



# POORNIMA

## COLLEGE OF ENGINEERING

### LECTURE NOTES

Campus: PCE Course: BTECH Class/Section: III<sup>rd</sup> IV/C Date: 22.01.21  
Name of Faculty: Rawan K. YADAV Name of Subject: Machine Learning Code: 6C54-02  
Date (Prep.): 22.01.21 Date (Del.): 01.02.21 Unit No./Topic: 1 Lect. No: 3

OBJECTIVE: To be written before taking the lecture (Pl. write in bullet points the main topics/concepts etc. which will be taught in this lecture)

Linear Regression

IMPORTANT & RELEVANT QUESTIONS:

① what is Linear Regression? Explain with the help of any eg.

FEED BACK QUESTIONS (AFTER 20 MINUTES):

① what are the differences between dependent and Independent variable.

OUTCOME OF THE DELIVERED LECTURE: To be written after taking the lecture (Pl. write in bullet points about students' feedback on this lecture, level of understanding of this lecture by students etc.)

REFERENCES: Text/Ref. Book with Page No. and relevant Internet Websites:

Hands on Machine Learning, Aurlien Geron.



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#### Linear Regression Model:-

- Profit estimation of a company.
- Independent variable - A variable whose value does not change by the effect of other variable and used to manipulate the dependent variable. It is often denoted as  $x$ .  
eg- Rainfall - Independent variable (beac rainfall can't be controlled by human being but rainfall can effect the crop).
- Dependent variable - Are those variable whose value change when there is a change in the independent variable. It is often denoted as  $y$ .  
eg- crop yield depends on the amount of rainfall received.

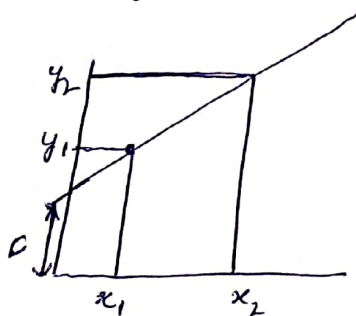
## Applications of Linear Regression:-

- + Economic Growth - Used to determine the economic growth of a country or state in coming quarter.
- can be used to predict the GDP of a country.
- " " " " " the price of a product in the future.
- To estimate the number of houses a builder would sell and at what prices in the coming month.
- score prediction - To predict the number of runs a player would score in the coming match based on previous performance.

Understanding Linear Regression:- Linear Regression is a statistical model used to predict the relationship between independent and dependent variable.

The simplest form of a simple linear regression equation with one dependent and one independent variable is represented by-

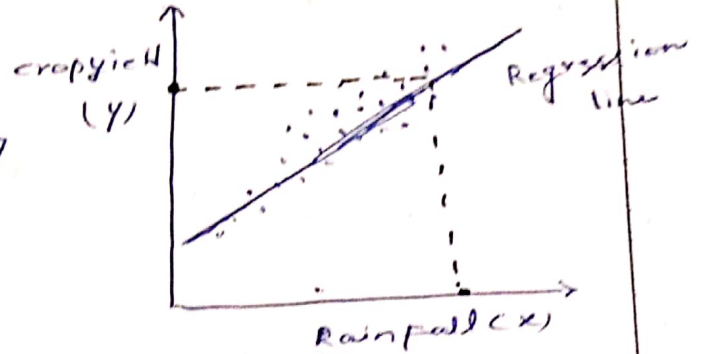
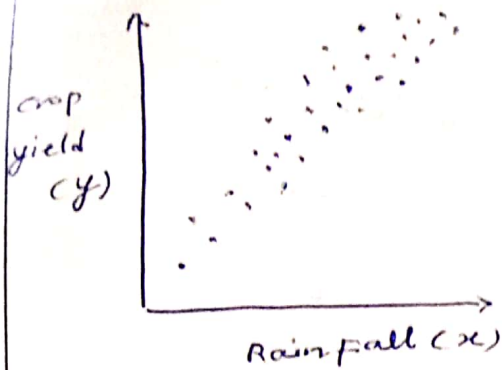
$$y = mx + c$$



- y - dependent variable
- x - independent variable
- m - slope of line  $m = \frac{y_2 - y_1}{x_2 - x_1}$
- c - intercept or coefficient of the line.

