

## LECTURE NOTES

Campus: PCE Course: BTECH in CSE Class/Section: III Yr. Section- A Date: 22-03-20  
Name of Faculty: Praveen Kumar Yadav Name of Subject: Machine Learning Code: 6CS4-02  
Date (Prep.): 3-03-21 Date (Del.): 9/4/21 Unit No.: II Lect. No.: 19-14

**OBJECTIVE:** To be written before taking the lecture (Pl. write in bullet points the main topics/concepts etc., which will be taught in this lecture)

K-Means clustering  
Hierarchical clustering

### IMPORTANT & RELEVANT QUESTIONS:

what is K in K-Means clustering  
Algo<sup>m</sup>?

### FEED BACK QUESTIONS (AFTER 20 MINUTES):

How to determine the best K in  
K-means clustering Algo<sup>m</sup>

**OUTCOME OF THE DELIVERED LECTURE:** To be written after taking the lecture (Pl. write in bullet points about students' feedback on this lecture, level of understanding of this lecture by students etc.)

good

**REFERENCES:** Text/Ref. Book with Page No. and relevant Internet Websites:

scikit learn with ML.

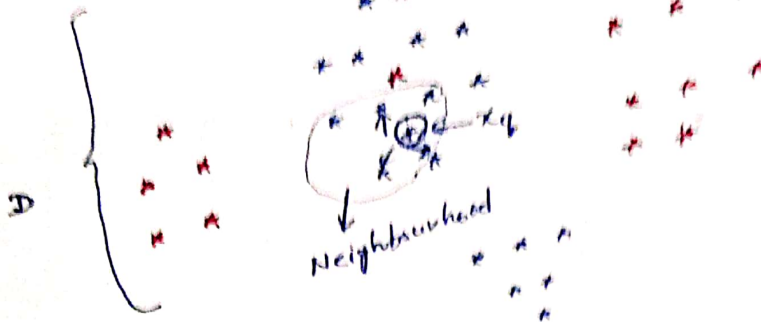
K-Nearest NN Algorithm:-

is K-Neighbour Algorithm

is classification Use case =

$$ED = \sqrt{(x_i - x_j)^2 + (y_i - y_j)^2}$$

Manhattan distance =



+ ; +ve data point

\* ; -ve data point

$$D = \left\{ x_i, y_i \mid \begin{array}{l} x_i \in \mathbb{R}^2 \\ y_i \in \{0, 1\} \end{array} \right\}$$

$\downarrow$  -ve       $\downarrow$  +ve

which are geometrical also

Take points to  $x_q$ :

conclude  $x_q \rightarrow$  the (+ve)

$D \rightarrow ML \rightarrow \text{func}$

$x_q \rightarrow \boxed{f} \rightarrow \begin{cases} +ve \\ -ve \end{cases}$

$x_q \rightarrow y_q$

given task

$$x_q \rightarrow y_q \in \{0, 1\}$$

$\downarrow$  -ve       $\downarrow$  +ve

1. Find k-nearest points to  $x_q$  in D  
let  $k=3$

$$(x_1, x_2, x_3) \rightarrow 3 \text{ NN to } x_q$$

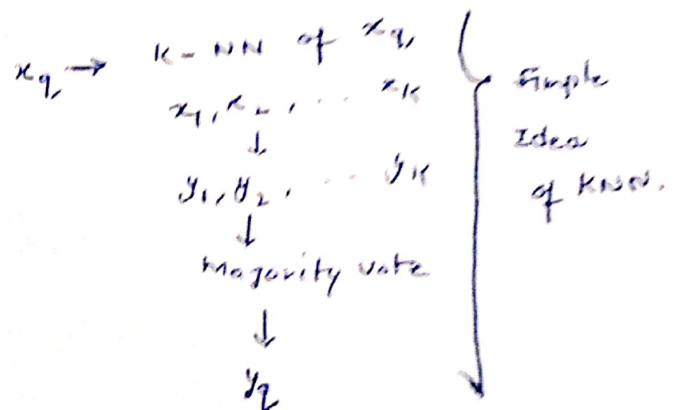
$\downarrow \quad \downarrow \quad \downarrow$   
 $y_1 \quad y_2 \quad y_3$

2. Take their class-labels  $\{y_1, y_2, y_3\} \rightarrow$  Majority vote

+ + +  $\rightarrow y_q = +ve$

+ + -  $\rightarrow y_q = +ve$

$k = \text{odd}$  (preferable)





# POORNIMA

## COLLEGE OF ENGINEERING

### DETAILED LECTURE NOTES

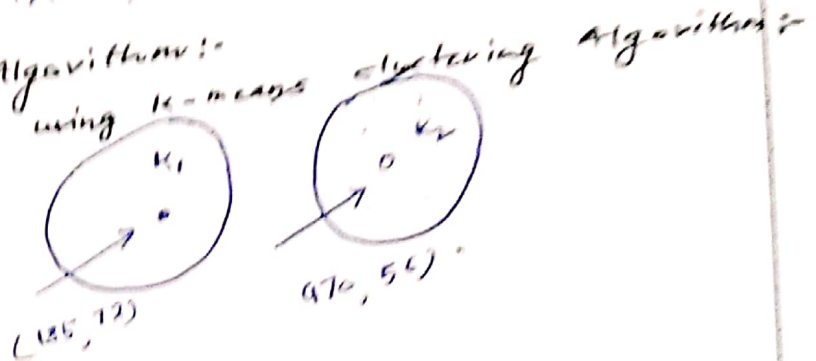
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clustering use case -  
all students - 1st

