interface

Implementatio Linked list

Array

Sets



User's view

ADTs

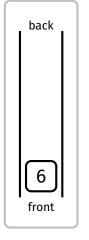
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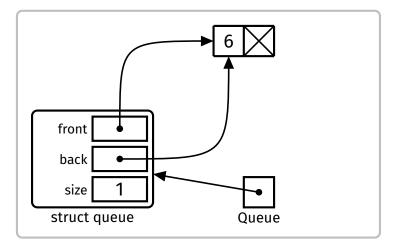
Queues
Interface
Implementatio
Linked list

Array

Sets







User's view

Concrete representation

ADTs

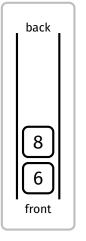
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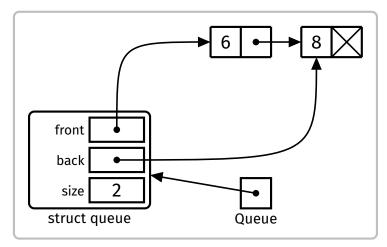
Queues
Interface
Implementatio
Linked list

Array

Sets







User's view

ADTs

Stacks

Queues Interface Implementation

> Linked list Array

Sets

Cost of enqueue:

• Inserting at the end of the linked list is O(1)

Cost of dequeue:

• Removing from the beginning of the linked list is $\mathcal{O}(1)$

ADTs

Stacks Oueues

Interface Implementation

Array

Sets

Dynamically allocate an array with an initial capacity

Maintain an index to the front of the queue

Maintain a counter of the number of items in the queue

Array implementation

Abstraction

ADTs

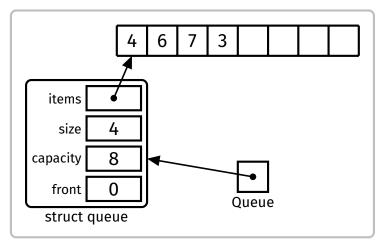
Stacks

Interface Implementation

Array

Sets





User's view

Concrete representation

ADTs Stacks Oueues

Interface Implementatio

Array

Sets

Example

Perform the following operations:

 $\mathrm{enQ}(9)$, $\mathrm{enQ}(2)$, $\mathrm{enQ}(6)$, deQ , deQ , $\mathrm{enQ}(8)$

Array implementation

ENQ(8)

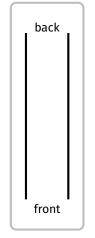
Abstraction

ADTs Stacks

Oueues

Interface Implementation Linked list

Array



ENQ(9)

ENQ(2)

ENQ(6)

struct queue

DEQ

items size capacity 8 front

DEQ

Queue

User's view

Array implementation

Abstraction

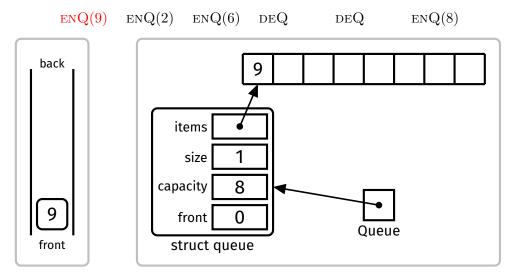
ADTs

Stacks

Interface
Implementation

Array

Sets



User's view

Array implementation

Abstraction

ADTs

Stacks

Interface
Implementation
Linked list

Array

ENQ(9)ENQ(2) ENQ(6)ENQ(8)DEQDEQ back items size capacity 8 front Queue front struct queue

