

## **Must Do Binary Tree problems for Placement**

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<b>Binary Trees</b>	<a href="#"><u>Check if a Binary Tree contains duplicate subtrees of size 2 or more [ IMP ]</u></a>
<b>Binary Trees</b>	<a href="#"><u>Check if 2 trees are mirror or not</u></a>
<b>Binary Trees</b>	<a href="#"><u>Sum of Nodes on the Longest path from root to leaf node</u></a>

<b>Binary Trees</b>	<a href="#">Check if given graph is tree or not. [ IMP ]</a>
<b>Binary Trees</b>	<a href="#">Find Largest subtree sum in a tree</a>
<b>Binary Trees</b>	<a href="#">Maximum Sum of nodes in Binary tree such that no two are adjacent</a>
<b>Binary Trees</b>	<a href="#">Print all "K" Sum paths in a Binary tree</a>
<b>Binary Trees</b>	<a href="#">Find LCA in a Binary tree</a>
<b>Binary Trees</b>	<a href="#">Find distance between 2 nodes in a Binary tree</a>
<b>Binary Trees</b>	<a href="#">Kth Ancestor of node in a Binary tree</a>
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<b>Binary Trees</b>	<a href="#">Tree Isomorphism Problem</a>

Ques → First non-repeating character in a Stream

Given input stream of 'A' on n lower case alphabet. Task is to find non-repeating char, each time a char. is inserted to the stream. if there is no such char then append '#'.  
 Stream [a a b c]

\* Example :-

a a b c

↑ ↑ ↑

Stream

[a a b c]

ans = a # b # . // ∵ 1st non repeating ele.

\* Intuition :-

→ ∵ we have to maintain count of each alphabet we'll use a 'counter' variable.

→ Now, here we've to maintain freq. as well as its order of alphabet

→ so we'll take a vector or map, to maintain order.

\* Implementation :-

string NonRepeat (string s)



int n = s.size(); unordered\_map<char, int> map;

string ans = ""; queue<char> q;

for (int i=0; i < n; i++)

if (!map[s[i]]) q.push(s[i]);

map[s[i]]++;

while (!q.empty() && map[q.front()] > 1) q.pop();

if (q.empty()) ans += "#";

else ans += q.front();

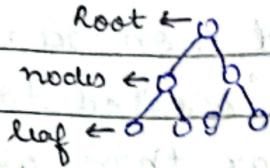
return ans;



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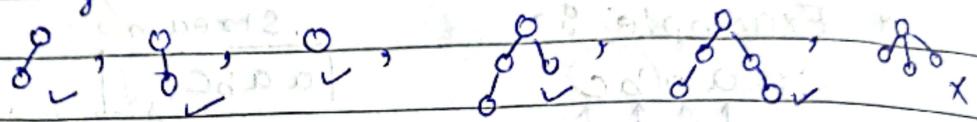
## Binary Tree

\* Tree :- A graph with no cycle.



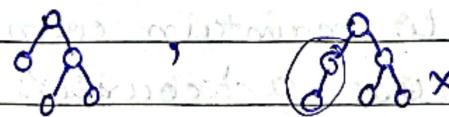
we don't have a loop/cycle in tree  
structure: Root, Internal node, leaf.

→ Binary tree: At most 2 children. (0, 1, 2)



→ Full / strict Binary tree:-

either 0 or 2 children.

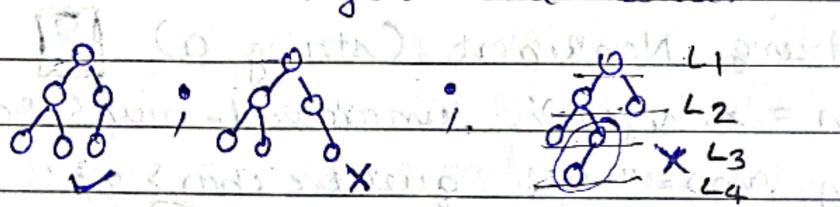


→ ACBT (Almost complete BT).

↳ not ACBT, missing for left child

↳ not ACBT, missing for right child

↳ Yes, Bcoz always left after right  
then goto next level.



(Left) Aug. 20 (11:13) contd.)

↳ if left child is null then right child must be null

↳ if right child is null then left child must be null

↳ if left child is not null then right child must be null

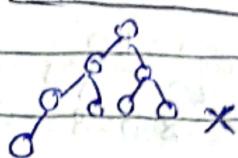
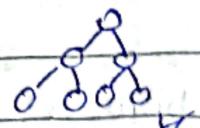
↳ if right child is not null then left child must be null



↳ and vice versa

→ perfect/complete Binary Tree :-

NO holes



(It is ACBT,  
but not CBT)

→ Binary Search tree :-

① Create BST, with following keys.

4, 2, 3, 6, 5, 7, 1

in BST, there is no systematic order,

e.g.:- , after storing the data,

for 2, 7 and 3 we have to search for particular data afterward

6  
8

And, if we don't put data in systematic order, then we'll definitely face complexity in searching particular data.

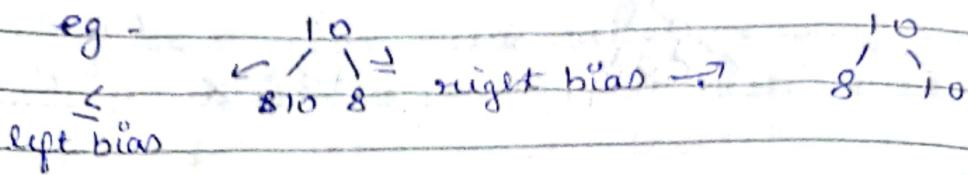
average TC -  $O(n)$ .

# Now, BST says, while entering data.  
left child should be less than root,  
and right child should be greater than root.

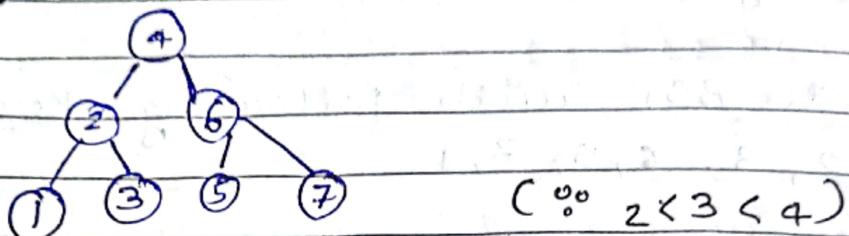


# If in case keys are equal,  
then you can put either side.

eg -



Sol:



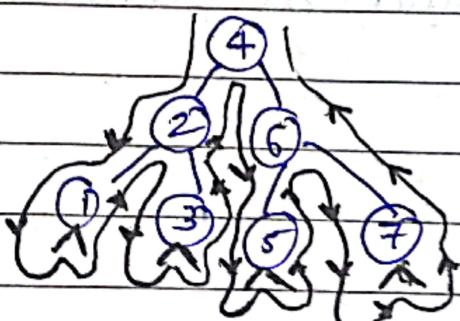
Binary search tree.

→ Least element in the end of left side will be smallest key.

→ Least element at the end of right side will be biggest element in key.

→ Inorder: always give sorted array.  
make 2 child of each node (dummy)

check; if we reach any element 2<sup>nd</sup>/more time, is its inorder.



1, 2, 3, 4, 5, 6, 7

# (Binary Tree)

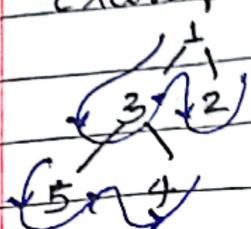
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Ques → Level Order traversal

Given BT, find its level order traversal.

LOT → nothing but breadth-first travel of tree.

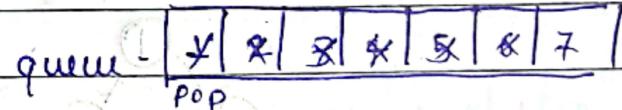
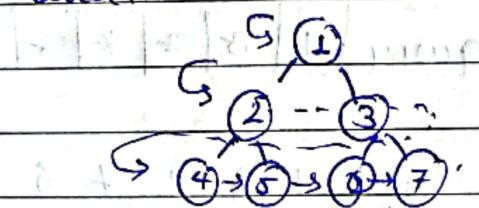
Example :-



Ans - 1, 3, 2, 5, 4.

