



Continuous Assessment Test (CAT)- I- November 2022

Programme	B.Tech.	Semester	Fall 2022-2023
Course Title	Calculus	Code	BMAT101L/IMAT101L
Faculty	Dr. Karan Kumar Pradhan, Dr. Manoj Kumar Singh, Dr. Pankaj Shukla, Dr. Abhishek Kumar Singh, Dr Dhansekhar, Dr Berin Alan, Dr. Kirti Aarya, Dr Kalyan Manna, Dr Vijay Kumar Poshala, Dr. Sandeep Saha	Slot	B1+TB1
Duration	1 ½ Hours	Class No.	CH2022231700262, CH2022231700260, CH2022231700270, CH2022231700272, CH2022231700268, CH2022231700481, CH2022231700612, CH2022231700751, CH2022231700482, CH2022231700484

Answer all the Questions (50 marks)

- | Q.No. | Question Description   | Marks |
|-------|--|-------|
| 1.    | (a) Let $f(x)$ be twice differentiable on $[0,2]$ . Show that if $f(0) = 0$ , $f(1) = 2$ and $f(2) = 4$ , then there exists $x_0 \in (0,2)$ such that $f''(x_0) = 0$ .<br>(b) Show that $f(x) = \sin x (1 + \cos x)$ has a local maximum at $x = \frac{\pi}{3}$ , and then find the local maximum value. | [5+5] |
| 2.    | Find the critical points of $f(x) = x^{\frac{1}{3}}(x^2 - 4)$ . Identify the intervals on which $f(x)$ is increasing and decreasing. Further, find the function's local extreme values.  | [10]  |
| 3.    | Find the volume of the solid generated by revolving the region bounded by the graphs of $y = \sqrt{x}$ , $y = 2 - x$ and $y = 0$ about the x-axis. Sketch the region under consideration.  | [10]  |
| 4.    | Using $\varepsilon - \delta$ definition the limit of the function $f(x,y) = \frac{4xy^2}{x^2+y^2}$ exists or not?  | [10]  |
| 5.    | If $u = 3x + 2y - z$ , $v = x - 2y + z$ and $w = x(x + 2y - z)$ , show that they are functionally related, and find the relation between them.   | [10]  |