User's view

Array implementation

Abstraction

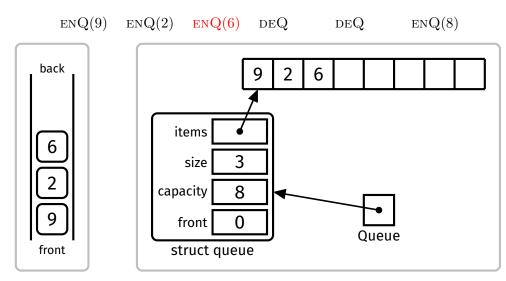
ADTs

Stacks

Interface
Implementation

Array

Sets



User's view

Array implementation

Abstraction

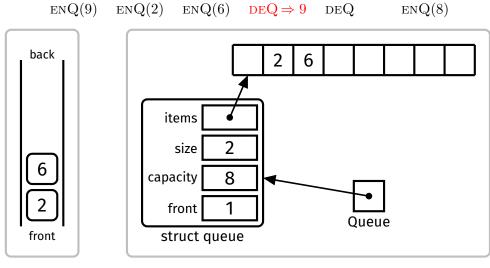
ADTs

Stacks

Interface
Implementation

Array

Sets



User's view

Array implementation

Abstraction

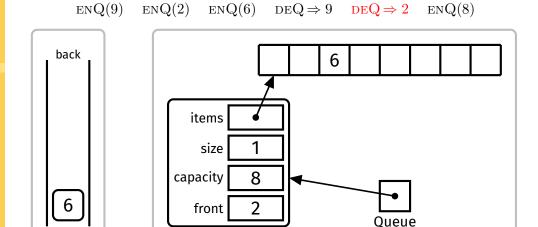
ADTs

Stacks

Interface
Implementation

Array

Sets



struct queue

User's view

front

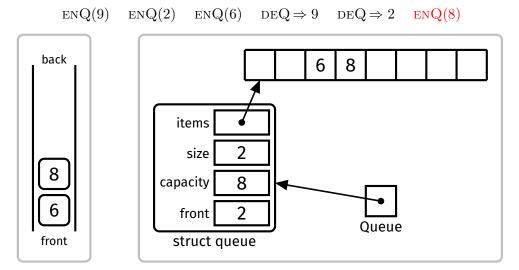
Array implementation

Abstraction

ADTs

Stacks

Array Sets



User's view

ADTs Stacks

Cost of enqueue:

 Dequeue involves calculating insertion index and inserting item at that index $\Rightarrow O(1)$

Cost of dequeue:

• Dequeue involves accessing item at index front $\Rightarrow O(1)$

ADTs

Stacks

Oueues

Sets

Example Usage Implementation

A set is an unordered collection of distinct elements.

In this lecture we are concerned with sets of integers.

ADTs Stacks

Queues

Sets

Basic set operations:

- Create an empty set
- Insert an item into the set
- Delete an item from the set
- Check if an item is in the set
- Get the size of the set
- Display the set

Set

```
Abstraction
```

ADTs

Stacks Queues

Sets Interface

```
typedef struct set *Set;
/** Creates a new empty set */
Set SetNew(void);
/** Free memory used by set */
void SetFree(Set set);
/** Inserts an item into the set */
void SetInsert(Set set, int item);
/** Deletes an item from the set */
void SetDelete(Set set, int item);
/** Checks if an item is in the set */
bool SetContains(Set set, int item);
/** Returns the size of the set */
int SetSize(Set set);
/** Displays the set */
void SetShow(Set set);
```

#include <stdbool.h>

Stacks

Queues

Sets Interface

Example Usage Implementation

```
Counting and displaying distinct numbers:
```

```
#include <stdio.h>
#include "Set.h"
int main(void) {
    Set s = SetNew();
    int val;
    while (scanf("%d", &val) == 1) {
        SetInsert(s, val);
    printf("Number of distinct values: %d\n", SetSize(s));
    printf("Values: ");
    SetShow(s);
    SetFree(s);
```

Abstraction

ADTs **Stacks**

Queues

Sets

Interface

Implementation

Different ways to implement a set:

- Unordered array
- Ordered array
- Ordered linked list

Unordered array

Abstraction

ADTs Stacks

Queues

Sets

Interface Example Usage

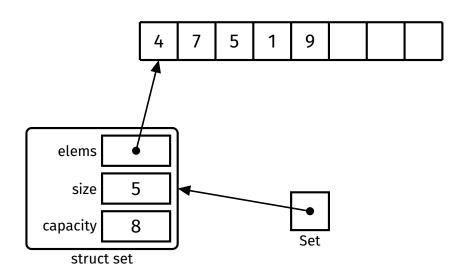
Implementation

Unordered array

Ordered array

Linked list

Summary



Unordered array

Abstraction

ADTs

Stacks Oueues

Sets

Interface Example Usage

Implementation
Unordered array

Ordered array

How do we check if an element exists?

• Perform linear scan of array $\Rightarrow O(n)$

```
bool SetContains(Set s, int elem) {
    for (int i = 0; i < s->size; i++) {
        if (s->elems[i] == elem) {
            return true;
        }
    }
    return false;
}
```

Unordered array

Abstraction

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ADTs Stacks

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Sets Interface

Example Usage Implementation

Ordered array Linked list

How do we insert an element?