Unsupervised Learning Algorithm:-

grouping unlabelled items  
eg- Height / weight

185	72
170	56
168	60
179	68
182	72
188	77
180	71
180	70
183	84
180	88
180	67
177	76



ED for 3rd row

$$K_1 \rightarrow \sqrt{(168-185)^2 + (60-72)^2}$$

$$= 20.60$$

$$K_2 = \sqrt{(168-170)^2 + (60-56)^2}$$

$$= 4.48$$

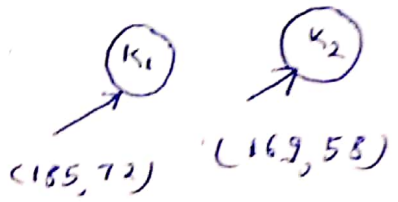
Here value 3rd row goes  $K_2$   
 $K_2 = \{2, 3\}$

New centroid calculation -

$$K_2 = \left( \frac{170+168}{2}, \frac{56+60}{2} \right)$$

$$= (169, 58)$$

New clusters are -



Euclidean Distance -

$$= \sqrt{(x_o - x_c)^2 + (y_o - y_c)^2}$$

↑                      ↑  
observed value    Centroid Value



New Euclidean distance for  $k_1 = \sqrt{(179-185)^2 + (65-72)^2}$   
 4th row.  
 $= 6.32$

$\rightarrow k_2 = \sqrt{(179-169)^2 + (65-58)^2}$   
 $= 14.14$

So 4th row goes to cluster  $k_1$ . So we again  
 calculate the <sup>new</sup> centroid for that row.

$k_1 \rightarrow \{1, 4, 5, 6, 7, 8, 9, 10, 11, 12\}$

$k_2 \rightarrow \{2, 3\}$



# J. J. SOMAIYA

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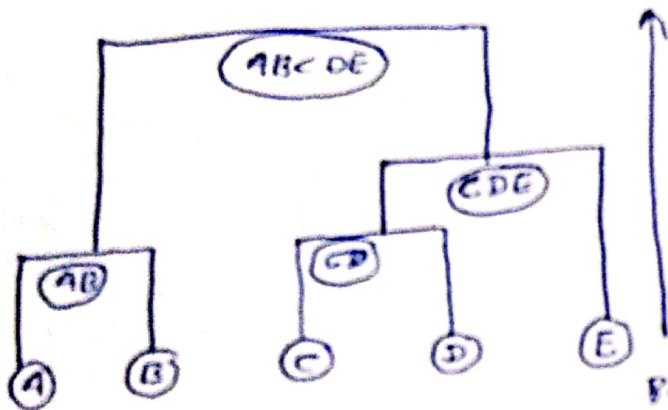
### DETAILED LECTURE NOTES

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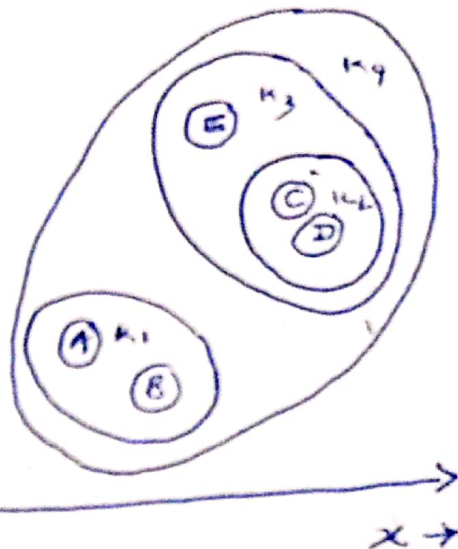
Hierarchical clustering:-

Agglomerative clustering -

- starts from Bottom to top.



y



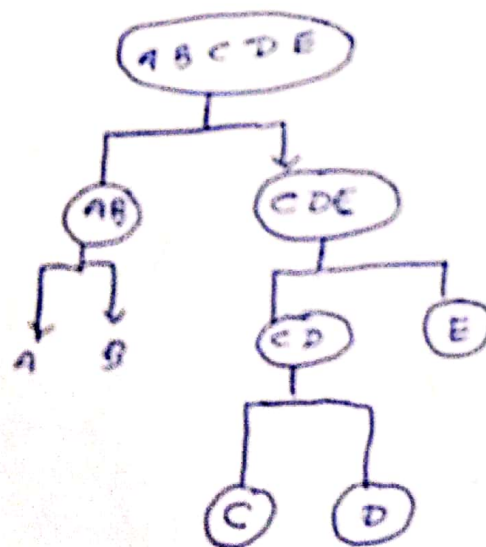
Bottom

up representation

(also known as Dendrogram)

Divisive Approach -

- Top-to Bottom approach



Voronoi assignment



Agglomerative clustering:-  
(with single linkage technique)

→ Agglomerative clustering starts with each individual data points.