\* Intuition :-

- 1) Solve it using queue.
- 2) store element in queue, and push back queue element in a vector 'ans'.
- 3) Now check if element's left node exist, if yes push in queue, and pop root.
- 4) same with right node.
- 5) Repeat process for entire tree, for every level.



ans = 1, 2, 3, 4, 5, 6, 7

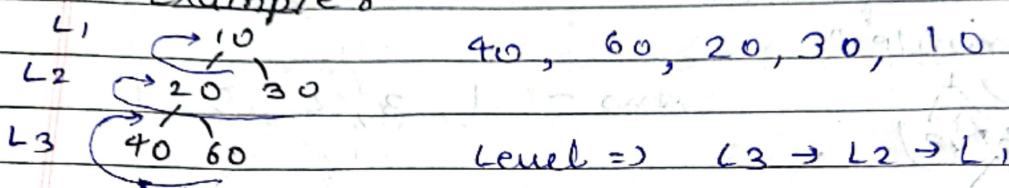
at the end queue = empty,  
Break the loop.

### Ques → Reverse Level Order Traversal

Given binary tree of size  $N$ , find its reverse level order traversal.

( traversal must begin from last level )

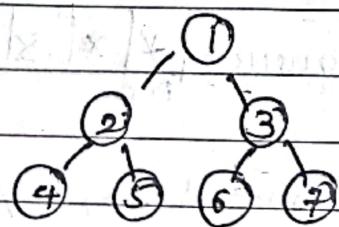
Example :-



#### \* Intuition :-

- Maintain queue and ans vector.
- firstly enter root, then check if right exist, push in queue and check left if exist push in queue.
- keep pop root and push back in the vector.
- do the same for every element in respective level.

( when we reverse ans we'll get the o/p )



queue  $\{ + 3 | 2 | 7 | 6 | 5 | 4 \}$

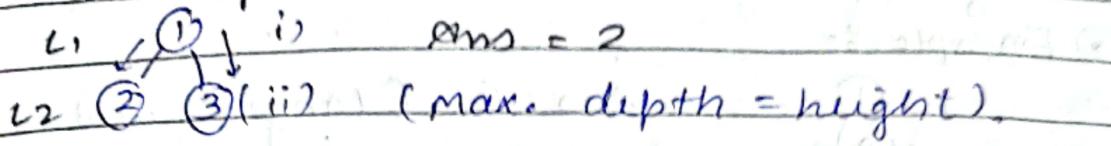
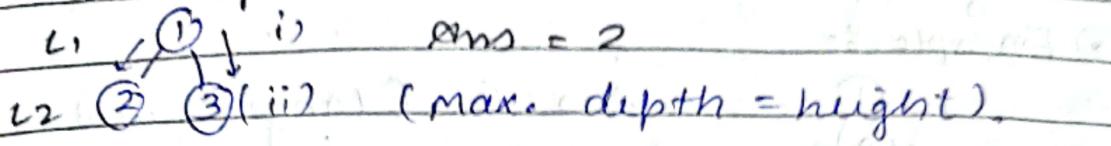
ans - 1 3 2 7 6 5 4  
↓ reverse

$\Rightarrow$  4 5 6 7 2 3 1

## Ques → Height of Binary Tree

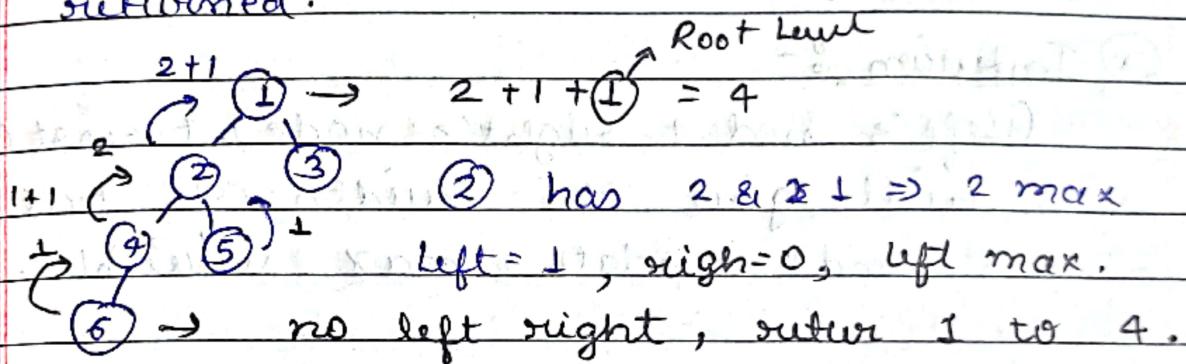
Given BT, find its height.

Example :-

1.  i) Ans = 2
2.  (Max. depth = height).

### ① Intuition :- (Recursion)

→ We'll check for height in both left and right side, max will be returned.



$$\text{Ans} = 4$$

### ② Implementation :- int height (struct Node\* node)

```
(1) if (node == NULL) return 0;  
int left = height (node->left);  
int right = height (node->right);  
int height;  
if (left > right)  
    height = 1 + left;
```

else

$$\text{height} = 1 + \text{right};$$

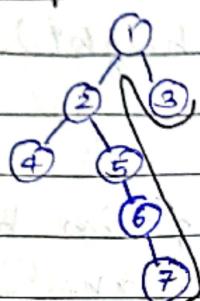
return height;

(3)

## Ques- Diameter of binary tree,

Diameter/width is no. of nodes on the longest path b/w two end nodes.

### ② Example :-



$\text{ans} = 6$ , (longest width)

### ③ Intuition :-

(Left's node + right's node) + root(1)  
will give the width of tree  
and update max variable.

### ④ Implementation :-

```
int ma;
int func(Node *root) {
    if (!root) return 0;
    int x = func(root->left);
    int y = func(root->right);
    ma = max(ma, x+y+1);
    return (max(x,y)+1);
}
```

```
int diameter(Node *root)
```

⑤  $ma = INT\_MIN;$

```
int x = func(root);
```

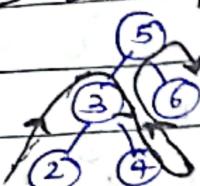
```
return ma;
```

⑥

Ans → Create a mirror tree from the given binary tree

Given a BT, create a new binary tree which is a mirror image of given BT.

① Example :-



Inorder of original T : 2 3 4 5 6

Inorder of mirror T : 6 5 4 3 2

② Intuition :-

In order to change original tree in its mirror tree, then we simply swap the left and right link of each node.

If the node is leaf node then do nothing.

③ Code :-

```
if (root == NULL)
    return root;
node * t = root->left;
root->left = root->right;
root->right = t;
```

```
if (root->left)
    mirrorTree (root->left);
```

```
if (root->right)
    mirrorTree (root->right);
```

```
return root;
```

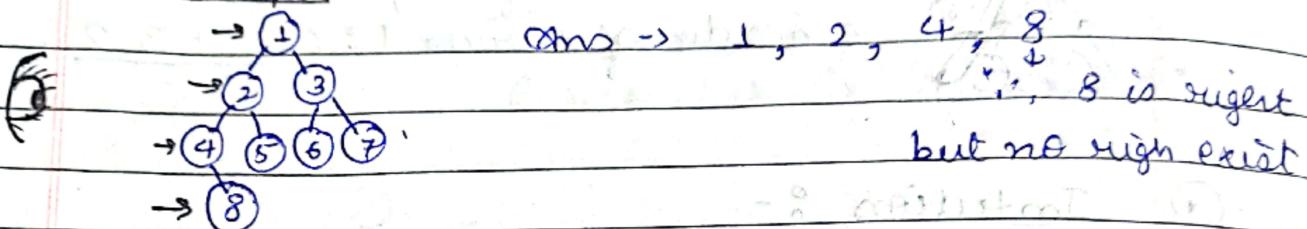
④

## Ques - Left view of Binary Tree

Given BT, print left view of tree.

Left view :- node visible, when tree visited from left side.

\* Example :-



Intuition :-

- take vector 'ans' :- put root a default value in tree ans.
- Do the level order traversal, at level 2 enter the 1<sup>st</sup> element and change the level.
- Do the above step for entire tree.

