

Question 1

	B	B'	Total
A	10	30	40
A'	25	35	60
Total	35	65	100

a. $P(A) = 40/100 = \mathbf{0.4}$

b. $P(A') = 60/100 = \mathbf{0.6}$

c. $P(A \text{ and } B) = 10/100 = \mathbf{0.1}$

d. $P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$
 $= 0.4 + 0.35 - 0.1 = \mathbf{0.65}$

e. $P(A|B) = P(A \text{ and } B) / P(B)$

$$= 0.1/0.35 = 10/35 \text{ or } \mathbf{0.29}$$

f. **A** and B are not independent. Probability of A given B is not equal to probability of A.

$$P(A|B) \neq P(A) \{0.29 \neq 0.4\}$$

$$\text{Similarly, } P(A \text{ and } B) \neq P(A) P(B) \{0.1 \neq 0.14\}$$

Question Two

	Female	Male	Total
Coke	120	95	215
Pepsi	95	80	175
Neither	65	45	110
Total	280	220	500

a. $P(\text{Pepsi} \mid \text{Male}) = P(\text{Pepsi and Male}) / P(\text{Male})$

$$P(\text{Pepsi and Male}) = 80/500 = 0.16$$

$$P(\text{Male}) = 220/500 = 0.44$$

$$P(\text{Pepsi} \mid \text{Male}) = 0.16/0.44 = \mathbf{0.36}$$

b. $P(\text{Pepsi} \mid \text{Female}) = P(\text{Pepsi and Female}) / P(\text{Female})$

$$P(\text{Pepsi and Female}) = 95/500 = 0.19$$

$$P(\text{Female}) = 280/500 = 0.56$$

$$P(\text{Pepsi} \mid \text{Female}) = 0.19/0.56 = \mathbf{0.34}$$

- c. The preference for Pepsi depends on gender. The probability one prefers Pepsi given that he is male is not equal to probability that one is a male customer. That is;

$$P(\text{Pepsi} \mid \text{Male}) \neq P(\text{Male}) \quad \{ 0.36 \neq 0.44 \}$$

$$\text{Similarly, } P(\text{Pepsi} \mid \text{Female}) \neq P(\text{Female}) \quad \{ 0.34 \neq 0.56 \}$$

Question Three

Bill (x)	(x - \bar{x})	(x - \bar{x}) ²
96	-53.72	2886.077
171	21.28	452.7438
202	52.28	2732.966
178	28.28	799.6327
147	-2.72	7.410494
102	-47.72	2277.41
153	3.28	10.74383
197	47.28	2235.188
127	-22.72	516.2994
157	7.28	52.96605
185	35.28	1244.522
90	-59.72	3566.744
116	-33.72	1137.188
172	22.28	496.2994
111	-38.72	1499.41
148	-1.72	2.966049
213	63.28	4004.077
130	-19.72	388.966
$\Sigma = 2695$	$\Sigma=0$	$\Sigma = 24311.61$

a. Mean = $2695/18$

$$= \$149.72$$

b. Variance = $23311.61 / 17$

$$= 1430.10$$

c. Standard deviation = $\sqrt{1430.10}$

$$= \$37.82$$

d. Histogram

i. Order Data

ii. range: 90 – 123

iii. width: 123

iv. Bins: 7

v. Size of bin: \$18