• If the element doesn't exist, insert it after the last element

```
void SetInsert(Set s, int elem) {
    if (SetContains(s, elem)) {
        return;
    }

    if (s->size == s->capacity) {
        // error message
    }

    s->elems[s->size] = elem;
    s->size++;
}
```

Time complexity: O(n)

• SetContains is O(n) and inserting after the last element is O(1)



Unordered array

Abstraction

ADTs

Stacks

Sets

Example Usage

Ordered array Linked list

How do we delete an element?

• If the element exists, overwrite it with the last element

Time complexity: O(n)

• Finding the element is O(n), overwriting it with the last element is O(1)

Ordered array

Abstraction

ADTs

Stacks

Queues

Sets

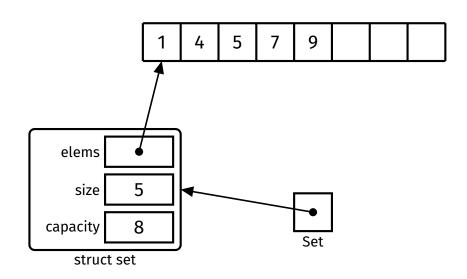
Interface Example Usage

Implementatio

Ordered array

Ordered array

Linked list



Ordered array

Abstraction

ADTs

Stacks

Oueues

Sets

Interface Example Usage Implementation

Ordered array

Linked list

How do we check if an element exists?

• Perform binary search $\Rightarrow O(\log n)$

```
bool SetContains(Set s, int elem) {
    int lo = 0;
    int hi = s->size - 1;
    while (lo <= hi) {</pre>
        int mid = (lo + hi) / 2;
        if (elem < s->elems[mid]) {
            hi = mid - 1;
        } else if (elem > s->elems[mid]) {
            lo = mid + 1;
        } else {
            return true;
    return false;
```

Ordered array

Abstraction

ADTs Stacks

Ougua

Sets
Interface
Example Usage
Implementation

Ordered array Linked list Summary

How do we insert an element?

- Use binary search to find the index of the smallest element which is greater than or equal to the given element
- If this element *is* the given element, then it already exists, so no need to do anything
- Otherwise, insert the element at that index and shift everything greater than it up

Ordered array

Abstraction

ADTs Stacks

Oueues

Sets Interface

Example Usage

Unordered a

Ordered array Linked list Time complexity of insertion?

- Binary search lets us find the insertion point in $O(\log n)$ time
- ...but we still have to potentially shift up to n elements, which is O(n)

Ordered array

Abstraction

ADTs

Stacks

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Sets

Example Usage Implementation Unordered arra

Ordered array Linked list Summary

How do we delete an element?

- Use binary search to find the element
- If the element exists, shift everything greater than it down

Time complexity?

- Binary search lets us find the element in $O(\log n)$ time
- ...but we still have to potentially shift up to n elements, which is O(n)

Ordered linked list

Abstraction

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ADTs Stacks

Queues

Sets

Interface

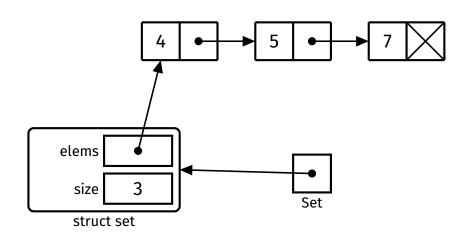
Example Usage

Implementation

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Linked list

C.....



Ordered linked list

Abstraction

ADTs

Stacks

Queues

Sets

Interface

Linked list

How do we check if an element exists?

• Traverse the list $\Rightarrow O(n)$

```
bool SetContains(Set s, int elem) {
    for (struct node *curr = s->elems; curr != NULL; curr = curr->next) {
        if (curr->elem == elem) {
            return true;
    return false;
```

Ordered linked list

Abstraction

.....

ADTs Stack

Juck

Sets
Interface
Example Usag

Unordered ar Ordered array Linked list We always have to traverse the list from the start. Therefore...

• Insertion and deletion are also O(n)

However, this analysis hides a crucial advantage of linked lists:

- Finding the insertion/deletion point is O(n)
- But inserting/deleting a node is O(1), as no shifting is required

Abstraction

ADTs Stacks

Queues

Sets

Interface Example Usage

Implementation

Summary

Data Structure	Contains	Insert	Delete
Unordered array	O(n)	O(n)	O(n)
Ordered array	$O(\log n)$	O(n)	O(n)
Ordered linked list	O(n)	O(n)	O(n)

Abstraction

ADTs Stacks

Queues

Sets

Interface Example Usage

Summary

https://forms.office.com/r/zEqxUXvmLR