\* Implementation :- left view (Node\* root)

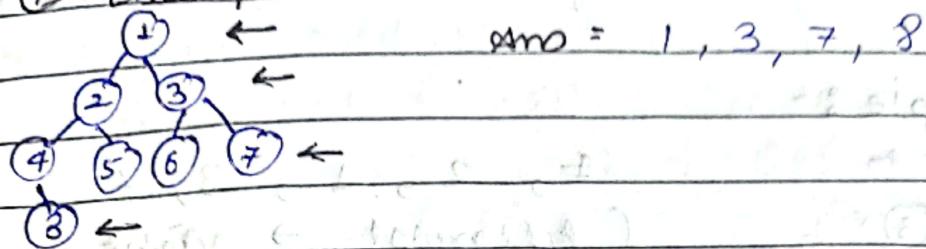
```

vector<int> ans;
queue<node*> q;
if (!root) return ans;
q.push(root);
while (!q.empty()) {
    int sz = q.size();
    ans.push_back(q.front() -> data);
    while (sz--) {
        node* t = q.front();
        q.pop();
        if (t -> left) q.push(t -> left);
        if (t -> right) q.push(t -> left);
    }
}
return ans;
  
```

Ans → Right view of tree

Gives BT, find Right view of tree.

④ Example :-



ans = 1, 3, 7, 8

⑤ Intuition :-

- take vector ans, and push root into it.
- then traverse level by level  
and push the last element of  
that level.
- do the above process for entire  
tree.

⑥ Implement :- void RightView(Node\* root)

```

⑦ queue<node*> q;
if (!root) return;
q.push(root);
while (!q.empty()) {
    int sz = q.size();
    Node* t; while (sz--) {
        t = q.front();
        q.pop();
        if (t->left) q.push(t->left);
        if (t->right) q.push(t->right);
    }
}
  
```

cout << " ";

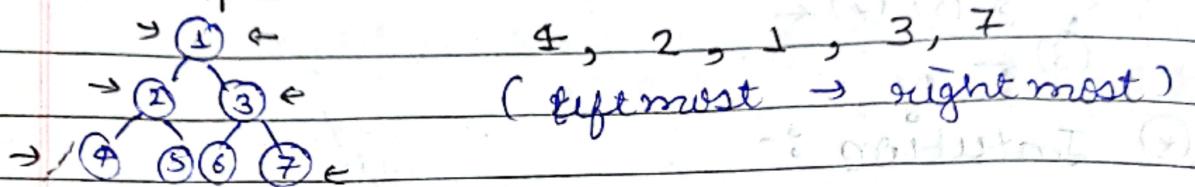
⑧

## Ques- Top View of tree

Given BT, find its top view.

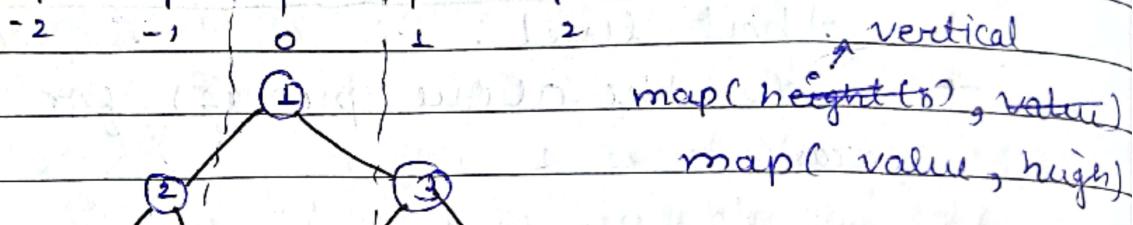
Top view = left most + right most + root.

Example :-



Intuition :-

Level  $\rightarrow$  1, 2, 3, 4, 5, 6, 7



at Level 0, element or 1, 5, 6, x,

$\therefore$ , 5, 6 covered & not visible so ans = 1.

map :- (inf)

0  $\rightarrow$  1

queue(node\* h)

NULL

1  $\rightarrow$  3

$\overbrace{5}^1 (1,0) (2,-1) (4,-2) (3,1) (7,2)$

2  $\rightarrow$  7

-1  $\rightarrow$  2

$\star \text{ans} = 1, 3, 7, 2, 4,$

2  $\rightarrow$  4

root

print in level order  $-2 \rightarrow -1 \rightarrow 0 \rightarrow 1 \rightarrow 2$

$\Rightarrow 4, 2, 1, 3, 7$

Implement :-

```
struct Void TopView (node * root)
```

```
    map<int, int> m;
```

```
    queue<pair<Node*, int>> q;
```

```
    if (!root) return;
```

```
    q.push({root, 0});
```

```
    while (!q.empty()) {
```

```
        Node* t = q.front().first;
```

```
        int h = q.front().second;
```

```
        q.pop();
```

```
        if (!m[h]) m[h] = t->data;
```

```
        if (t->left) q.push({t->left, h-1});
```

```
        if (t->right) q.push({t->right, h+1});
```

```
    }
```

```
    for (auto x : m) cout << x.second << " ";
```

```
    }
```

TC -  $O(N) \times \log n \Rightarrow n \log n$ .

SC -  $O(N)$  // extra space of queue

## Implementation :-

```
start void Topview(node *root)
    ④ map<int, int> m;
    queue<pair<Node*, int>> q;
    if (!root) return;
    q.push({root, 0});
    while (!q.empty())
        node *t = q.front().first;
        int n = q.front().second;
        q.pop();
        if (!m[n]) m[n] = t->data;
        if (t->left) q.push({t->left, n-1});
        if (t->right) q.push({t->right, n+1});
```

③ for (auto x:m) cout << x.second << " "

TC -  $O(N) \times \log n \Rightarrow n \log n$ .

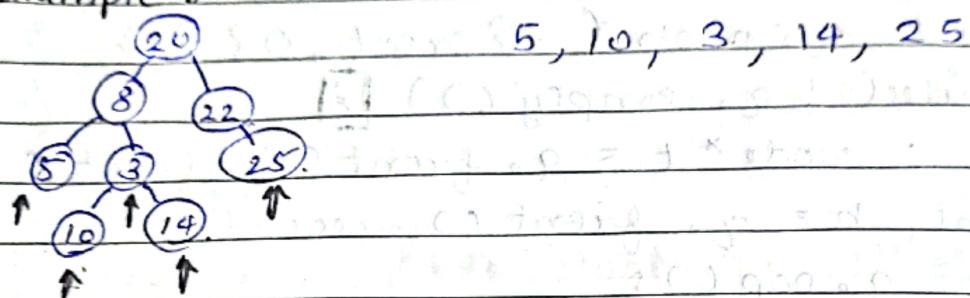
SC -  $O(N)$  // extra space of queue

Ques - Bottom View of Binary Tree

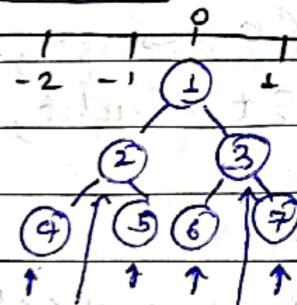
Given BT, print bottom view from left to right.

A node is included in bottom view if it can be seen when we look at tree from bottom.

\* Example :-



\* Intuition :-



Here, 2 is invisible b/w 4 & 5

3 is visible b/w 6 & 7

Here, 5 & 6 both at 0 level,

the print which comes later.

map<val, h>, queue<node\* h> required

Pick each and every element, and put into map and the element which come in the end or last will be the answer.

queue

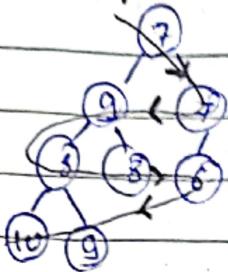
map :-  $(1, 0) (2, -1) (3, 1) (4, -2), (5, 0) (6, 0) (7, 2)$

$0 \rightarrow 0 \times 6$        $\downarrow$       update  
 $1 \rightarrow 2 \times 3$       when queue end, break.  
 $2 \rightarrow 2 \times 7$       and our ans. will be  
 $-1 \rightarrow 2 \times 2$       stored in the map.  
 $-2 \rightarrow 2 \times 4$        $(0, 0, 2, 8, 1, 5, 3)$   
 Ans:  $4, 2, 0, 3, 7,$

Ques - Zig Zag traversal of binary tree

Given a BT. find zig-zag level order traversal of BT.

