





Ref.: Data Mining: Concepts and Techniques

Classification

Prediction Problems: Classification vs. Numeric Prediction

Classification

- predicts categorical class labels (discrete or nominal)
- classifies data (constructs a model) based on the training set and the values (class labels) in a classifying attribute and uses it in classifying new data

Numeric Prediction

- models continuous-valued functions, i.e., predicts unknown or missing values
- Typical applications
 - Credit/loan approval:
 - Medical diagnosis: if a tumor is cancerous or benign
 - Fraud detection: if a transaction is fraudulent
 - · Web page categorization: which category it is

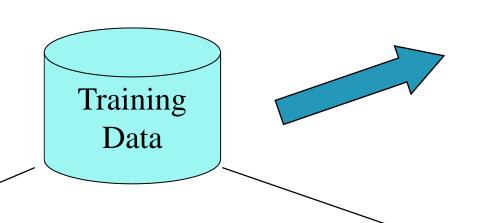


Classification—A Two-Step Process

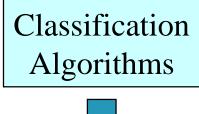
- Model construction: describing a set of predetermined classes
 - Each tuple/sample is assumed to belong to a predefined class, as determined by the class label attribute
 - The set of tuples used for model construction is training set
 - The model is represented as classification rules, decision trees, or mathematical formulae
- Model usage: for classifying future or unknown objects
 - Estimate accuracy of the model
 - The known label of test sample is compared with the classified result from the model
 - Accuracy rate is the percentage of test set samples that are correctly classified by the model
 - Test set is independent of training set (otherwise overfitting)
 - · If the accuracy is acceptable, use the model to classify new data
- Note: If the test set is used to select models, it is called validation (test) set

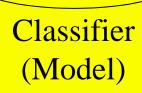


Process (1): Model Construction



NAME	RANK	YEARS	TENURED
Mike	Assistant Prof	3	no
Mary	Assistant Prof	7	yes
Bill	Professor	2	yes
Jim	Associate Prof	7	yes
Dave	Assistant Prof	6	no
Anne	Associate Prof	3	no

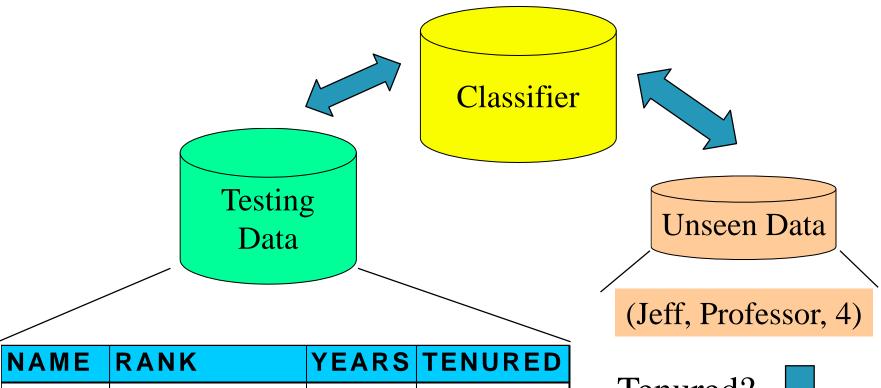




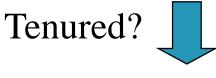
IF rank = 'professor'
OR years > 6
THEN tenured = 'yes'



Process (2): Using the Model in Prediction



NAME	RANK	YEARS	TENURED
Tom	Assistant Prof	2	no
Merlisa	Associate Prof	7	no
George	Professor	5	yes
Joseph	Assistant Prof	7	yes