→ Then we make cluster of these data points until we get single cluster which represent each data point.

Distance Matrix.

eg-

	$P_1$	$P_2$	$P_3$	$P_4$	$P_5$
$P_1$	0				
$P_2$	9	0			
$P_3$	3	7	0		
$P_4$	6	5	9	0	
$P_5$	11	10	2	8	0

$P_3, P_5$



	$P_1$	$P_2$	$[P_3, P_5]$	$P_4$
$P_1$	0			
$P_2$	9	0		
$[P_3, P_5]$	3	7	0	
$P_4$	6	5	8	0

$$\Rightarrow d(P_1, [P_3, P_5])$$

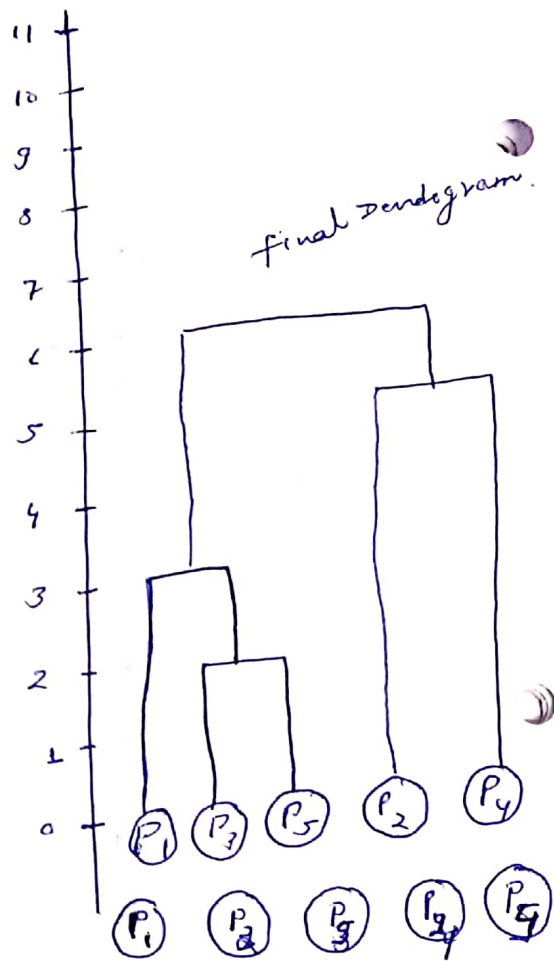
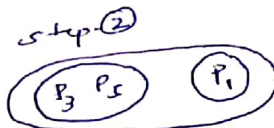
$$\Rightarrow \min(d(P_1, P_3), d(P_1, P_5))$$

$$\Rightarrow \min(3, 11) \Rightarrow 3$$

$$\begin{aligned} &\Rightarrow d(P_2, [P_3, P_5]) \\ &\Rightarrow \min(d(P_2, P_3), d(P_2, P_5)) \\ &\Rightarrow \min(7, 10) \Rightarrow 7 \end{aligned}$$

$$\begin{aligned} &\Rightarrow d(P_4, [P_3, P_5]) \\ &\Rightarrow \min(d(P_4, P_3), d(P_4, P_5)) \\ &\Rightarrow \min(9, 8) \Rightarrow 8 \end{aligned}$$

Here we choose minimum as 3 and make a cluster between  $(P_3, P_5)$  and  $(P_1)$



Updated distance matrix are as-

	$[P_1, P_3, P_5]$	$P_2$	$P_4$
$[P_1, P_3, P_5]$	0		
$P_2$	7	0	
$P_4$	6	5	0

take min - 5 so make cluster  $(P_2, P_4)$

$$d(P_2, [P_1, P_3, P_5])$$

$$= \min(d(P_2, P_1), d(P_2, P_3), d(P_2, P_5))$$

$$= \min(9, 7, 10) \Rightarrow 7$$

$$d(P_4, [P_1, P_3, P_5])$$

$$\Rightarrow \min(d(P_4, P_1), d(P_4, P_3), d(P_4, P_5))$$

$$\Rightarrow \min(5, 9, 8) \Rightarrow 5$$

	$[p_1, p_3, p_5]$	$[p_2, p_4]$
$[p_1, p_3, p_5]$	0	
$[p_2, p_4]$		0

$$d([p_1, p_3, p_5], [p_2, p_4])$$

$$= \min(d[p_1, p_2], d[p_1, p_4], d[p_3, p_2], d[p_3, p_4],$$

$$d[p_5, p_2], d[p_5, p_4])$$

$$\Rightarrow \min(9, 6, 7, 10, 8, 9)$$

$$\Rightarrow \min 6$$

make a single cluster