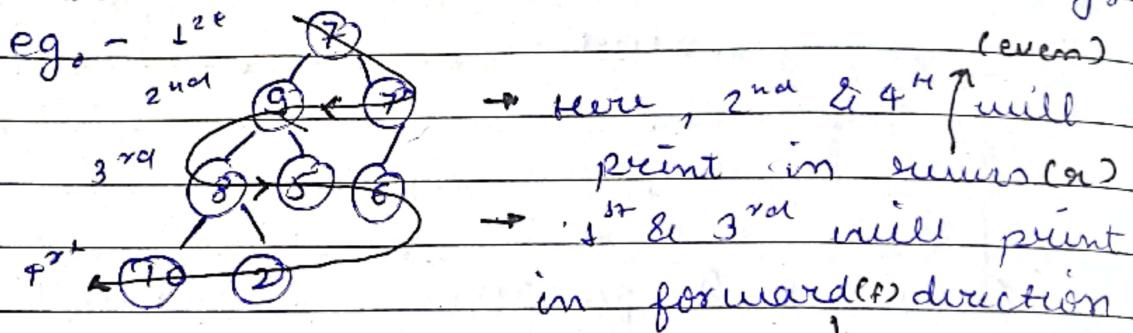
\* Example :-



Ans : 7, 7, 9, 8, 8, 6, 9, 10

Intuition :-

Logic :- take root as 1<sup>st</sup> element, do the level order traversal, and print 2<sup>nd</sup> alternative level reversely.



Ans - 7, 7, 9, 8, 5, 6, 2, 10 (odd)  
F(odd) R R (even) R

we'll use vector to print all the elements of that particular level and if level become odd or even, we'll print accordingly.

\* Code :-

```
vector<int> ZigZag(Node* root)
```

```
vector<int> ans;
```

```
queue<Node*> q;
```

```
q.push(root);
```

```
int f=1; // to check for odd even
```

```
while(!q.empty())
```

```
vector<int> temp;
```

```
int sz=q.size();
```

```
while(sz--)
```

```
Node* t=q.front();
```

```
temp.push_back(t->data);
```

```
q.pop();
```

```
if(t->left) q.push(t->left);
```

```
if(t->right) q.push(t->right);
```

(3)

```
if(f==0)
```

```
reverse(temp.begin(), temp.end());
```

```
for(int i=0; i<temp.size(); i++)
```

```
ans.push_back(temp[i]);
```

```
f=!f;
```

(3)

```
return ans;
```

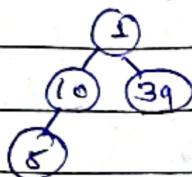
(3)

Ques :- Check if tree is balanced or not

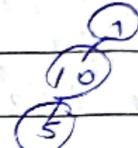
Given BT, find if it is height balanced or not.

Balanced : if height diff b/w left and right subtree is not more than one for all nodes.

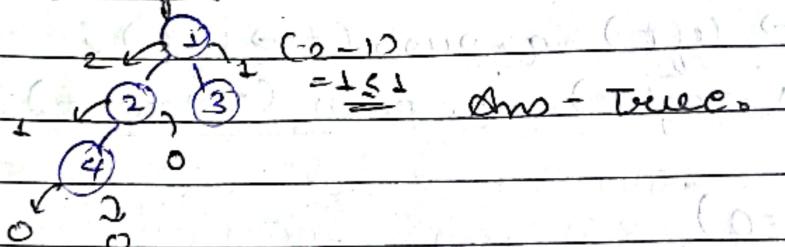
Balanced



Unbalanced



Example :-



\* Intuition :- (Using Recursion)

→ In PCT we have to find the height of every node

→ and the check if difference b/w left & right is ≤ 1 or not

→ then true else false & break

## ④ Implementation

```

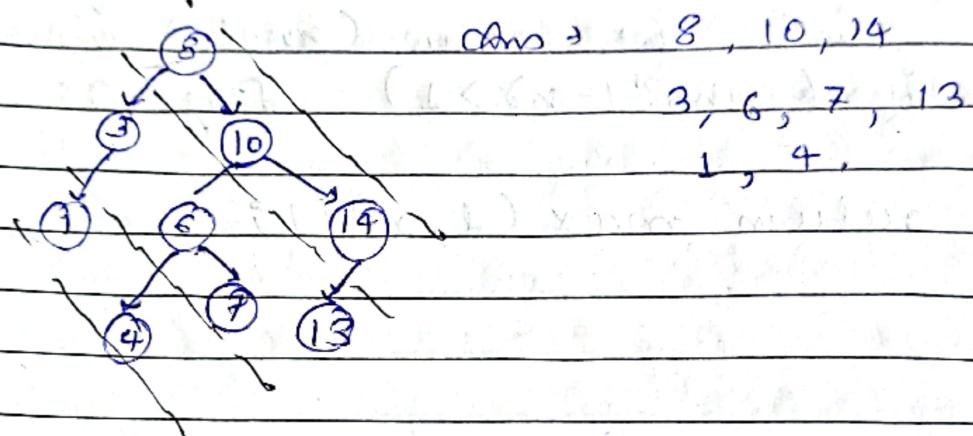
int int flag = 1;
int solve( node* root ) {
    if ( !root ) return 0;
    int l = solve( root->left );
    int r = solve( root->right );
    if ( abs(l-r) > 1 ) flag = 0;
    return max( l, r ) + 1;
}

```

## Ques → Diagonal Traversal of BT

Consider lines of slope -1, passing b/w nodes.  
 Given BT, print all elements of BT  
 belong to same line.

Example :-



### \* Intuition :-

- The idea is use map.
- we use diff. slope dist., and use it as key of map!
- Value will be stored in map as vector
- Traverse tree to store values in the map. Once map built, then print its content.

TC -  $N \log n$

SC -  $O(N)$

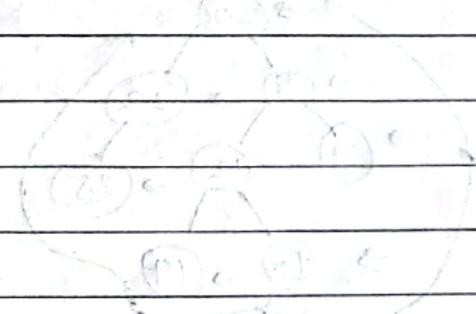
Implementation :-

```
void diagonalPrint(Node* root) {
    map<int, vector<int>> diag;
    diagonalPrintUtil(root, 0, diagonalPrint);
    cout << "diagonal traversal of BT" << endl;
    for (auto it : diagonalPrint)
        for (auto v : it.second)
            cout << v << " ";
    cout << endl;
}
```

(3)

(3)

→ diagonal

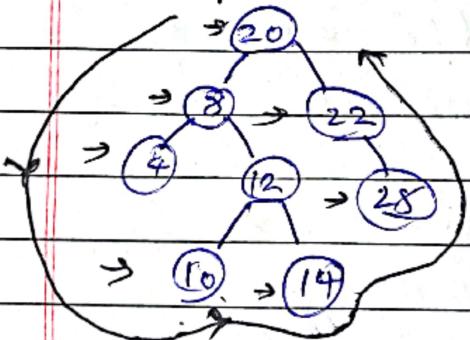


## Ques → Boundary Traversal of BT

Given BT, find its boundary traversal.

- ① Left boundary node: path from root to left most node, i.e. leaf node you could reach, when you always travel preferring left subtree over the right.
- ② Leaf node: all leaf node, except for the one who is part of left or right Boundary.
- ③ Reverse right boundary node:- path from right most node of the root. Right most node is leaf node you could reach when you always travel preferring right subtree over the left.

Example :-



Ans = 20, 8, 4, 10, 14, 22, 28

## Intuition

- (\*) we'll break problem in 3 parts.
  - (1) print left-boundary in top down manner
  - (2) print all leaf node from L to R,  
which can be subdivided.
    - 2.1) print all leaf node of <sup>left</sup> sub tree from L to R
    - 2.2) " " " " " " " " Right sub-tree , , ,
  - (3) Print the right boundary in bottom up

NOTE - We take care 1 thing that node are not printing again.  
e.g. - left most node is also leaf node of tree.

Ques → Construct BT from string with bracket representation

Construct bt from a string consisting of parenthesis and integers. The whole input represent. The whole input represent it contain an integer followed by zero, one or two pair of parenthesis.

Integer represents root's value & a pair of parenthesis contains a child binary tree with same structure.