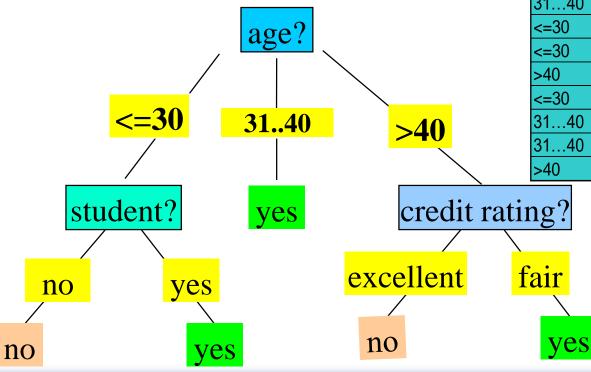






Decision Tree Induction: An Example

- □ Training data set: Buys_computer
- □ The data set follows an example of Quinlan's ID3 (Playing Tennis)
- □ Resulting tree:



age	income	student	credit_rating	buys_computer
<=30	high	no	fair	no
<=30	high	no	excellent	no
3140	high	no	fair	yes
>40	medium	no	fair	yes
>40	low	yes	fair	yes
>40	low	yes	excellent	no
3140	low	yes	excellent	yes
<=30	medium	no	fair	no
<=30	low	yes	fair	yes
>40	medium	yes	fair	yes
<=30	medium	yes	excellent	yes
3140	medium	no	excellent	yes
3140	high	yes	fair	yes
>40	medium	no	excellent	no



Decision Tree Induction - Basics

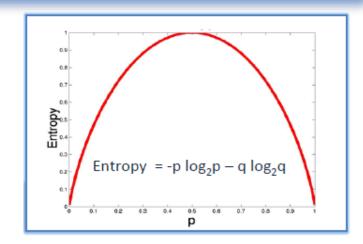
Decision tree builds classification or regression models in the form of a tree structure. It breaks down a dataset into smaller and smaller subsets while at the same time an associated decision tree is incrementally developed. The final result is a tree with decision nodes and leaf nodes. A decision node (e.g., Outlook) has two or more branches (e.g., Sunny, Overcast and Rainy). Leaf node (e.g., Play) represents a classification or decision. The topmost decision node in a tree which corresponds to the best predictor called root node. Decision trees can handle both categorical and numerical data.

	Pre	edictors		Target	
					Decision T
Outlook	Temp.	Humidity	Windy	Play Golf	Outlook
Rainy	Hot	High	Falce	No	
Rainy	Hot	High	True	No	
Overoast	Hot	High	Falce	Yes	Sunny Overcast Rainy
Sunny	Mild	High	Falce	Yes	Sunny Overcast Rainy
Sunny	Cool	Normal	Falce	Yes	
Sunny	Cool	Normal	True	No	
Overoast	Cool	Normal	True	Yes	Windy Yes Humidity
Rainy	MIIId	High	Falce	No	-
Rainy	Cool	Normal	Falce	Yes	
Sunny	Milid	Normal	False	Yes	FALSE TRUE High Norn
Rainy	Mild	Normal	True	Yes	
Overoast	Mild	High	True	Yes	
Overoast	Hot	Normal	Falce	Yes	Yes No No Yes
Sunny	Mild	High	True	No	

Decision Tree - Entropy

A decision tree is built top-down from a root node and involves partitioning the data into subsets that contain instances with similar values (homogenous). ID3 algorithm uses entropy to calculate the homogeneity of a sample. If the sample is completely homogeneous the entropy is zero and if the sample is an equally divided it has entropy of one.

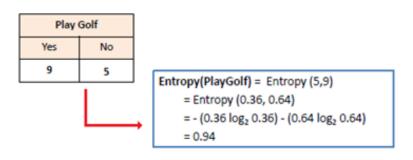
To build a decision tree, we need to calculate two types of entropy using frequency tables as follows:



Entropy = $-0.5 \log_2 0.5 - 0.5 \log_2 0.5 = 1$

a) Entropy using the frequency table of one attribute: b) Entropy using the frequency table of two attributes:

$$E(S) = \sum_{i=1}^{c} -p_i \log_2 p_i$$



$$E(T, X) = \sum_{c \in X} P(c)E(c)$$

	1						
			Yes	No			
		Sunny	3	2	5		
	Outlook	Overcast	4	0	4		
		Rainy	2	3	5		
					14		
1							
E(PlayGolf, Outlook) = P(Sunny)*E(3,2) + P(Overcast)*E(4,0) + P(Rainy)*E(2,3)							
= (5/14)*0.971 + (4/14)*0.0 + (5/14)*0.971							
= 0.693							



