

When assessing the performance of regression models, R-squared ( $R^2$ ) and Adjusted R-squared are commonly used metrics. Both provide insights into how well the model fits the data, but have distinct purposes. Let's get into the details of these metrics to understand their strengths and limitations.

### Introduction to R-squared ( $R^2$ )

R-squared measures the proportion of the variance in the dependent variable (let's say, house prices) that is explained by the independent variables (features like square footage, bedrooms, and neighborhood characteristics).

Formula:

$$R^2 = 1 - \frac{\sum_{i=1}^n (y_i - \bar{y})^2}{\sum_{i=1}^n (y_i - \hat{y}_i)^2}$$

Where:

- $y_i$  is the actual value
- $\hat{y}_i$  is the predicted value
- $\bar{y}$  is the mean of the actual values
- $n$  is the number of data points

Interpretation:

- $R^2$  ranges from 0 to 1.
- A higher  $R^2$  value indicates a better fit.
- However,  $R^2$  has limitations, particularly when it comes to model complexity and the addition of unnecessary predictors.

### Introduction to Adjusted R-squared

While  $R^2$  provides a fit measure, it doesn't account for the number of predictors in the model. Adjusted R-squared addresses this limitation by penalizing the inclusion of unnecessary predictors.

Formula:

$$R_{adj}^2 = 1 - (n - p - 1) \frac{(1 - R^2)}{(n - 1)}$$

Where:

- $R_{adj}^2$  is the adjusted  $R^2$
- $n$  is the number of data points
- $p$  is the number of independent variables (predictors)

### **Choosing Between $R^2$ and Adjusted $R^2$**

- $R^2$  is useful for comparing models with the same predictors.
- Adjusted  $R^2$  is better for comparing models with different numbers of predictors because it accounts for the number of predictors, helping to find the simplest model that fits the data well.

### **Conclusion**

The choice between  $R^2$  and Adjusted  $R^2$  depends on the specific goals of the analysis. While  $R^2$  gives a general sense of fit, Adjusted  $R^2$  considers model complexity.

Understanding these metrics, along with residuals and graphical representations, provides a holistic approach to model evaluation. This knowledge is invaluable in making informed decisions when building regression models for predicting house prices or any other dependent variable.