#### \* Example :-

I/P : 1(2)(3) O/P : 1 2 3

① → 1<sup>st</sup> pair of parenthesis  
 ② ③ contains left subtree and second one contains the right subtree.  
 (preorder → 1 2 3).

4 ( 2 ( 3 ) ( 1 ) ) ( 6 ( 5 ) )  
 Root      Left subtree      Right subtree

we need to find the substring corresponding to left substring & substring to right subtree, and then call recursively call on both the substring.

## \* Recursive Approach

- ① The very first element is of string is root.
- ② The next two consecutive elements are "(" & ")", this means there is no left child otherwise we will create and add the left child to the parent node recursively.
- ③ Once the left child added recursively we will look for consecutive "(" and add the right child to parent node.
- ④ Encountering ")" means the end of either left or right node and we will see start index.
- ⑤ The recursion end when the start index is greater than equal to the end index.

## \* Preorder (node\* root)

```
if (root == NULL)
```

```
cout << root->data << " " ;
```

```
preorder((root->left));
```

```
preorder((root->right));
```

3

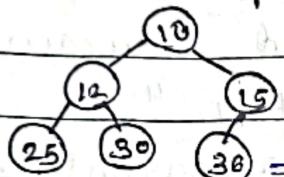
Ques → Binary Tree to DLL

Given BT, convert it to DLL in place.

left and right pointers in node are to be used as previous and next pointer respectively in converted DLL.

Order of node in DLL is same as inorder of given BT.

Example :-



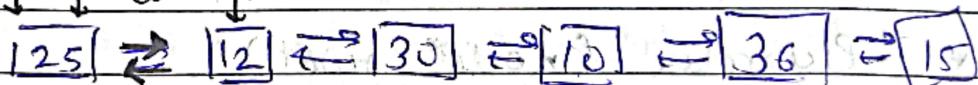
The above tree should be in-place

convert to DLL,

$25 \Rightarrow 12 \Rightarrow 30 \Rightarrow 10 \Rightarrow 36 \Rightarrow 15$

\* Intuition :-

→ Right ptr = next ptr. and Left ptr = prev.ptr  
→ firstly (head == NULL), and taking forward with a flag variable.  
next ↓ prev ↓ root



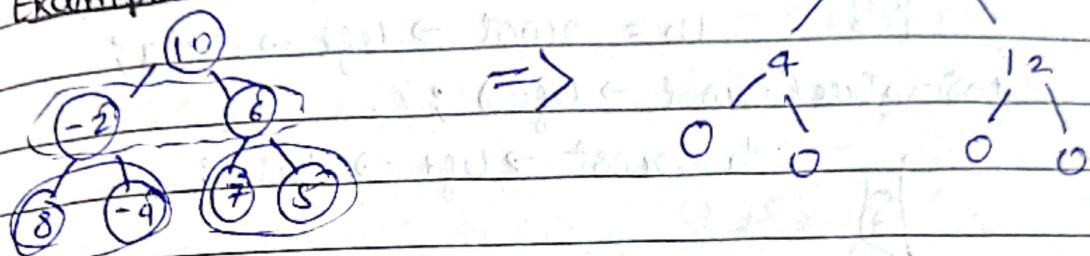
- ① now, at the next node, (prev  $\rightarrow$  next = root)
- ② then, prev  $\rightarrow$  right  $\rightarrow$  left = prev.
- ③ then, prev = prev  $\rightarrow$  right

→ Repeat this step for entire inorder traversal

## Transform to Sum Tree

Given BT of size  $N$ , where each node can have +ve or -ve values. Convert this to tree where each node contains the sum of left and right subtree of the original tree.

Example :-



### Intuition :-

Traverse given tree. In traversal store old value of current node, recursively call for left and right subtree and change the value of current node as sum of values returned by recursive calls.

In the end, return sum of new value which is subtree rooted with this node.

## ④ Implementation :-

```

int ToSumTree (Node* Node)
{
    if (node == NULL)
        return 0;

    int l1 = 0;
    int r1 = 0;

    if (root == left)
    {
        l1 = root->left->data;
        toSumTree (root->left);
        r1 = root->left->data;
    }

    int r2 = 0;
    int l2 = 0;

    if (root == right)
    {
        r2 = root->right->data;
        toSumTree (root->right);
        l2 = root->right->data;
    }

    root->data = r1 + r2 + l1 + l2;

    return;
}

```

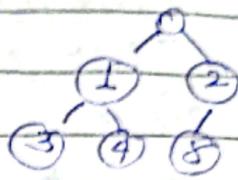
Ques → Construct tree from Inorder & Preorder.

Given 2 arrays of Inorder & Preorder traversal construct tree and print postorder traversal

\* Example :-

Inorder - 3, 1, 4, 0, 5, 2

Preorder - 0, 1, 3, 4, 2, 5



Intuition :-

- + Traverse in preorder, make node element as a node.
- Search node in inorder, now if present in inorder,
- all the element present in left, send to the left side of tree.
- and all the element present in right of node send to right side of tree.

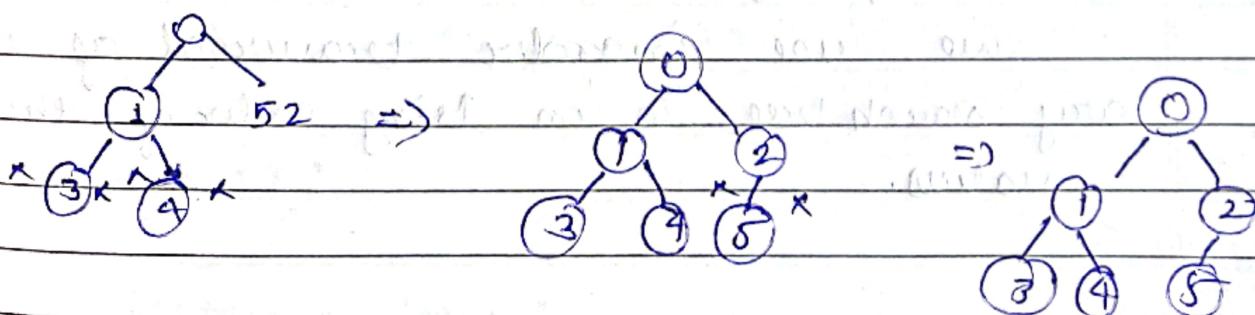
① Dry Run :-

3 1 4 0 5 2 - In

0 1 3 4 2 5 - pre

↑ ↑ ↑ ↑ ↑

3 1 4 0 5 2



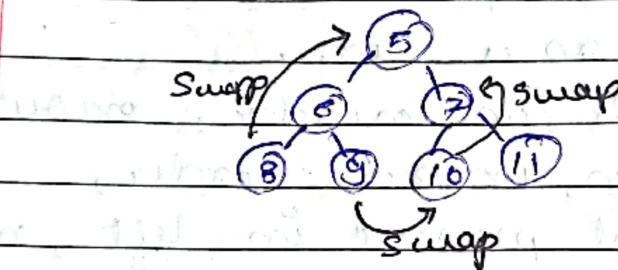
Ques → Find min. swap require to convert BT to BST.

Given the array  $A$ , represents complete BT, i.e. if index  $i$  is parent, index  $2*i+1$  is left child and  $2*i+2$  is right child. find min no. of swap require to convert into BST.

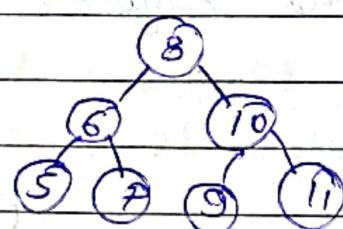
Example :-

Input : arr[ ] = { 5, 6, 7, 8, 9, 10, 11, 13 }

O/P = 3



Swap 8 to 5, 9 to 10, and 10 to 7.



∴ 3 swap required

→ Intuition :-

We use inorder traversal of Binary search tree is in rising order of their values.

we find inorder traversal of BT and store it in array.  
They sort the array.  
Then, min no. of swap required to get array sorted will be answer.