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$$m = \frac{(n * \sum(x * y)) - (\sum(x) * \sum(y))}{(n * \sum(x^2)) - (\sum(x)^2)}$$

x	y (actual y values)	$\hat{y}$ (predicted)
1	2	2.8
2	4	3.4
3	5	4
4	6	4.6
5	5	5.2

$$= \frac{(5 * 66) - (15 * 20)}{(5 * 55) - 225} = 0.6$$

$$c = \frac{(\sum(y) * \sum(x^2)) - (\sum(x) * \sum(x * y))}{(n * \sum(x^2)) - (\sum(x)^2)}$$

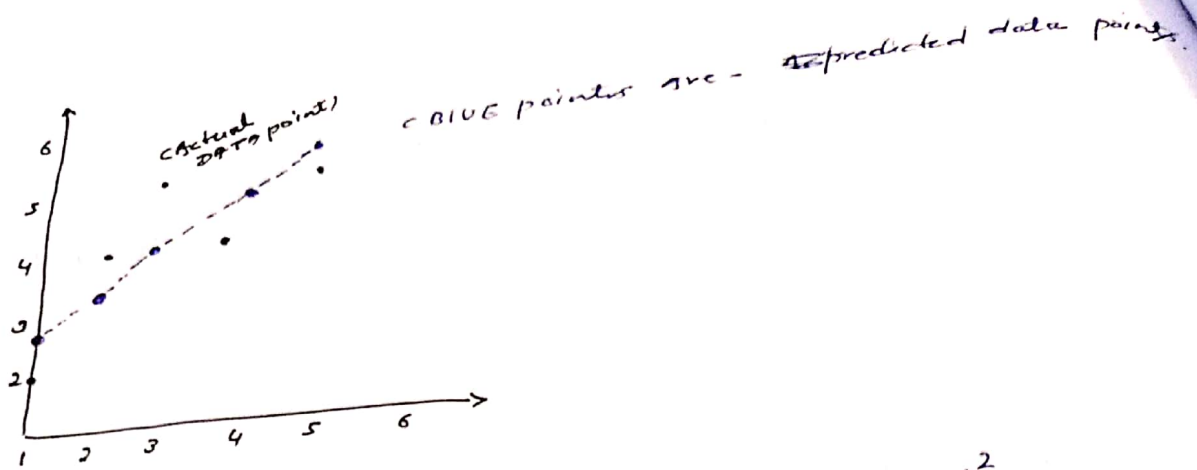
$$= 2.2$$

$$y = m * x + c$$

$$= 0.6 * 3 + 2.2$$

$$= 4$$





$x$	$y$	$y_{pred}$	$y - y_{pred}$	$(y - y_{pred})^2$
1	2	2.8	-0.8	0.64
2	4	4.4	0.6	0.36
3	5	4	1	1
4	4	4.6	-0.6	0.36
5	5	5.2	-0.2	0.04
				$\Sigma = 2.4$

Residual of errors - The distance between actual and predicted values are known as residual or errors.

The best fit line should have the least sum of squares of these errors also known as e-square.

The sum of squared errors of this regression line is 2.4. we check this error for each line and conclude the best fit line having the least e-square value.



# P. O. R. N. I. M. A.

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#### MULTIPLE LINEAR REGRESSION:-

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Multiple Linear Regression  $\longrightarrow$   $y = m_1x_1 + m_2x_2 + \dots + m_nx_n + c$

$\downarrow$   $\downarrow$   $\downarrow$

Dependent variable  $\downarrow$  slopes  $\downarrow$  coefficient

Independent Variables (IDV's)