Attribute Selection Measure: Information Gain (ID3/C4.5)

- Select the attribute with the highest information gain
- Let p_i be the probability that an arbitrary tuple in D belongs to class C_i , estimated by $|C_{i,D}|/|D|$
- Expected information (entropy) needed to classify a tuple in D: $Info(D) = -\sum_{i=1}^{m} p_i \log_2(p_i)$
- Information needed (after using A to split D into v partitions) to classify D: $Info_A(D) = \sum_{j=1}^{v} \frac{|D_j|}{|D|} \times Info(D_j)$
- Information gained by branching on attribute A $Gain(A) = Info(D) Info_{A}(D)$



Attribute Selection: Information Gain

- Class P: buys_computer = "yes"
- Class N: buys_computer = "no"

Info (D) =
$$I(9,5) = -\frac{9}{14}\log_2(\frac{9}{14}) - \frac{5}{14}\log_2(\frac{5}{14}) = 0.940$$

age	p _i	n _i	I(p _i , n _i)
<=30	2	3	0.971
3140	4	0	0
>40	3	2	0.971

age	income	student	credit_rating	buys_computer
<=30	high	no	fair	no
<=30	high	no	excellent	no
3140	high	no	fair	yes
>40	medium	no	fair	yes
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3140	medium	no	excellent	yes
3140	high	yes	fair	yes
>40	medium	no	excellent	no

Info_{age} (D) =
$$\frac{5}{14}I(2,3) + \frac{4}{14}I(4,0)$$

+ $\frac{5}{14}I(3,2) = 0.694$

$$\frac{5}{14}I(2,3)$$
 means "age <= 30" has 5 out of 14 samples, with 2 yes'es and 3 no's. Hence

$$Gain(age) = Info(D) - Info_{age}(D) = 0.246$$

Similarly,
$$Gain(income) = 0.029$$

$$Gain(student) = 0.151$$

$$Gain(credit_rating) = 0.048$$



Computation of Gini Index

Ex. D has 9 tuples in buys_computer = "yes" and 5 in "no"

$$gin(D) = 1 - \left(\frac{9}{14}\right)^2 - \left(\frac{5}{14}\right)^2 = 0.459$$

Suppose the attribute income partitions D into 10 in D_1 : {low, medium} and 4 in D_2 (10) C_1 (4) C_2 (10)

$$gini_{income \in \{low, medium\}}(D) = \left(\frac{10}{14}\right)Gini(D_1) + \left(\frac{4}{14}\right)Gini(D_2)$$

$$= \frac{10}{14} \left(1 - \left(\frac{7}{10} \right)^2 - \left(\frac{3}{10} \right)^2 \right) + \frac{4}{14} \left(1 - \left(\frac{2}{4} \right)^2 - \left(\frac{2}{4} \right)^2 \right)$$
$$= 0.443$$

 $= Gini_{income \in \{high\}}(D).$

 $Gini_{low,high}$ is 0.458; $Gini_{medium,high}$ is 0.450. Thus, split on the $\{low,medium\}$ (and $\{high\}$) since it has the lowest Gini index

- All attributes are assumed continuous-valued
- May need other tools, e.g., clustering, to get the possible split values
- Can be modified for categorical attributes



Comparing Attribute Selection Measures

- ▶ The three measures, in general, return good results:
 - Information gain:
 - biased towards multivalued attributes
 - Gain ratio:
 - tends to prefer unbalanced splits in which one partition is much smaller than the others
 - Gini index:
 - biased to multivalued attributes
 - has difficulty when # of classes is large
 - tends to favor tests that result in equal-sized partitions and purity in both partitions



Overfitting and Tree Pruning

- Overfitting: An induced tree may overfit the training data
 - Too many branches, some may reflect anomalies due to noise or outliers
 - Poor accuracy for unseen samples
- Two approaches to avoid overfitting
 - Prepruning: Halt tree construction early-do not split a node if this would result in the goodness measure falling below a threshold
 - · Difficult to choose an appropriate threshold
 - Postpruning: Remove branches from a "fully grown" tree get a sequence of progressively pruned trees
 - Use a set of data different from the training data to decide which is the "best pruned tree"



Evaluation