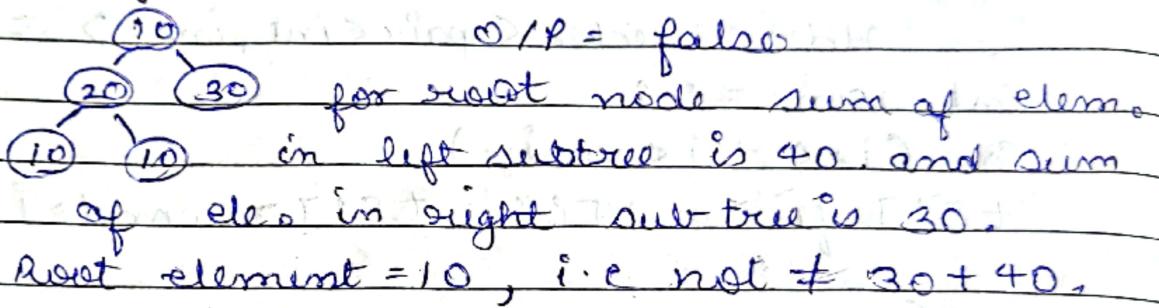
### Implementation :-

```
int minSwap (std :: vector<int>& v)
{
    std :: vector< pair<int, int>> t (v.size());
    int ans = 0;
    for (int i = 0; i < v.size(); i++)
        t[i].first = v[i], t[i].second = i;
    sort (t.begin(), t.end());
    for (int i = 0; i < t.size(); i++)
    {
        if (i == t[i].second)
            continue;
        else
            swap (t[i].first, t[t[i].second].first);
        swap (t[i].second, t[t[i].second].second);
        if (i != t[i].second)
            ans++;
    }
    return ans;
}
```

Ques → Check if BT is sum tree or not.

Given a BT, return true if, for every node X in the tree other than the leaves, its value is equal to the sum of its left subtree's value and its right subtree's value. else return false.

Example :-



Intuition :-

- (1) Same as postorder traversal, iteratively find the sum in each step.
- (2) Return left + right + current - data, if  $left + right = current\ node\ data$
- (3) else return -1

## Implementation

```
bool isSumTree (node *root),
```

(1) if (!root).

```
    return true;
```

(2)

if (!root → left && !root → right)

(3)

```
    return true;
```

(4)

```
int count = 1;
```

```
helper (root, count);
```

if (count == 1)

(5)

```
    return true;
```

(6)

else

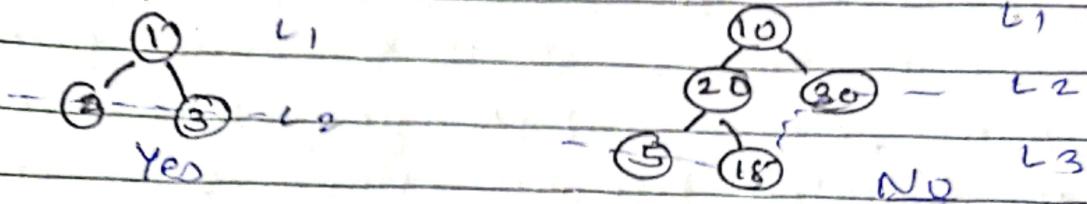
```
    return false;
```

(7)

Ques :- leaf at same level

Given a BT, check if all leaves are at same level or not.

Example :-



Intuition :-

- (1) The idea is iteratively traverse tree, & when encounter 1<sup>st</sup> leaf node, store its level in result variable.
- (2) Now whenever you encounter any leaf node, compare its level with prev stored result, they are the same then proceed for rest of the tree, else return false

Snippt :-

```
bool chick(Node* node)
```

```
{ if (!root) return true;
```

```
if (!root -> left && !root -> right)
```

```
return true;
```

```
vector<int> v;
```

```
levelLeaf (root, v, 0);
```

```
for (auto x : v)
```

```
{ if (x != v[0])
```

```
return false;
```

```
}
```

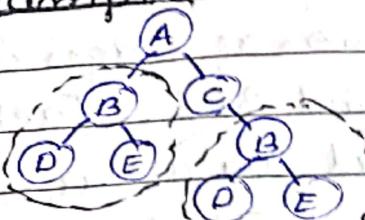
```
return true;
```

```
3
```

## Duplicate Subtree in Binary Tree

Given BT, check if BT contain any sub tree of size  $n^2$  or more.

Example :-



Intuition :- (Serialization & Hashing)

Firstly we serialize the subtree as string. Store the string in hash table.

Once we find a serialized tree (which is not a leaf) already existing in hash-table, we return true.

① Implement :- string Duplicate (node \* root)

② string s = ""; if (root == NULL) return s + "#";

string lstr = duplicate (root -> left);

if (lstr. compare (s) == 0) return s;

return s;

string rstr = duplicate (root -> right);

if (rstr. compare (s) == 0) return s;

s = s + root -> key + lstr + rstr;

subtree insert (s);

return s;

③

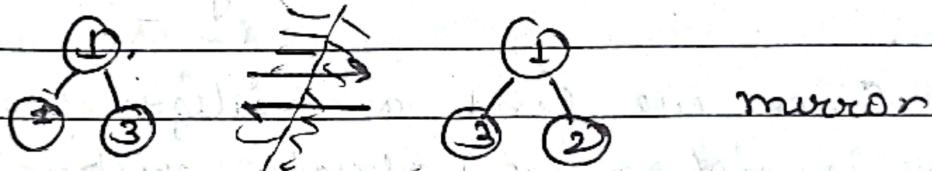
Ques - Check if 2 tree are mirror or not

Given 2 n-array trees. Check if they are mirror img. of each other or not, also given  $e$  denote no. of edges in both tree, & 2 array  $A[J]$  and  $B[J]$ . Each array has  $2 \times e$  space separated values.  $u, v$  denoting edge from  $u$  to  $v$  from both tree.

\* Example :-

$$n=3, e=2$$

$$A[J] = \{1, 2, 1, 3\} \quad B[J] = \{1, 3, 1, 2\} \Rightarrow O/P = 1 (\text{true})$$



\* Polution :-

The main approach is to use list of stack and one list of queue to store to value of node given in form of 2 array.

## ④ Approach (algo) :-

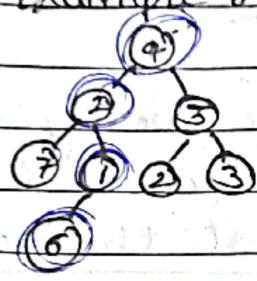
- Init both lists with empty stack and empty queue.
- Now, iterate over list, push all connected node of each node first tree in list of stack and second tree list of queue.
- Now iterate over the array & pop items from both stack & queue & check if they are same, if not then return 0.

Ques :- Sum of longest bloodline of tree.

Given BT, find sum of all nodes on the longest path from root to leaf node.

If 2 or more paths complete for longest path, then the path having max. sum of node is being considered.

Example :-



Highest node  $\Rightarrow$  4, 2, 1, 6.

$$\text{Sum} = 4 + 6 + 6 + 1 = 17$$

$$O/P \Rightarrow 17$$

Intuition :- (use use BFS)

- ① Create structure containing current node, level & sum in the path.
- ② Push root element with level 0 & sum as root's data.
- ③ Pop front data/element & update max. level, sum & max. level if needed.
- ④ Push left & right node if exist.
- ⑤ Do same for all node in tree.

Implement :-

```

void solve (node* root, int len, int & maxlen,
           int sum, int & maxsum) {
    if (root == NULL) {
        if (len > maxlen) {
            maxlen = len;
            maxsum = max (sum, maxsum);
        }
    } else if (len == maxlen) {
        maxsum = max (sum, maxsum);
    }
    sum = sum + root->data;
    maxlen++;
    solve (root->left, len+1, maxlen, sum, maxsum);
    solve (root->right, len+1, maxlen, sum, maxsum);
}

```

(3)

5. Find maximum width of binary tree

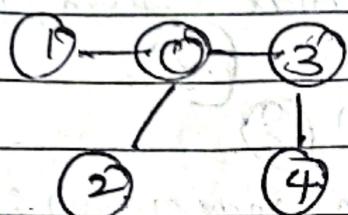
\* \* \* **Ques -> Check if given graph is tree or not**

Write func<sup>n</sup> that return true if given undirected graph is tree and false otherwise.

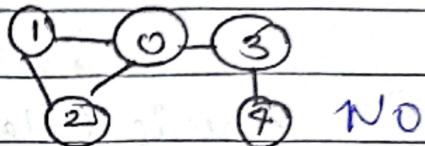
an undirected graph is tree has :-

- (1) no cycle
- (2) graph is connected

Example :-



Yes



NO

\* **Intuition :-**

How to detect cycle?

We can use either BFS or DFS, for every unvisited vertex 'v', if there is an adjacent 'u' such that 'u' is already visited and 'u' is not parent of 'v', then there is cycle in graph.

How to check connectivity?

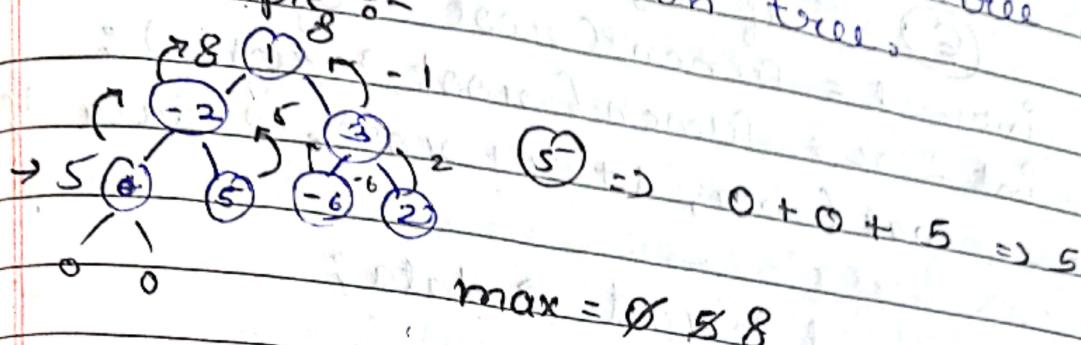
As the graph is undirected, we can start BFS or DFS from any vertex, and check if all vertices are reachable or not. If all vertices are reachable, then graph is connected.

19/3/22

Ques → Find largest subtree sum in tree

Given BT, task is find subtree with maximum sum in tree.

Example :-



$$\text{node } 2 = 5 + 5 + (-2) = 8$$

$$\text{node } 3 = -6 + 2 + 3 = -1$$

$$\text{node } 1 = 8 + (-1) + 1 = 8$$

return max; (ans = 8)

\* Intuition :-

(1) Take left data, take right data.  
(2) maintain 'max' variable.

(3) now add all 3 data i.e  
sum = left + right + curr data.

(4) if sum > max, update max  
else return max in end.

\* Intuition algo :-

```

int funcn(node* root)
{
    if (!root) return 0;
    int l = funcn(root->left);
    int r = funcn(root->right);
    ma = max(ma, 1 + l + root->data);
    return l + root->data;
}
  
```

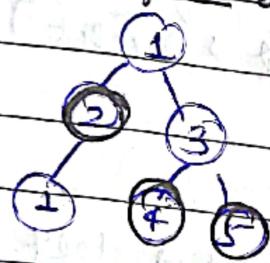
Tc - O(n)

Sc - O(height)

Ques → Maximum sum of nodes is BT such that no two are adjacent.

Given BT, with node associated values, we need to choose subset of these nodes such that sum of chosen node is max under a constraint that no two chosen nodes in subset should be directly connected that is, if we've taken node in our sum then we can't take a node in our sum if we can't take any of its children in consideration.

### ① Example :-



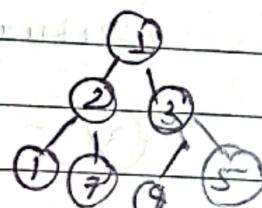
If we pick 2, then can't pick 1, coz they are adjacent.  
So, we choose 2, 4, 5  
 $\Rightarrow 2 + 4 + 5 = 11$  (ans)

### ② Intuition :-

(memorization)

2 possible soln, ( $G^{st}$ ) we include 1 (root) (2nd) doesn't include 1.

- ( $G^{st}$ ) if we include 1 then can't pick 2 & 3, rest we can pick them all - inc
  - $\Rightarrow$  root  $\rightarrow$  left  $\rightarrow$  left
  - $\Rightarrow$  root  $\rightarrow$  left  $\rightarrow$  right
  - $\Rightarrow$  root  $\rightarrow$  right  $\rightarrow$  right
  - $\Rightarrow$  root  $\rightarrow$  right  $\rightarrow$  left



simply add these steps in ans.

### Implementation :-

unordered\_map<Node\*, int> dp;

```
int func(Node* root) {
```

```
    if (!root) return 0;
```

```
    if (dp[root]) return dp[root]; // memoization
```

```
    int inc = root->data;
```

```
    if (root->left) {
```

```
        inc += func(root->left->left);
```

```
        inc += func(root->left->right);
```

3

```
    if (root->right) {
```

```
        inc += func(root->right->left);
```

```
        inc += func(root->right->right);
```

3

```
    int exc = func(root->left) + func(root->right);
```

```
    dp[root] = max(inc, exc);
```

return dp[root];

3

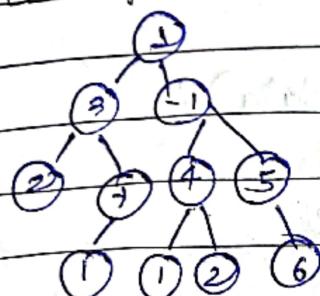
Ques: Print all K-sum path in BT.

(1) BT de work is given, print every path in tree with sum of node in path as K.

Path can start from any node & end at any node & must be downward only.

i.e., they need not be root node & leaf node.

(2) Example :-



$$K = 5$$

3, 2; 3, 1, 1; 131;  
4, 1; 1 - 1 + 1; -1 4 2;  
15; 1 - 1 5.

(All possible ans)

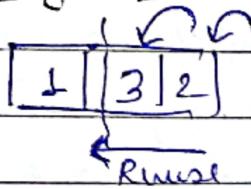
(\*) Partition :-

As we traverse in the tree downward, we'll store all the root path in a vector.

When we reach at any leaf node,

we'll start a loop in that path which is stored in vector, whether it is == K or not (loop in reverse).

Dry Run



$$\text{sum} = 2 + 3 = 5 \Rightarrow \text{break}$$

print 3 | 2

Now 2's work is over & we'll backtrack to 3, again do the same steps above.

1 1 | 3 | + | 1 |

$$\leftarrow \text{sum} = 1 + 1 + 3 = 5$$

[3 | 1 | 1]

Back track 1.

### ④ Implement :-

void func(Node\* root, vector<int>& path, int k)

⑤

if (!root) return;

path.push\_back(root->data);

func(root->left, path, k);

func(root->right, path, k);

int f = 0;

for (int j = path.size() - 1; j >= 0; j--)

⑥

f += path[j];

if (f == k)

for (int m = j; m < path.size(); m++)

⑦

cout << "path[m] <= ";

cout << endl;

⑧

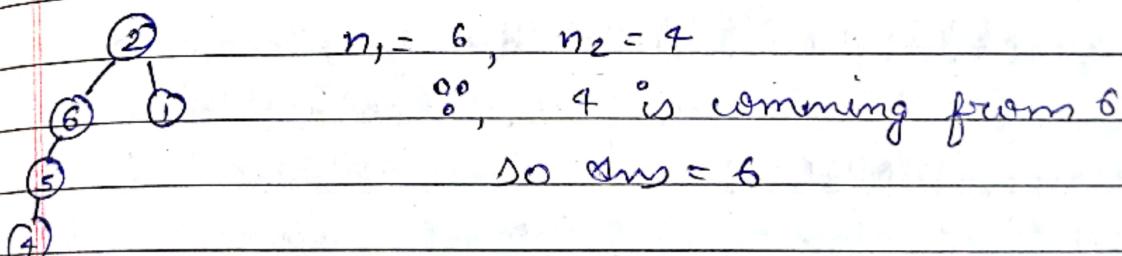
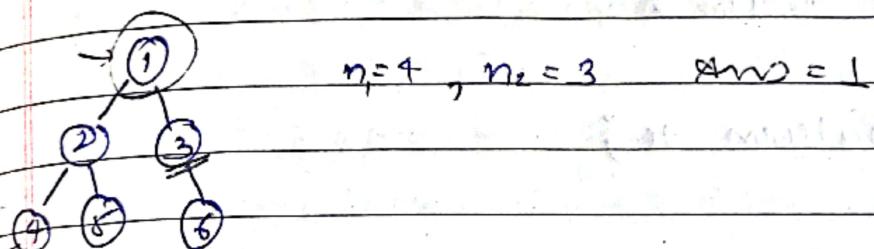
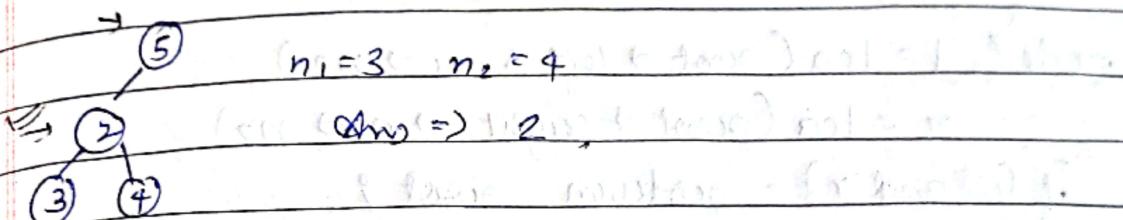
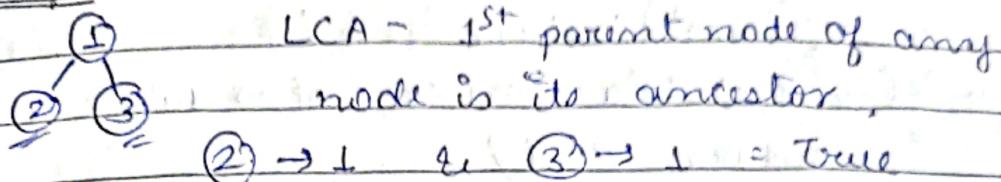
path.pop\_back();

⑨

## Ques :- Longest Common Ancestors in a BT

Given BT with all unique value & two nodes value  $n_1$  &  $n_2$ . Find LCA of BT.

Example :-



\* Intuition :-

- (1) firstly we'll find  $n_1$  &  $n_2$ , if any of them encounter, return them to backstack
- (2) For any node, we are getting value from left & right which is not null, i.e LCA confirmed.
- (3) Above step follow for entire tree till we find  $n_1$  &  $n_2$ .

\* Code :-

```

node * lca(node * root, int n1, int n2)
{
    if(!root) return root;
    if((root->data == n1 || root->data == n2))
        return root;

    node * l = lca(root->left, n1, n2);
    node * r = lca(root->right, n1, n2);

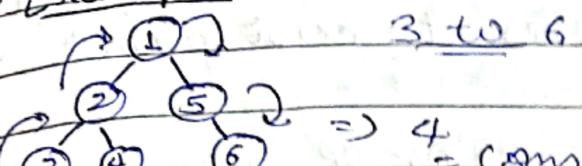
    if(l & r) return root;
    if(l) return l;
    else return r;
}

```

Ques → Find dist b/w 2 nodes in BT

Given BT, & 2 node values, find min. dist. b/w them

\* Example :-



3 to 5  $\Rightarrow$  3 (ans)

\* Intuition :-

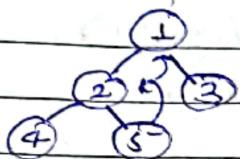
- we've to count the edges b/w nodes  $n_1$  &  $n_2$ .
- + %, we've to find the common point b/w  $n_1$  &  $n_2$ , so we use LCA.
- firstly find the LCA, then find / calculate left distance and right distance.
- add both left and right and return the answer.

Ques  $\rightarrow$   $k^{\text{th}}$  ancestor of node in BT

Given BT, in which nodes are numbered from 1 to n. Given node  $x$  & tree  $K$ .

We've to print  $k^{\text{th}}$  ancestor of given node in BT. If doesn't exist print -1.

\* Example :-



$2^{\text{nd}}$  ancestor of 5 = 1

$3^{\text{rd}}$  ancestor of 5 = -1

\* Intuition :-

One can solve with the help of DFS.

First find given node in tree & then backtrack  $k$  times to reach to  $k^{\text{th}}$  ancestor.

Once we've find/reached  $k^{\text{th}}$  ancestor parent, we'll simply print the node & return NULL.

We'll simply print the node & return NULL.

## ② Implement :-

```
node* kthAncestor(Node* root, int node, int k)
```

Σ

```
if (!root) return NULL;
```

```
node* temp = NULL;
```

```
if (root->data == Node ||
```

```
(temp = kthAncestor(root->left, node, k)) ||
```

```
(temp = kthAncestor(root->right, node, k)))
```

Σ

```
if (k > 0) k--;
```

```
else if (k == 0)
```

```
cout << "kth ancestor is: " << root->data;
```

```
return temp;
```

β

at this point we have to move to left child

we can ignore left subtree because this

function doesn't need left subtree

so we can ignore left subtree

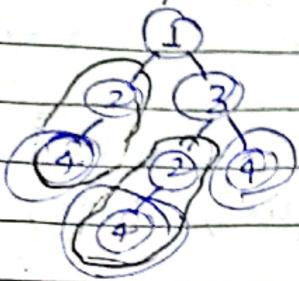
similarly ignore right subtree

so we can ignore right subtree

Ques  $\Rightarrow$  find all duplicate subtree in BT

Given BT of size  $N$ , task is find all duplicate subtree from given BT.

\* Example :-



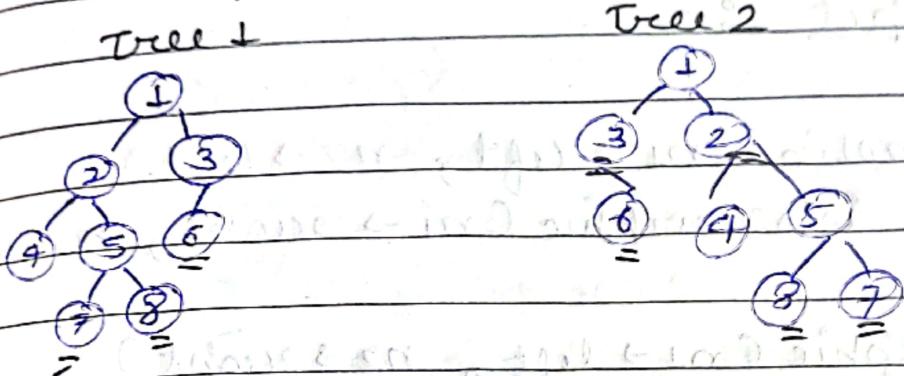
\* Intuition :-

- $\rightarrow$  we'll use hashing. we store inorder traversal of subtree in a hash.
- $\rightarrow$   $\therefore$  simple inorder traversal can't uniquely identify a tree we can use symbol like 'c' and 'l' to represent NULL nodes.
- $\rightarrow$  we pass unordered map as argument to helper func<sup>n</sup>, which recursively calculates inorder string & its count in map.
- $\rightarrow$  If str get repeated, then it will imply duplication of subtree rooted at that node so push that node in final result and return vector of these nodes.

## Ques 3) Check if tree is isomorphic

Check whether tree is isomorphic or not  
isomorphic : 2 tree are called isomorphic if one can be obtained from another by series of flip.  
i.e. by swapping left and right children of several node.

Example :-



flip : 2 & 3, NULL and 6, 7 & 8.  
(isomorphic)

### ② Postution :-

we simultaneously traverse both tree.

Let current internal node of two tree being traversed be  $n_1$  and  $n_2$  respect.

following 2 condtn for subtree rooted with  $n_1$  &  $n_2$  to be isomorphic :

- 1) Data on  $n_1$  &  $n_2$  same,
- 2) one of the following two condtn for children of  $n_1$  and  $n_2$ .

(a) Left child of  $n_1$  is isomorphic to left child of  $n_2$  and right child of  $n_1$  is isomorphic to right child of  $n_2$ .

(b) Left child of  $n_1$  is isomorphic to right child of  $n_2$  & right child of  $n_1$  is isomorphic to left child of  $n_2$ .

④ Snippet :-

C is isomorphic ( $n_1 \rightarrow$  left,  $n_2 \rightarrow$  left)

E1& E2 is isomorphic ( $n_1 \rightarrow$  right,  $n_2 \rightarrow$  right)

C is isomorphic ( $n_1 \rightarrow$  left,  $n_2 \rightarrow$  right)

E1& E2 is isomorphic ( $n_1 \rightarrow$  right,  $n_2 \rightarrow$  left).